

Topic :- Basics of R software.

- R is a software for statistical analysis and data computing.
- It is an effective data handing software and outcome storage is possible.
- It is capable of graphical display.
- It is a free software.

Q1) Solve the following:-

$$1) 4 + 6 + 8 \div 2 - 5$$

$$2) 2^2 + | -3 | + \sqrt{15}$$

$$3) 5^3 + 7 \times 5 \times 8 + 46 / 5$$

$$4) \sqrt{4^2 + 5 \times 3 + 7 / 6}$$

$$5) \text{round of } 46 \div 7 + 9 \times 8$$

180

$$> 4t + 8/2 - 5$$

{1} 9

$$> 2^2 + \text{abs}(-3) + \sqrt{45}$$

{1} 13.7082

$$> 5^3 + 7 * 5 * 8 + 4615$$

{1} 414.2

$$> \sqrt{4^2 + 5^3 + 7^6}$$

{1} 5.67

$$> \text{round}(4617 + 9^8)$$

{1} 79.

6) $c(1, 6, 2, 3)^* c(-2, -3, -4, -1)$

$$> c(1, 6, 2, 3)^* c(-2, -3, -4, -1)$$

{1} - -2 - 18 - 8

7) $c(2, 3, 5, 7)^2$

$$> c(2, 3, 5, 7)^2$$

{1} 4 9 25 49.

8) $c(4, 6, 8, 9, 4, 5) ^ c(1, 2, 3)$

$$> c(4, 6, 8, 9, 4, 5) ^ c(1, 2, 3)$$

{1} 4 36 512 9 16

125

9) $c(6, 2, 7, 5) / c(4, 5)$

$$> c(6, 2, 7, 5) / c(4, 5)$$

{1} 1.5 0.4 1.75 1

10) $x=20, y=30, z=2$.

find i) $x^2 + y^3 + z$

ii) $\sqrt{x^2 + y^2}$, iii) $x^2 + y^2$.

032

> $x = 20$

> $y = 30$

> $z = 2$

> $x^2 + y^3 + z$

[1] 29402

> $\sqrt{x^2 + y^2}$

[1] 20.73

> $x^2 + y^2$

[1] 1300

11) $x = \text{matrix}(\text{nrow}=4, \text{ncol}=2, \text{data}=\{(1, 2, 3, 4, 5, 6, 7, 8)\})$

> x

	{, 1}	{, 2}
[1,]	1	5
[2,]	2	6
[3,]	3	7
[4,]	4	8

12) find $x+y$ and $2x+3y$ where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$, $y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$

> $x = \text{matrix}(\text{nrow}=3, \text{ncol}=3, \text{data}=\{4, 7, 9, -2, 0, -5, 6, 7, 3\})$

> $y = \text{matrix}(\text{nrow}=3, \text{ncol}=3, \text{data}=\{10, 12, 15, -5, -4, -6, 7, 9, 5\})$

> $x+y$

	{, 1}	{, 2}	{, 3}
[1,]	14	-7	13
[2,]	19	-4	6
[3,]	24	-11	8

> $2x + 3y$

	{, 1}	{, 2}	{, 3}
[1,]	38	-19	33
[2,]	50	-12	41
[3,]	60	-28	21

SE0

(3) Marks of stats of CS division batch-A. :- 59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39

> $x = (59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39)$

> breaks = seq(20, 60, 5)

> a = cut(x, breaks, right = FALSE)

> b = table(a)

> c = transform(b)

> c

	a	x	freq
1	[20, 25)		3
2	{25, 30)		2
3	{30, 35)		1
4	{35, 40)		4
5	{40, 45)		1
6	{45, 50)		3
7	{50, 55)		2
8	{55, 60)		4

Ans
28.11

PRACTICAL-02

Aim :- Probability Distribution.

Q1) Check whether the following are pmf or not :-

i)	x	0	1	2	3	4	5
	$P(x)$	0.1	0.2	0.5	0.4	0.3	0.5

Since, $P(2) = -0.5$

Therefore, it cannot be a pmf as in pmf $P(x) \geq 0 \forall x$.

ii)	x	1	2	3	4	5
	$P(x)$	0.2	0.2	0.3	0.2	0.2

$\Rightarrow p_{\text{prob}} = c(0.2, 0.2, 0.3, 0.2, 0.2)$

$\Rightarrow \text{sum}(p_{\text{prob}})$

[1] 1.

It cannot be a pmf as in pmf $\sum P(x) = 1$

iii)	x	10	20	30	40	50
	$P(x)$	0.2	0.2	0.35	0.15	0.1

$\Rightarrow p = c(0.2, 0.2, 0.35, 0.15, 0.1)$

$\Rightarrow \text{sum}(p)$

[1] 1.

$\because \sum P(x) = 1$, it is a pmf and $P(x) \geq 0$

Q2) Find the wf for the following pmf and sketch the graph.

i)	x	10	20	30	40	50
	$p(x)$	0.2	0.2	0.35	0.15	0.1

$$\rightarrow x = \{10, 20, 30, 40, 50\}$$

$$\rightarrow \text{prob} = c(0.2, 0.2, 0.35, 0.15, 0.1)$$

$$\rightarrow \text{sum(prob)}$$

{131}

> cumsum(prob)

$$\rightarrow [1] 0.2 \quad 0.4 \quad 0.75 \quad 0.9 \quad 1.0$$

$$\rightarrow \text{plot}(x, \text{cumsum(prob)}, "s")$$

$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.9 & 40 \leq x < 50 \\ 1.0 & x \geq 50 \end{cases}$$

