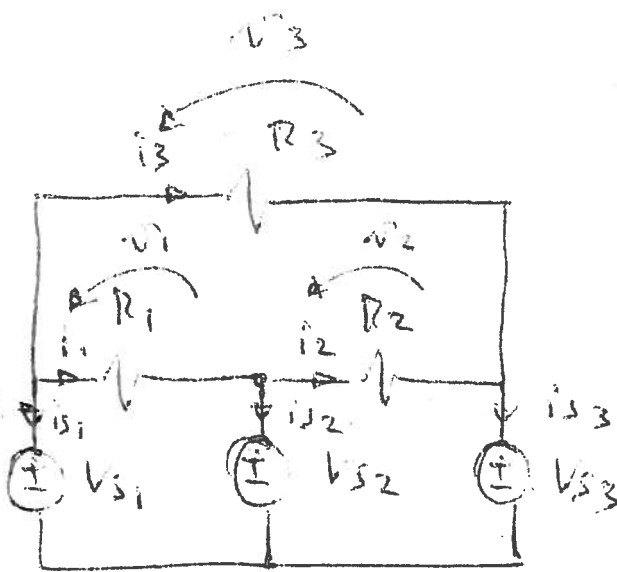


Problema 11

Problema 11

Calcolare tutti le tensioni e tutti le correnti e verificare il bilancio di potenza.

Verificare il bilancio di potenza.



$$V_{S1} = 5V$$

$$V_{S2} = 10V$$

$$V_{S3} = 5V$$

$$R_1 = 100\Omega$$

$$R_2 = 100\Omega$$

$$R_3 = 50\Omega$$

LUT) $V_1 - V_{S1} + V_{S2} = 0 \Rightarrow V_1 = V_{S1} - V_{S2} = -5V$

$V_2 - V_{S2} + V_{S3} = 0 \Rightarrow V_2 = V_{S2} - V_{S3} = 10 - 5 = 5V$

$V_3 - V_{S1} + V_{S3} = 0 \Rightarrow V_3 = V_{S1} - V_{S3} = 0$

Dalle leggi di Ohm:

$$i_1 = \frac{v_1}{R_1} = \frac{-5}{100} = -\frac{1}{20} A$$

$$i_2 = \frac{v_2}{R_2} = \frac{5}{100} = \frac{1}{20} A$$

$$i_3 = \frac{v_3}{R_3} = 0$$

Dalle LK e di conseguenza le i_{s1} , i_{s2} e i_{s3} :

$$i_{s1} + i_1 + i_3 = 0 \Rightarrow i_{s1} = -i_1 = \frac{1}{20} A$$

$$i_{s2} + i_2 - i_1 = 0 \Rightarrow i_{s2} = i_1 - i_2 = \frac{1}{20} - \frac{1}{20} = -\frac{1}{10} A$$

$$i_{s3} - i_2 - i_3 = 0 \Rightarrow i_{s3} = i_2 + i_3 = \frac{1}{20} A$$

Verifichiamo la conservazione dell'energia:

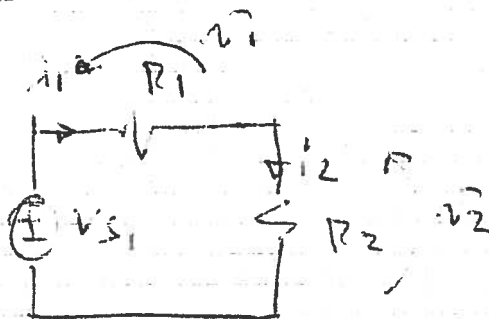
$$v_1 i_1 + v_2 i_2 + v_3 i_3 + v_{s1} i_{s1} + v_{s2} i_{s2} +$$

$$+ v_{s3} i_{s3} = \frac{1}{4} + \frac{1}{4} + 0 + \frac{1}{4} - 1 + \frac{1}{4} = 0$$

ESERCIZIO 12

Calcolare v_1 e v_2

X



$$V_{S1} = 20V$$

$$R_1 = 2\Omega$$

$$R_2 = 3\Omega$$

$$i_1 = i_2 = i$$

$$v_1 = R_1 i$$

$$v_2 = R_2 i \Rightarrow$$

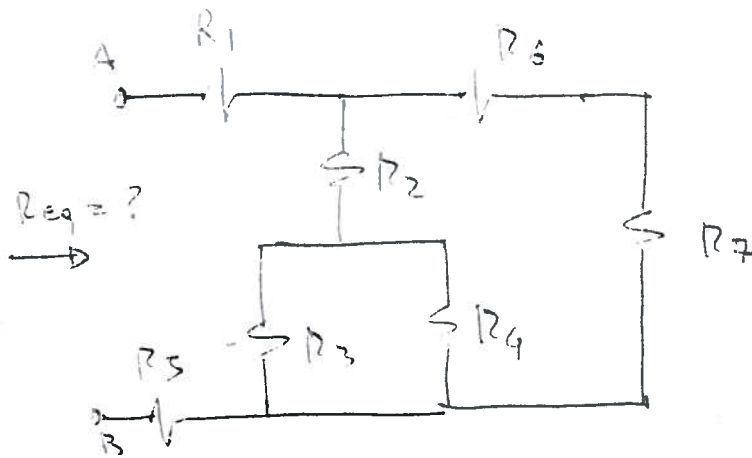
$$v_{S1} - v_1 - v_2 = 0 \Rightarrow v_{S1} - R_1 i - R_2 i = 0 \Rightarrow$$

$$i = \frac{V_{S1}}{R_1 + R_2} = \frac{20}{5} = 4A$$

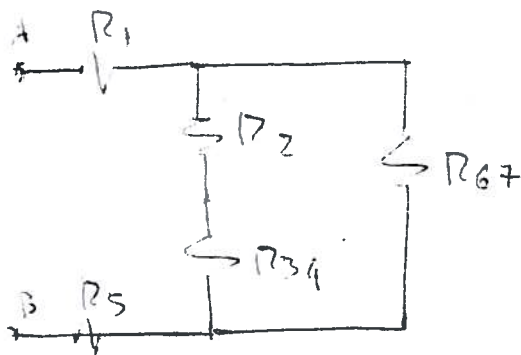
$$v_1 = R_1 i = V_{S1} \frac{R_1}{R_1 + R_2} = 8V$$

$$v_2 = R_2 i = V_{S1} \frac{R_2}{R_1 + R_2} = 12V$$

ESEMPIO DI RESISTENZE EQUIVALENTI



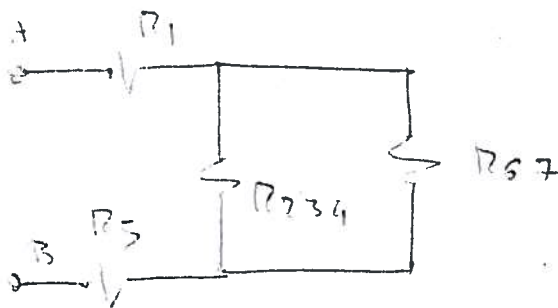
$$\begin{aligned} R_1 &= 4 \Omega \\ R_2 &= 2 \Omega \\ R_3 &= 6 \Omega \\ R_4 &= 3 \Omega \\ R_5 &= 8 \Omega \\ R_6 &= 1 \Omega \\ R_7 &= 5 \Omega \end{aligned}$$



