

R Software:-

1. R is a software for statistical analysis and data computing.
2. It is an effective data handling software and outcome storage is possible.
3. It is capable of graphical display.
4. It is free software.

Q1. Solve the following:-

1. $4 + 6 + 8 \div 2 - 5$

> $4 + 6 + 8/2 - 5$

> 9

2. $2^2 + 1 - 31 + \sqrt{45}$

> $2^2 + 1 - 31 + \text{sqrt}(45)$

> 13.7082

3. $5^3 + 7 \times 5 \times 8 + 46 \div 5$

> $5^3 + 7 * 8 * 5 + 46/5$

> 414.2

4. $\sqrt{4^2 + 5 \times 3 + 7 \div 6}$

> $\text{sqrt}(4^2 + 5 * 3 + 7/6)$

> 5.671567

5. roundoff $46 \div 7 + 9 \times 8$
 $> \text{round}(46 / 7 + 9 * 8)$
 > 79

Q2. Solve the following:-

① $> C(2, 3, 5, 7) * 2$
 $> 4, 6, 10, 14$

② $> C(2, 3, 5, 7) * C(2, 3)$
 $> 4, 9, 10, 21$

③ $> X(2, 3, 5, 7) * C(2, 3, 6, 2)$
 $> 4, 9, 30, 14$

④ $> X(1, 6, 2, 3) * C(-2, -3, -4, -1)$
 $[1] -2, -18, -8, -3$

⑤ $> X(2, 3, 5, 7)^2$
 $[1] 4, 9, 25, 49$

⑥ $> C(1, 6, 8, 9, 4, 5)^2 C(1, 2, 3)$
 $[1] 4, 36, 512, 9, 16, 125$

⑦ $> C(6, 2, 7, 5) / C(4, 5)$
 $[2] 1.50, 0.40, 1.75, 1.00$

Q3. Solve the following:-

1] $> x = 20$
 $> y = 30$
 $> z = 2$
 $> x^2 + y^3 + z$
 $[1] 27402$

2] $\sqrt{x^2 + y^2}$
 $> \text{sqrt}(x^2 + y^2)$
 $> [1] 20.73649$

3] $x^2 + y^2$
 $> x^2 + y^2$
 $[2] 1300$

Q4. Solve:-

(i) $\begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \end{bmatrix}$

$> z = \text{matrix}(\text{nrow}=4, \text{ncol}=2, \text{data}=(1:8))$

$> x$

	[1]	[2]
[1]	1	5
[2]	2	6
[3]	3	7
[4]	4	8

(ii) $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$ $y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$

$> x = \text{matrix}(\text{nrow}=3, \text{ncol}=3, \text{data}=(4, 7, 9, -2, 0, -6, 6, 7, 3))$
 $> y = \text{matrix}(\text{nrow}=3, \text{ncol}=3, \text{data}=(10, 12, 15, -5, -4, -6, 7, 9, 6))$

Q5. Prints of marks of computer science students are as follows:-

Data: 59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 17, 58, 54, 40, 50, 32, 36, 29, 35, 39

```
> x = c(given data)
> length(x)
> [1] 20
> breaks = seq(20, 60, 5)
> a = cut(x, breaks, right = FALSE)
> b = table(a)
> c = transform(b)
```

	x	freq
1	[20, 25)	3
2	[25, 30)	1
3	[30, 35)	4
4	[35, 40)	1
5	[40, 45)	3
6	[45, 50)	2
7	[50, 55)	4
8	[55, 60)	4

Practical no 2.

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Probability distribution.

Q1. check whether the followings are p.m.f or not.

(i)	x	p(x)
	0	0.1
	1	0.2
	2	-0.5
	3	0.4
	4	0.3
	5	0.5

Since $p(2) = -0.5$,

can't be a probability mass function.

Since in p.m.f $p(x) \geq 0 \forall x$

(ii)	x	1	2	3	4	5
	p(x)	0.2	0.2	0.3	0.2	0.2

It can't be a p.m.f,

as in p.m.f

$\sum p(x) = 1$

(ii)

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

> prob=c(0.2,0.2,0.35,0.15,0.1)

> sum(prob)

[1] 1

As $\sum p(x) = 1$,

it is a p.m.f

Q2.
(i) Find C.d.f for the following p.m.f and sketch the graph.

