FORECASTING IN R



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#### Regression model with ARIMA errors

$$y_t = \beta_0 + \beta_1 x_{1,t} + \cdots + \beta_r x_{r,t} + e_t$$

ullet  $y_t$  modeled as function of r explanatory variables  $x_{1,t},...,x_{r,t}$ 

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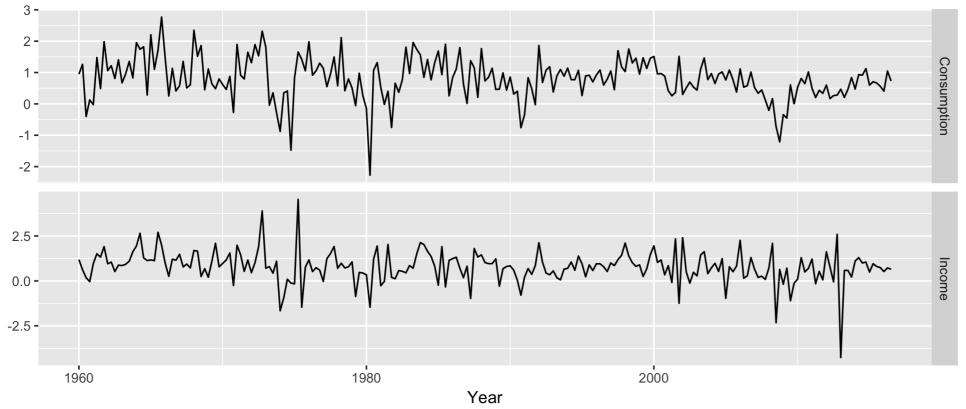
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- ullet  $y_t$  modeled as function of r explanatory variables  $x_{1,t},...,x_{r,t}$
- ullet In dynamic regression, we allow  $e_t$  to be an ARIMA process
- ullet In ordinary regression, we assume that  $e_t$  is white noise

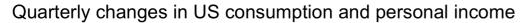
### US personal consumption and income

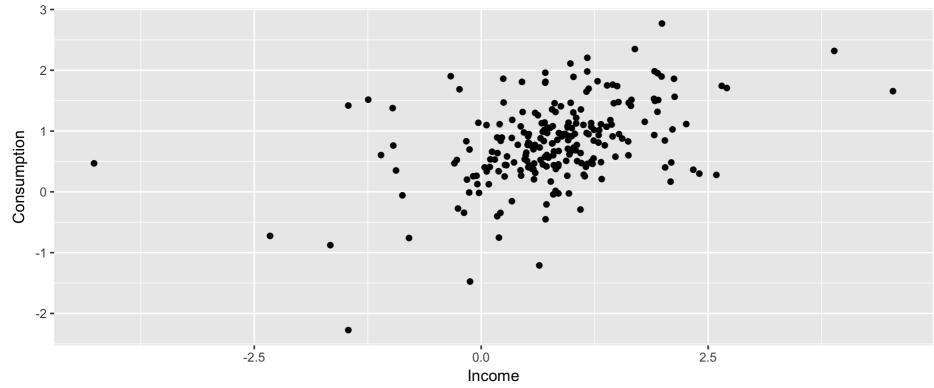






### US personal consumption and income







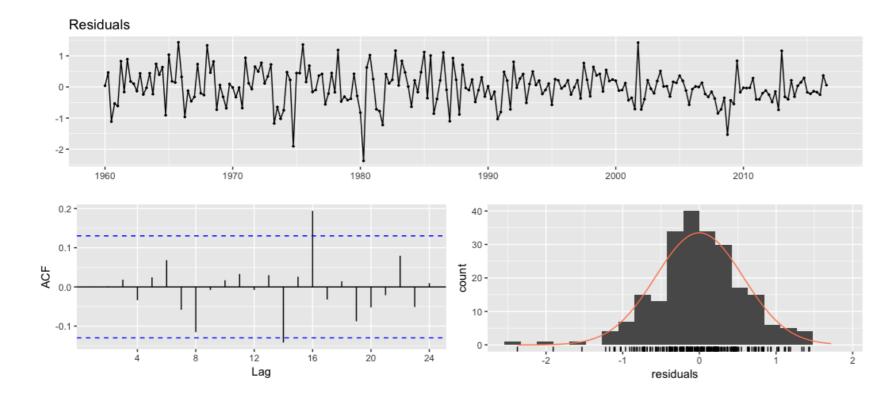
# Dynamic regression model for US personal consumption

```
Series: uschange[, "Consumption"]
Regression with ARIMA(1,0,2) errors
Coefficients:
                       ma2 intercept origxreg
        ar1
             ma1
     0.6191 -0.5424 0.2367
                               0.6099
                                        0.2492
s.e. 0.1422 0.1475 0.0685
                               0.0777
                                        0.0459
sigma^2 estimated as 0.334: log likelihood=-195.22
AIC=402.44
           AICc=402.82
                        BIC=422.99
```