ii)	x	1	2	3	4	5	6
	$p(x)$	0.15	0.25	0.1	0.2	0.2	0.1

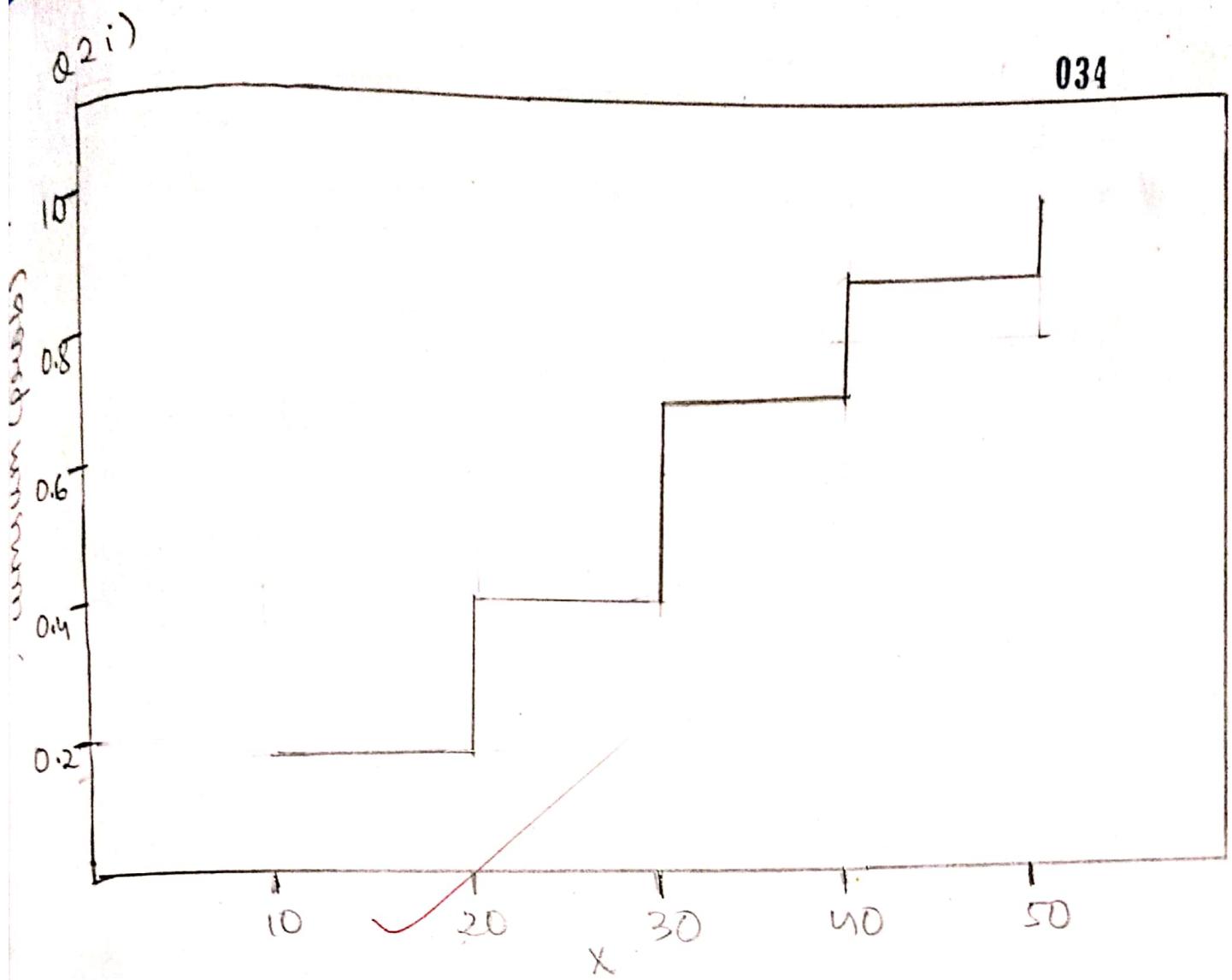
$$\rightarrow \text{prob} = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$$

> cumsum(prob)

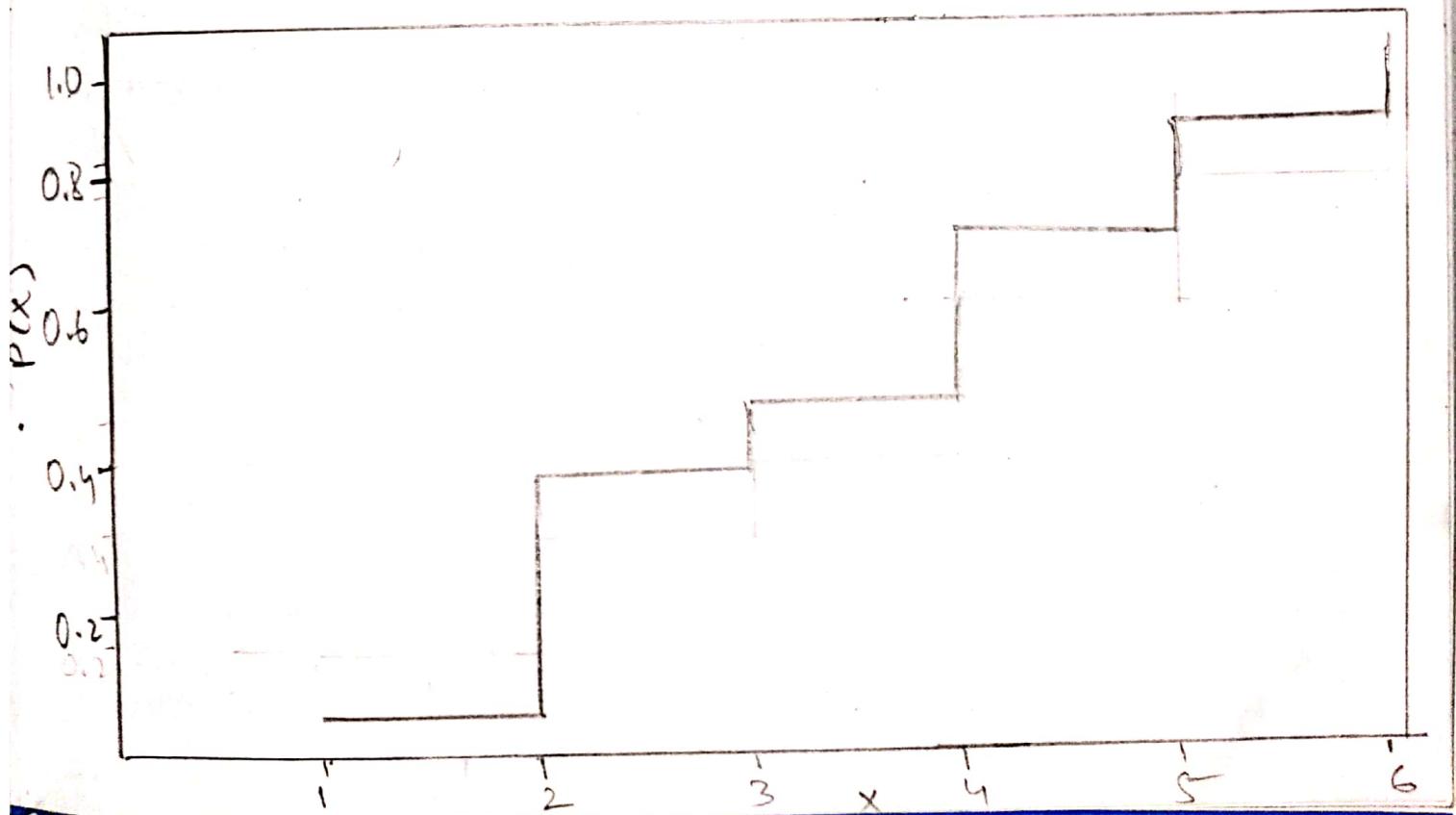
$$\rightarrow [1] 0.15 \quad 0.40 \quad 0.5 \quad 0.7 \quad 0.9 \quad 1.0$$

$$\rightarrow x = 1:6$$

$$F(x) = \begin{cases} 0 & x < 1 \\ 0.15 & 1 \leq x < 2 \\ 0.4 & 2 \leq x < 3 \\ 0.5 & 3 \leq x < 4 \\ 0.7 & 4 \leq x < 5 \\ 0.9 & 5 \leq x < 6 \\ 1.0 & x \geq 6 \end{cases}$$



Q2ii) `> plot(x, cumsum(prab), "s", xlab="x", ylab="P(x)")`



(3) Check whether the following is p.d.f or not:-

$$\text{i)} f(x) = 3 - 2x, \quad 0 \leq x \leq 1$$

$$\Rightarrow \int_0^1 f(x) dx$$

$$= \int_0^1 (3 - 2x) dx$$

$$\therefore \int_0^1 3dx - \int_0^1 2x dx$$

$$= 3[x]_0^1 - 2\left[\frac{x^2}{2}\right]_0^1$$

$$= 3(1-0) - (0-0)$$

$$= 3 - 1 = 2 \neq 1$$

∴ It is not a p.d.f

$$\text{ii)} f(x) = 3x^2 dx, \quad 0 < x < 1$$

$$\Rightarrow \int_0^1 f(x) dx$$

$$= \int_0^1 3x^2 dx \quad \text{Ans} \checkmark$$

$$= 3 \int_0^1 x^2 dx$$

$$= 3 \left[\frac{x^3}{3} \right]_0^1$$

$$= 1 - 0 = 1$$

∴ It is a p.d.f.

