Trend spotting!

TIME SERIES ANALYSIS IN R



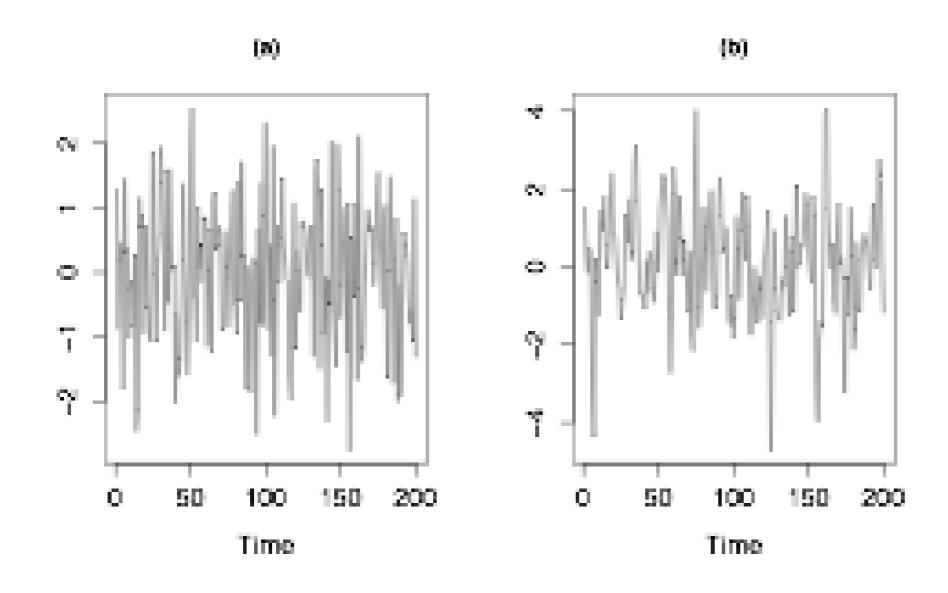
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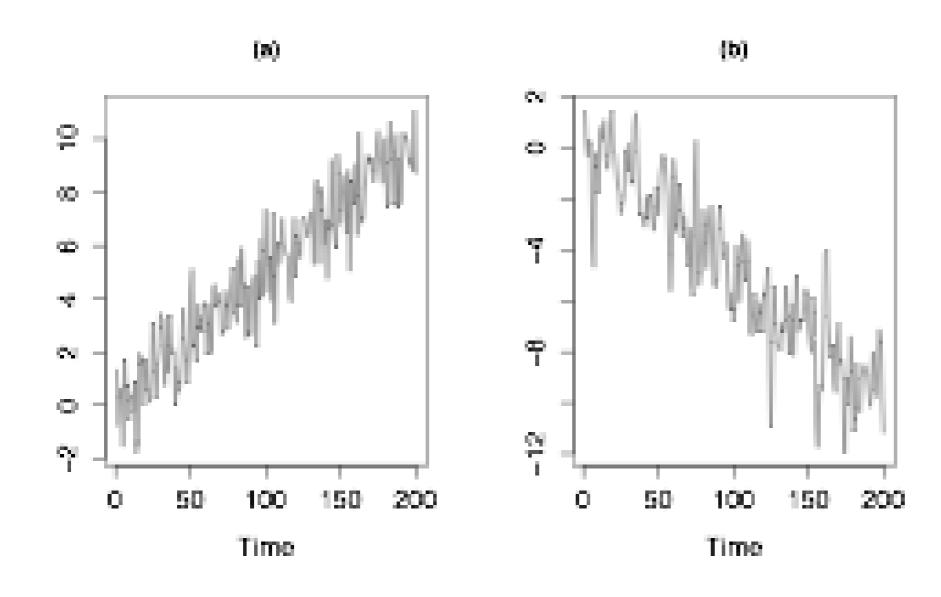
Trends

Some time series do not exhibit any clear trends over time:



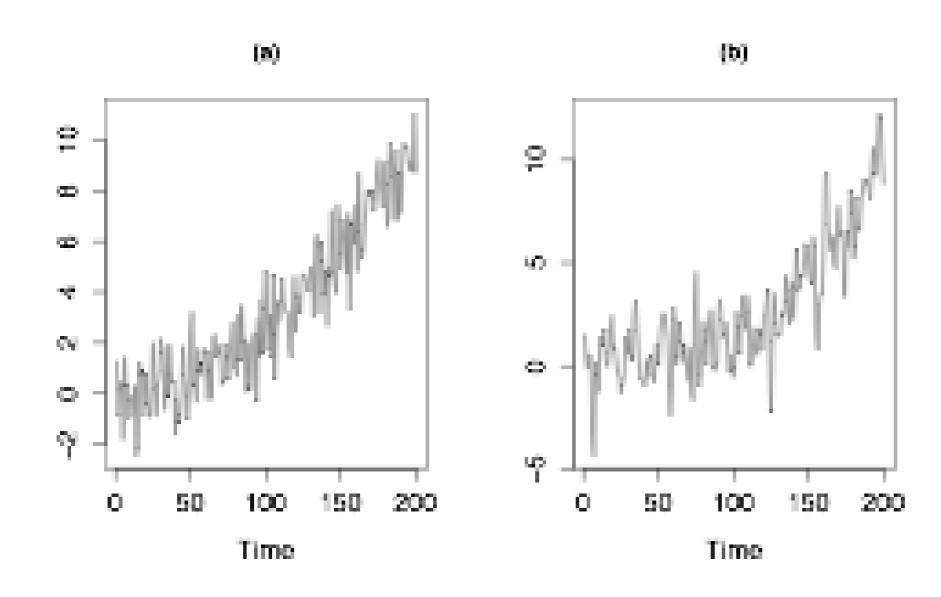
Trends: linear

Examples of linear trends over time:



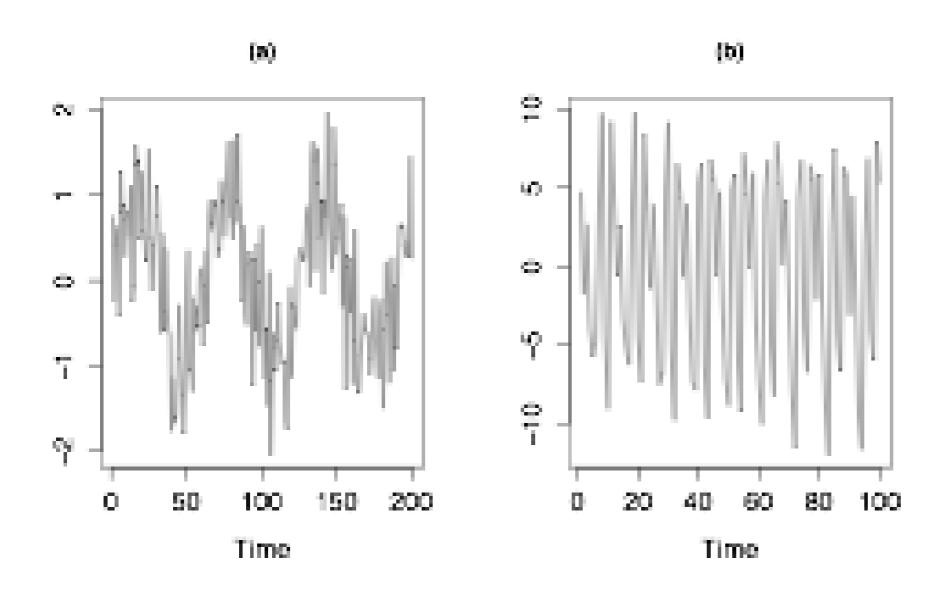
Trends: rapid growth

Examples of rapid growth trends over time:



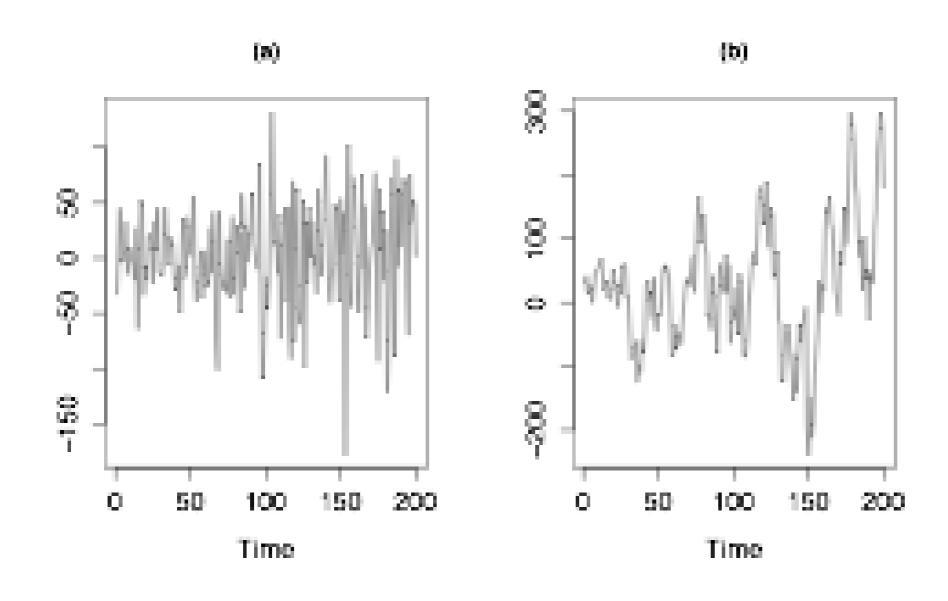
Trends: periodic

Examples of periodic or sinusoidal trends over time:



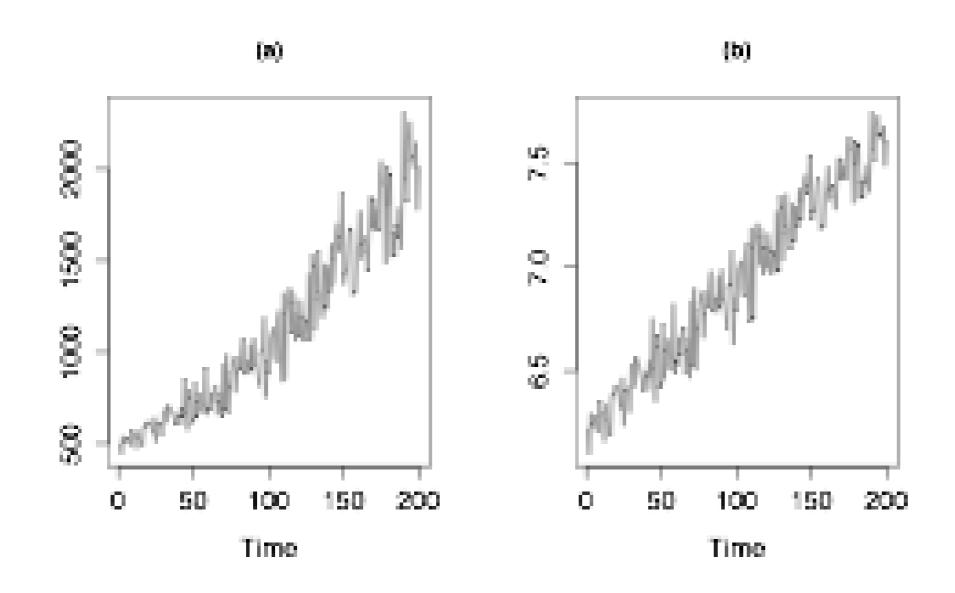
Trends: variance

Examples of increasing variance trends over time:



Sample transformations: log()

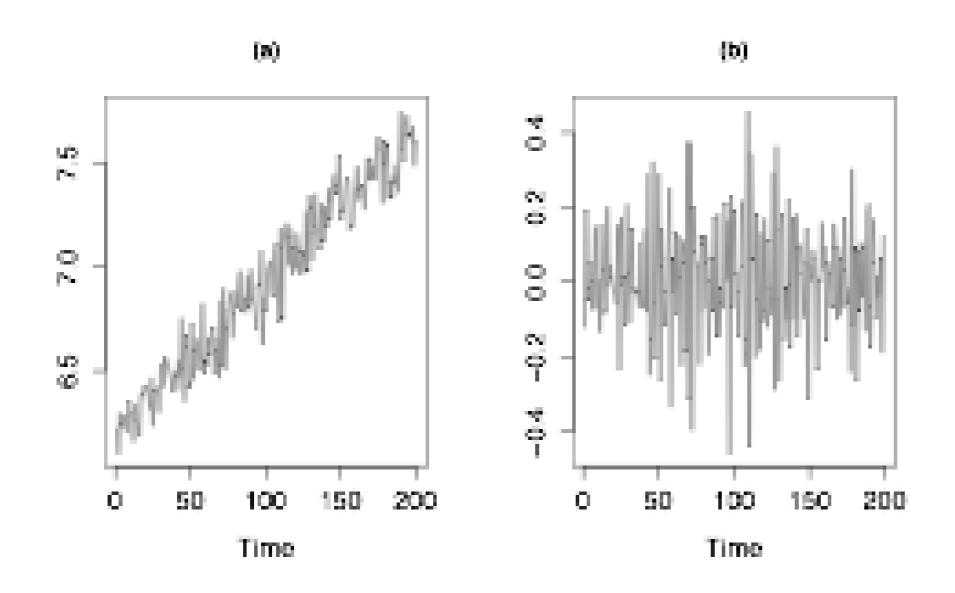
The log() function can linearize a rapid growth trend:





Sample transformations: diff()

The diff() function can remove a linear trend:

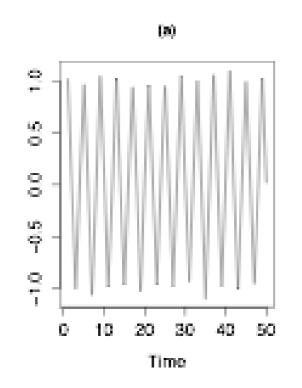


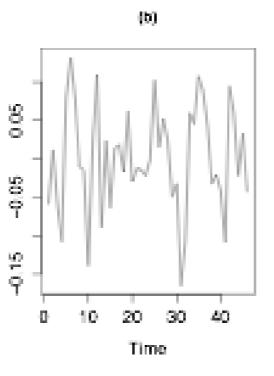


Sample transformations: diff(..., s)

The diff(..., s) function, or seasonal difference transformation, can remove periodic trends.

diff(x, s = 4)





Let's practice!

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The white noise (WN) model

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White noise

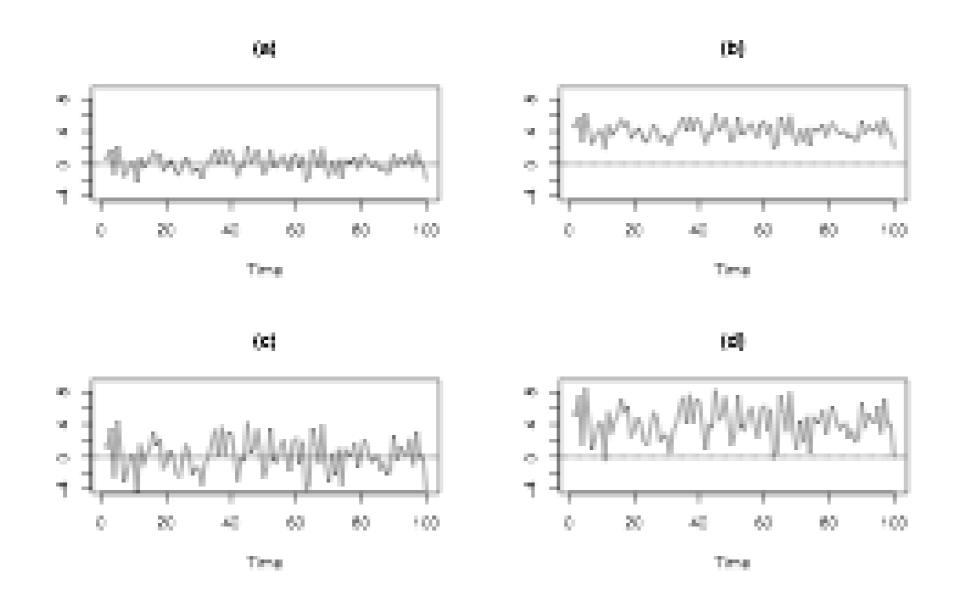
White Noise (WN) is the simplest example of a stationary process.

A weak white noise process has:

- A fixed, constant mean.
- A fixed, constant variance.
- No correlation over time.