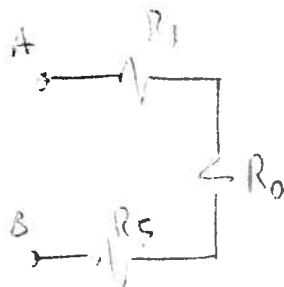
$$\begin{aligned} R_{67} &= R_6 + R_7 = 6 \Omega \\ R_{34} &= R_3 + R_4 = 9 \Omega \end{aligned}$$

$$\frac{1}{R_{34}} = \frac{1}{R_3} + \frac{1}{R_4} = \frac{1}{6} + \frac{1}{3} = \frac{1}{2} \text{ S}$$

$$\Rightarrow R_{34} = 2 \Omega$$



$$R_{234} = 4 \Omega$$



$$\begin{aligned} \frac{1}{R_0} &= \frac{1}{R_{234}} + \frac{1}{R_{67}} = \frac{1}{4} + \frac{1}{6} = \\ &= \frac{6+4}{24} = \frac{5}{12} \text{ S} \end{aligned}$$

$$\Rightarrow R_0 = \frac{12}{5} \Omega$$

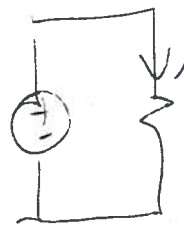
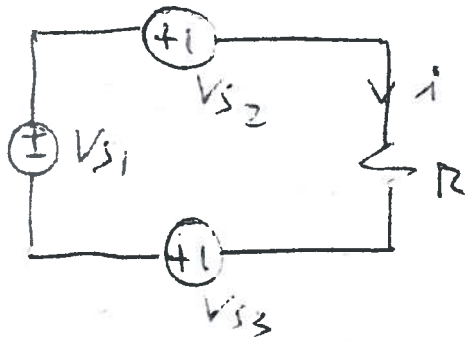
$$R_{AB} = R_1 + R_5 + R_0 =$$

$$= 4 + 8 + \frac{12}{5} = 12 + \frac{12}{5} = \frac{72}{5} \Omega$$

ESERCIZIO 13

Calcolare la corrente i

⑦



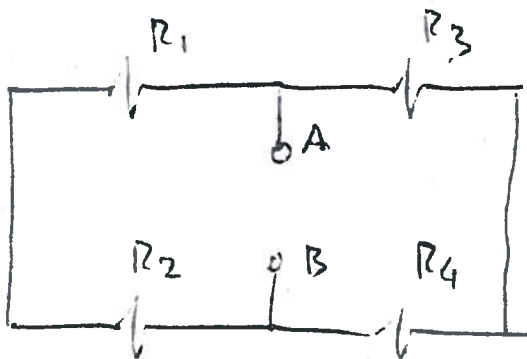
$$\begin{aligned} V_{S1} &= 4V \\ V_{S2} &= 2V \\ V_{S3} &= 8V \\ R &= 2\Omega \end{aligned}$$

ND

$$i = \frac{V_{S1} - V_{S2} + V_{S3}}{R} = \frac{4 - 2 + 8}{2} = 5A$$

ESERCIZIO 14 Calcolare la resistenza equivalente

① X



$$\begin{aligned} R_1 &= 2\Omega \\ R_2 &= 4\Omega \\ R_3 &= 1\Omega \\ R_4 &= 1\Omega \end{aligned}$$

$$\begin{aligned} R_{AB} &= (R_1 + R_2) \parallel (R_3 + R_4) = 6 \parallel 2 = \frac{1}{\frac{1}{6} + \frac{1}{2}} = \\ &= \frac{3}{2} \Omega \end{aligned}$$