19/12/19

2806

PRACTICAL - 3

Aim:- To study binomial distribution

- i) $P(X=x) = \text{dbinom}(x, n, p)$
- ii) $P(X \leq x) = \text{pbinom}(x, n, p)$
- iii) $P(X > x) = 1 - \text{pbinom}(x, n, p)$
- iv) If x is unknown,
 $P_i = P(X \leq x)$ (given)
 $\text{qbinom}(P_i, n, p)$

- Q1) Find the probability of exactly 10 success in 100 trials with $p = P = 0.1$.
- Q2) Suppose there are 12 MCQ. Each question has 5 options out of which 1 is correct. Find the probability of:
i) Exactly 4 correct answers.
ii) Atmost 4 correct answers.
iii) More than 5 correct answers.
- Q3) Find the complete distribution when $n=5$, $p=0.1$.
- Q4) $n=12$, $p=0.25$. Find:-
i) $P(X=5)$, ii) $P(X \leq 5)$, iii) $P(X > 7)$, iv) $P(5 \leq X \leq 7)$

Q1) $\rightarrow \text{dbinom}(10, 100, 0.1)$
 {1} 0.1318653.

Q2) i) $\rightarrow \text{dbinom}(4, 12, 1/5)$
 {1} 0.1328756.

ii) $\rightarrow \text{pbinom}(4, 12, 1/5)$
 {1} 0.9274445.

iii) $\rightarrow 1 - \text{pbinom}(4, 12, 1/5)$
 {1} 0.0725555.

Q3) $\rightarrow \text{dbinom}(0.5, 5, 0.1)$
 {1} 0.59049
 0.32805
 0.07290
 0.00810
 0.00045
 0.00001.

Q4) i) $\rightarrow \text{dbinom}(5, 12, 0.25)$
 {1} 0.1032414.

ii) $\rightarrow \text{pbinom}(5, 12, 0.25)$
 {1} 0.9455978.

iii) $\rightarrow 1 - \text{pbinom}(7, 12, 0.25)$
 {1} 0.00278151.

iv) $\rightarrow \text{dbinom}(6, 12, 0.25)$
 {1} 0.64014945.

Q5)

Probability of salesman making a sale to customer 0.15. find the probability of :-

i) no sells out of 10 customer

ii) more than 3 sells out of 20 customer

Q6) A salesman has a 20% probability of making a sell to a customer. Out of 30 customers, what minimum no. of sells he can make with 88% probability.

Q7) X followed binomial distribution with $n=10$, $p=0.3$. Plot the graph of pmf and cdf.

Q8) Answers:-

i) `>dbinom(0,10,0.15)`

[1] 0.1968744

ii) `1-pbinom(3,20,0.15)`

[1] 0.3522748

Q6) `>abinom(0.88,30,0.2)`

[1] 9.