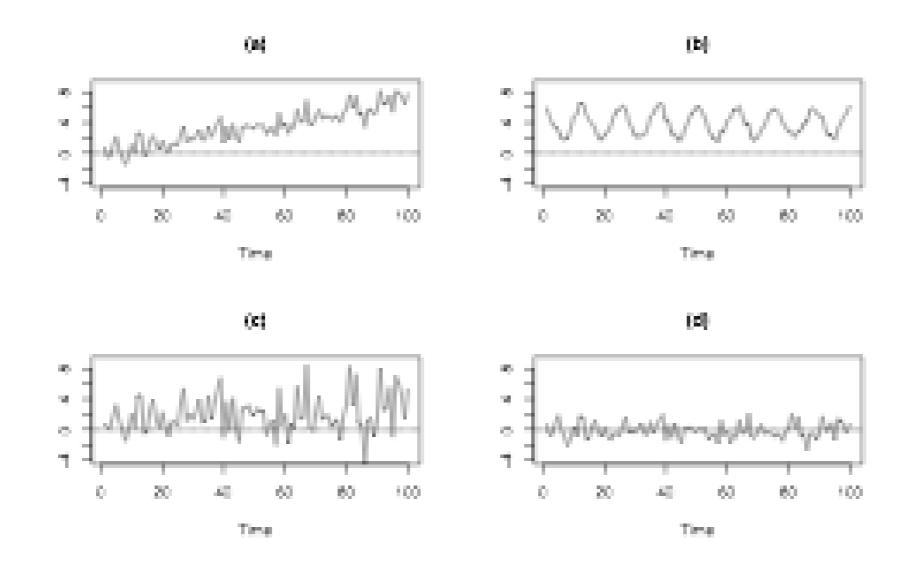
White noise

Time series plots of White Noise:



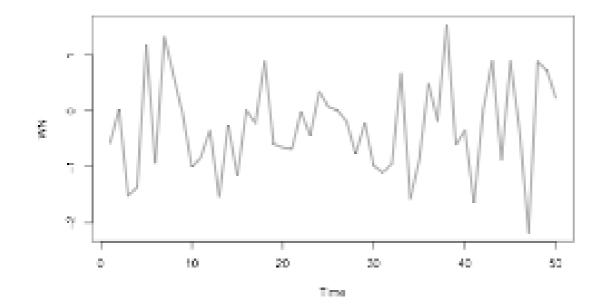
White noise

Time series plots of White Noise?

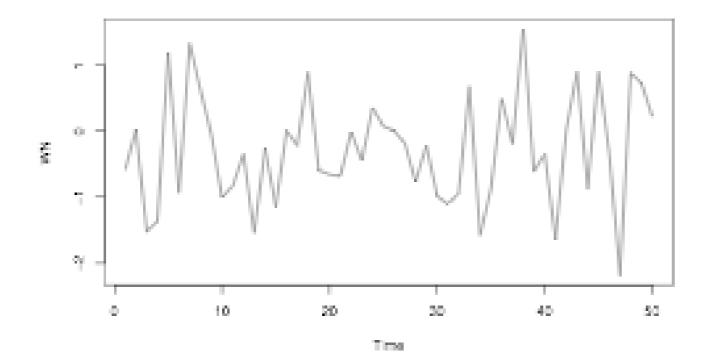


```
-0.005052984 0.042669765 3.261154066 2.486431235 0.283119322 1.543525773
```

ts.plot(WN_1)



ts.plot(WN_2)



Estimating white noise

```
# Fit the WN model with # Calculat # arima()arima(WN_2, # mean and order = # of WN c(0, 0, 0) mean(WN_2)
```

```
# Calculate the sample
# mean and sample variance
# of WN
mean(WN_2)
```

```
Coefficients:

intercept
4.0739
s.e. 0.2698
sigma^2 estimated as 3.639
```

```
4.0739
var(WN_2)
```

3.713

Let's practice!

TIME SERIES ANALYSIS IN R



The random walk (RW) model

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Random walk

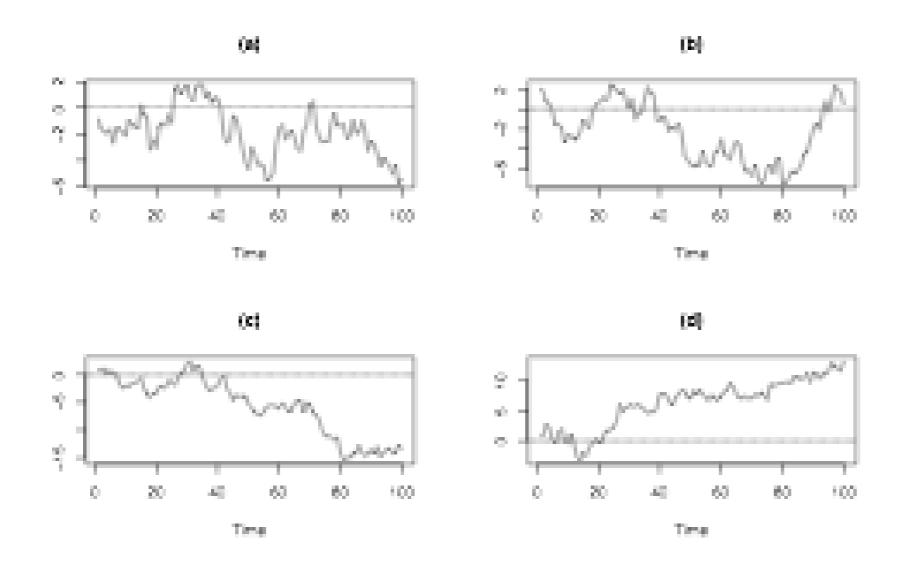
Random Walk (RW) is a simple example of a non-stationary process.

