

Basics of R Software

- ① R is a Software for Statistical analysis and data computing
- ② It is an effective data handling Software and outcome storage is Possible.
- ③ It is Capable of graphical display.
- ④ Its a free Software

Problem 1:- Solve the following

$$① 4 + 6 + 8 \div 2 - 5$$

$$> 4 + 6 + 8 / 2 - 5$$

[1] 9

$$② 2^2 + |-3| + \sqrt{45}$$

$$> 2^2 + \text{abs}(-3) + \text{sqrt}(45)$$

[1] 13.7082

$$③ 5^3 + 7 \times 5 \times 8 + 46 / 5$$

$$> 5^3 + 7 * 5 * 8 + 46 / 5$$

[1] 513.2

$$④ \sqrt{4^2 + 5 \times 3 + 7 / 6}$$

$$> \text{sqrt}(4^2 + 5 * 3 + 7 / 6)$$

[1] 5671567

⑤ Round off

$$46.7 + 9 \times 8$$

Problem ②

- (i) $c(2,3,5,7) * 2$
- (ii) $c(2,3,5,7) \times (2,3)$
- (iii) $c(2,3,5,7) * c(2,3,6,2)$
- (iv) $c(1,6,2,3) * (-2, -3, -4, -1)$
- (v) $c(2,3,5,7) \wedge 2$
- (vi) $c(4,6,8,9,4,5) \wedge c(1,2,3)$
- (vii) $c(6,2,7,5) / (4,5)$

- (i) $c(2,3,5,7) * 2$
0) 4 6 10 14
- (ii) $c(2,3,5,7) * c(2,3)$
0) 4 9 10 21
- (iii) $c(2,3,5,7) * c(2,3,6,2)$
0) 4 9 30 14
- (iv) $c(1,6,2,3) * (-2, -3, -4, -1)$
0) -2 -18 -8 -3
- (v) $c(2,3,5,7) \wedge 2$
0) 4 9 25 49
- (vi) $c(4,6,8,9,4,5) \wedge c(1,2,3)$
0) 4 36 512 9 16 125
- (vii) $c(6,2,7,5) / (4,5)$
0) 1.50 0.40 1.75 1.00

3:

Problem 3:

$$\text{Q. } \begin{aligned} x &= 20 \\ y &= 30 \\ z &= 2 \end{aligned}$$

- Find i) $x^2 + y^3 + z$
ii) $\sqrt{x^2 + y}$
iii) $x^2 + y^2$

Ans

```
>x=20
>y=30
>z=2
>x^2+y^3+z
[1] 2+30^3
>598+(x^2+y)
[1] 20.73655
>x^2+y^2
[1] 1300
```

Problem 4:-

Create matrix

$$x = \begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{bmatrix}$$

```
>x <- matrix (nrow=4, ncol=2, data = c(1:8))
>x
[1] [2]
[1,] 1 5
[2,] 2 6
[3,] 3 7
[4,] 4 8
```

Q5) Find $x + y$ and $2x + 3y$ such that

$$x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix} \quad y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 13 & -6 & 5 \end{bmatrix}$$

```
>x=matrix (nrow=3, ncol=3, data = c(4,7,9,-20,-5,6,7,3))
>y=matrix (nrow=3, ncol=3, data = c(10,12,15,-5,-4,-6,7,9,5))
```

 $x + y$

$$\begin{bmatrix} 1,1 & 1,2 & 1,3 \\ 2,1 & 19 & 16 \\ 3,1 & 25 & 8 \end{bmatrix}$$

 $2 \star x + 3 \star y$

$$\begin{bmatrix} 1,1 & 1,2 & 1,3 \\ 2,1 & 38 & 33 \\ 3,1 & 50 & 41 \end{bmatrix}$$

Q6) Matrix of Statistics of Computer Science Students

59, 26, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54,
40, 50, 32, 36, 29, 35, 39

> $x = c(\text{data})$

> $\sum \text{length}(x)$

[1] 20

> $\text{breaks} = \text{Seq}(20, 60, 5)$

> $A = \text{cut}(x, \text{breaks}, \text{right} = \text{FALSE})$

> $b = \text{table}(A)$

> $c = \text{transform}(b)$

> c

		freq
1	[20, 25)	3
2	[25, 30]	2
3	[30, 35]	1
4	[35, 40]	3
5	[40, 45]	1
6	[45, 50]	3
7	[50, 55]	2
8	[55, 60]	3

Practical - 2

(Probability Distribution)

Check whether the following are Pmf or not

x	$P(x)$
0	0.1
1	0.2
2	0.5
3	0.4
4	0.3
5	0.5

x	1	2	3	4	5
$P(x)$	0.2	0.2	0.3	0.2	0.2

x	10	20	30	40	50
$P(x)$	0.2	0.2	0.35	0.15	0.1

Since $\sum P(x) = 0.5$, it cannot be a Pmf
 Since $P_{\text{mf}} \Rightarrow P(x) \geq 0 \forall x$

It cannot be a Pmf as in Pmf
 $\sum P(x) \neq 1$

$$\text{Prob} = (0.2, 0.2, 0.3, 0.2, 0.2) \\ > \sum \text{Prob}$$

[1] 1.1

Ans

Since $\sum p(x) = 1$, it is a P.m.f
 $\therefore \text{Prob} = \{0.2, 0.2, 0.35, 0.15, 0.1\}$

> Sum(Prob)
> [1]

Q2)

i) Find C.d.f for the following P.m.f and sketch graph.