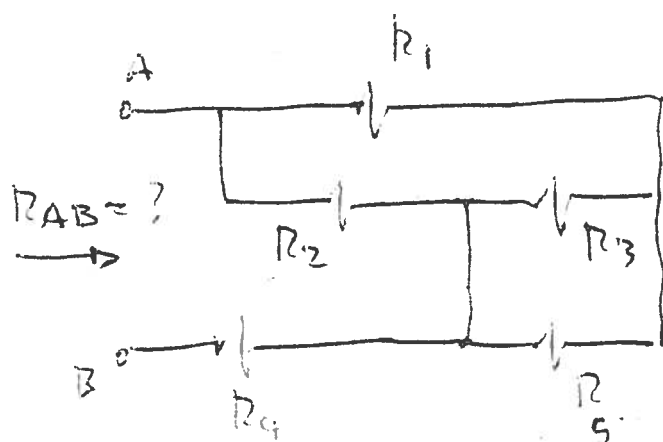
~~ESERCIZIO 13~~

ESEMPI 16

Calcolare la resistenza equivalente

②

X



$$R_1 = \frac{2}{3} \Omega$$

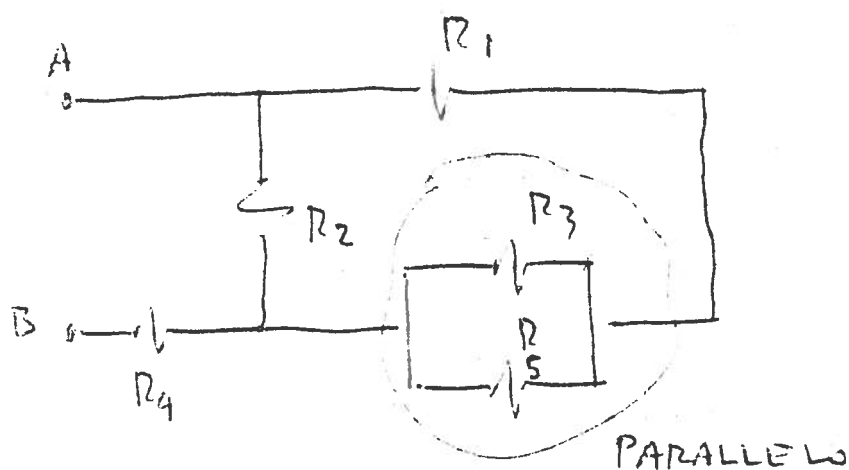
$$R_2 = 2 \Omega$$

$$R_3 = 4 \Omega$$

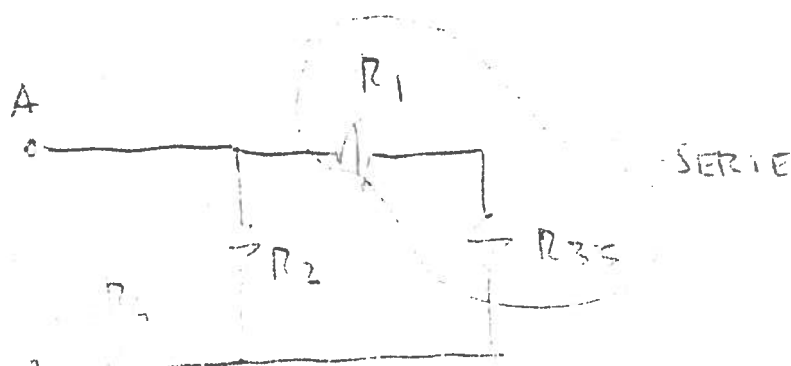
$$R_4 = 1 \Omega$$

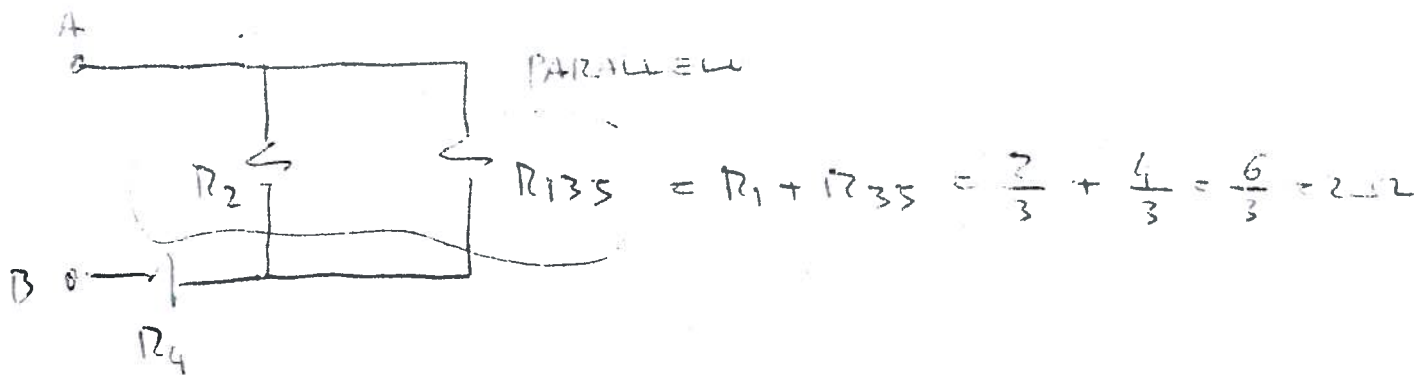
$$R_5 = 2 \Omega$$

Ridisegnare il circuito



$$R_{35} = R_3 // R_5 = \frac{1}{\frac{1}{R_3} + \frac{1}{R_5}} = \frac{1}{\frac{1}{4} + \frac{1}{2}} = \frac{4}{3} \Omega$$



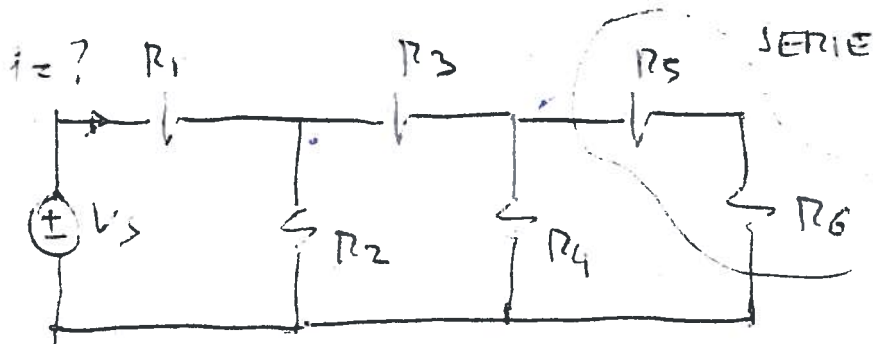


$$R_0 = R_2 \parallel R_{135} = \frac{1}{\frac{1}{R_2} + \frac{1}{R_{135}}} = \frac{1}{\frac{1}{2} + \frac{1}{2}} = 1\Omega$$

$$R_{AB} = R_0 + R_4 = 2\Omega$$

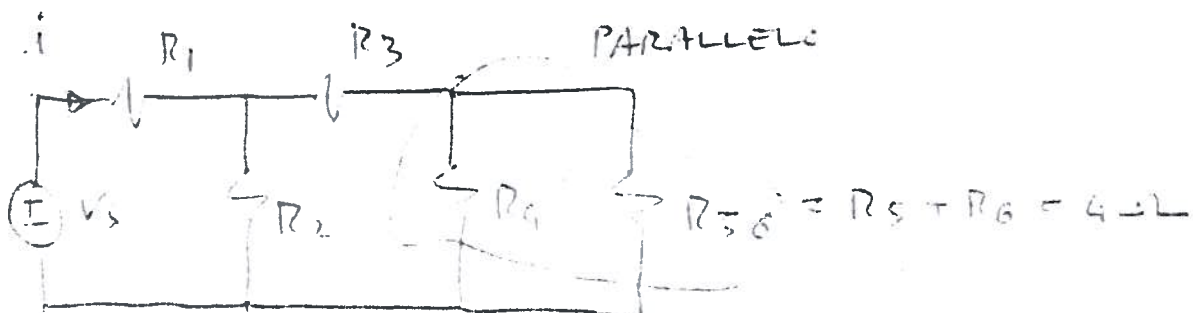
③ X

ESERCIZIO 16 Calcolare la corrente i

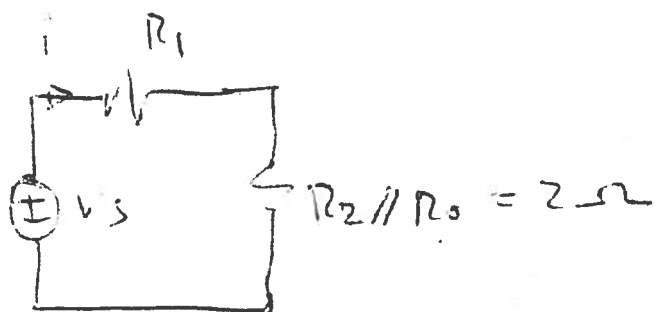
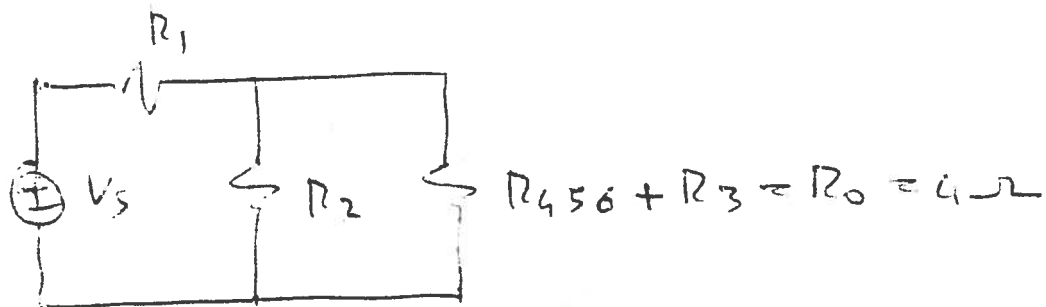


$$\begin{aligned} V_s &= 50V \\ R_1 &= 2\Omega \\ R_2 &= 4\Omega \\ R_3 &= 2\Omega \\ R_4 &= 4\Omega \\ R_5 &= 2\Omega \\ R_6 &= 2\Omega \end{aligned}$$

Semplificare il circuito tramite il concetto di resistenza equivalente



$$R_{456} = R_4 // R_{56} = \frac{1}{\frac{1}{4} + \frac{1}{4}} = 2 \Omega$$

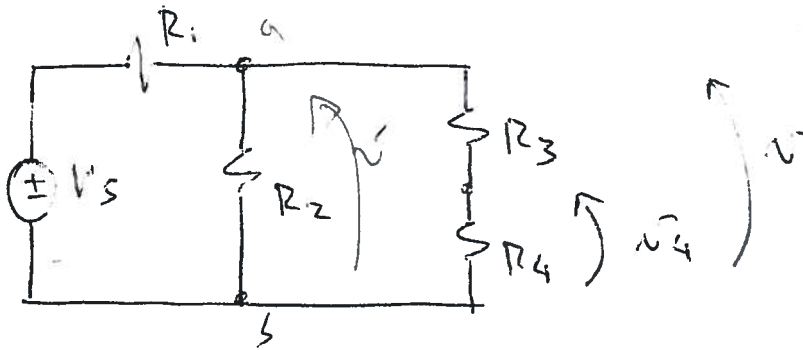


$$i = \frac{V_s}{R_1 + R_2 // R_0} = \frac{25}{2} \text{ A}$$

10 Magnitude of Answer is 13

Calcolare v_4 e v .