### Residuals from dynamic regression model

checkresiduals(fit)

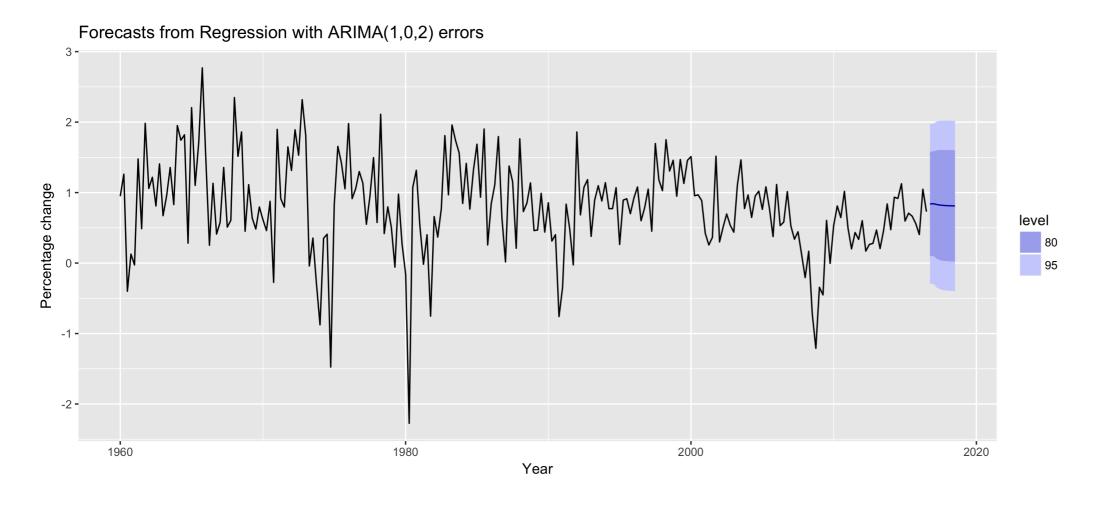
```
Ljung-Box test
data: residuals
Q* = 5.5543, df = 3, p-value = 0.1354
Model df: 5. Total lags used: 8
```





### Forecasts from dynamic regression model

```
fcast <- forecast(fit, xreg = rep(0.8, 8))
autoplot(fcast) +
  xlab("Year") + ylab("Percentage change")</pre>
```





# Let's practice!

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Periodic seasonality can be handled using pairs of Fourier terms:

$$s_k(t) = \sin\left(\frac{2\pi kt}{m}\right)$$
  $c_k(t) = \cos\left(\frac{2\pi kt}{m}\right)$ 

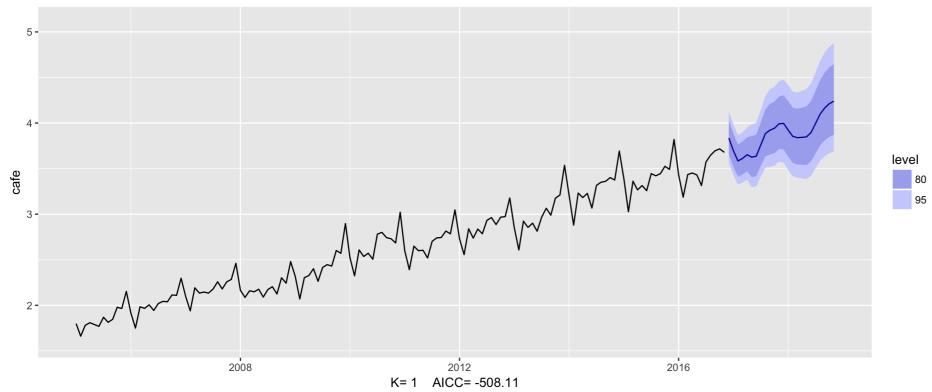
Periodic seasonality can be handled using pairs of Fourier terms:

$$s_k(t) = \sin\left(\frac{2\pi kt}{m}\right)$$
  $c_k(t) = \cos\left(\frac{2\pi kt}{m}\right)$ 

$$y_t = \beta_0 + \sum_{k=1}^K \left[\alpha_k s_k(t) + \gamma_k c_k(t)\right] + e_t$$