Q7) `>n=10`

`>p=0.3`

`>x=0:n`

`>prob=dbinom(x,n,p)`

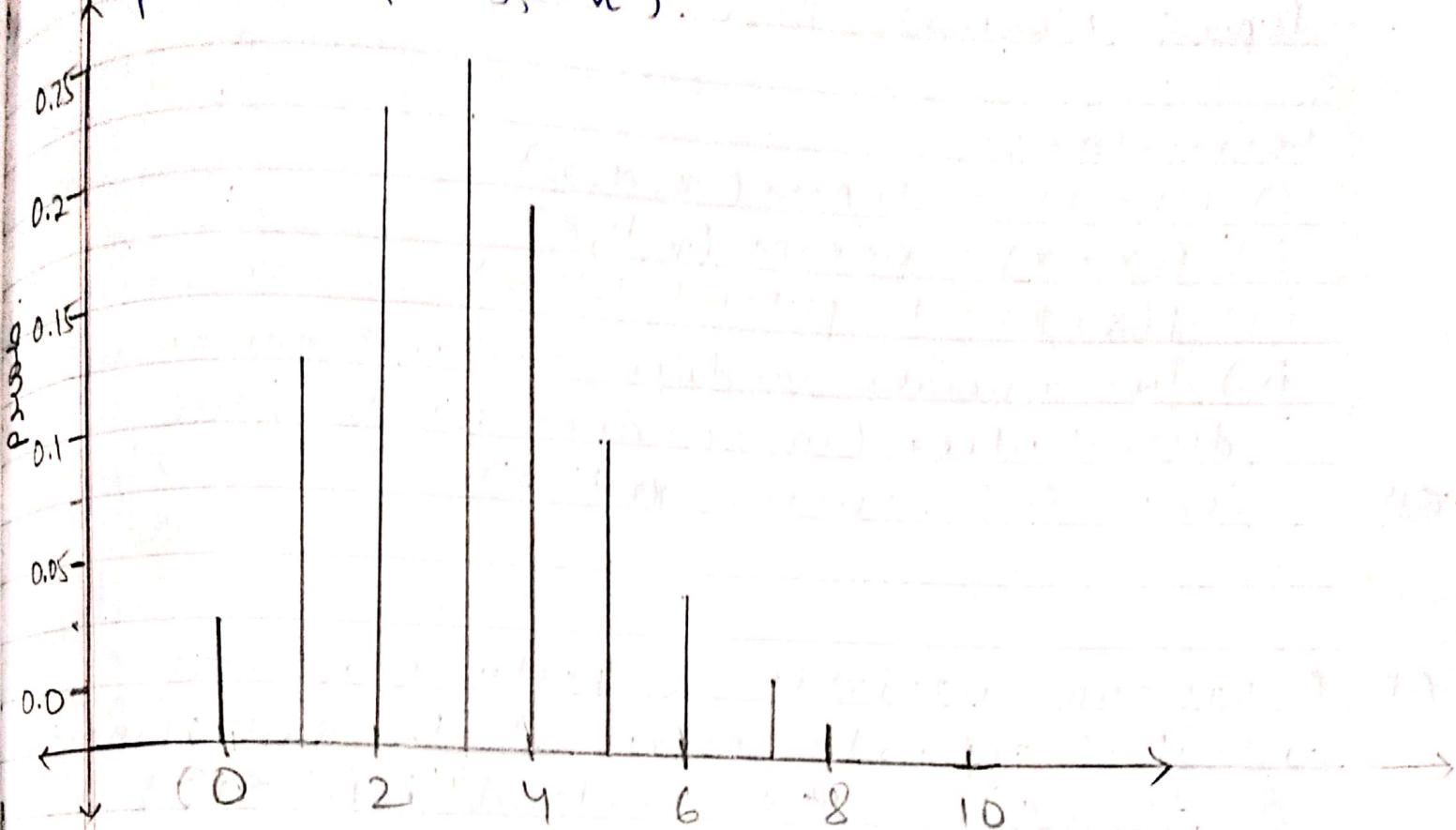
`>cumprob=pbisnom(x,n,p)`

`>d=data.frame("xvalues": x, "probability": prob).`

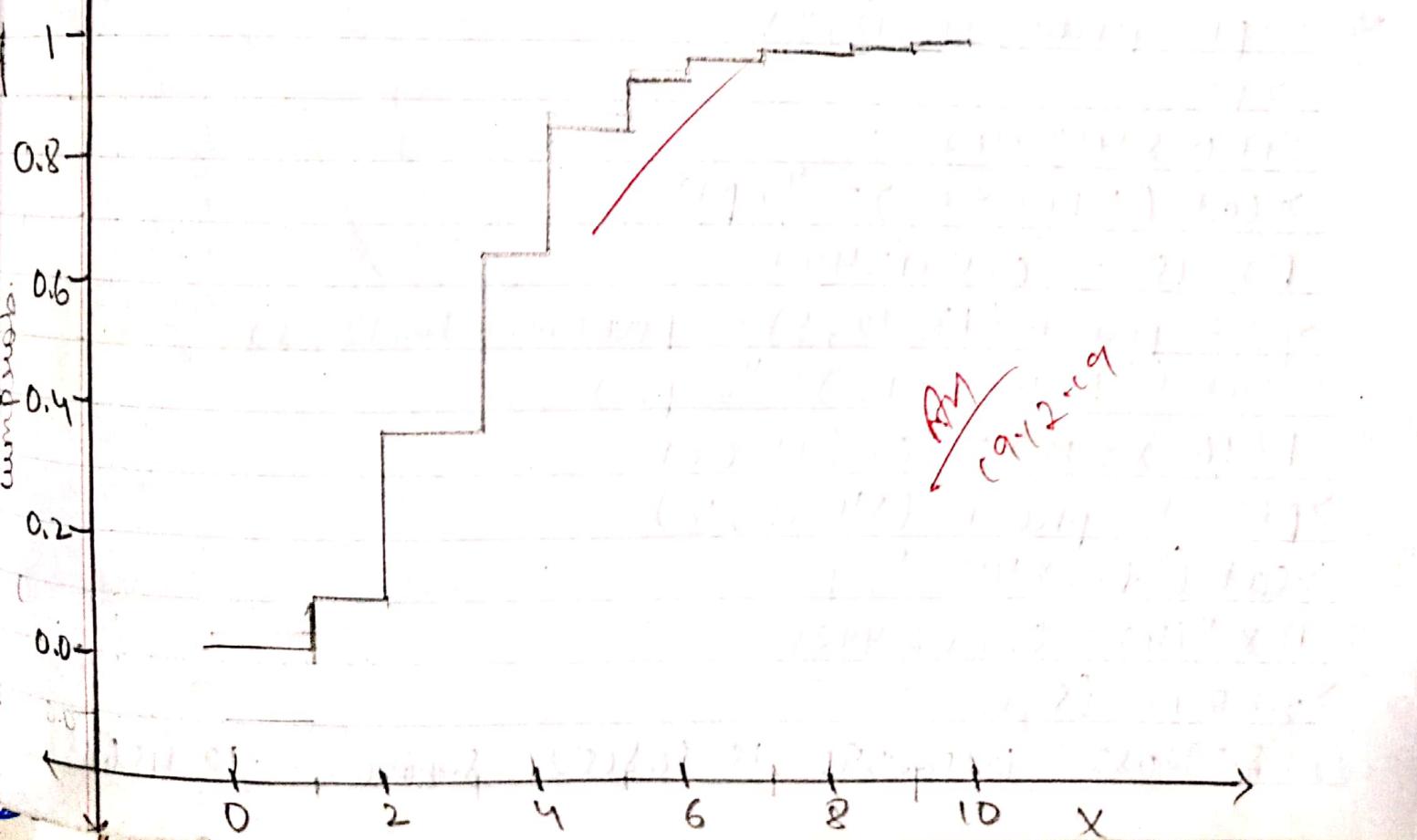
`>print(d)`

xvalues	probability	xvalues	probability
0	0.0282475249	8	0.0090016912
1	0.1210608210	9	0.001446701
2	0.2334744405	10	0.00013778
3	0.2668279320	11	0.000005904
4	0.2001209490		
5	0.1029193452		
6	0.0367569090		

$\rightarrow \text{plot}(u, \text{prob}, "u")$.



$\rightarrow \text{plot}(u, \text{cumprob}, "S")$.



21/11/2020 580

PRACTICAL 4

Topic:- Normal Distribution

Formulas:-

i) $P(x = u) = dnorm(u, \mu, \sigma)$

ii) $P(x \leq u) = pnorm(u, \mu, \sigma)$

iii) $P(x > u) = 1 - pnorm(u, \mu, \sigma)$

iv) To generate random number from normal distribution (in random number), the code is :- $rnorm(n, \mu, \sigma)$

Q1) A random variable x follows normal distribution with mean $= \mu = 12$ and standard deviation $= \sigma = 3$. Find i) $P(x \leq 15)$, ii) $P(10 \leq x \leq 13)$, iii) $P(x > 14)$, iv) generate 5 observations (random numbers).

» $\text{>} p1 = pnorm(15, 12, 3)$

» $\text{>} p1$

[1] 0.8413447

» $\text{>} cat("P(x \leq 15) = ", p1)$

$P(x \leq 15) = 0.8413447$

» $\text{>} p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)$

» $\text{>} cat("P(10 \leq x \leq 13) = ", p2)$

$P(10 \leq x \leq 13) = 0.3780661$

» $\text{>} p3 = 1 - pnorm(14, 12, 3)$

» $\text{>} cat("P(x > 14) = ", p3)$

$P(x > 14) = 0.2524925$

» $\text{>} rnorm(5, 12, 3)$

[1] 8.592085 12.862390 15.568052 8.7696 12.456383

Q2) X follows normal distribution with $\mu = 10$, $\sigma = 2$. Find i) $P(X \leq 7)$, ii) $P(5 < X < 12)$, iii) $P(X > 12)$, iv) generate 10 obs; v) find K such that $P(X < K) = 0.4$

038
 >> pnorm(7, 10, 2)
 [1] 0.0668072
 > pnorm(12, 10, 2) - pnorm(5, 10, 2)
 [1] 0.8351351
 > 1 - pnorm(12, 10, 2)
 [1] 0.1586553
 > rnorm(10, 10, 2)
 [1] 7.91262 8.759731 9.313712 11.896202 10.6757
 10.737545 11.728618 9.526577 12.613503 11.2564
 > qnorm(0.4, 10, 2)
 [1] 9.493306.

Q3) Generate 5 random no.s from normal distribution $\mu = 15$, $\sigma = 4$. Find sample mean, median, standard deviation and print it.
 Q4) X follows normal (μ, σ^2) . Find i) $P(X \leq 40)$, ii) $P(X > 35)$, iii) $P(25 \leq X < 35)$, iv) find K such that $P(X < K) = 0.6$.