④ X



$$V_s = 10V$$

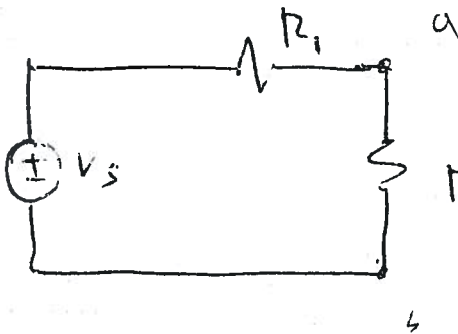
$$R_1 = 1\Omega$$

$$R_2 = 2\Omega$$

$$R_3 = 3\Omega$$

$$R_4 = 1\Omega$$

$$R_0 = R_2 \parallel (R_3 + R_4) = \frac{1}{\frac{1}{2} + \frac{1}{4}} = \frac{4}{3} \Omega$$



$$v = V_s \frac{R_0}{R_0 + R_1} = \frac{40}{7} V$$

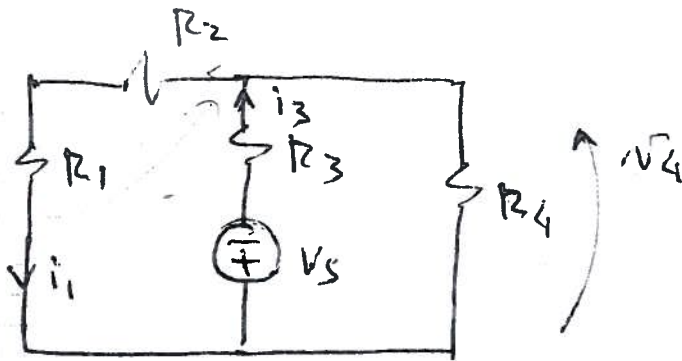
 Per calcolare v_4 si torna al circuito di partenza

$$v_4 = v \frac{R_4}{R_3 + R_4} = \frac{10}{7} V$$

PARTITORE DI TENSIONE

⑤ X

Calcolare i_3 , v_4 e i_3



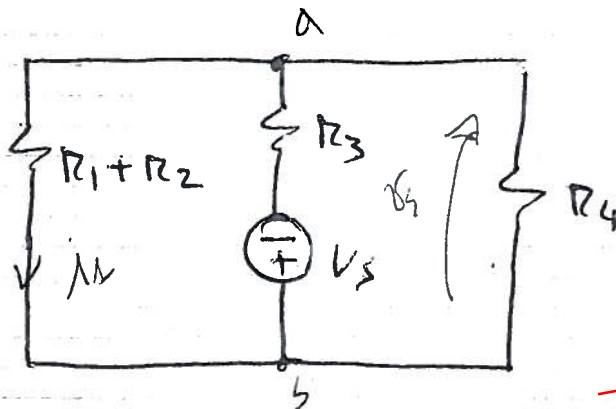
$$V_S = 6V$$

$$R_1 = R_2 = 1\Omega$$

$$R_3 = 3\Omega$$

$$R_4 = 2\Omega$$

R_1 e R_2 sono in serie



$(R_1 + R_2)$ e R_4 sono in parallelo

$$R_{12} = R_1 + R_2 = 2\Omega$$

$$G_{12} = \frac{1}{R_1 + R_2} = \frac{1}{2} S$$

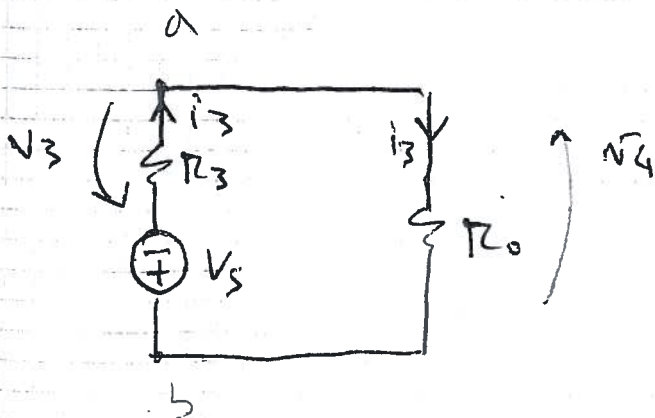
$$G_4 = \frac{1}{R_4} = \frac{1}{2} S$$

$$G_0 = G_{12} + G_4 = 1 S, \quad R_0 = \frac{1}{G_0}$$

$$V_4 = R_0 i_3$$

$$R_0 = R_{12} // R_4 = 1\Omega$$

$$V_3 = R_3 i_3$$



$$V_3 + V_S + V_4 = 0 \Rightarrow (R_3 + R_0) i_3 = -V_S$$

$$i_3 = - \frac{V_S}{R_0 + R_3} = - \frac{3}{2} A$$

$$V_4 = R_0 i_3 = -\frac{3}{2} V$$

$$i_1 = \frac{V_4}{R_1 + R_2} = -\frac{3}{4} A$$

$$V_4 = -\frac{v_s R_0}{R_0 + R_3} = -\frac{3}{2} V$$

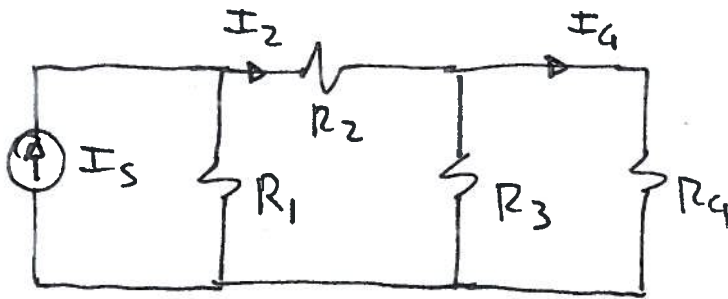
$$i_3 = \frac{V_4}{R_0} = -\frac{3}{2} A$$

$$i_1 = \frac{V_4}{R_1 + R_2} = -\frac{3}{4} A$$

ESERCIZIO 2

Determinare I_2 e I_4

⑥ X



$$I_s = 5 \text{ A}$$

$$R_1 = 3 \Omega$$

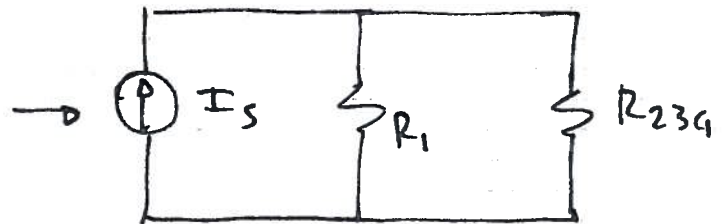
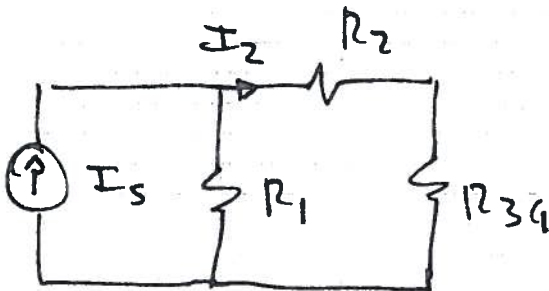
$$R_2 = 1 \Omega$$

$$R_3 = 2 \Omega$$

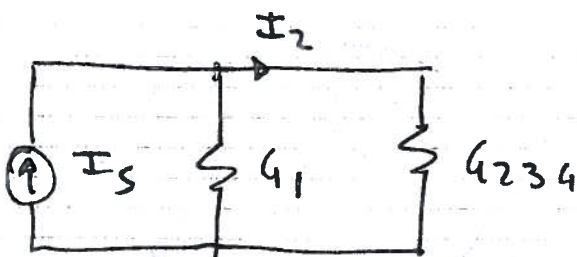
$$R_4 = 2 \Omega$$

~~$$G_{34} = G_3 + G_4 = \frac{1}{2} + \frac{1}{2} = 1 \text{ S} \Rightarrow R_{34} = 1 \Omega$$~~

$$R_{34} = R_3 // R_4 = 1 \Omega$$



$$R_{234} = R_2 + R_{34} = 2 \Omega$$



~~$$G_1 = \frac{1}{R_1} = \frac{1}{3} \text{ S}$$~~

~~$$G_{234} = \frac{1}{R_{234}} = \frac{1}{2} \text{ S}$$~~

~~$$I_2 = I_s \cdot \frac{G_{234}}{G_1 + G_{234}} = 5 \cdot \frac{\frac{1}{2}}{\frac{1}{3} + \frac{1}{2}} = 3 \text{ A}$$~~