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

Ans > Prob = $\{0.2, 0.2, 0.35, 0.15, 0.1\}$

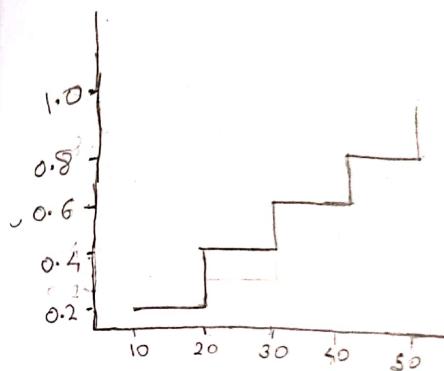
> Sum(Prob)

[1] 0.20 0.40 0.75 0.90 1.00

$$\begin{aligned} f(x) &= 0 & x < 10 \\ &= 0.2 & 10 \leq x < 20 \\ &= 0.4 & 20 \leq x < 30 \\ &= 0.75 & 30 \leq x < 40 \\ &= 0.95 & 40 \leq x < 50 \\ &= 1.0 & x \geq 50 \end{aligned}$$

$$\therefore x = \{10, 20, 30, 40, 50\}$$

> Plot (x, CumSum(Prob), "S")



$$\begin{array}{lllllll} x & 1 & 2 & 3 & 4 & 5 & 6 \\ p(x) & 0.15 & 0.25 & 0.1 & 0.2 & 0.2 & 0.1 \end{array}$$

Prob = $\{0.15, 0.25, 0.1, 0.2, 0.2, 0.1\}$
Sum(Prob)

[1]

CumSum(Prob)

[1] 0.15 0.40 0.50 0.70 0.90 1.00

$$\begin{array}{ll} f(x) & 0 & x < 1 \\ & 0.15 & 1 \leq x < 2 \\ & 0.40 & 2 \leq x < 3 \\ & 0.50 & 3 \leq x < 4 \\ & 0.70 & 4 \leq x < 5 \\ & 0.90 & 5 \leq x < 6 \\ & 1.00 & x \geq 6 \end{array}$$

check whether the following P.d.f or not

$$\begin{cases} f(x) = 3-2x & : 0 < x < 1 \\ f(x) = 3x^2 & : 0 < x < 1 \end{cases}$$

$$\text{i)} \int_0^1 f(x) dx$$

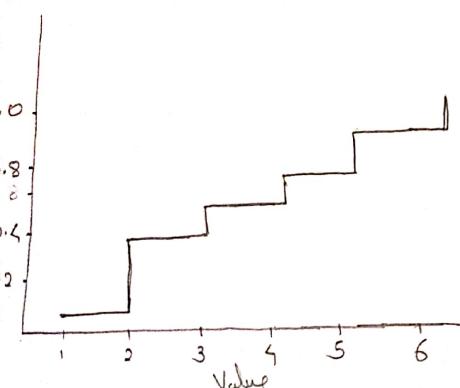
$$\int_0^1 (3-2x) dx$$

$$\int_0^1 (3dx - \int_0^1 2xdx) \\ = [3x - x^2]_0^1 = 2$$

$$\text{ii)} \int_0^1 3x^2 dx \\ \int_0^1 x^2 dx \\ 3 \left[\frac{x^3}{3} \right]_0^1 \\ \frac{3^1}{3} [x^3]_0^1 \\ = [1-0] \\ = 1$$

AM

x: ((1, 2, 3, 4, 5, 6)
 Splt(x, main = "Prob", sub = "Value", ylab = "Value", ylab = "Sum(Prob)", "5"))



Practical - 3

Topic:- Binomial distribution

- i) $P(X=x) = \text{dbinom}(x, n, p)$
- ii) $P(X \leq x) = \text{Pbinom}(x, n, p)$
- iii) $P(X > x) = 1 - \text{Pbinom}(x, n, p)$
- iv) $P_i = P(X \leq x) = \text{dbinom}(P_i, n, p)$

Q1) Find the Probability of exactly 10 Success in 100 trials with $P=0.1$

Q2) Suppose there are 12 MCQ each question have 5 option one of which is correct. Find the Probability of having

- i) exactly 0 correct answer
- ii) atmost 10 correct answer
- iii) more than 5 correct answer

Q3) Find the Complete distribution when $n=5$ and $P=0.1$

Q4) $n=12, P=0.25$ Find the following Probability

- i) $P(X=5)$
- ii) $P(X \leq 5)$
- iii) $P(X > 7)$
- iv) $P(5 < X < 7)$

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Ans
[1] dbinom(10, 100, 0.1)
[1] 0.1318653

[1] dbinom(4, 12, 0.2)

[1] 0.1328756

[1] Pbinom(4, 12, 0.2)

[1] 0.9274443

[1] 1 - Pbinom(4, 12, 0.2)

[1] 0.072555

[1] > dbinom(0: 5, 5, 0.1)

[1] 0.59049 0.32805 0.07290 0.00810
0.00043 0.00001

[1] > dbinom(5, 12, 0.25)

[1] 0.1032914

[1] Pbinom(5, 12, 0.25)

[1] 0.4455978

[1] 1 - Pbinom(7, 12, 0.25)

[1] 0.0027815,

[1] > dbinom(6, 12, 0.25)

[1] 0.04014953

Q5) The Probability of 0 Salesman making a Sale -
 to a Customer of 0.5
 i) No Sales out of 10 customers
 ii) More than 3 Sales out of 20 customers