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

$F(x) = 0$	$x < 10$
0.2	$10 \leq x < 20$
0.4	$20 \leq x < 30$
0.75	$30 \leq x < 40$
0.95	$40 \leq x < 50$
1.0	$x \geq 50$

Q2

(i)

> prob=c(0.2,0.2,0.35,0.15,0.1)

> sum(prob)

[1] 1

As $\sum p(x) = 1$,

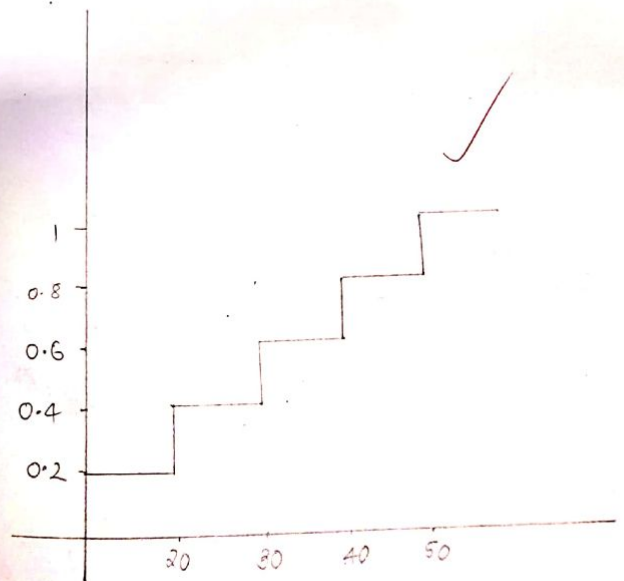
it is a p.m.f

> cumsum(prob)

[1] 0.20 0.40 0.75 0.90 1.00

> x=c(10,20,30,40,50)

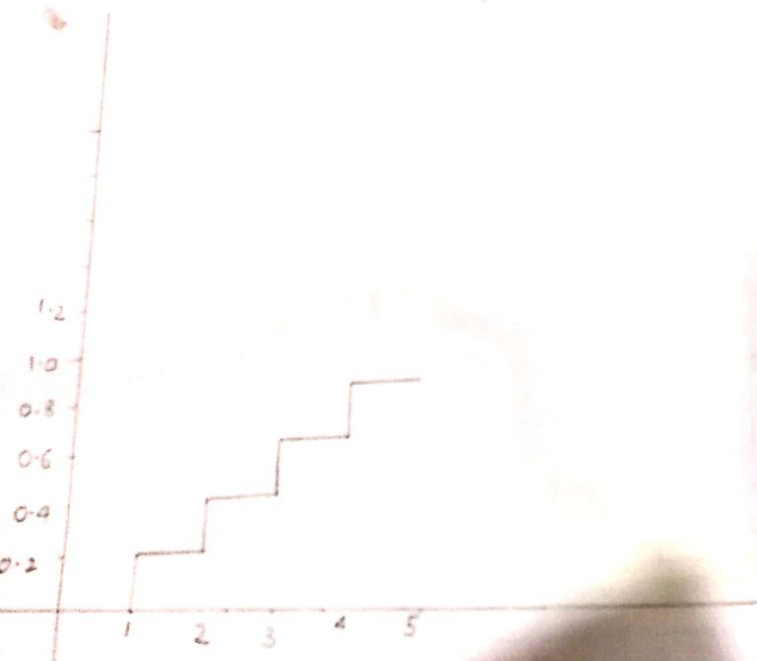
> plot(x,cumsum(prob),"s")




```

> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)
> sum(prob)
[1] 1
> cumsum(prob)
[1] 0.15 0.40 0.50 0.70 0.90 1.00
> x = c(1, 2, 3, 4, 5, 6)
> plot(x, cumsum(prob), "s")

```



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x	1	2	3	4	5	6
$p(x)$	0.15	0.25	0.1	0.2	0.2	0.1
$F(x) = 0$						
	0.15					
	0.40					
	0.50					
	0.70					
	0.90					
	1.00					

$x < 1$
$1 \leq x < 2$
$2 \leq x < 3$
$3 \leq x < 4$
$4 \leq x < 5$
$5 \leq x < 6$
$x \geq 6$

Q.3) check whether the following is p.d.f or not.