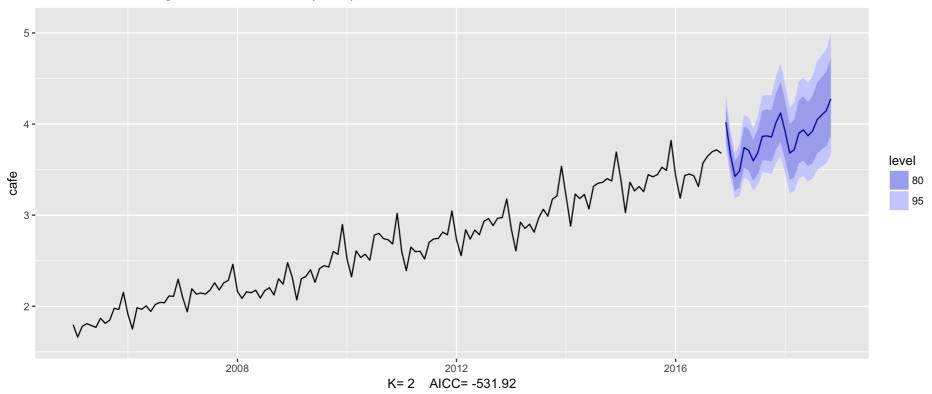
- ullet  $m={\sf seasonal}$  period
- Every periodic function can be approximated by sums of sin and cos terms for large enough K
- Regression coefficients:  $lpha_k$  and  $\gamma_k$
- ullet  $e_t$  can be modeled as a non-seasonal ARIMA process
- Assumes seasonal pattern is unchanging

#### Forecasts from Regression with ARIMA(4,1,5) errors

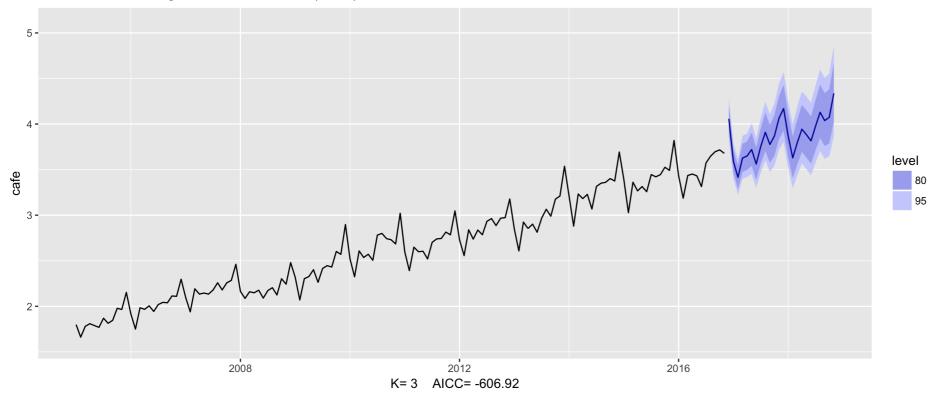


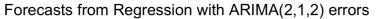


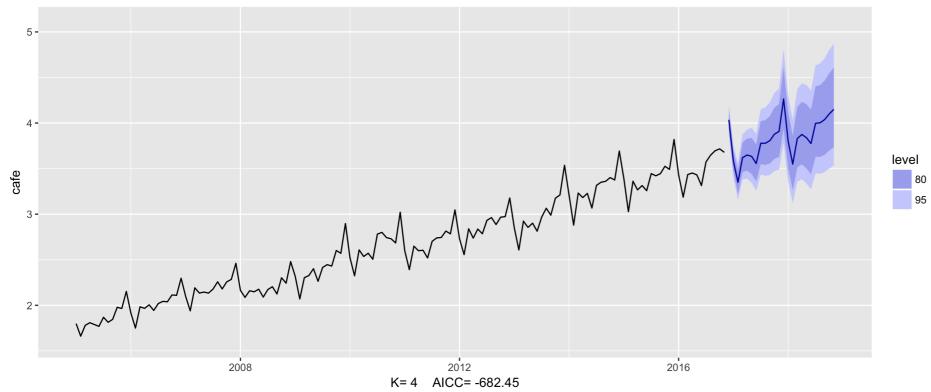
#### Forecasts from Regression with ARIMA(3,1,2) errors