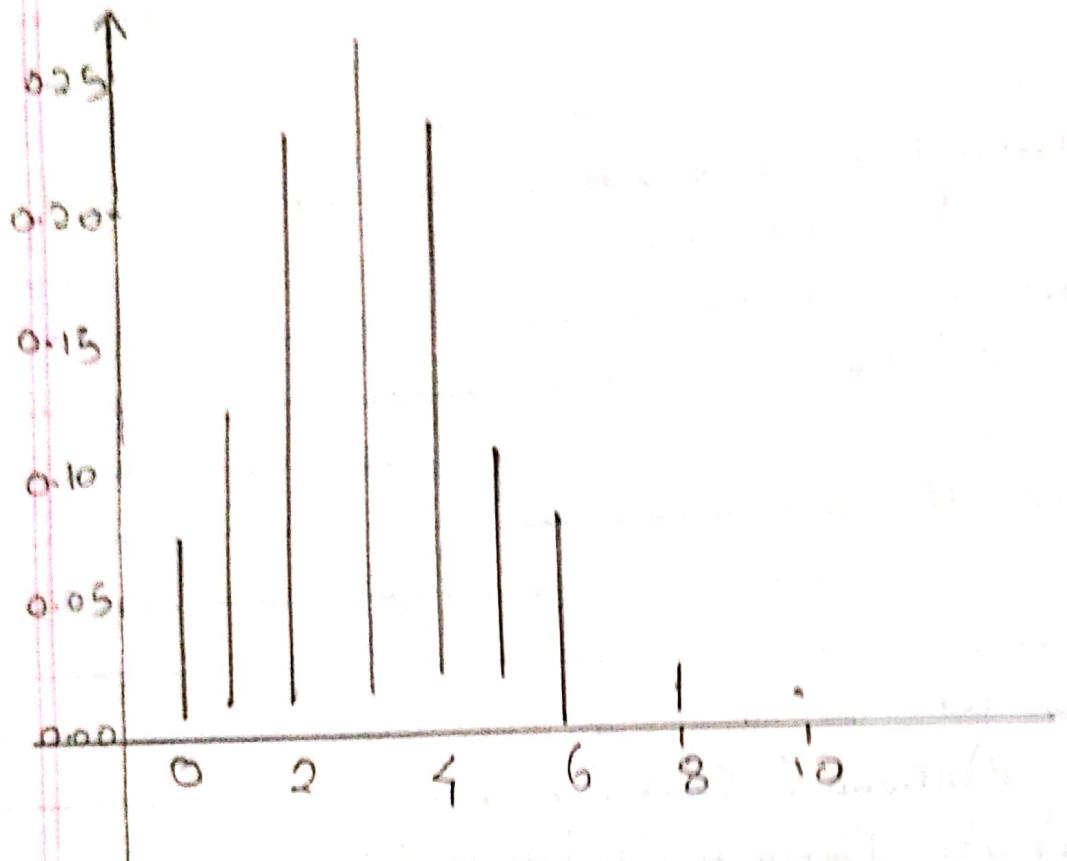
Q6) A Salesman has a 20% Probability of making a Sale to a Customer out of 30 customers what minimum number of Sales with 88% Probability.

Q7) follows binomial distribution with $x \sim P = 0.3$
 Plot the graph of P.m.f and C.d.f.

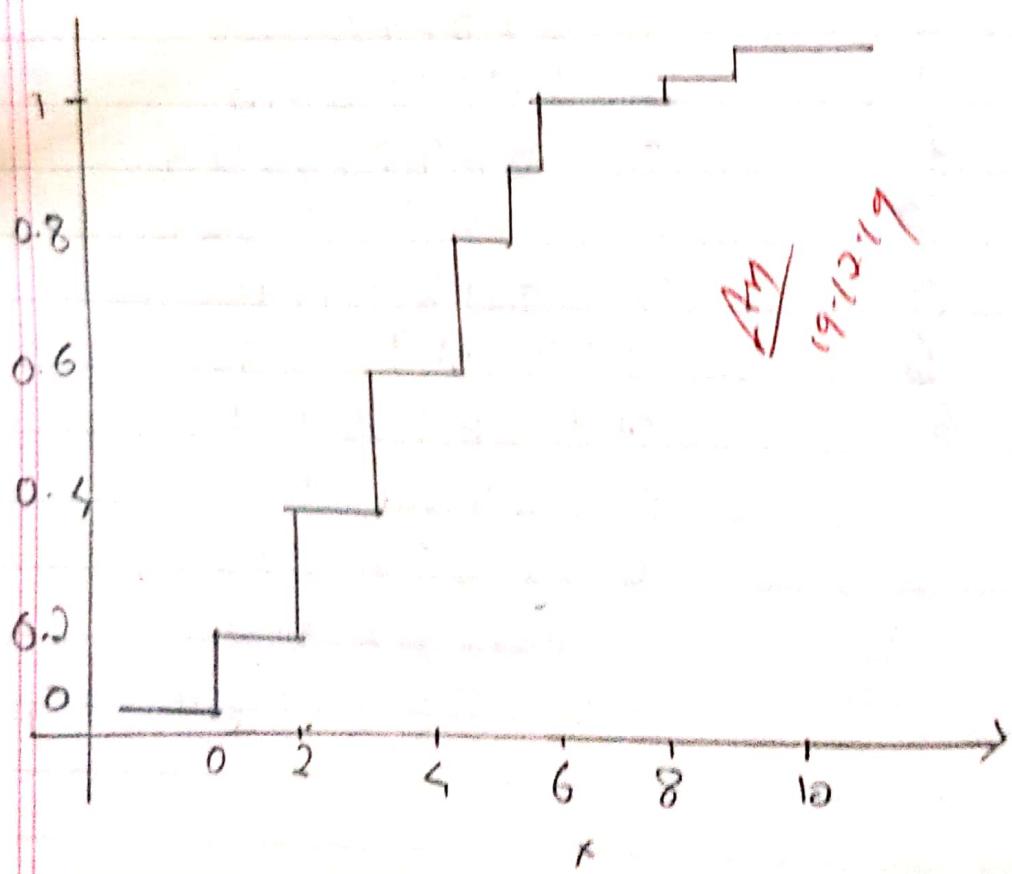
59

Ans
 Q5) $> \text{dbinom}(0, 10, 0.5)$
 [I] 0.0009765625
 $> 1 - \text{Pbinom}(3, 20, 0.5)$
 [I] 0.9987116
 6) $> \text{qbinom}(0.88, 30, 0.2)$
 [I] 9
 7) $> x = 0 : 10$
 $> \text{Prob} = \text{dbinom}(x, 10, 0.3)$
 $> \text{CumProb} = \text{Pbinom}(x, 10, 0.3)$
 $> \text{df} = \text{data.frame}(\text{"x values"} = x, \text{"Probability"} = \text{Prob})$
 $> \text{Print}$

x	Probability
0	0.028247
1	0.1210608210
2	0.2334744405
3	0.2668274320
4	0.2001204490
5	0.1029193432
6	0.0367569090
7	0.0090016920
8	0.0014467005
9	0.0001377810
10	0.00005059059
11	0.0000059059



>plot (1, CurrProb, "g")



Practical. 4

TOPIC: Normal distribution

$P(X = x) = \text{dnorm}(x, \mu, \sigma)$

$P(X \leq x) = \text{pnorm}(x, \mu, \sigma)$

$P(X > x) = 1 - \text{pnorm}(x, \mu, \sigma)$

To generate random numbers from a normal distribution (n random no.)

the R code is $\text{rnorm}(n, \mu, \sigma)$

A random variable X follows normal distribution with mean = $\mu = 12$ and

$SD = \sigma = 3$ find

i) $P(X \leq 15)$

ii) $P(10 \leq X \leq 13)$

iii) $P(X > 15)$

iv) generate 5 observations (random no.)