(i) $f(x) = 3 - 2x$; $0 \leq x \leq 1$

$$= \int_0^1 f(x) dx$$

$$= \int_0^1 (3 - 2x) dx$$

$$= \int_0^1 3 dx - \int_0^1 2x dx$$

$$= [3x - x^2]_0^1$$

$$= 2.$$

(ii) $f(x) = 3x^2$ $0 < x < 1$

$$= \int_0^1 f(x) dx$$

$$= \int_0^1 3x^2$$

$$= \left[\frac{3x^3}{3} \right]_0^1$$

$$= x^3$$

$$= 1$$

$$\textcircled{1} \\ > \text{dbinom}(10, 100, 0.1) \\ [1] 0.1318653$$

$$\textcircled{2} \\ \text{i)} > \text{dbinom}(4, 12, 1/5) \\ [1] 0.1328756$$

$$\text{ii)} \\ > \text{pbinom}(4, 12, 1/5) \\ [1] 0.9274445$$

$$\text{iii)} \\ > 1 - \text{pbinom}(5, 12, 1/5) \\ [1] 0.01940528$$

$$\textcircled{3} \\ > \text{dbinom}(0:5, 5, 0.1) \\ [1] 0.59049 \quad 0.32805 \quad 0.07290 \quad 0.00810 \quad 0.00045 \quad 0.00001$$

$$\textcircled{4} \\ \text{i)} > \text{dbinom}(5, 12, 0.25) \\ [1] 0.1032414$$

$$\text{ii)} \\ > \text{pbinom}(5, 12, 0.25) \\ [1] 0.9455978$$

$$\text{iii)} \\ > 1 - \text{pbinom}(7, 12, 0.25) \\ [1] 0.00278151$$

$$\text{iv)} > \text{dbinom}(6, 12, 0.25) \\ [1] 0.04014995$$

Practical no. 2.

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Binomial distribution

1. Find the probability of 10 success in 100 trials with $p=0.1$
2. Suppose there are 12 MCQ's, each question has 5 options out of which 1 is correct, find the probability of having exactly 4 correct answers.
3. almost 4 correct answers
4. More than 5 correct answers.

3. Find the complete distribution when $n=5$ and $p=0.1$

$$n=12 \\ p=0.25$$

Find the following probabilities

1. $p(X=5)$
2. $p(X \leq 5)$
3. $p(X > 7)$
4. $p(5 < X < 7)$

- ⑤ The probability of a salesman making a sell to a customer is 0.15.
Find the probability of
- No sells out of 10 customer.
 - More than 3 sells out of 20 customers.
- ⑥ A salesman has a 20% probability of making a sale to a customer. out of 30 customers what minimum number of sales he can make with 88% probability.
- ⑦ X follows binomial distribution
 $n = 10$
 $p = 0.3$
 plot the graph of p.m.f and C.b.f.

⑤ `> dbinom(0, 10, 0.15)`
`[1] 0.1968744`

⑥ `> 1 - pbinom(3, 20, 0.15)`
`[1] 0.3522748`

⑦ `> qbinom(0.88, 30, 0.2)`
`> 6`

⑦ `> prob = dbinom(0:n, 10, 0.3)`
`> cumprob = pbinom(0:n, 10, 0.3)`
`> d = data.frame("x values" = x, "probability" = prob)`
`> print(d)`

	x values	probability
1	0	0.0282
2	1	0.1210
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0370
8	7	0.009
9	8	0.001
10	9	0.0001
11	10	0.00005


```
> p3 = 1 - pnorm(10, 10, 2)
> p3
[1] 0.2824925
```

```
> rnorm(5, 12, 5)
[1] 8.25718 13.798805 11.058683 15.467502 13.781833
```

2. X follows normal distribution with $\mu = 10$, $\sigma = 2$.
Find:

- (i) $P(X \leq 7)$
- (ii) $P(5 \leq X < 12)$
- (iii) $P(X > 12)$
- (iv) generate 10 observation
- (v) Find K such that probability $P(X < K) = 0.4$

```
> pnorm(7, 10, 2)
[1] 0.0668072
```

```
> pnorm(12, 10, 2) - pnorm(5, 10, 2)
[1] 0.5351351
```

```
> 1 - pnorm(13, 10, 2)
[1] 0.1586553
```

```
> rnorm(10, 10, 2)
[1] 10.806022 11.238265 8.444346 8.047978 6.380050
13.063895 11.512423 11.553602 13.010855 11.221799
```

```
> qnorm(0.4, 10, 2)
[1] 9.493306
```

3. Generate 5 random numbers from normal distribution with $\mu = 15$, $\sigma = 4$. Find Sample mean, median, S.D and print it.
4. X follows normal i.e. $X \sim N(30, 100)$
 $\mu = 30$, $\sigma = 10$. Find.