Answers:-
 Q3) > rnorm(40, 30, 10)
 [1] 0.8413447
 > 1 - pnorm(35, 30, 10)
 [1] 0.3085375
 > pnorm(35, 30, 10) - pnorm(25, 30, 10)
 [1] 0.3829249
 > qnorm(0.6, 30, 10)
 [1] 32.53347

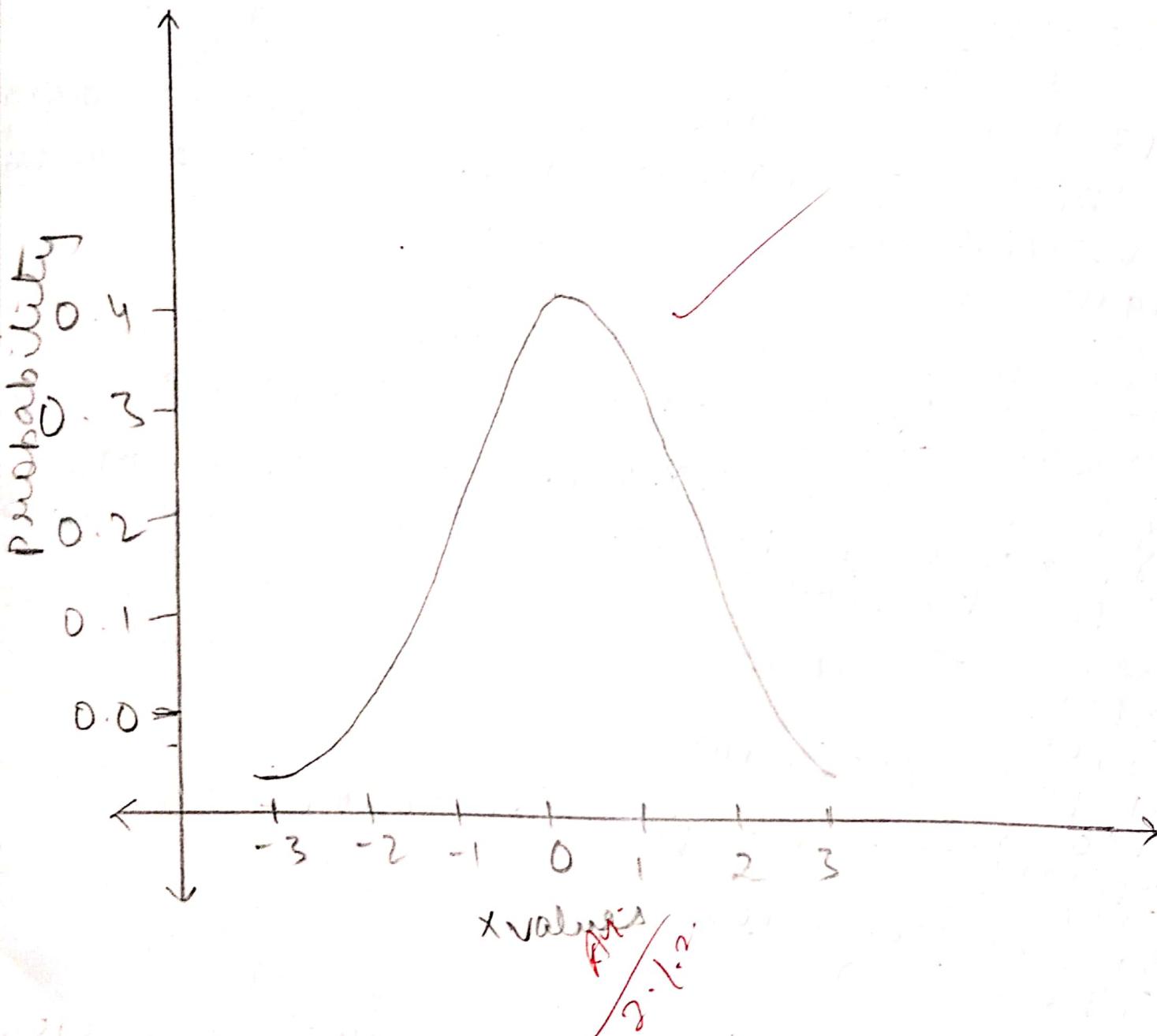
Q4) > rnorm(5, 15, 4)
 [1] 22.32830 12.89411 15.77568 14.22375 23.59594
 > x = rnorm(5, 15, 4)
 > x
 [1] 14.93497 14.65413 12.48667
 > am = mean(x)
 > md = median(x)
 > n = 5
 > variance = (n-1) * var(x) / n
 > sd = sqrt(variance).

	<u>18.29222</u>	<u>18.43272</u>
> cat("Mean = ", am)	Mean = 15.76014	
> cat("Median = ", md)	Median = 14.93497	
> cat("Standard Deviation = ", sd)	Standard Deviation = 2.287965	

Q5) Plot standard normal graph.

```
> x = seq(-3, 3, by = 0.1)
> y = dnorm(x)
> plot(x, y, xlab = "x values", ylab = "Probability",
       main = "standard normal graph")
```

standard Normal Graph



PRACTICAL-5

Aim:- Normal & T-test

(1) Test the hypothesis :-

$$H_0: \mu = 15$$

against

$$H_1: \mu \neq 15.$$

Random sample of size 400 is drawn and it is calculated that the sample mean is 14 and the standard deviation is 3. Test the hypothesis at 5% level of significance

$$> m = 15; ml = 14; sd = 3; n = 400;$$

$$>z_{cal} = (ml - m) / (sd / (\sqrt{n}))$$

$$z_{cal}$$

$$\{1\} z = -6.66667$$

$$>pvalue = 2 * (1 - pnorm(abs(zcal)))$$

$$>pvalue$$

$$\{1\} 2.616796e^{-11}$$

\because The pvalue is less than 0.5, we reject the value $H_0: \mu = 15$

(2) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$. Random sample of size 400 is drawn with sample mean 10.2 and standard deviation 2.25. Test the hypothesis at 5% level of significance.

$$>m = 10; ml = 10.2; sd = 2.25; n = 400;$$

$$>z_{cal} = (ml - m) / (sd / (\sqrt{n}))$$

$$z_{cal}$$

$$\{1\} 1.777778$$

$$>pvalue = 2 * (1 - pnorm(abs(zcal)))$$

$$>pvalue$$

$$\{1\} 0.07$$

Since the pvalue is greater than 0.05, we accept the value $H_0: \mu = 10$.

- 3) Test the hypothesis $H_0: \text{proportion of smokers in a college is } 0.2$. A sample is collected and it is calculated as 0.125. Test the hypothesis at 5% level of significance. (sample size = 400)

$$> P = 0.2; p = 0.125; n = 400; Q = 1 - P$$

$$> z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$$

$$> z_{\text{cal}}$$

$$\{1\} -3.75$$

$$> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> \text{pvalue}$$

$$\{1\} 0.0001768346$$

Since the pvalue is less than 0.05, we reject the value $H_0: \text{proportion of smokers as } 0.2$.

- 4) Last year farmers lost ~~field~~ 20% of their crop. A random sample of 60 fields were collected and it was found that 9 fields crops are insect polluted. Test the hypothesis at 1% level of significance.

$$> P = 0.2; p = 9/60; n = 60; Q = 1 - P$$

$$> z_{\text{cal}} = (p - P) / (\sqrt{P * Q / n})$$

$$> z_{\text{cal}}$$

$$\{1\} -0.96$$

$$> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> \text{pvalue}$$

$$\{1\} 0.33$$

Since the pvalue is greater than 0.01, we accept the value of H_0 .