> $P_1 = \text{pnorm}(15, 12, 3)$

[1] 0.8413447

> cat("P(X <= 15) =", P1)

[1] $P(X \leq 15) = 0.8413447$

> $P_2 = \text{pnorm}(13, 12, 3)$

> cat("P(10 \leq X \leq 13) =", P2)

[1] $P(10 \leq X \leq 13) = 0.378066$

> $P_3 = 1 - \text{pnorm}(15, 12, 3)$

> cat("P(X > 15) =", P3)

[1] $P(X > 15) = 0.2524925$

> $\text{rnorm}(5, 12, 3)$

[1] 12.639812 13.091270

6.865470

3) generate 5 random numbers with
mean = 15 & $\sigma = 4$
Find Sample mean, median, S.D.
and Print it

4) X follows normal

$$X \sim N(30, 100)$$

Find i) $P(X \leq 40)$ ii) $P(X > 35)$
iii) $P(25 < X < 35)$ iv) Find K such that
 $P(X < K) = 0.6$

$$> P_1 = \text{pnorm}(40, 30, 10)$$

$$> P_1$$

$$[1] 0.8413447$$

$$> P_2 = 1 - \text{pnorm}(35, 30, 10)$$

$$> P_2$$

$$[1] 0.3085375$$

$$> P_3 = \text{pnorm}(25, 30, 10) - \text{pnorm}(35, 30, 10)$$

$$> P_3$$

$$[1] -0.382949$$

$$> P_4 = \text{qnorm}(0.6, 30, 10)$$

$$> P_4$$

$$[1] 32.53347$$

8) $x = \text{rnorm}(5, 15, 5)$

$$> x$$

$$[1] 12.73337 \quad 12.30235 \quad 16.62240 \quad 23.24345$$

$$13.08828$$

> $\text{mean}(x)$

> sd

$$[1] 15.33276$$

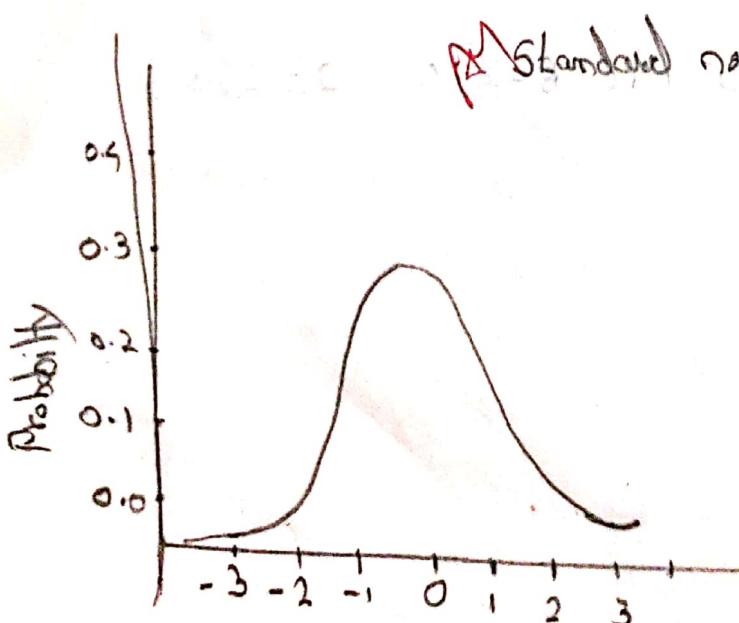
> me=median(X)
(1) 14.86556

> n=5
> V=(n-1)*Var(x)/n
> V
(1) 2.574805
> Sd=Sqrt(V)
> Sd

(1) 1.60462
> Cat ("Sample mean", mean)
Sample mean 15.33276
> Cat ("Sample Sd", Sd)
Sample Sd 1.60462

5) Plot the normal graph (Standard)

> X=Seq(-3,3,by=0.1)
> Y=dnorm(x)
> Plot(x, Y, xlab="X Value", ylab="Probability",
main="Standard normal graph")



PRACTICAL - 5

TOPIC: Normal and t-test

$$H_0: \mu = 15 \quad H_1: \mu \neq 15$$

Test the hypothesis

Random Sample of Size 400 is drawn

and it is calculated. The Sample mean is 15.

And S.D is 3. test the hypothesis at 5% level of Significance

$0.05 >$ accept the Value

$0.05 <$ less than Reject

$$> m_0 = 15$$

$$> m_x = 15$$

$$> S_d = 3$$

$$> n = 400$$

$$> z_{cal} = (m_x - m_0) / (S_d / (\text{Sqrt}(n)))$$

$$> z_{cal}$$

$$[1] \sim 6.666667$$

$$> Cal = ("Calculated Value of Z is : ", z_{cal})$$

$$\text{Calculated Value of } Z \text{ is } = -6.666667$$

$$> P \text{ value} = 2 * (1 - \text{Norm}(\text{abs}(z_{cal})))$$

$$> P \text{ value}$$

$$[1] 2.616795e-11$$

\therefore The P-value is less than 0.05 we will reject the Value of $H_0: \mu = 15$

$>z_{cal} = (P - P_0) / \sqrt{P_0(1-P_0)/n}$
 $>z_{cal} ("Calculated Value of z is" = z_{cal})$
 $[1] \text{Calculated Value of } z \text{ is } = -3.75$
 $>PValue = 2 \times (1 - \text{Norm}(abs(z_{cal})))$
 $>PValue$
 $[1] 0.00017683 < 6 \text{ (Reject)}$