- i) $P(X \leq 40)$
- ii) $P(X > 35)$
- iii) $P(25 < X < 35)$
- iv) Find K such that $P(X < K) = 0.6$

@ code:-

```
> pnorm(40, 30, 10)
[1] 0.8413447
```

```
> 1 - pnorm(35, 30, 10)
[1] 0.3085375
```

```
> pnorm(35, 30, 10) - pnorm(25, 30, 10)
[1] 0.3929249
```

```
> qnorm(0.6, 30, 10)
[1] 32.53347
```

③ Code:-

```
> x = rnorm(5, 15, 4)
> x
[1] 14.29548 16.93377 14.20567 19.73212 11.87906
```

```
> am = mean(x)
> am
[1] 15.30922
```

```
> me = median(x)
> me
[1] 14.29548
```

```
> n = 5
> variance = (n-1) * var(x)/n
> variance
[1] 6.967641
```

```
> sd = sqrt(variance)
> sd
```

```
[1] 2.639629
```

```
> cat("Sample mean is", am)
Sample mean is 15.30922
```

```
> cat("Sample median is", me)
Sample median is 14.29548
```

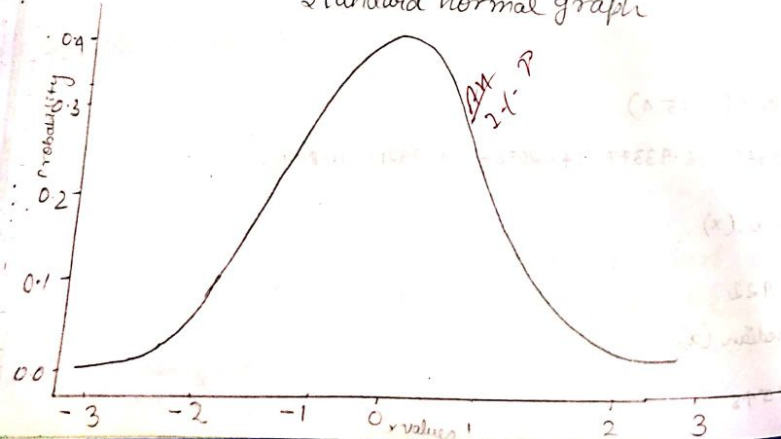
```
> cat("Sample S.D.", sd)
Sample S.D. = 2.639629
```

5. Plot standard normal graph.

```
> x = seq(-3, 3, by = 0.1)
> y = dnorm(x)
```

```
> plot(x, y, xlab = "x values", ylab = "probability", main = "Standard normal graph")
```

Standard normal graph



Normal and t-test:

Test the hypothesis $H_0: \mu = 15$ against $H_1: \mu \neq 15$.
Random sample of size 400 is drawn and it is calculate.
Sample mean is 14 and standard deviation is 3. test
the hypothesis at 5% level of significance.

```
> m0 = 15
```

```
> mx = 14
```

```
> sd = 3
```

```
> n = 400
```

```
> zcal = (mx - m0) / (sd / sqrt(n))
```

```
> zcal
```

```
> [1] -6.666667
```

```
> cat("calculated value of z is", zcal)
```

```
> calculated value of z is -6.666667
```

```
> pvalue = 2 * (1 - pnorm(abs(zcal)))
```

```
> pvalue
```

```
> [1] 2.616796e-11
```

Since pvalue is ~~more~~ less than 0.05,

\therefore we accept the value of $H_0: \mu = 15$ and
reject the value of $H_1: \mu \neq 15$.

Q2. Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$. Random sample of size 400 is drawn with sample mean 10.2 and standard deviation 2.25. Test the hypothesis at 5% level of significance.

```
> m0 = 10
> mx = 10.2
> sd = 2.25
> n = 400
> zcal = (m0 - mx) / (sd / sqrt(n))
> zcal =
[1] -1.777778
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.07544036
```

Since the pvalue is more than 0.05, we accept the value of $H_0: \mu = 10$.

Q3. Test the hypothesis $H_0: \mu$ proportion of smokers in a college is 0.2. A sample is collected and is calculated sample proportion = 0.125. Test the hypothesis at 5% level of significance. Sample size is 400.

```
> P = 0.2
> p = 0.125
> n = 400
> q = 1 - P
> zcal = (p - P) / (sqrt(P * q / n))
> zcal
[1] -3.75
```

```
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.0001768396
```

Since the pvalue is less than 0.05, we do not accept the value.

Q4. Last year the farmers lost 20% of their crops, a random sample of 60 fields are collected and found that 9 fields crops are insect polluted. Test the hypothesis at 1% level of significance.

```
> P = 0.2
> p = 9/60
> n = 60
> q = 1 - P
> zcal = (p - P) / (sqrt(P * q / n))
> zcal
[1] -0.9682458
```

```
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.3329216
```

Since the pvalue is more than 0.01, we accept the value.