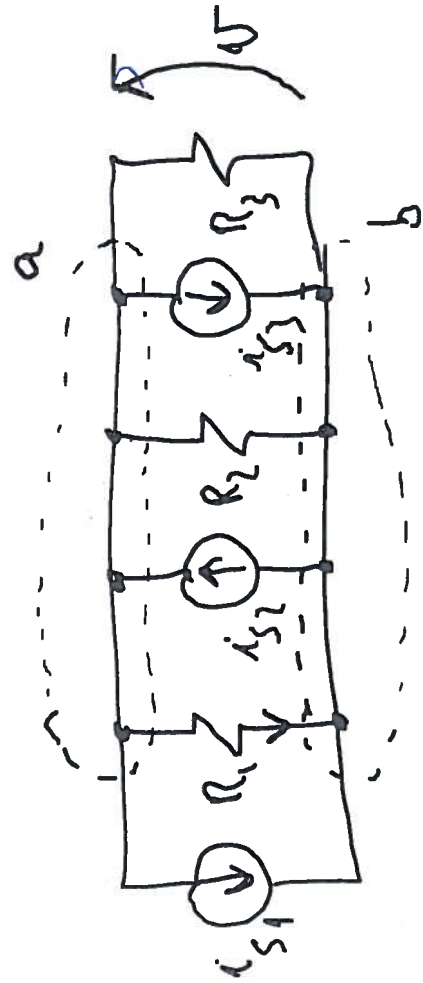
Torniamo al circuito di partenza:

~~$$I_4 = I_2 \cdot \frac{G_4}{G_3 + G_4} = \frac{3}{2} \text{ A}$$~~

$$I_2 = I_S \frac{R_1}{R_1 + R_{235}} = 3A$$

$$I_4 = I_2 \frac{R_4}{R_2 + R_4} = \frac{3}{2} A$$

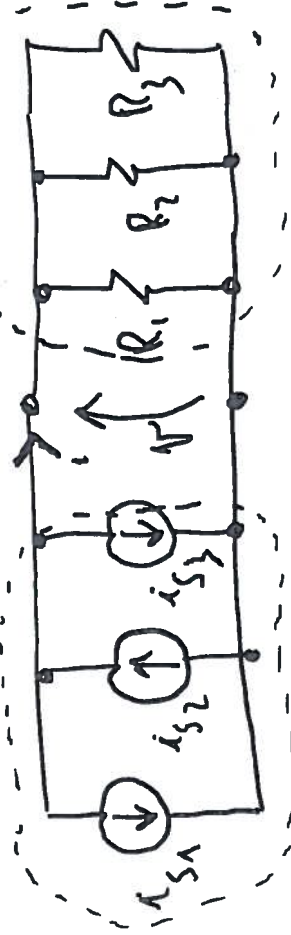
CIRCUITI BINODALI



$$i_{s1} = 1 \text{ A} \quad i_{s2} = 2 \text{ A} \quad i_{s3} = 3 \text{ A}$$

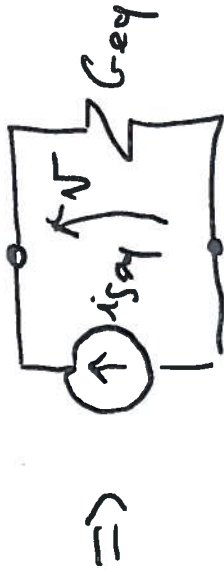
$$R_1 = 1 \Omega \quad R_2 = \frac{1}{2} \Omega \quad R_3 = \frac{1}{3} \Omega$$

LKC a (oppure b) + L Ω \Rightarrow $V = \dots$



$$i = -i_{s1} + i_{s2} - i_{s3} = i_{seq}$$

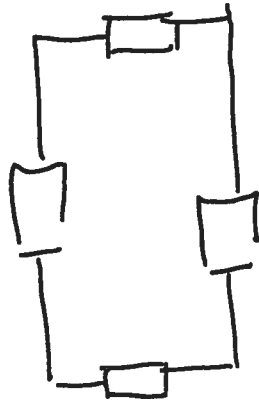
$$G_{eq} = G_1 + G_2 + G_3$$



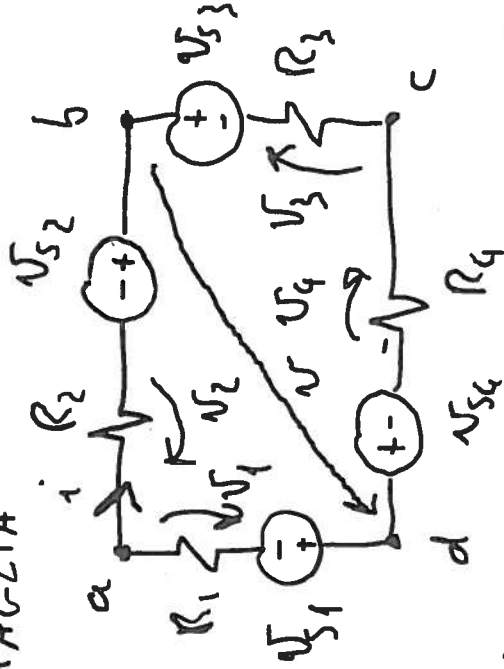
$$V = \frac{i_{seq}}{-\frac{1}{3} V G_{eq}} = \frac{-i_{s1} + i_{s2} - i_{s3}}{G_1 + G_2 + G_3}$$