\rightarrow Last Year farmer's land 20% of their crops A random Sample of 60 fields are counted And it is found that a field crops are indeed Polluted.
 Test the hypothesis at 1% level of Significance

$>P = 0.2$
 $>P = 0.160$
 $>n = 60$
 $>z_{cal} = (P - P_0) / \sqrt{P_0(1-P_0)/n}$
 $>z_{cal}$
 $[1] -0.9682 < 5.8$
 $>PValue = 2 \times (1 - \text{Norm}(abs(z_{cal})))$
 $>PValue$
 $[1] 0.3329216$

\therefore The Value is 0.1 So Value is accepted
 \rightarrow Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of Significance
 $>X = [12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.93, 11.89, 12.16]$
 $>n = \text{length}(x)$
 $>n$
 $[1] 10$
 $>\bar{x} = \text{mean}(x)$
 $>\bar{x}$
 $[1] 12.107$

\rightarrow Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$
 A random Sample Size of 500 is drawn with
 Sample mean = 10.2 and S.D = 2.25
 Test the hypothesis at

$>m_0 = 10$
 $>n = 500$
 $>\bar{x} = 10.2$
 $>s_d = 2.25$
 $>z_{cal} = (\bar{x} - m_0) / (s_d / \sqrt{n})$
 $>z_{cal}$
 $[1] 1.77778$
 $>PValue = 2 \times (1 - \text{Norm}(abs(z_{cal})))$
 $>PValue$
 $[1] 0.0755 < 0.05$
 \therefore The Value is greater than 0.05
 \therefore The Value is accepted

\rightarrow Test the hypothesis $H_0: \text{Proportion of Smokers in College is } 0.2$
 A Sample is Collected and Calculated the Sample Proportion as 0.125. Test the hypothesis at 5% level of Significance
 (Sample size is 400)

$>P = 0.2$
 $>P = 0.125$
 $>n = 400$
 $>q = 1 - P$

Practical - 6

Topic :- Large Sample Test

Let the Population mean (Amount Spent per Customer in a restaurant) is 250. A Sample of 100 Customers Selected the Sample mean is Calculated as 275 and Standard d is 30. Test the hypothesis that Population is 250 and not at level of 5% of Significance

In a random Sample of 1000 Student it is found that 1.50 We'd blue pen test hypothesis that the population Proposition is 0.8 at level of Significance

$\mu_0 = 250;$

$\mu_x = 275$ against $H_1: \mu > 275$

$s_d = 30$

$n = 100$

$Z_{cal} = (\mu_x - \mu_0) / (s_d / (\sqrt{n}))$

Z_{cal}

(1) 8.33333

$PValue = 2 * (1 - Pnorm(abs(zcal)))$

$PValue$

(1) 0

PValue is less than 0.05 We reject. H_0 at 5% level of Significance.

$$2) H_0: P = 0.8 \text{ against } H_1: P > 0.8$$

$$P = 0.8$$

$$q = 1 - P$$

$$P = 760/1000$$

$$h = 100$$

$$> z_{\text{cal}} = (P - p) / (\sqrt{pq})$$

$$[1] -3.952857$$

$$> P\text{Value} = 2 * (1 - \text{norm}(abs(z_{\text{cal}})))$$

$$> P\text{Value}$$

$$[1] 7.7226805$$

3) Two random Sample of size 1000 and 2000 are drawn from two population with same Standard deviation 2.5. The Sample means are 67.5 and 68 respectively. Test the hypothesis at 5% level of Significance

4) A Study of Noise level in a 2 hospital is given below. Test the claim that the two hospitals are same level of Noise at 1% level Significance

	Hos A	Hos B
Size	85	35
Mean	61.2	69.5
S.D	7.9	7.5

5) In a Sample of 600 Student in a College 400 used blue unit in another city from a Sample of 900 Student 450 used blue unit. Test the hypothesis that the Proportion of Student using blue unit in 2 college are equal at molc at 1% level of Significance

$$3) H_0: H_1 = H_2 \text{ against } H_1: H_1 \neq H_2$$

$$n_1 = 1000$$

$$n_2 = 2000$$

$$molc = 675$$

$$mrx_2 = 68$$

$$sd_1 = 62.5$$

$$sd_2 = 2.5$$

$$> z_{\text{cal}} = (mrx_1 - mrx_2) / \sqrt{\frac{(sd_1^2/n_1) + (sd_2^2/n_2)}{}}$$

$$[1] -5.163978$$

$$> P\text{Value} = 2 * (1 - \text{norm}(abs(z_{\text{cal}})))$$

$$> P\text{Value}$$

$$[1] 2.417564e-07$$

P Value is < 0.05

We reject H_0 at 5%.

$$4) H_0: H_1 = H_2 \text{ against } H_1: H_1 \neq H_2$$

$$n_1 = 85$$

$$n_2 = 35$$

$$mrx_1 = 61.2$$

$$mrx_2 = 69.5$$

$$sd_1 = 7.9$$

$$sd_2 = 7.5$$

$$> z_{\text{cal}} = (mrx_1 - mrx_2) / \sqrt{\frac{(sd_1^2/n_1) + (sd_2^2/n_2)}{}}$$

$$> z_{\text{cal}}.$$

[1] 1.162528

$$> P\text{Value} = 2 * (1 - \text{Norm}(\text{abs}(z_{\text{cal}})))$$

> PValue

[1] 0.240571

∴ P value is greater than 0.05 We accept H_0 at 1% level of significance

5) $H_0: P_1 = P_2$ against $H_1: \mu_1 \neq \mu_2$

$$n_1 = 600$$

$$n_2 = 900$$

$$P_1 = 500/600$$

$$P^2 = 450/900$$

$$P = (n_1 * P_1 + n_2 * P^2) / (n_1 + n_2)$$

$$q = 1 - P$$

$$> z_{\text{cal}} = (P^1 - P^2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

> z_{cal}

[1] 6.381635

$$> P\text{Value} = 2 * (1 - \text{Norm}(\text{abs}(z_{\text{cal}})))$$

> PValue

[1] 1.75322e-10...