5) Test the hypotheses $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

> $x = c(12.25, 11.97, 12.15, 11.89, 12.16, 12.04, 12.08, 12.31, 12.28, 11.94,$
> $n = length(x)$

> n

[1] 10

> $mx = mean(x)$

> $var = (n-1) * var(x) / n$

> $sd = sqrt(var)$

> $mo = 12.5$

> $t = (mx - mo) / (sd / sqrt(n))$

> t

[1] -8.89

> ~~pvalue = 2 * (1 - pnorm(abs(t)))~~

> ~~pvalue~~

[1] 0.

Since the p-value is less than 0.05, value is rejected.

~~AM
16/120~~

PRACTICAL-06

Topic:- ^{large} ~~large~~ Sample test.

- (1) Let the population mean (the amount spent by customer in a restaurant) is 250. A sample of 100 customers selected. The sample mean is collected as ²⁷⁵~~250~~ and the standard deviation is 30. Test the hypothesis that the population is 250 at 5% level of significance.

- (2) In a random sample of 1000, it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

$$\text{H}_0: \mu = 250 \text{ against } \text{H}_1: \mu \neq 250$$

$$\sigma_d = 30; m = 250; m_1 = 275; n = 100;$$

$$z_{\text{cal}} = (m_1 - m) / (\sigma_d / \sqrt{n})$$

$$z_{\text{cal}}$$

$$2.7833$$

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$p\text{value}$$

$$0.002$$

\therefore The value is less than 0.05, we reject H_0 at 5% level of significance.

$$(2) \text{H}_0: p = 0.8 \text{ against } \text{H}_1: p \neq 0.8$$

$$P = 0.8; p = 750/1000; n = 1000; Q = 1 - P$$

$$z_{\text{cal}} = (p - P) / \sqrt{PQ/n}$$

100

>zcal

[1] -3.952847

>pvalue t = 2 * (1 - pnorm(abs(zcal)))

>pvalue

[1] 7.72268e-05

Since, the pvalue is less than 1% level of significance, we reject the hypothesis.

- Q3) Two random sample of size 1000 & 2000 are drawn from two population with the same sample sd 2.5. The sample means are 67.5 & 68 respectively. Test the Hypothesis $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$ at 5% level of significance.

- Q4) A study of noise level in 2 hospital is given below. Test the claim that the 2 hospitals have same level of noise at 1% level of significance.

Hos.A	Size	Mean	SD
Size	84	61.2	7.9
Hos.B	34	59.4	7.5

- Q5) In a sample of 600 students in a college, 400 use blue ink. In another college from a sample of 900 students, 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in 2 colleges are equal or not at 1% level of significance.

Q3) $H_0: H_1 = H_2$ against $H_1: H_1 \neq H_2$
 $n_1=1000; n_2=2000; m_1=67.5; m_2=68; sd_1=2.5; sd_2=2.5$
 $\text{z}_{\text{cal}} = (m_1 - m_2) / \sqrt{(\text{sd}_1^2/n_1) + (\text{sd}_2^2/n_2)}$
 z_{cal}
 $\{1\} \cancel{-1.62528} -5.163978$
 $\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(\text{z}_{\text{cal}})))$
 pvalue
 $\{1\} 2.417564e^{-07}$
 Since, the pvalue is less than 5% level of significance,
 we reject the hypothesis.

Q4) $n_1=84; n_2=34; m_1=61.2; m_2=59.4; sd_1=7.9; sd_2=7.5$
 $\text{z}_{\text{cal}} = (m_1 - m_2) / \sqrt{(\text{sd}_1^2/n_1) + (\text{sd}_2^2/n_2)}$
 z_{cal}
 $\{1\} 1.162528$
 $\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(\text{z}_{\text{cal}})))$
 pvalue
 $\{1\} 0.2450211$
 The pvalue is greater than 1% level of significance, we
 accept the hypothesis.

Q5) $n_1=600; n_2=900; p_1=400/600; p_2=450/900$
 $p = (n_1*p_1 + n_2*p_2) / (n_1 + n_2)$
 p
 $\{1\} 0.5666667$
 $q = 1 - p$
 q
 $\{1\} 0.4333333$
 $\text{z}_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$
 z_{cal}
 $\{1\} 6.381534$
 $\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(\text{z}_{\text{cal}})))$
 pvalue
 $\{1\} 1.753222e^{-10}$
 The pvalue is less than 1% level of significance,
 we reject the hypothesis ✓

Q6) $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$
 $n_1 = 200; n_2 = 200; p_1 = 44/200; p_2 = 30/200;$

$$>p = \frac{p_1 + p_2}{n_1 + n_2}$$

$$= 0.395$$

$$\{ 0.395$$

$$>q = 1 - p$$

$$\{ 0.605$$

$$\tilde{z}_{\text{cal}} = \frac{(p_1 - p_2)}{\sqrt{p * q * (1/n_1 + 1/n_2)}}$$

$$\tilde{z}_{\text{cal}}$$

$$\{ 1.80274$$

$$>\text{pvalue} = 2 * (\text{pnorm}(\text{abs}(\tilde{z}_{\text{cal}})))$$

$$\text{pvalue}$$

$$\{ 0.07$$

As p-value is greater than 0.07, we accept the hypothesis.

~~Ans~~
Ans

PRACTICA - 07

Topic :- Small sample test

Q1) The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from the population with the average 66.

$$\rightarrow H_0: \mu_0 = 66$$

$$\rightarrow x = [63, 63, 66, 67, 68, 69, 70, 70, 71].$$

`t.t.test(x)`

par One sample t-test

data: x

$t = 68.319$, $df = 9$, $pvalue = 1.558e^{-13}$.

alternative hypothesis: true mean is not equal to 0.

95 percent confidence interval:

65.65171 to 70.14829

sample estimates:

mean of x

67.9

∴ The pvalue is less than 0.5, we reject the hypothesis at 1% level of significance.

Q2) Two groups are of student score the following marks. Test the hypothesis that there is no significant difference between the two groups.

Group1 :- 18, 22, 21, 17, 20, 17, 23, 20, 22, 21.

Group2 :- 16, 20, 14, 21, 20, 18, 13, 15, 17, 21.

H_0 : No difference between the two groups.

EAO

> $x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$

> $y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

> t.test(x, y)

Welch Two Sample t-test

data: x and y

t = 2.2573, df = 16.376, p-value = 0.03798

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

0.1628205 5.0371795

sample estimates:

mean of x mean of y

20.1

\therefore p-value is less than 0.5, we reject the hypothesis at 5% level of significance.

Q3) The sales of 6 shops before & after a special campaign given below.

Below;

Before: 53, 28, 31, 48, 50, 42,

After: 58, 29, 30, 55, 56, 45

Test the hypothesis that the campaign is effective or not.

\Rightarrow No, there is no significance difference before and after the campaign.

> $x = c(53, 28, 31, 48, 50, 42)$

> $y = c(58, 29, 30, 55, 56, 45)$

> t.test(x, y, paired = T, alternative = "greater")

Paired t-test

data: x and y .
 $t = -2.7815$, $df = 5$, $p\text{value} = 0.9806$
alternative hypothesis: true difference in means is greater than 0.

