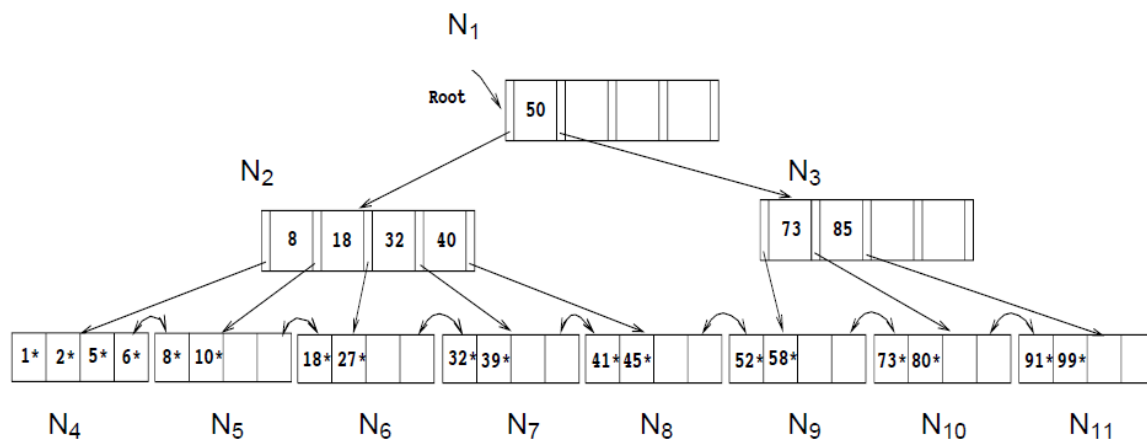


Tutorial 6

Question 1 Consider the B+ tree index of order $p = 5$ shown in the figure below. Answer each of the following questions:

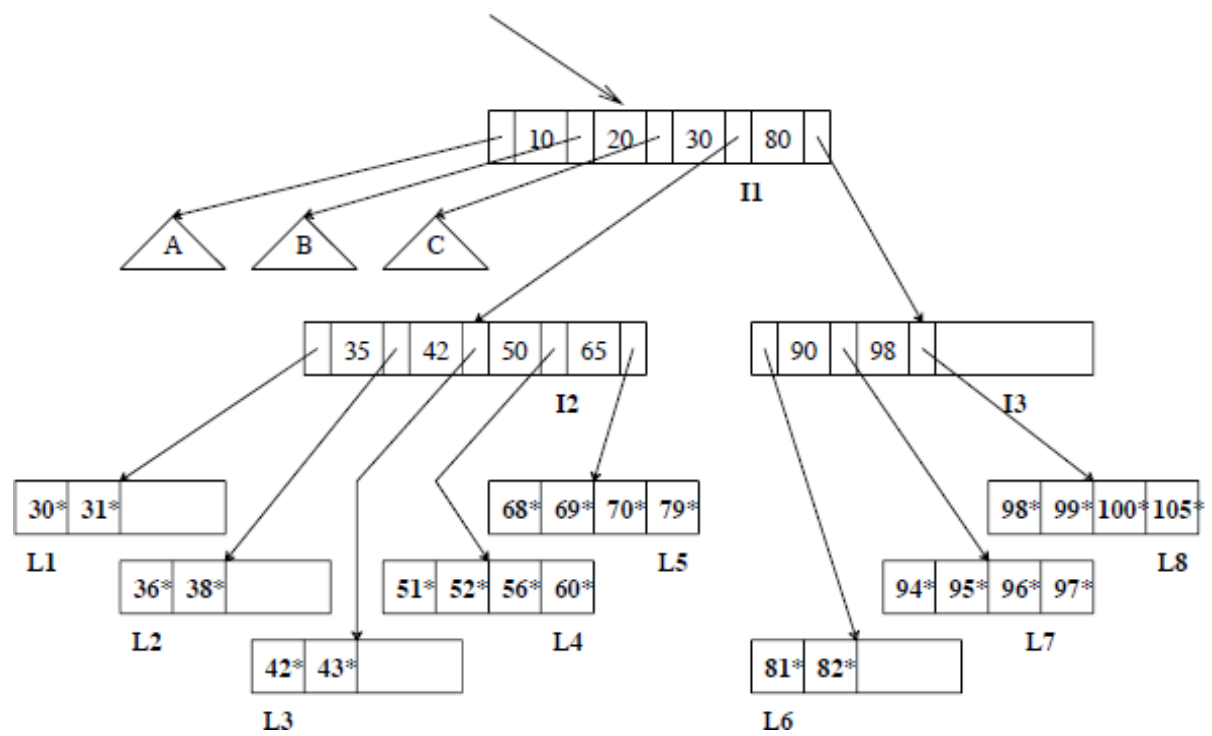
- A. List all the tree nodes that must be visited to answer the following query: “Get all records with search key equal to 10”.
- B. What is the minimum number of tree nodes that must be visited to answer the following query: “Get all records with search key greater than 30”? List all the visited tree nodes.