P value is < 0.05 (reject)

H_0 at 1% level of significance

For Sample Size

$$n_1 = 200$$

$$n_2 = 200$$

$$P_1 = 44/200$$

$$P_2 = 30/200$$

$$P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$> z_{\text{cal}} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

> z_{cal}

[1] 1.802741

> P

[1] 0.185.

$$> P\text{Value} = 2 * (1 - \text{Norm}(\text{abs}(z_{\text{cal}})))$$

> PValue

[1] 0.07142888

P Value is > 0.05 We accept.

H_0 at 5% level of significance.

Practical - 7

Topic: Small Sample Test

(Q1) The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that sample comes from population with the average 66.

$$H_0: \mu = 66 \quad H_1: \mu \neq 66$$

$$\geq n = \text{length}(x)$$

$$\geq n$$

$$[1] \geq 10$$

$$\geq t\text{-test}(y)$$

One Sample t-test

$$\text{data} : x$$

$$t = 68.319, df = 9, P\text{-Value} = 1.658e-13$$

Alternative hypothesis: true mean is not equal to 0

90 Percent confidence interval: 65.66 (T) ≥ 0.14829

Sample estimate:

mean of x

$$67.9$$

\because P-value is less than 0.05. Hence, we reject the H_0 at 5% level of significance.

\geq if (P-value > 0.05) {or ("Accept H_0 ") } else {or ("Reject H_0 ") }

Reject H_0 .

(Q2) Two groups of Student Score the following marks. Test the hypothesis that there is no level of Significance difference between 2 groups.

$$\text{Group A} : 18, 22, 21, 17, 20, 17, 23, 20, 22, 21$$

$$\text{Group B} : 16, 20, 14, 21, 20, 18, 13, 15, 17, 21$$

$\Rightarrow H_0$: There is no difference between two groups

$$x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$$

$$y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$$

$$t\text{-test}(x, y)$$

Welch Two Sample t-test

data: x and y

$$t = 2.2573, df = 16.376, P\text{-Value} = 0.03798$$

alternative hypothesis: true difference in means is not equal to 0

$$0.1628206 \quad 6.0371795$$

Sample estimates:

$$\text{mean of } x \text{mean of } y$$

$$20.1 \quad 17.5$$

\geq if (P-value > 0.05) {or ("Accept H_0 ") } else {or ("Reject H_0 ") }

Reject H_0 .

Q3) Sales data of 6 shop before and after one Special Campaign
given below:-

Before: 53, 28, 31, 48, 50, 47

After: 58, 29, 30, 55, 56, 45.

Test the hypothesis the Campaign is effective or not.

H_0 : There is no significant difference of Sales before
and after the Campaign

$> x = c(53, 28, 31, 48, 50, 47)$

$> y = c(58, 29, 30, 55, 56, 45)$

$> t.test(x, y, paired = T, alternative = "greater")$

Paired t-test

Data: x and y

$t = -2.7815, df = 5, P\text{-Value} = 0.9806$

Alternative hypothesis: true difference in means is greater
than 0.

-0.035547 Inf.

Sample estimates:

mean of the differences

-3.5

$P\text{-Value} = 0.9806$

$> \text{if}(P\text{-Value} > 0.05) \{ \text{cat}("Accept } H_0") \} \text{ else} \{ \text{cat}("Reject } H_0") \}$

Accept H_0 .

Two medicines are applied to 2 group of Patient

Group 1: 10, 12, 13, 11, 15

Group 2: 8, 9, 12, 14, 15, 10, 9

is there any significant difference between two groups?

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$a = c(10, 12, 13, 11, 15)$

$b = c(8, 9, 12, 14, 15, 10, 9)$

$> t.test(a, b)$

Welch Two Sample t-test

Data: a and b

$t = 0.65591, df = 9.567, P\text{-Value} = 0.5272$

alternative hypothesis: true difference in mean is
not equal to 0. 90 percent Confidence interval:

-1.964382 3.534382

Sample estimates:

mean of x mean of y

11.8 11.0

$> P\text{-Value} = 0.5272$

$> \text{if}(P\text{-Value} > 0.05) \{ \text{cat}("Accept } H_0") \} \text{ else} \{ \text{cat}("Reject } H_0") \}$

Accept H_0 .

Q5) H_0 : There is no significance difference between before and after.

> A = ((120, 125, 115, 130, 123, 119))

> B = ((100, 114, 95, 90, 115, 99))

> t-test(A, B, paired = T, alternative = "less")

Paired t-test

data : A and B.

t = -5.345, df = 5, P-Value = 0.9963

alternative hypothesis : True difference in mean is less than 0 95. Percent Confidence interval:

Inf 29.0293

Sample estimates :

mean of the differences

19.8333

> P Value : 0.9963

> if (PValue > 0.05) { cat ("Accept H.") } else { cat ("Reject H.") }

Accept H.



Practical - 8

Topic: Large and Small Sample tests

$$H_0: \mu = 65, H_1: \mu \neq 65$$

$$n = 10$$

$$m_x = 52$$

$$m_0 = 55$$

$$S_d = 7$$

$$z_{cal} = (m_x - m_0) / (S_d / (\sqrt{n}))$$

$$z_{cal}$$

$$[1] = -4.285714$$

$$\rightarrow P\text{value} = 2 * (1 - \text{Prnorm}(\text{abs}(z_{cal})))$$

$$\rightarrow P\text{value}$$

$$[1] 1.82153e-0.5$$

As Pvalue is less than 0.05 we reject H_0 at 5% level of significance.

$$(2) H_0: p = 0.5 \text{ against } H_1: p \neq 0.5$$

$$P = 0.5$$

$$q = 1 - P$$

$$n = 700$$

$$z_{cal} = (P - p) / (q / \sqrt{n})$$

$$z_{cal}$$

$$[1] 0$$

$$> P\text{Value} = 2 \times (1 - \text{Norm}(abs(z_{cal})))$$

> P Value

[1]