95 percent confidence interval:

-6.035547 Inf

sample estimates:

mean of the differences

-3.5

$p\text{value}$ is greater than 0.05, we accept the hypothesis at 5% level of significance.

Q4) Two medicines are applied to two groups of patient respectively.

Group1:- 10, 12, 13, 11, 14.

Group2:- 8, 9, 12, 14, 15, 10, 9.

Is there any significance between the two medicines?

Q5) following are the weights before & after the diet program. Is the diet program effective?

Before:- 120, 125, 115, 130, 123, 119.

After:- 100, 114, 95, 90, 115, 99.

H_0 : No significant difference

Q4) $x \leftarrow c(10, 12, 13, 11, 14)$

$y \leftarrow c(8, 9, 12, 14, 15, 10, 9)$

$t\text{t.test}(x, y)$

Welch Two sample t-test.

data: x and y .

$t = 0.80384$, $df = 9.7594$, $p\text{value} = 0.4406$

alternative hypothesis: true difference in means is not equal to 0.

95 percent confidence interval:

-1.781171 3.781171

sample estimates:

mean of x mean of y .

$p\text{value}$ is greater than 0.05, we accept the hypothesis at 5% level of significance.

H_0 : diet program ~~positive~~ not effective

(25) > $x = c(120, 123, 115, 130, 123, 119)$

> $y = c(100, 114, 95, 90, 115, 99)$

> $t.test(x, y, paired = T, alternative = "less")$

Paired t-Test

data: x and y

t = 4.3458, df = 5, pvalue = 0.9963

alternative hypothesis: true difference in means is less than 0

95 percent confidence interval:

-Inf 29.0295

sample estimates:

mean of the differences

~~19.8333~~

A.V
6.2.20

Practical 08

Large and Small Sample tests

Q.1 The arithmetic mean of a sample of 100 items from a large population is 52. If the standard is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% LOS.

Q.2 In a big city 350 out of 700 males are found to be smokers. Does the information supports that exactly half of the males in the city are smokers ? Test at 1% LOS.

Q.3 Thousand article from a factory:A are found to have 2% defectives ,1500 articles from a 2nd factory:B are found to have 1% defective. Test at 5% LOS that the two factory are similar are not.

Q.4. A sample of size 400 was drawn at a sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.

Q.5. The flower stems are selected and the heights are found to be(cm) 63,63,68,69,71,71,72 test the hypothesis that the mean height is 66 or not at 1% LOS.

Q.6. Two random samples were drawn from 2 normal populations and their values are A-
66,67,75,76,82,84,88,90,92 B-64,66,74,78,82,85,87,92,93,95,97. Test whether the populations have the same variance at 5% LOS.

7. A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d. 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference between population and sample mean is significantly different?

8. From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1 % LOS.?

	Sample size	No. of bad apples
Consignment 1	200	44
Consignment 2	300	56

PRACTICAL-8

Aim - Large & small sample tests.

$$H_0: \mu = 55$$

$$>n=100$$

$$>m=52$$

$$>sd=7$$

$$>m1=55$$

$$>zcal = (m1 - m) / (sd / \sqrt{n})$$

$$>zcal$$

$$\{1\} 4.285714$$

$$>pvalue = 2 * (1 - pnorm(abs(zcal)))$$

$$>pvalue$$

$$\{1\} 1.82153e^{-05}$$

\because P-value is less than 0.05 we reject the hypothesis at 5% level of significance.

$$H_0: -\mu = 12$$

$$>n=700$$

$$>p = 350/700$$

$$>P = 0.5$$

$$>Q = 1 - P$$

$$>zcal = (p - P) / \sqrt{P + Q/n}$$

$$>zcal$$

$$\{1\} 0$$

$$>pvalue = 2 * (1 - pnorm(abs(zcal)))$$

$$>pvalue$$

$$\{1\} 1$$

\because P-value is greater than 0.5, we accept the hypothesis at 1% level of significance.

280

$$Q3) H_0: p_1 = p_2$$

$$> n_1 = 1000$$

$$> n_2 = 1500$$

$$> p_1 = 20/1000$$

$$> p_2 = 15/1500$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p$$

$$\{1\} 0.014$$

$$> z_{cal} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z_{cal}$$

$$\{1\} 2.081283$$

$$> pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

$$> pvalue$$

$$\{1\} 0.03740801$$

\because P-value is less than 0.05, we reject the hypothesis H_0 at 5% level of significance.

$$Q3) H_0: \mu = 100$$

$$> n = 400$$

$$> m = 99$$

$$> m_1 = 100$$

$$> s_d = 64$$

$$> z_{cal} = (m - m_1) / (s_d / \sqrt{n})$$

$$> z_{cal}$$

$$\{1\} -2.5$$

$$> pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

$$> pvalue$$

$$\{1\} 0.012493$$

$p\text{value}$ is less than 0.05, we reject the hypothesis.

Q6) $H_0: \mu = 66$
 $x = [63, 63, 68, 69, 71, 71, 72]$

046

> t.test(x)

One sample t-test

data: x

t = 47.94, df = 6, pvalue = 5.22e-09

alternative hypothesis: true mean is not equal to 0

sample estimates:

mean of x

68.14286

$p\text{value}$ is less than 0.01, we reject the hypothesis at 1% level of significance.

Q7) ~~8.7~~ H₀: $\mu = 1200$

>n = 100

>mx = 1150

>md = 1200

>sd = 125

>zcal = (mx - md) / (sd / sqrt(n))

>zcal

>zcal

{13} -4

>pvalue = 1 - pnorm(abs(zcal))

{13} 6.334248e-05

$p\text{value}$ is less than 0.05, we reject the hypothesis

$H_0: \sigma_1^2 = \sigma_2^2$

Q6) $x = [66, 67, 75, 76, 82, 84, 88, 90, 92]$

$y = [64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97]$

> var.test(x, y)

f test to compare two variances

data: x & y

F = 0.70686, num df = 8, denom df = 10, p-value = 0.6359

alternative hypothesis: true ratio of variances is not 1

sample estimates:

ratio of variances

0.706862

\therefore P-value is less than 0.05, we ~~accept~~ ^{accept} the hypothesis at 5% level of significance.

Q8)

$$H_0: p_1 \neq p_2$$

$$> n_1 = 200$$

$$> n_2 = 300$$

$$> p_1 = 44/200$$

$$> p_2 = 56/300$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p$$

$$\{ 0.2$$

$$> q = 1 - p$$

$$> z_{\text{real}} = (p_1 - p_2) / \sqrt{p * q * ((1/n_1) + (1/n_2))}$$

$$> z_{\text{cal}}$$

$$\{ 70.9128$$

$$> p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p_{\text{value}}$$

$$\{ 0.3613 \text{ more than } 0.05,$$

\therefore P-value is ~~more~~, hence it accepts H_0

~~AH~~
~~/~~
~~x~~

Topic :- Chi-square test and ANOVA.