Q5. Test the hypothesis $H_0: \mu = 12.5$, from the following sample at 5% level of significance.

```
> mx = mean(x)
> variance = (n-1) * var(x) / n
> sd = sqrt(variance)
> m0 = 12.5
> t = (mx - m0) / (sd / (sqrt(n)))
> pvalue = 2 * (1 - pnorm(abs(t)))
> pvalue
[1] 0
```

Since the pvalue is less than 0.05, we do not accept the value.

Practical no. 6.

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Large Sample test.

- ① Let the population mean (the amount spent per customer in a restaurant) is 250 a sample of 100 customers selected the sample mean is calculated as 275 and S.D. 30, test the hypothesis that population mean is 250 or not at 5% level of significance.
- ② In a random sample of 1000 students it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

$H_0: \mu = 275$ against $H_1: \mu \neq 275$

> mx = 275

> mo = 250

> sd = 30

> n = 100

> zcal = (mx - mo) / (sd / sqrt(n))

> zcal

[1] 8.3333

> pvalue = 2 * (1 - pnorm(zcal))

> pvalue

[1] 0

pvalue = 0 < 0.05

we reject H_0 at 5% level of significance.

2. $P = 0.8$
 $Q = 1 - P$
 $p = 750/1000$
 $n = 1000$
 $Z_{cal} = (p - P) / \sqrt{P \cdot Q / n}$
 $[Z] = 3.952847$
 $p\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(Z_{cal})))$
 $7.722682e-05$
 $p\text{-value} = 7.722682e-05 < 0.01$
 we do not accept it.

③ Two random sample of size 1000 and 2000 are drawn from 2 population with the same standard deviation^{2.5}. The sample means are 67.5 and 68 respectively. Test the hypothesis $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$ at 5% level of significance.

④ A study of noise level in 2 hospital is given below. Test the claim that the two hospitals are same level of noise at 1% level of significance.

	Hospital A	Hospital B
Size	84	34
Mean	61.2	59.4
S.D	7.9	7.5

⑤ In a sample of 600 students in a college 400 use blue ink in another college from a sample of 900 students 450 use blue ink test the hypothesis that the proportion of students using blue ink in two colleges are equal or not. at 1% level of significance.

3. $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$

$n_1 = 1000$
 $n_2 = 2000$
 $m_{x1} = 67.5$
 $m_{x2} = 68$
 $sd_1 = 2.5$
 $sd_2 = 2.5$
 $Z_{cal} = (m_{x1} - m_{x2}) / \sqrt{(sd_1^2 / n_1) + (sd_2^2 / n_2)}$
 Z_{cal}
 $[Z] = 5.163978$
 $p\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(Z_{cal})))$
 $p\text{-value}$
 $[Z] = 2.417564e-07$
 $p\text{-value} = 2.417564e-07 < 0.05$
 we reject it.

```

4.
> n1 = 84
> n2 = 34
> m1 = 61.2
> m2 = 59.4
> sd1 = 7.9
> sd2 = 7.5
> zcal = (m1 - m2) / sqrt((sd1^2/n1) + (sd2^2/n2))
> zcal
[1] 1.162528
> pval = (2 * (1 - pnorm(abs(zcal))))
> pval
[1] 0.2450211
pval = 0.2450211 > 0.1
we accept H0

```

5. $H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

```

> n1 = 600
> n2 = 900
> p1 = 400/600
> p2 = 450/900
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> q = 1 - p
> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
> zcal
[1] 0.01322646 3.51534
> pval = (2 * (1 - pnorm(abs(zcal))))
> pval
[1] 1.753222e-10
pval = 1.753222e-10 < 0.1
we do not accept H0

```

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for sample size
 $n_1 = 200, n_2 = 200$
 $p_1 = 44/200$
 $p_2 = 30/200$
 test at 5% level of significance.

$H_0: P_1 = P_2$ vs. $H_1: P_1 \neq P_2$

```

> n1 = 200
> n2 = 200
> p1 = 44/200
> p2 = 30/200
> zcal = (p1 - p2) / sqrt((p + q) * (1/n1 + 1/n2))
> zcal
[1] 1.412613
> pval = (2 * (1 - pnorm(abs(zcal))))
> pval
[1] 0.1577696
pval = 0.1577696 < 0.5
we reject H0

```

Ans
 23.1.20

Practical no. 7.

Small sample test.

- The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from population that the sample with average 66.

$H_0: \mu = 66$

$x = c(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)$

$t\text{-test}(x)$

one sample t-test

data: x

$t = 68.319$, $df = 9$, $p\text{-value} = 1.558 \times 10^{-13}$

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

65.65171 70.14829

Sample estimates:

mean of x

67.9

As $1.558 \times 10^{-13} < 0.05$, we reject it.

