

# Complex Networks

## Project 3: Network models

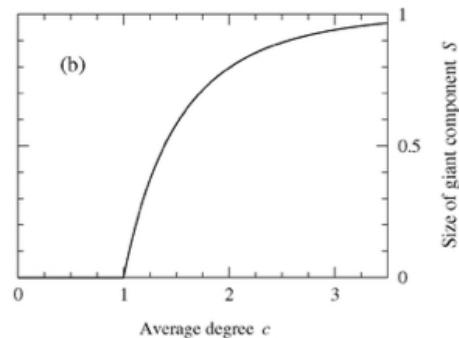
Send the solutions to: [projetosicmc@gmail.com](mailto:projetosicmc@gmail.com)

### 1 – Comparison of network models

- Generate 30 networks according to the models: Erdős-Rényi, Watts-Strogatz ( $p=0.01$  and  $p=0.1$ ) e Barabási-Albert. Consider  $N = 1000$  and  $\langle k \rangle = 10$ .
- In table, include the mean and standard deviation of the following measures: (i) number of nodes, (ii) average degree, (iii) second moment of degree distribution, (iv) average shortest path length, (v) average clustering coefficient, (vi) transitivity, (vii) assortativity coefficient.
- Show the degree distributions of the ER, WS and BA networks
- Discuss the main differences and similarities between the models.

### 2 – Erdős-Rényi network model

- For the model ER ( $N, p$ ), obtain the phase transition curve:



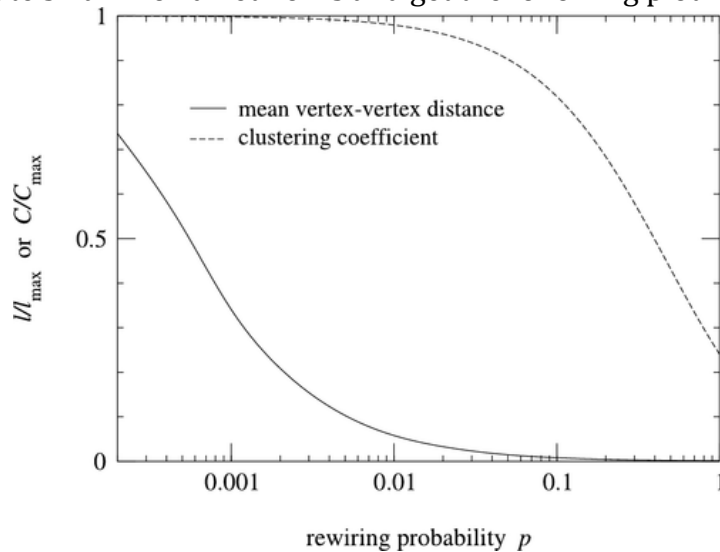
- Verify the small-world property by plotting the average shortest path length and diameter in terms of the number of nodes:

$$d_{\max} = \frac{\log N}{\log \langle k \rangle}$$

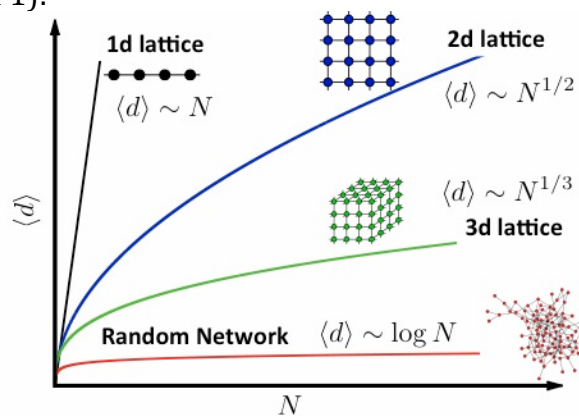
Consider  $\langle k \rangle = 4, 10, 20$  and  $30$  and  $N$  from  $100$  to  $1000$  in steps of  $100$ .

### 3 – Watts-Strogatz model

- Generate small-world networks and get the following plot:



- Verify the variance of the degree distribution in terms of the parameter  $p$ , i.e., construct a plot of the second moment of degree distribution in terms of  $p$ .
- Plot the degree distribution of the small-world model for  $p=0.001, 0.01$  and  $0.1$ .
- Obtain the following plot in terms of  $p$  (consider curves for  $p=0, 0.001, 0.01, 0.1$  and  $1$ ):

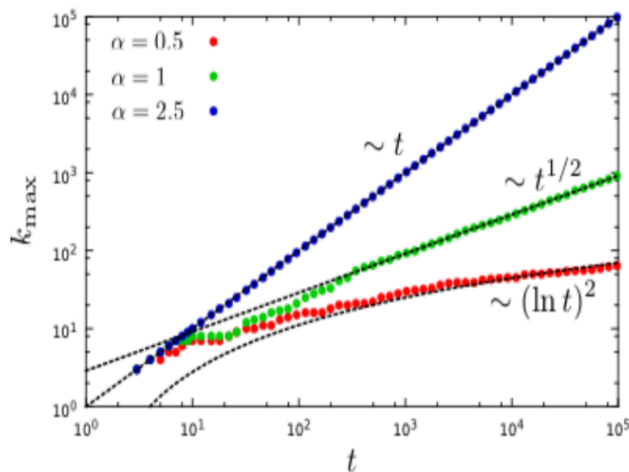


### 4 – Scale-free network model

- Compare the Barabási-Albert with the configuration model ( $\gamma = -3$ ) in terms of the following measures (construct a table): (i) number of nodes, (ii) average degree, (iii) second moment of degree distribution, (iv) average shortest path length, (v) average clustering coefficient, (vi) transitivity, (vii) assortativity coefficient.
- Using the igraph package, generate networks according to the non-linear Barabási model:

[https://igraph.org/c/doc/igraph-Generators.html#igraph\\_barabasi\\_game](https://igraph.org/c/doc/igraph-Generators.html#igraph_barabasi_game)

Obtain this curve and discuss the results (t is the number of steps in the model, network size):



For  $\alpha = 0.5, 1$  and  $1.5$  and  $2.5$ , obtain the table:

- (i) number of nodes, (ii) average degree, (iii) second moment of degree distribution, (iv) average shortest path length, (v) average clustering coefficient, (vi) transitivity, (vii) assortativity coefficient.

## 5 – Classification of networks

- Choose three networks and perform the classification. Show the results by using the PCA. For example (real network represented by X):

