

CMSC 651, Spring 2018, University of Maryland  
HW4, due as PDF to the address *cmssc651.umd@gmail.com* by 11:59PM on April 18, 2018

**Notes:** (i) Please work on this with your group (one writeup per group). Consulting other sources (including the Web) is not allowed. (ii) Write your solutions neatly and *include your names*; if you are able to make partial progress by making some additional assumptions, then **state these assumptions clearly and submit your partial solution**. (iii) **Please make the subject line of your email “651 HW4”** followed by your full name, and email a PDF to *cmssc651.umd@gmail.com*: PDF generated from Word or LaTeX strongly encouraged.

1. Complete the quick proof we showed in class that the sum of the elements of an  $n$ -element array can be computed using  $n$  processors and in  $O(\log n)$  time on an EREW PRAM. **(12 points)**
2. In studying how to do processor emulation with fewer processors, we considered the following algorithm  $A$  on a DAG  $G = (V, E)$ :

```
i = 0;
while (G is not empty) {
    i = i + 1;
    L(i) = current set of sources (nodes with no incoming edges) in G;
    Remove L(i) (and all edges incident on vertices in L(i)) from G;
}
```

Suppose  $A$  partitions  $V$  into  $L(1), L(2), \dots, L(\ell)$ . We used the following fact without proof, in proving that our processor assignment led to a 2-approximation of the maximum completion time:  $\ell$  equals the number of vertices in a longest (directed) path in  $G$ . Prove this fact. **(15 points)**

3. Problem 5.3 from the Lau-Ravi-Singh book that is posted under “Resources”. **(10 + 8 points)**
4. Problem 5.6 from the Lau-Ravi-Singh book that is posted under “Resources”. (The notation “ $X - Y$  paths” does not mean “ $X$  minus  $Y$ ”, but refers to “from  $X$  to  $Y$ ”.) **(15 points)**