$p\text{-value} = 1.558 \times 10^{-13}$

$\text{if } (p\text{-value} > 0.05) \{ \text{cat}("accept H_0") \} \text{ else } \{ \text{cat}("reject H_0") \}$

Reject H_0

- Two groups of students scored the following marks. Test the hypothesis that there is no significant difference between the two groups.

Group 1 - 18, 22, 21, 17, 20, 17, 23, 20, 22, 21.

Group 2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H_0 - there is no difference between the two groups.

$x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$

$y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

$t\text{-test}(x, y)$

welch Two sample t-test

data: x and y

$t = 2.2573$, $df = 16.376$, $p\text{-value} = 0.03798$

alternative hypothesis: true difference in mean is not equal to 0.

95 percent confidence interval:

0.1605205 5.0371795

Sample estimates:

mean of x mean of y

20.1 17.5

$p\text{-value} = 0.03798$

$\text{if } (p\text{-value} > 0.05) \{ \text{cat}("accept H_0") \} \text{ else } \{ \text{cat}("reject H_0") \}$

reject H_0

3. The sales data of 6 shops before and after a special campaign given below
 before - 53, 28, 31, 48, 50, 42
 After - 58, 29, 30, 55, 56, 45
 Test the hypothesis that the campaign is effective or not.
 H_0 there is no significant difference of sales before and after the campaign.

> x = c(53, 28, 31, 48, 50, 42)
 > y = c(58, 29, 30, 55, 56, 45)
 > t.test(x, y, paired = T, alternative = "greater")
 Paired t-test

data: x and y

t = -2.7815, df = 5, p-value = 0.9806

alternative hypothesis: true difference in means is greater than 0.

95 percent confidence interval:

-6.035547 Inf

Sample estimates:

mean of the differences
 -3.5

> pvalue = 0.9806

> if (pvalue > 0.05) {cat("accept H_0 ")} else {cat("reject H_0 ")}
 accept H_0 .

4. Two medicines are applied to two groups of patients respectively.

Grp1 - 10, 12, 13, 11, 14

Grp2 - 8, 9, 12, 14, 15, 10, 9

Is there any significant difference between the two elements.

5. The following are the weight before and after a diet program. Is the diet program effective.

Before - 120, 125, 115, 130, 123, 119

After - 100, 114, 95, 90, 115, 99.

> x = c(10, 12, 13, 11, 14)

> y = c(8, 9, 12, 14, 15, 10, 9)

> t.test(x, y)

> pvalue = 0.4406

> if (pvalue > 0.05) {cat("accept H_0 ")} else {cat("reject H_0 ")}
 accept H_0

5. H_0 there is no significant differences between before and after.

> x = c(120, 125, 115, 130, 123, 119)

> y = c(100, 114, 95, 90, 115, 99)

> t.test(x, y, paired = T, alternative = "less")

> pvalue = 0.9963

> if (pvalue > 0.05) {cat("accept H_0 ")} else {cat("reject H_0 ")}
 accept H_0

AM
 6-2-20

Large and small sample test:

Q1. $H_0: \mu = 55, H_1: \mu \neq 55$

```
> n = 100
> mx = 52
> mo = 55
> sd = 7
> zcal = (mx - mo) / (sd / sqrt(n))
> zcal
> -4.285714
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.00003053
```

As $pvalue < 0.05$ we reject.

Q2. $H_0: P = 0.5, H_1: P \neq 0.5$

```
> P = 0.5
> p = 350 / 700
> n = 700
> q = 1 - P
> zcal = ((p - P) / sqrt(P * q / n))
> zcal
[1] 0
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 1
```

As $pvalue > 0.01$, we accept.

Q3. $H_0: p_1 = p_2, H_1: p_1 \neq p_2$

```
> n1 = 1000
> n2 = 1500
> p1 = 0.02
> p2 = 0.01
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> q = 1 - p
> zcal = ((p1 - p2) / sqrt(p * q * (1/n1 + 1/n2)))
> zcal
[1] 2.084842
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.03708364
As  $pvalue < 0.05$ , we reject.

```

Q4. $H_0: \mu = 99, H_1: \mu \neq 99$

```
> mx = 100
> mo = 99
> n = 400
> var = 64
> sd = sqrt(var)
> zcal = (mx - mo) / (sd / sqrt(n))
> zcal
[1] 2.5
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.01241933
```

Q5: $H_0: \mu = 66$

> x = c(63, 63, 68, 69, 71, 71, 72)

> t.test(x)

One sample t-test

data: x

t = 47.94, df = 6, p-value = 5.522e-09

alternative hypothesis: true mean is not equal to 0.