A random walk has:

- No specified mean or variance.
- Strong dependence over time.
- Its changes or increments are white noise (WN).

Random walk

Time series plots of Random Walk:



Random walk

The random walk recursion:

$$Today = Yesterday + Noise$$

More formally:

$$Y_t = Y_{t-1} + \epsilon_t$$

where ϵ_t is mean zero white noise (WN).

- Simulation requires an initial point Y_0 .
- Only one parameter, the WN variance σ_{ϵ}^2 .

Random walk - I

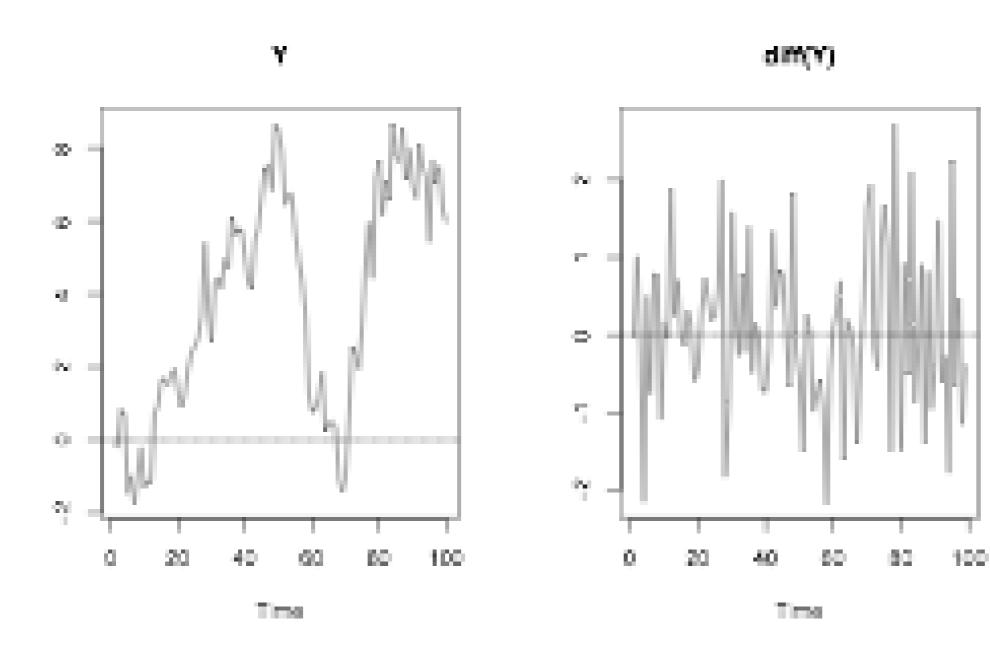
The random walk process:

$$Y_t = Y_{t-1} + \epsilon_t$$

where ϵ_t is mean zero WN

As
$$Y_t - Y_{t-1} = \epsilon_t o exttt{diff(Y)}$$
 is WN

Random walk - II





Random walk with drift - I

The random walk with a drift:

$$Today = Constant + Yesterday + Noise$$

More formally:

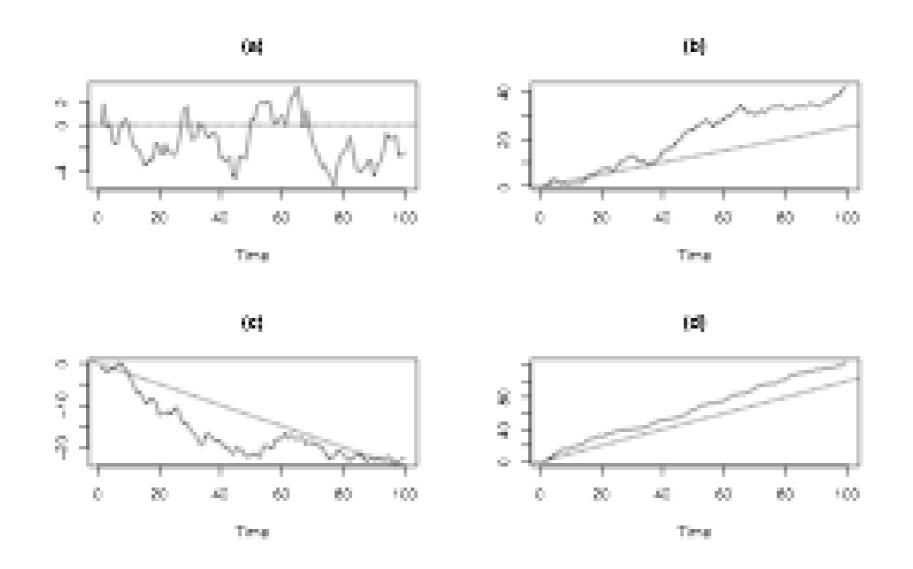
$$Y_t = c + Y_{t-1} + \epsilon_t$$

where ϵ_t is mean zero white noise (WN).

- Two parameters, the constant c , and the WN variance σ_ϵ^2 .
- $Y_t Y_{t-1} = ? o \mathsf{WN}$ with mean c!

Random walk with drift - II

Time series plots of Random Walk with drift:



Let's practice!

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Stationary processes

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Stationarity

- Stationary models are parsimonious.
- Stationary processes have distributional stability over time.

Observed time series:

- Fluctuate randomly.
- But behave similarly from one time period to the next.

Weak stationarity - I

Weak stationary: mean, variance, covariance constant over time.

 Y_1, Y_2 , ...is a weakly stationary process if:

- Mean μ of Y_t is same (constant) for all t.
- Variance σ^2 of Y_t is same (constant) for all t.
- And....

Weak stationarity - II

Covariance of Y_t and Y_s is same (constant) for all |t-s|=h, for all h.

$$Cov(Y_2,Y_5) = Cov(Y_7,Y_{10})$$

since each pair is separated by three units of time.

Stationarity: why?

A stationary process can be modeled with fewer parameters.

For example, we do not need a different expectation for each Y_t ; rather they all have a common expectation, μ .

• Estimate μ accurately by $ar{y}$.

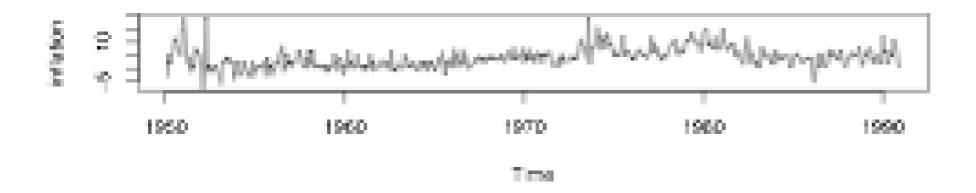
Stationarity: when?

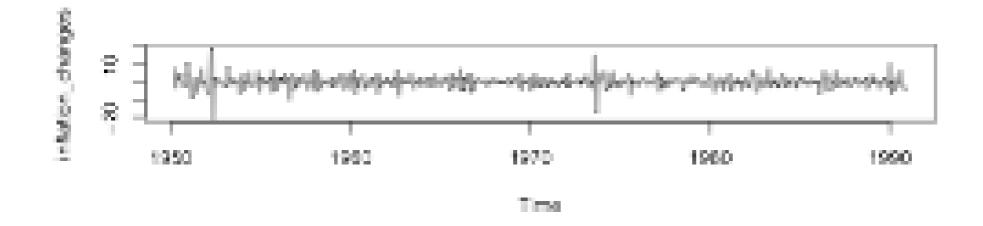
Many financial time series do not exhibit stationarity, however:

- The **changes** in the series are often approximately stationary.
- A stationary series should show random oscillation around some fixed level; a phenomenon called **mean-reversion**.

Stationarity example

Inflation rates and *changes* in inflation rates:







Let's practice!

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