\Rightarrow NODALI

CIRCUITI A UNA MAGLIA



$$\begin{aligned} V_{S1} &= 1V & V_{S2} &= 2V \\ V_{S3} &= 3V & V_{S4} &= 4V \\ R_1 &= 1\Omega & R_2 &= 2\Omega \\ R_3 &= 3\Omega & R_4 &= 4\Omega \end{aligned}$$



$$\text{LKT} \quad -V_{S1} - V_1 - V_2 + V_{S2} - V_{S3}$$

$$-V_3 - V_4 + V_{S4} = 0$$

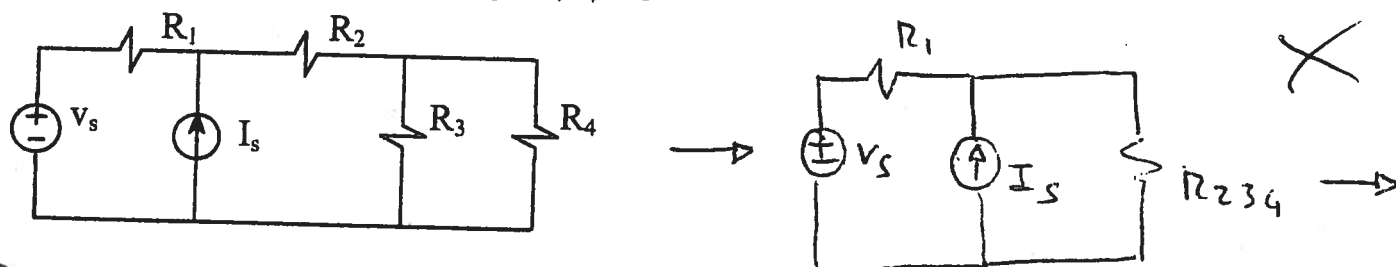
$$\begin{aligned} \Rightarrow i &= \frac{-V_{S1} + V_{S2} - V_{S3} + V_{S4}}{R_1 + R_2 + R_3 + R_4} \\ &= \frac{1}{5} A \end{aligned}$$

$$V_1 = R_1 i \quad V_2 = R_2 i \quad V_3 = R_3 i \quad V_4 = R_4 i$$

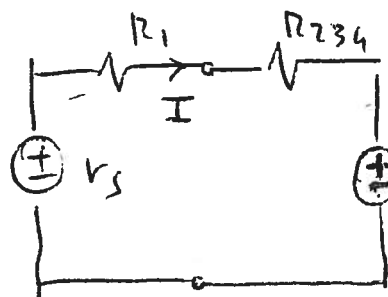


$$V = V_{S1} - V_{S2} + (R_1 + R_2) i = -\frac{2}{5} V$$

Esercizio 2 (*): Nel circuito di figura, funzionante in regime stazionario, calcolare la potenza generata da V_s .
 Dati: $V_s = 12 \text{ V}$; $I_s = 2 \text{ A}$; $R_1 = 6 \Omega$; $R_2 = 6 \Omega$; $R_3 = 4 \Omega$; $R_4 = 2 \Omega$



$$R_{234} = R_2 + R_3 // R_4 = \frac{22}{3} \Omega \approx 7,3 \Omega$$



$$I = \frac{V_s - R_{234} I_s}{R_1 + R_{234}} = -0,2 \text{ A}$$

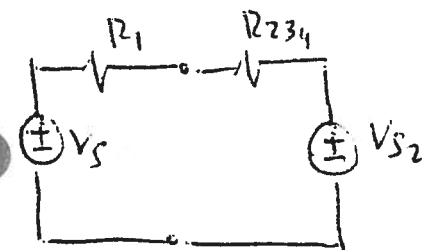
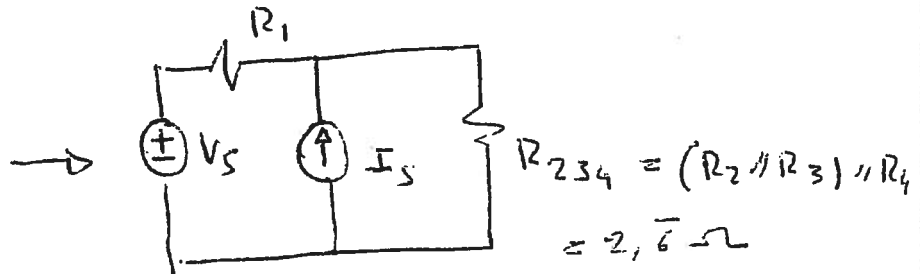
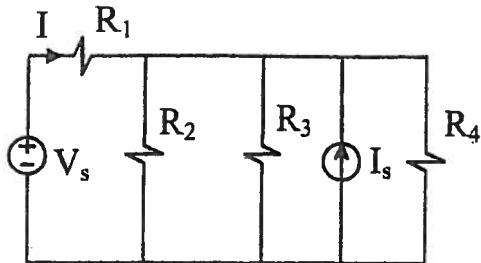
$$P_{V_s} = V_s I = -2,4 \text{ W}$$

POLITECNICO DI MILANO

Insegnamento di Elettrotecnica - Ing. Edile - Nuovo Ordinamento - Prof. L. Di Rienzo

Prova d'esame del 21 settembre 2005 - Parte I

ND

Esercizio 1: Nel circuito resistivo di figura determinare il valore della corrente I .Dati: $V_S = 10$ V; $I_S = 10$ A; $R_1 = 5$ Ω ; $R_2 = 6$ Ω ; $R_3 = 8$ Ω ; $R_4 = 12$ Ω ;

$$I = \frac{V_S - R_{234} I_S}{R_1 + R_{234}} = -2,1737 \text{ A}$$

$$V_{S2} = R_{234} I_S$$

Esercizio 2 (*): Nel circuito di figura, funzionante in regime stazionario, calcolare la potenza generata da V_S .Dati: $V_S = 12$ V; $I_S = 2$ A; $R_1 = 6$ Ω ; $R_2 = 6$ Ω ; $R_3 = 4$ Ω ; $R_4 = 2$ Ω 

POLITECNICO DI MILANO

Insegnamento di Elettrotecnica - Ing. Edile - Nuovo Ordinamento - Prof. L. Di Rienzo
Prova d'esame del 26 novembre 2004 - Tema A

Esercizio 1: Nel circuito resistivo di Fig. 1 determinare il valore della corrente i che fluisce nel resistore di resistenza R_3 . Calcolare inoltre la potenza erogata dal generatore di tensione V_s .

Dati: $V_s = 10 \text{ V}$; $I_{S1} = 2 \text{ A}$; $I_{S2} = 2 \text{ A}$; $R_1 = 10 \Omega$; $R_2 = 6 \Omega$; $R_3 = 24 \Omega$.

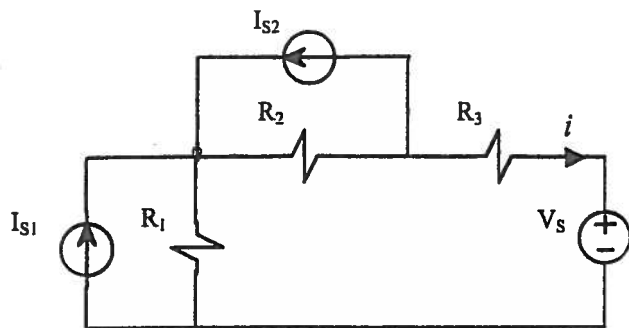
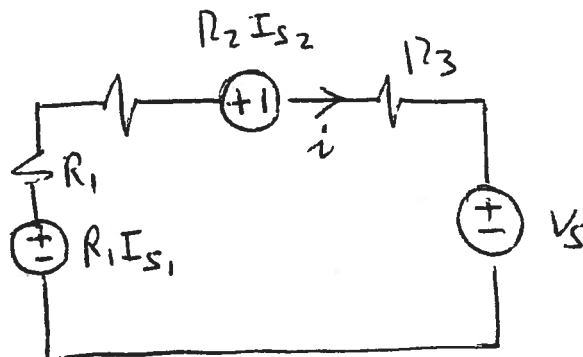
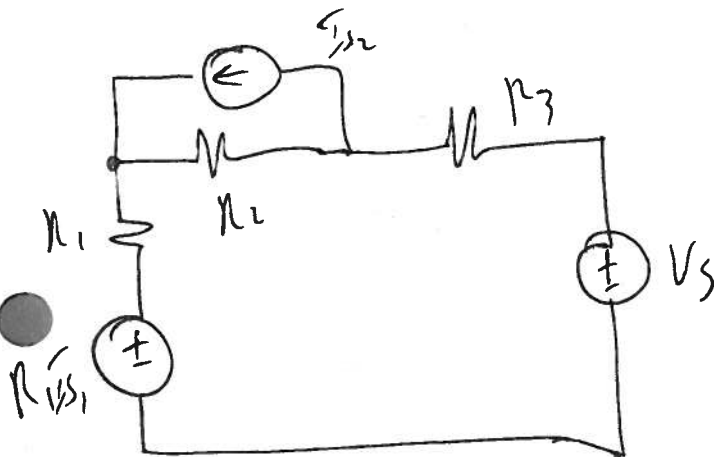