As value is greater than 0.05 we accept H_0 at 1% level of significance

3) $H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

$$> n_1 = 1000$$

$$> n_2 = 1500$$

$$> P_1 = 2/1000$$

$$> P_2 = 1/1500$$

$$> P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$> P$$

[1] 0.0012

$$> q = 1 - P$$

[1] 0.9988

$$> z_{cal} = (P_1 - P_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

$$> z_{cal}$$

[1] 0.9433752

$$> P\text{Value} = 2 \times (1 - \text{Norm}(abs(z_{cal})))$$

> PValue

[1] 0.345489

P Value is greater than 0.05 we accept H_0 and 1% level of significance

④ H_0

$$> Var_x = 64$$

$$> n = 400$$

$$> m_0 = 100$$

$$> m_x = 99$$

$$> Sd = \sqrt{Var_x}$$

$$> Sd$$

[1] 8

$$> Z_{cal} = (m_x - m_0) / (Sd / \sqrt{n})$$

$$> Z_{cal}$$

$$> Z_{cal} - fm.$$

[1] -2.5

$$> P\text{Value} = 2 \times (1 - \text{Norm}(abs(z_{cal})))$$

> PValue

[1] 0.01241933

Since PValue is less than 0.05 we reject H_0 at 5% level of significance

⑤ $H_0: \mu = 66$ against $H_1: \mu \neq 66$

$$> x = c(63, 63, 68, 69, 71, 71, 72)$$

> t.test(x)

One Sample t-test

data: x

$$t = 4.79, df = 6, P\text{Value} = 5.322e-09$$

alternative hypothesis: true mean is not equal to 66
95 Percent Confidence Interval:

$$61.66479 \text{ to } 71.62092$$

Estimate of mean of x

$$68.14286$$

Soln ⑥ $H_0: \sigma_1 = \sigma_2$ against $H_1: \sigma_1 \neq \sigma_2$

$$> x = (166, 62, 75, 76, 82, 88, 90, 92)$$

$$> y = (164, 66, 74, 78, 82, 85, 82, 92, 93, 95, 97)$$

Var. test (x, y)

F test to compare two Variances

data: x & y

$$F = 0.788803, \text{num df} = 7, \text{denom df} = 10, P\text{-Value} = 0.7732$$

alternative hypothesis: true ratio of Variances

is not equal to 1

95 Percent Confidence interval:

$$0.199509 \text{ to } 3.751881$$

Sample estimates:

ratio of Variances

$$0.7880255$$

P-Value is greater than 0.05 we accept

Soln ⑦ H_0 at 5% level of significance

$H_0: \mu = 1150$ against $H_1: \mu \neq 1150$

$$> n = 100$$

$$> m_x = 1150$$

$$> m_0 = 1200$$

$$> S_d = 125$$

$$> Z_{cal} = (m_x - m_0) / (S_d / \sqrt{n})$$

> Z_Crit

[1] -1.96

> P Value

[1] 6.334248 P = 0.5

, P Value is less than 0.05 we reject H_0 at

⑧ $H_0: P_2$ against $H_1: P_1 \neq P_2$

$$> n_1 = 200$$

$$> n_2 = 300$$

$$> P_1 = 45/200$$

$$> P_2 = 56/300$$

$$> P = (n_1 * P_1 + n_2 * P_2) / (n_1 + n_2)$$

$$> P$$

$$[1] 0.2$$

$$> q = 1 - P$$

$$[1] 0.8$$

$$> z_{cal} = (P_1 - P_2) / \sqrt{q * ((1/n_1) + (1/n_2))}$$

$$[1] 0.9128704$$

$$> P Value = 2 * (1 - \text{Norm}(abs(z_{cal})))$$

$$> P Value$$

$$[1] 0.3613104$$

P Value is greater than 0.05 we accept H_0 at 5% level of significance

Practical - 9

Aim:- chi Square Test & ANOVA (Analysis of Variance)

- Q1) Use the following data to test whether the conditions of the home and child are independent or not.

Condition of Home

	clean	dirty
clean	70	50
dirty	35	45

> $x = c(70, 80, 35, 50, 20, 45)$

> m = 3

> n = 2

> Y = matrix(x, nrow = m, ncol = n)

> y

[1,]	[1,]	[2,]
70	50	
[2,]	80	20
[3,]	35	45

> PV = chisq.test(y)
> PV

Pearson's Chi-Squared Test

data : y

x - Squared = 25.66, df = 1, P-Value = 2.698e-06

∴ P Value is less than 0.05

∴ We reject H₀

Test the hypothesis that vaccines and diseases are independent or not

Vaccines

	Affected	Not Affected
Affected	70	56
Not Affected	35	37

> X = c(70, 35, 56, 37)

> m = 2

> n = 2

> Y = matrix(X, nrow = m, ncol = n)

> Y

> T = Y[, 1] + Y[, 2]

[1,] 70 56

[2,] 35 37

> PV = chisq.test(Y)

> PV

Pearson's Chi-Squared Test with Yates' Continuity Correction

data : y

x - Squared = 2.0275, df = 1, P-Value = 0.1543

(Q3) Perform ANOVA for following data

Type	Observation
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 55, 55, 55

H_0 : The mean are equal for A, B, C, D

```

> x1 = c(50, 52)
> x2 = c(53, 55, 53)
> x3 = c(60, 58, 57, 56)
> x4 = c(52, 55, 55, 55)

> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "Values" "ind"
> One way. test(Values ~ ind, data=d, var.equal=T)
  One-way analysis of means
data: Values and ind
f: 11.735, num df: 3, denom df: 9, P-value: 0.00183
> anova = aov(Values ~ ind, data=d)
> summary(anova)

```

ind	df	Sum Sq	mean Sq	F Value	P > F
Residual	9	71.06	7.89	11.73	0.0083***
Signif. Codes:					0.001 *** 0.01 ** 0.05 . 0.1 !
					0.05, 0.01

The following data gives the life of the tube of 4 brands

Type	L, f
A	20, 23, 17, 18, 20, 23
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16