95 percent confidence interval:

64.66679 71.62092

Sample estimates:

mean of x

68.14286

As p-value < 0.01 we reject.

Q7: $H_0: \mu = 1200$, $H_1: \mu \neq 1200$

> n = 100

> mx = 1150

> mo = 1200

> sd = 125

> zcal = (mx - mo) / (sd / sqrt(n))

> zcal

[1] -4

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 6.334148e-05

As p-value < 0.01, we reject.

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$H_0: \sigma_1 = \sigma_2$, $H_1: \sigma_1 \neq \sigma_2$

> x = c(66, 67, 75, 76, 82, 88, 84, 90, 92)

> y = c(64, 66, 74, 78, 82, 85, 87, 92, 95, 93, 97)

> var.test(x, y)

F test to compare two variance

data: x and y

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6359.

alternative hypothesis: true ratio of variance is not equal to 1

95 percent confidence interval:

0.1833662 3.0360393

Sample estimates:

ratio of variances

0.7068567

As p-value > 0.05, we accept.

Q8: $H_0: p_1 = p_2$, $H_1: p_1 \neq p_2$

> n1 = 200

> n2 = 300

> p1 = 44/200

> p2 = 56/300

> p = (n1 * p1 + n2 * p2) / (n1 + n2)

> q = 1 - p

> zcal = ((p1 - p2) / (sqrt(p * q) * (1/n1 + 1/n2)))

> zcal

[1] 0.9128709

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.3613104 > 0.01, we accept.

Topic: Chi square test and ANOVA

- ① use the following data to test whether the condition of the home and the condition of child are independent or not.

clean	Dirty	clean	} condition of child.
70	50	Fairly clean	
80	20	Dirty	
35	45		

Solⁿ:

H_0 : Condition of home and child are independent

$H_0 \neq$

$x = \text{scan}(70, 80, 35, 60, 20, 45)$

$m = 3$

$n = 2$

$y = \text{matrix}(x, \text{nrow} = m, \text{ncol} = n)$

$\text{chisq.test}(y)$

Pearson's Chi-Squared test

data = y

$\chi^2\text{-squared} = 25.646$, $df = 2$, $p\text{-value} = 2.698 \times 10^{-6}$

Ans Since $p\text{-value} < 0.01$, we don't accept H_0 .

- ② Test H_0 that vaccination and disease are independent or not.

vaccine

All	Not all	
70	46	All
35	37	Not all

} Disease.

H_0 : vacc and disease are independent

$x = c(70, 35, 46, 37)$

$m = 2$

$n = 2$

$y = \text{matrix}(x, \text{nrow} = m, \text{ncol} = n)$

$\text{chisq.test}(y)$

Pearson's chi sq with yate's cont. corr.

data = y

$\chi^2_{sq} = 2.0275$, $df = 1$, $p\text{-value} = 0.1545$

Since > 0.01 , we accept H_0 .

Perform a ANOVA for the following data

Type	Observations
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

Solⁿ:

H₀: Means are equal for A, B, C, D

$\gamma_{x1} = c(50, 52)$

$\gamma_{x2} = c(53, 55, 53)$

$\gamma_{x3} = c(60, 58, 57, 56)$

$\gamma_{x4} = c(52, 54, 54, 55)$

$\gamma_d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$

$\gamma_{names(b)}$

γ_d

values	ind
1 50	b ₁
2 52	b ₁
3 53	b ₂
4 55	b ₂
5 53	b ₂
6 60	b ₃
7 58	b ₃
8 57	b ₃
9 56	b ₃
10 52	b ₄
11 54	b ₄
12 54	b ₄
13 55	b ₄


```

> names(d)
[1] "values" "ind"
> oneway.test(values ~ ind, data=d, var.equal=T)
One way analysis of means
data: values and ind
F = 11.735, num df = 3, denom df = 9, p-value = 0.00183
> anova = aov(values ~ ind, data=d)
> summary(anova)

```

	DF	Sum Sq	Mean Sq	F value	Pr(>F)
ind	3	71.06	23.688	11.73	0.0018344
Residuals	9	18.17	2.019		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

④ Following gives the life of a tyres of 4 brands.

Type	life
A	20, 23, 18, 17, 22, 24
B	23, 19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 15

H_0 : The avg. life of A, B, C, D are equal.