Fig. 1



$$i = \frac{R_1 I_{S1} - R_2 I_{S2} - V_s}{R_1 + R_2 + R_3} = -0,05 \text{ A}$$

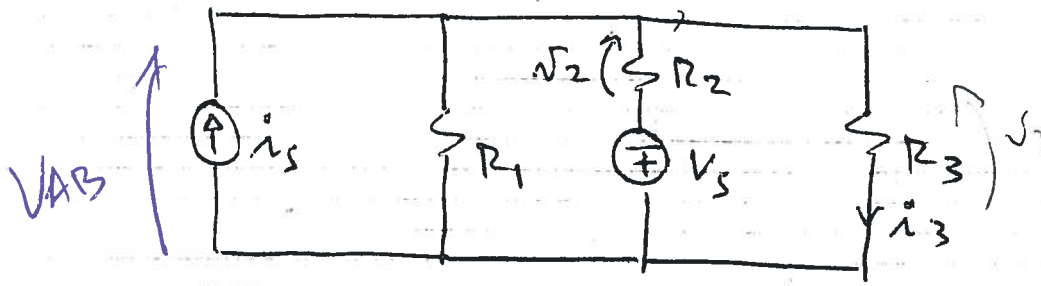
$$P_{V_s} = -V_s \cdot i = 0,5 \text{ W (erogata)}$$



TRASFORMAZIONE GENERATORI



● Calcolare i_3 e v_2



$$i_s = 4A$$

$$V_s = 3V$$

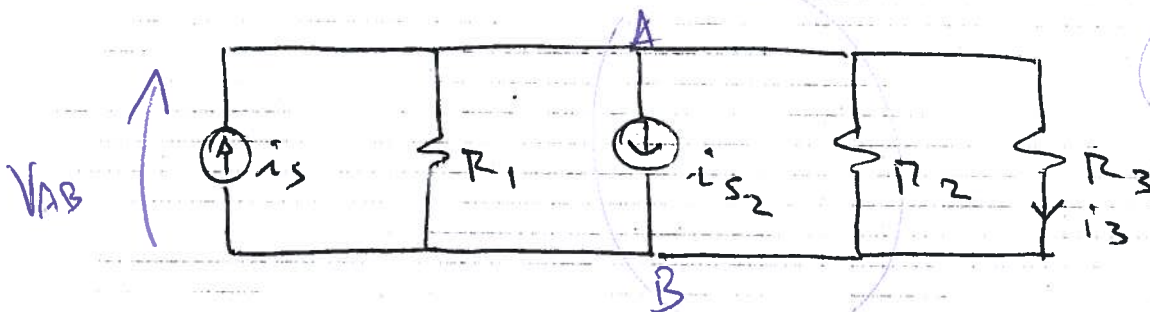
$$R_1 = 2\Omega$$

$$R_2 = 2\Omega$$

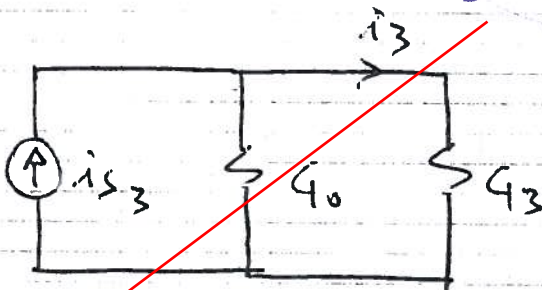
$$R_3 = 1\Omega$$

Cominciamo a calcolare i_3 .

● Trasformiamo la serie $V_s - R_2$ in parallelo



$$i_{s2} = \frac{V_s}{R_2} = \frac{3}{2}A$$



$$G_0 = \frac{1}{R_1} + \frac{1}{R_2} = 1S$$

$$G_3 = \frac{1}{R_3} = 1S$$

$$i_{s3} = 1S - i_{s2} = \frac{5}{2}A$$

$$i_3 = i_{s3} \frac{G_3}{G_0 + G_3} = \frac{5}{2} \cdot \frac{1}{2} = \frac{5}{4}A$$

Per calcolare v_2 dobbiamo tornare al circuito di partenza!

Anwendung des LUT:

$$V_5 + R_3 i_3 - V_2 = 0 \Rightarrow$$

$$V_2 = V_5 + R_3 i_3 = \frac{17}{4} V$$

$$V_{AB} = \frac{I_5 - I_{S_2}}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = \frac{4 - \frac{3}{2}}{\frac{1}{2} + \frac{1}{2} + 1}$$

$$= \frac{5}{4} V$$

$$I_3 = \frac{V_{AB}}{R_3} = \frac{5}{4} A$$

$$V_2 = V_{AB} + V_5 = \frac{17}{4} V$$

MILCHMANN

Esercizio 1: Nel circuito resistivo di Fig. 1 determinare il valore della corrente I .

Dati: $I_{S1} = 6 \text{ A}$; $I_{S2} = 10 \text{ A}$; $V_S = 4 \text{ V}$; $R_1 = 1 \Omega$; $R_2 = 2 \Omega$; $R_3 = 3 \Omega$

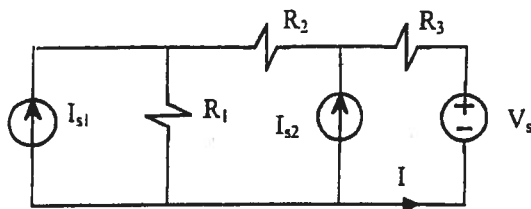
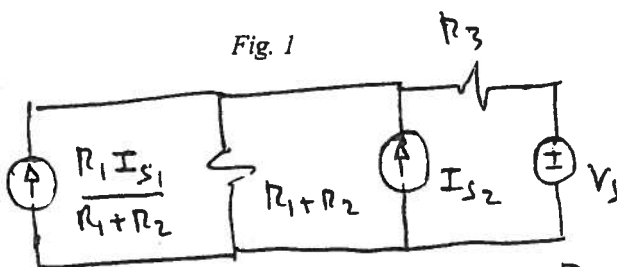
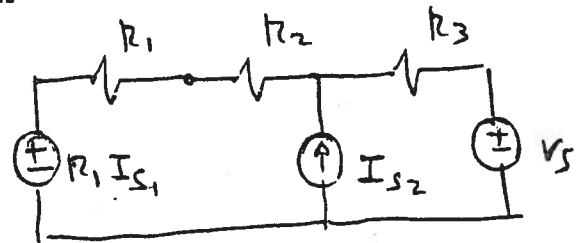
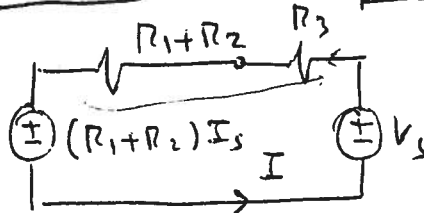


Fig. 1



$$I_S = \frac{R_1 I_{S1}}{R_1 + R_2} + I_{S2}$$



$$I = \frac{V_S - (R_1 + R_2) I_S}{R_1 + R_2 + R_3}$$

$$= -5,3 \text{ A}$$

Esercizio 2 (*): Nel circuito di Fig. 2, funzionante in regime stazionario, determinare il valore della corrente I_3 che fluisce

POLITECNICO DI MILANO

Insegnamento di Elettrotecnica - Ing. Fisica - Prof. L. Di Rienzo
 Prova d'esame del 27 giugno 2012 - Esercizi

Esercizio 1 (6 punti): Nel circuito resistivo di Fig. 1 calcolare la tensione v .