H_0 : The average life of A, B, C and D are equal,

$$x_1 = c(20, 23, 17, 18, 20, 23)$$

$$x_2 = c(19, 15, 17, 20, 16, 17)$$

$$x_3 = c(21, 19, 22, 17, 20)$$

$$x_4 = c(15)$$

```

> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "Values" "ind"
```

```

> one way. test(Values ~ ind, data=d, var.equal=T)
  One-way analysis of means
data: Values and ind

```

```

F = 6.8445, num df = 3, denom df = 20
P-Value = 6.002349
  P-Value is less than 0.05 we reject the hypothesis
> anova = aov(Values ~ ind, data=d)
  Signif. Codes: 0.001 *** 0.01 ** 0.05 . 0.1 !
```

ind	df	Sum Sq	mean Sq	F Value	P > F
Residual	20	89.06	4.453	6.8445	6.002349
Signif. Codes:					0.001 *** 0.01 ** 0.05 . 0.1 !

> x = read.csv("C:/users/admin/Desktop/
maths.csv")

> x	State	Maths
1	50	60
2	45	48
3	42	47
4	15	20
5	37	25
6	36	27
7	49	67
8	59	58
9	20	25
10	27	27

> am = mean(x\$State)

> am

[1] 37

> am1 = mean(x\$Maths)

> am1

[1] 89.5

> m1 = median(x\$State)

> m1

[1] 38.5

> m2 = median(x\$Maths)

[1] 37

> n = length(x\$State)

> n

[1] 10

> sd = sqrt((n-1) * var(x\$State)/n)

> sd

[1] 12.64911

> n1 = length(x\$Maths)

> n1

[1] 10

> sd1 = sqrt((n-1) * var(x\$Maths)/n)

> sd1

[1] 15.2

> cor(x\$State, x\$Maths)

[1] 0.830618

Ans
q?

Practical-10

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Aim:- Non Parametric Test

- (Q1) following are the amounts of Sulphur oxid. emitted by industries in 20 days. Apply Signs test to test the hypothesis that the population median is 21.5 at 5% LOS.

17, 15, 20, 24, 19, 18, 22, 23, 27, 9, 24, 20, 17, 6, 24,
13, 15, 23, 24, 26.

H_0 : Population median is 21.5

$$X = (12, 13, 20, \dots, 26)$$

$$> m_e = 21.5$$

$$> S_P = \text{length}(x[x > m_e])$$

$$> S_P$$

[1] 9

$$> S_N = \text{length}(x[x < m_e])$$

$$> S_N$$

[1] 11

$$> n = S_P + S_N$$

$$> n$$

[1] 20

$$> P_V = \text{Pbinom}(S_P, n, 0.5)$$

$$> P_V$$

[1] 0.5119015

Q1) If PV is less than 0.05 we accept H_0 at 5% level of significance

$$H_0: m_e \neq m_c \\ \text{then, } PV = P_{\text{binom}}(Sp, n, 0.5)$$

$$\text{If } H_0: m_e > m_c \text{ then,} \\ PV = P_{\text{binom}}(Sp, n, 0.5)$$

Q2) Following is the data of 10 observations, apply Sign test. The Null Population median is 625. The alternative H_1 is more than 625.

612, 619, 631, 623, 643, 650, 655, 639, 620, 663

$$H_0: \text{Population median} \leq 625 \\ H_1: m_e > 625$$

$$x = ((612, 619, 631, 623, 643, 650, 655, 639, 620, 663))$$

$$> m_e = 625$$

$$> SP = \text{length}(\{x | x > m_e\})$$

$$> Sn = \text{length}(\{x | x \leq m_e\})$$

$$[1] n = Sp + Sn$$

$$> n$$

$$[1] 10$$

$$\rightarrow PV = P_{\text{binom}}(Sp, n, 0.5) \\ \geq P$$

$$630, 655, 627.5$$

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$\therefore PV$ is greater than 0.05 we accept H_0 at

(3) Following are the data of samples. Test the hypothesis that the Population median is 60 against the alternative, i.e. more than 60 at 5%. Test of Significance using Wilcoxon Signed Rank test

63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 69, 58, 66, 72, 63, 87, 69.

$$\rightarrow H_0: m_p \leq 60 \text{ against } H_1: m_p > 60 \\ > x = (63, 65, 60, 89, \dots, 69)$$

Wilcoxon signed rank test ("one tailed" or "greater than 60")

Willcoxon Signed rank test with Continuity Correction

$$V = 145, P\text{-Value} = 0.02298$$

alternative hypothesis: true location is greater than 60

P Value is less than 0.05 we reject H_0 at 5% level of significance

Note:- If (1) $H_0: m_e < m_c$ then alt is "less"

(2) $H_0: m_e \neq m_c$ then alt is "two sided"

data : d
 $v = 4.5$, P-Value = 0.4982
 alternative hypothesis: true location is not equal to 0

\Rightarrow P-Value is greater than 0.05 therefore we accept H_0 .

An
4/3/14

Q4) Using wilcoxon test the population median is 12 or less than 12
 $13, 12, 24, 25, 20, 21, 32, 23, 12, 23, 24, 26$
 Soln:- $H_0: \mu = 12$ against $H_1: \mu < 12$.
 $> x = (13, 12, 24, 25, 20, 21, 32, 28, 12, 23, 24, 26)$
 $> \text{wilcox.test}(x, \text{alt} = \text{"less"}, \mu = 12)$

data : x
 $v = 66$, P-Value = 0.9986
 alternative hypothesis: true location is less than 12
 \because P-Value is greater than 0.05 we accept H_0

Q5) The weight of student before and after they stopped smoking are given below using Wilcoxon test that there is no significant change.

Before	After
65	72
75	74
75	72
62	66
72	73

Soln:- H_0 : Before and after there is no change against
 H_1 : There is change.
 $> x = (65, 75, 75, 62, 72)$
 $> y = (72, 74, 72, 66, 73)$
 $> d = x - y$
 $> \text{wilcox.test}(d, \text{alt} = \text{"two.sided"}, \mu = 0)$

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