- Q1) Use the following data to test whether the condition of the home and child are independent

		Cond" of Home	
		Clean	Dirty
Cond" of Child	Clean	70	50
	Fairly clean	80	20
	Dirty	35	45

Q2) H_0 : Cond" of child and home are independent

$$\sum x = (70, 80, 35, 50, 20, 45)$$

$$\sum m = 3$$

$$\sum n = 2$$

$\sum y = \text{matrix}(x, \text{ncol}=m, \text{nrow}=n)$

$\sum y$

	[1,1]	[1,2]
[1,1]	70	50
[2,1]	80	20
[3,1]	35	45

$\sum p_{v} = \text{chisq.test}(y)$

$\sum p_{v}$ Pearson's Chi-squared test

data: y
 $\chi^2 = 25.646$, $df = 2$, $p\text{value} = 2.698 \times 10^{-6}$.

"Pvalue is less than 0.05, we reject the hypothesis at 5% LOS.

∴ Cond" of child and home are dependent.

Q2) Test the hypothesis that vaccine and disease are independent or not.

		Vaccine	
Disease	Affected	Affected	Not affected
Affected	70	46	
Not Affected	35	37	

$$> \chi = c(70, 35, 46, 37)$$

$$> m = 2$$

$$> n = 2$$

$$> y = \text{matrix}(\chi, \text{ncol} = n, \text{nrow} = m)$$

$$> y$$

	{, 1}	{, 2}
{1, }	70	46
{2, }	35	37

$$> pV = \text{chisq.test}(y)$$

$$> pV$$

Pearson's Chi-squared test with Yates' continuity correction

data: y

X-squared: 2.0275, df = 1, pvalue = 0.1545

"Pvalue is greater than 0.05, we accept the hypothesis

∴ Vaccine and disease are independent.

H₀: Vaccine and disease are independent

True or not.

Q3) Perform a anova for the following data:-

048

Type	Observation
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

→ H_0 : The means are equal for A, B, C, D.

→ $x1 = c(50, 52)$

→ $x2 = c(53, 55, 53)$

→ $x3 = c(60, 58, 57, 56)$

→ $x4 = c(52, 54, 54, 55)$

→ d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

→ name(d)

[1] "values", "ind"

Ex:-

→ one way.test(values ~ ind, data = d, var.equal = T)

One-way Analysis of means

data: values and ind

F = 11.735, num df = 3, denom df = 9, pvalue = 0.00183

→ summary.anova = aov(values ~ ind, data = d)

→ summary(anova)

	DF	Sum Sq	Mean Sq	Fvalue	Pr(>F)
ind	3	71.06	23.688	11.73	0.00183
Residuals	9	18.17	2.019		

Signif. codes: 0 '***' 0.01 '**' 0.01 '*' 0.05 '.'

∴ P-values is less than 0.05, we reject the hypothesis at 5% LOS

∴ The means are not equal for A, B, C, D.

Q4) The following data gives the life of the tyres
of 4 brands

Type	Life
A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 16, 20, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 17, 16

→ H_0 : The average life of A, B, C, D are equal.

> $x1 = c(20, 23, 18, 17, 18, 22, 24)$

> $x2 = c(19, 15, 17, 16, 20, 17)$

> $x3 = c(21, 19, 22, 17, 20)$

> $x4 = c(15, 14, 16, 18, 17, 16)$

> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> names(d)

{1} "values" "ind"

> oneway.test(values ~ ind, data = d, var.equal = T)

One-way analysis of means

data: values and ind

f = 6.8445, num df = 3, denom df = 20, p-value = 0.001

"Pvalue is less than 0.05, we reject the hypothesis
at 5% LOS

∴ the average life of A, B, C, D are not equal.

Q4) > x = read.csv("C:/Users/Admin/Desktop/marks.csv")

> am = mean(x\$stats)

> am

{1} 33.7

> median(x\$stats)

{1} 38.5

> n = length(x\$stats)

> s = sqrt((n-1)*var(x\$stats)/n)

{1} 12.64911

>mean(n\$Maths)

[1] 39.4

>median(n\$Maths)

[1] 37

>sqrt((n-1) * var(n\$Maths))

[1] 15.2

>cor(n\$Stats, n\$Maths)

[1] 0.830618

PRACTICAL 10

Topic:- Non-parametric test

- Q1) Following are the amounts of sulphur oxide emitted by some industries in 20 days.
Apply sign test to test the hypothesis that the population median is 21.5 at 5% LOS.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.

H_0 : Population Median = 21.5.

> $x = c(17, 15, \dots, 26)$

> $me = 21.5$

> $sp = length(x[x > me])$

> $sn = length(x[x < me])$

> $n = sp + sn$

> n

{1} 20

> $pv = pbinom(sp, n, 0.5)$

> pv

{1} 0.4119015

\therefore P-value is greater than 0.05, we accept the hypothesis at 5% LOS.

Note:- If the alternative $H_1: me >$ then $pv = pbinom(n, n, 0.5)$

- Q2) The following is a data of 10 obs. Apply sign test to test the hypothesis that the population median is 625 against the alternative it is more than 625.

Values:- 612, 619, 631, 628, 643, 640, 655, 649, 670, 663

Population Median = 625 against $H_2: \neq 625$

$H_0: \mu = (612, \dots, 663)$

$\mu_{me} = 625$

$s_p = \text{length}(x[x > \mu_{me}])$

$s_n = \text{length}(x[x \leq \mu_{me}])$

$n = s_p + s_n$

$p_v = \text{pbinom}(s_n, n, 0.5)$

$p_v \approx 0.05 - 46875$

$\therefore p\text{-value is greater than } 0.05, \text{ we accept the hypothesis}$
 $\text{at } 5\% \text{ LOS.}$

(3) following are the values of a sample. Test the hypothesis that the population median is 60 against the hypothesis alternative it is more than 60.
 at 5% LOS using Wilcoxon signed rank test.
 Value:- 63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39,
 72, 69, 48, 66, 72, 63, 87, 69.

$H_0: \text{Population median} = 60$

$H_1: \text{Population median} > 60$

$\sum x = (63, 65, \dots, 69)$

$\text{wilcox.t.test}(x, \text{alter} = \text{"greater"}, \mu = 60)$.
 Wilcoxon signed rank test with continuity correction

data: x
 $V = 145, p\text{-value} = 0.02298$
 alternative hypothesis: true location > 60.
 $\therefore p\text{-value is less than } 0.05, \text{ we reject the hypothesis at } 5\% \text{ LOS.}$

Note: If alternative is less, alter = "less". If alternative is not equal to, alter = "two.sided".

Q4) Using WSRT, test the population median or less than 12.

Ans

Data: 15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26

$\cancel{H_0}$

H_0 : Population median = 12

H_1 : Population median \neq 12

> u = c(15, 17, ..., 26)

> wilcox.test(u, alter = "less", mu = 12)

Wilcoxon signed rank test

data: u

v = 66, pvalue = 0.9986

\therefore P-value is greater than 0.05, we accept the hypothesis at 5% LOS.

Q5) The ~~waves~~ weight of students before and after they stop smoking are given below. Using WSRT, test that there is no significant change.

Before: 65, 75, 75, 62, 72.

After: 72, 74, 72, 66, 73.

> u = c(65, 72, 75, 62, 72)

> v = c(72, 74, 72, 66, 73)

> d = u - v

> wilcox.test(d, alter = "two-sided", mu = 0)

Wilcoxon signed rank test

data: d

v = 4.5, pvalue = 0.4982

\therefore P-value is greater than 0.05, we accept the hypothesis at 5% LOS.

H_0 : There is no difference in weights

H_1 : There is difference in weights

~~(H₁)~~