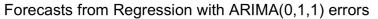


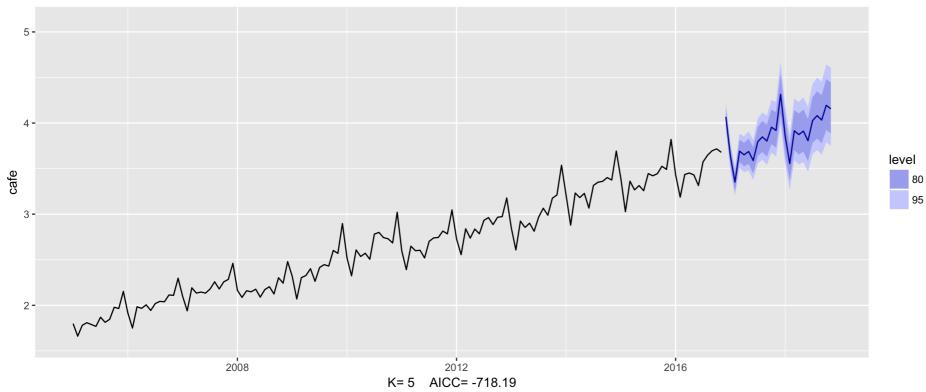
#### Forecasts from Regression with ARIMA(2,1,2) errors





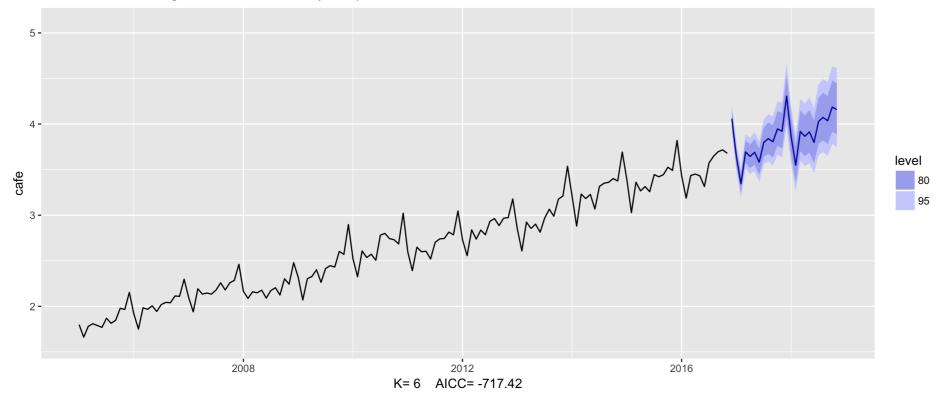








#### Forecasts from Regression with ARIMA(0,1,1) errors



$$y_t = \beta_0 + \beta_1 x_{t,1} + \dots + \beta_{t,r} x_{t,r} + \sum_{k=1}^K [\alpha_k s_k(t) + \gamma_k c_k(t)] + e_t$$

- Other predictor variables can be added as well:  $x_{t,1},...,x_{t,r}$
- Choose K to minimize the  $AIC_c$
- K can not be more than m/2
- This is particularly useful for weekly data, daily data and subdaily data.

# Let's practice!

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### **TBATS** models

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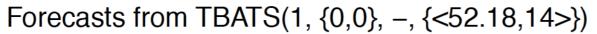