$x_1 = (20, 23, 18, 22, 24)$

$x_2 = (19, 15, 17, 20, 16, 17)$

$x_3 = (21, 19, 22, 17, 20)$

$x_4 = (15, 14, 16, 18, 14, 15)$

$d = \text{stack}(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4))$

```

> names(d)
> oneway.test(values ~ ind, data=d, var.equal=T)
One way analysis of means

```

data: values and ind

F = 7.4403, num df = 3, denom df = 19, p-value = 0.001719

```

⑤
> x = read.csv("/users/ritesh/Desktop/marks.csv")
> print(x)

```

	Statistics	marks
1	40	60
2	45	48
3	42	47
4	15	20
5	37	25
6	36	27
7	45	57
8	59	58
9	20	25
10	27	27

```

> am = mean(x$Statistics)

```

```

> am
[1] 36.6

```

```

> mean(x$marks)

```

```

[1] 39.4

```

```

> n = length(x$Statistics)

```

```

> n
[1] 10

```

```

> sqrt((n-1) * var(x$Statistics)/n)

```

```

[1] 12.32334

```

```

> sqrt((n-1) * var(x$marks)/n)

```

```

[1] 15.2

```

```

> cor(x$Statistics, x$marks)

```

```

[1] 0.8150581

```

AM
20.17.20

Topic: Non-parametric test.

Following are the amounts of sulphur oxide emitted by some industry in twenty days apply sign test to test hypothesis that the population median is 21.5 at 5% level of significance.
17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 25, 29, 25.

H_0 : population median is 21.5 against H_1 : population median ~~less than~~ ^{less than} ~~greater than~~ ^{greater than} 21.5

> x = c (.)

> me = 21.5

> sp = length (x [x > me])

> sn = length (x [x < me])

> n = sp + sn

> n

[1] 20

> pv = pbinom (sp, n, 0.5)

> pv

[1] 0.4119015

As p-value i.e. 0.4119015 > 0.05, we accept.

If the alternative H_1 is $me \neq$ or $me <$ then $pv = pbinom(sp, n, 0.5)$
and if $me >$ then $pv = pbinom(sn, n, 0.5)$

As $pv \times 0.05$, we accept.

Q2. Following is a data of 10 observations. Apply sign test.
 H₀: the hypothesis that the population median is 625
 against the alternative it is more than 625.
 612, 619, 631, 628, 643, 640, 655, 649, 670, 662
 H₀: population median is 625 against H₁: population $\mu > 625$

```
> x = c(612, 619, 631, 628, 643, 640, 655, 649, 670, 662)
> mc = 625
> Sp = length(x[x > mc])
> Sn = length(x[x < mc])
> n = Sp + Sn
> n
[1] 10
> pv = pbinom(Sn, n, 0.5)
> pv
[1] 0.0546875
As pv > 0.05 we accept.
```

Q3. The following are the values of a sample. Test the hypothesis that the population median is 60 against the alternative it is more than 60 at 5% LOS, using Wilcoxon signed Rank test.

63, 65, 60, 89, 61, 71, 58, 54, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 27, 69.

H₀: population median is 60 against H₁: population $\mu > 60$

```
> x = c(63, 65, 60, 89, 61, 71, 58, 54, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 27, 69)
> length(x)
[1] 20
```

> wilcox.test(x, alternative="greater", mu=60)

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Wilcoxon signed rank test with continuity correction

data: x
 V = 145, p-value = 0.02298
 As p-value < 0.05 we reject.

Note: If the alternative is less than alternative "less" and if the alternative is not + then alternative "two.sided"

Q4. Using WSR, test the population median is 12 or less than 12.
 15, 17, 24, 25, 20, 21, 32, 23, 12, 25, 24, 26
 H₀: population median is 12 against H₁: population $\mu < 12$

```
> x = c(15, 17, 24, 25, 20, 21, 32, 23, 12, 25, 24, 26)
> wilcox.test(x, alternative="less", mu=12)
```

Wilcoxon signed rank test with continuity correction:

data: x
 V = 66, p-value = 0.9926
 As p-value > 0.05, we accept.

Q5. The weights of students before and after they stopped smoking are given below. Using WSR, test that there is no significant change.

weights before	weights after
65	72
75	74
75	72
62	66
72	73

H_0 : before and after there is no change against

H_1 : there is change in their weight.

> $x = c(65, 75, 75, 62, 72)$

> $y = c(72, 74, 72, 66, 73)$

> $d = x - y$

> $wilcox.test(d, alter = "two.sided", mu = 0)$

$wilcox.test$ signed rank test with continuity correction

data: d

$V = 4.5$, p-value = 0.4982.

As p-value > 0.05 , we accept.

AM
27.02