Dati: $I_s = 3 \text{ A}$; $R = 4 \Omega$.

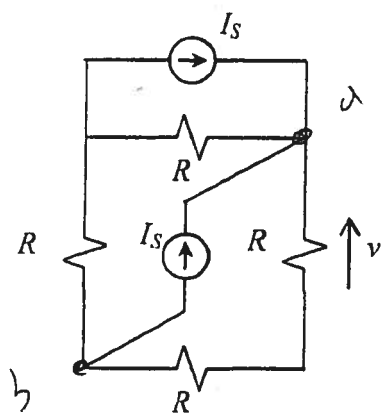
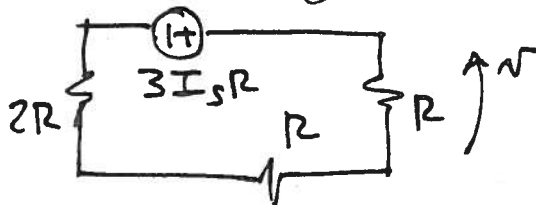
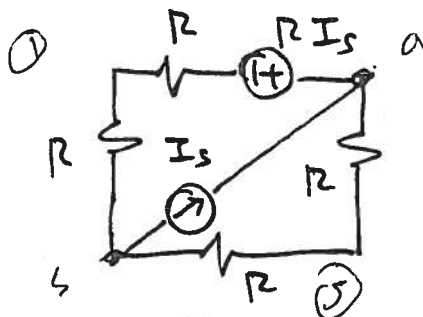


Fig. 1



$$v = 3 I_s R \frac{R}{4 R} = \frac{3}{4} I_s R = 9 \text{ V}$$

Esercizio 2 (6 punti): Nel circuito con trasformatore ideale di Fig. 2, funzionante in regime sinusoidale, determinare la potenza complessa erogata dal generatore di tensione, il valore efficace della tensione V_{R2} e l'angolo di sfasamento tra tale tensione e la tensione del generatore.

Dati: $V_s = 8 \text{ V}$ (valore efficace); $R_1 = 4 \Omega$; $R_2 = 8 \Omega$; $X_L = 5 \Omega$; $X_C = -6 \Omega$.

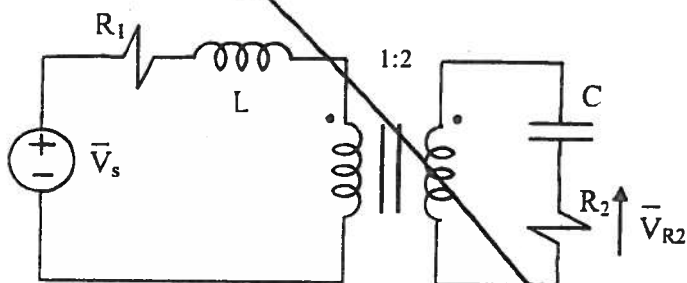
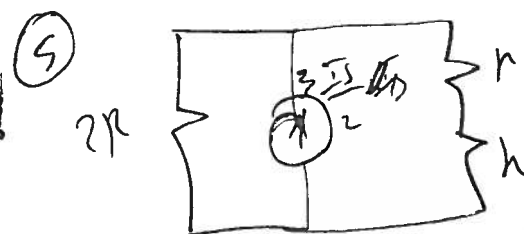
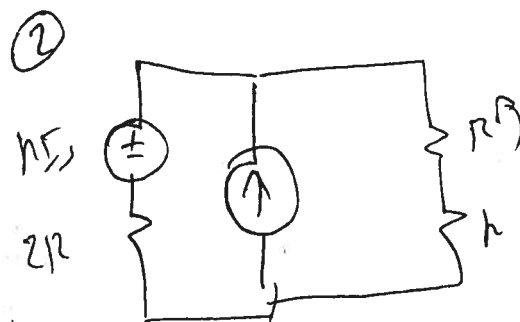


Fig. 2



POLITECNICO DI MILANO

Insegnamento di Elettrotecnica - Ing. Fisica - Prof. L. Di Rienzo
Prova d'esame del 27 giugno 2012 - Esercizi

Esercizio 1 (6 punti): Nel circuito resistivo di Fig. 1 calcolare la tensione v .

Dati: $I_s = 3 \text{ A}$; $R = 4 \Omega$.

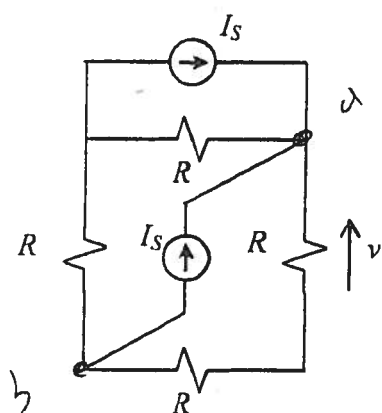
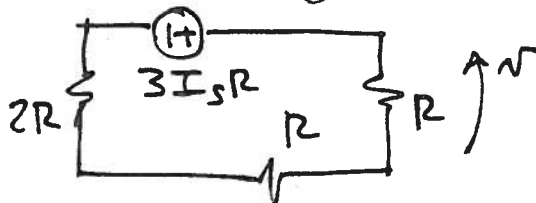
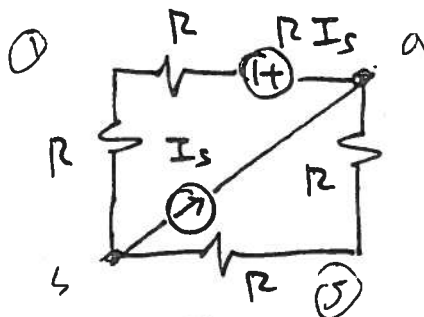


Fig. 1



$$v = 3 I_s R \frac{R}{4 R} = \frac{3}{4} I_s R = 9 \text{ V}$$

Esercizio 2 (6 punti): Nel circuito con trasformatore ideale di Fig. 2, funzionante in regime sinusoidale, determinare la potenza complessa erogata dal generatore di tensione, il valore efficace della tensione V_{R2} e l'angolo di sfasamento tra tale tensione e la tensione del generatore.

Dati: $V_s = 8 \text{ V}$ (valore efficace); $R_1 = 4 \Omega$; $R_2 = 8 \Omega$; $X_L = 5 \Omega$; $X_C = -6 \Omega$.

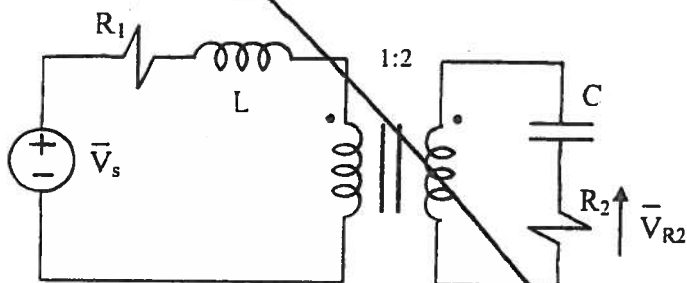


Fig. 2