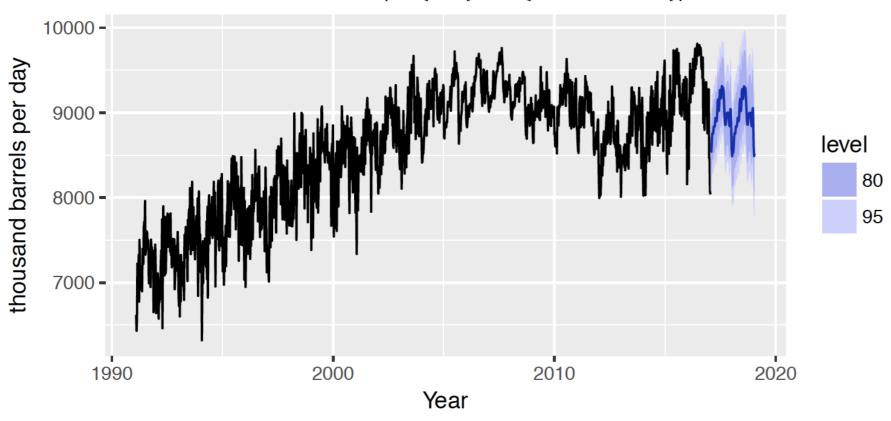
### **TBATS** model

- Trigonometric terms for seasonality
- Box-Cox transformations for heterogeneity
- ARMA errors for short-term dynamics
- Trend (possibly damped)
- Seasonal (including multiple and non-integer periods)

### **US Gasoline data**

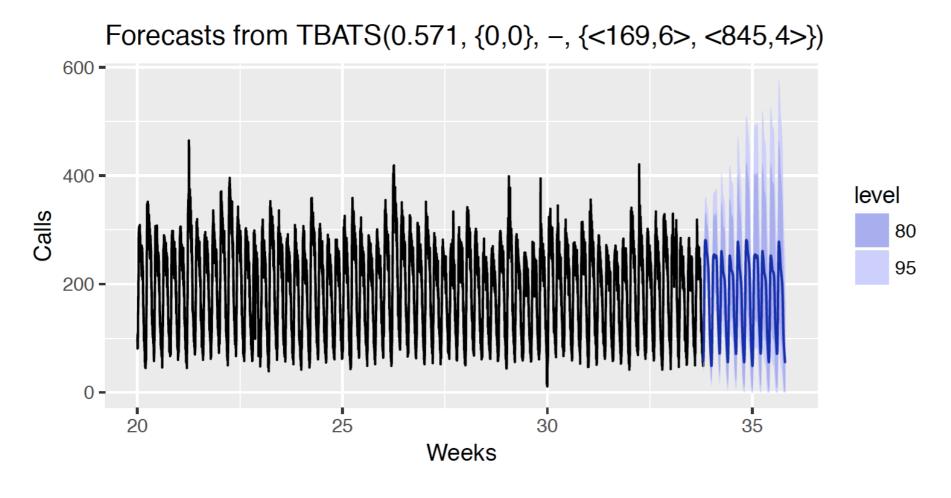
```
gasoline %>% tbats() %>% forecast() %>%
  autoplot() +
  xlab("Year") + ylab("thousand barrels per day")
```





### Call center data

```
calls %>% window(start = 20) %>%
  tbats() %>% forecast() %>%
  autoplot() + xlab("Weeks") + ylab("Calls")
```



### **TBATS** model

- Trigonometric terms for seasonality
- Box-Cox transformations for heterogeneity
- ARMA errors for short-term dynamics
- Trend (possibly damped)
- Seasonal (including multiple and non-integer periods)
- Handles non-integer seasonality, multiple seasonal periods
- Entirely automated
- Prediction intervals often too wide
- Very slow on long series

# Let's practice!

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# Your future in forecasting!

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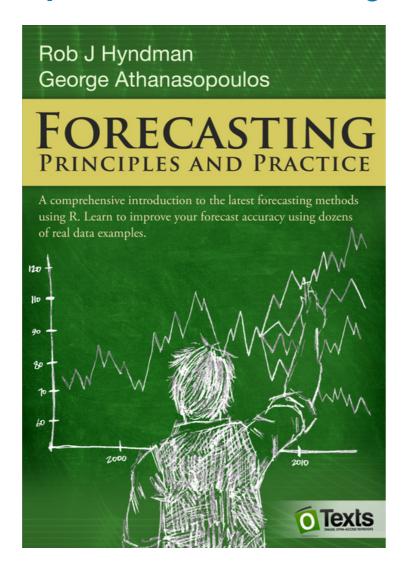
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### Your future in forecasting

Online textbook: https://www.otexts.org/fpp2/



### Your future in forecasting

- Other DataCamp courses:
- ARIMA modeling with R
- Introduction to Time Series Analysis
- Manipulating Time Series Data in R with xts and zoo



### Your future in forecasting

Practice forecasting lots of different time series, using many different methods



# Let's practice!

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