Question 2 Consider the B+ tree index of order $p = 5$ shown in the figure below. Note that subtrees A, B, and C are not fully specified and their content is not needed for answering this question. Assume that in the case of a leaf node split, the keys are redistributed according to the following rule: 2 keys stay in the old node and the remaining keys are moved to a new node.

Answer each of the following questions:

- A. Name all the tree nodes that must be fetched to answer the following query: “Get all records with search key greater than 38.”
- B. Show the B+ tree that would result from inserting a record with search key 109 into the tree.
- C. Name a search key value such that inserting it into the (original) tree would cause an increase in the height of the tree.



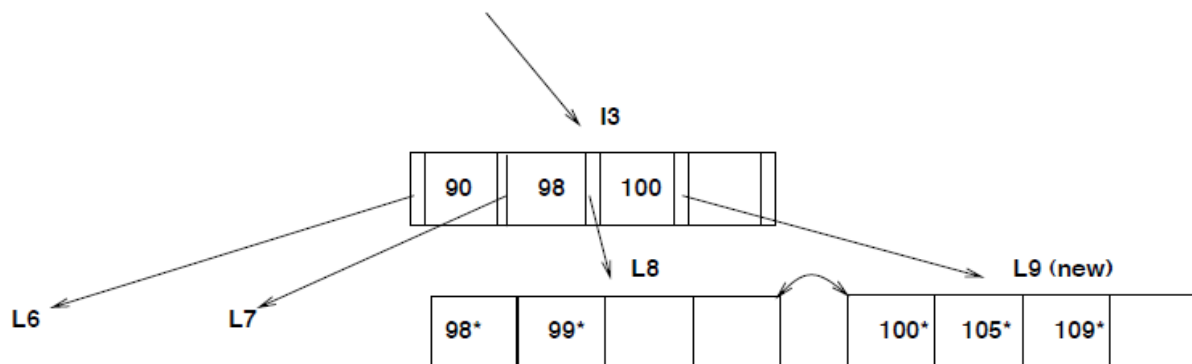
Answers for Question 1 are given below:

- A. We use top-down search in a B+ tree. Nodes N_1 , N_2 , N_5 need to be visited to answer the query “Get all records with search key equal to 10”.
- B. The p_{next} pointers in leaf nodes can be utilized to support range search in the B+ tree. To answer the query “Get all records with search key greater than 30”, we first use “30” to search in the B+ tree, and then follow the p_{next} pointers to fetch all the remaining matching blocks.

In total, there are 8 tree nodes visited: N_1 , N_2 , N_6 , N_7 , N_8 , N_9 , N_{10} , N_{11} .

Answers for Question 2 are given below:

- A. Nodes I_1 , I_2 , and everything in the range $[L_2 \dots L_8]$ must be fetched to answer the query “Get all records with search key greater than 38.”
- B. The resulting subtree nodes are shown below:



Note: Node L_8 is split into two nodes – L_8 and L_9 (new).

- C. There are many search keys X such that inserting X would increase the height of the tree. For example, any search key in the range $[65 \dots 79]$ would suffice. A key in this range would go into L_5 if there were room for it. But since L_5 is full already, it must split. This in turn causes I_2 to split, which causes I_1 to split. Since I_1 is the root node, a new root is created and the tree becomes taller.