Supplementary information for

2 Projecting urban land expansion and heat island

intensification globally through 2050

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- 5 Two models are built and integrated to project urban heat island (UHI) intensification globally:
- 6 1) a spatially explicit, probabilistic urban expansion model to predict the likelihood of a location
- 7 to convert to urban land, and 2) a sigmoid-based, two-step empirical model to relate UHI
- 8 intensities to urban cluster size. Applying these two models on the Shared Socioeconomic
- 9 Pathways(1, 2), we project how several plausible development scenarios will result in urban land
- expansion and heat island intensification through 2050 across the world.

1 Urban land expansion projections

- 12 The urban expansion model is built upon a previous global forecast model, URBANMOD(3),
- which first predicts the amounts of urban land then allocates them spatially with 5-km resolution.
- We develop a new forecast model, called URBANMOD-ZIPF, whose name indicates that Zipf's
- 15 law of urban size distribution is preserved. Zipf's law refers to the linear and inverse relationship
- between ranks and sizes of cities on log scales(4). Since UHI intensity increases with log urban
- size(5–8), without preserving the Zipf's law in the forecasts, we cannot reliably predict the log
- size-dependent UHI. To develop URBANMOD-ZIPF, we significantly modify both the quantity
- 19 prediction and land allocation processes of URBANMOD.

20 1.1 Delineating urban land

- We use the Global Human Settlement Layer(9) (GHSL) datasets to delineate existing urban
- 22 lands. By combing images from multiple satellite-born sensors, GHSL maps global human
- settlements in four years: 1975, 1990, 2000, and 2015. The global and multi-year coverage
- 24 allows us to build and validate our urban expansion model across the world. GHSL provides
- 25 three types of products, including built-up (GHS-BUILT), population (GHS-POP), and cities
- 26 (GHS-SMOD). Among these three types of produces, we choose GHS-SMOD as the delineation
- of urban lands, because it combines impervious surface and population density, which are the
- 28 two most commonly used criteria to define urban area. The GHS-SMOD is resampled from the
- original 1-km resolution to 5-km used in URBANMOD-ZIPF.

30 1.2 Forecasting urban land quantities

- 31 This first improvement of URBANMOD-ZIPF over URBANMOD is the use of fixed effect
- 32 panel data regression.
- According to a previous meta-analysis(10) on drivers of global urban land expansion, the growth
- of gross domestic production (GDP) is the most significant factor. However, the patterns of how
- 35 GPD drives urban expansion can vary across different regions of the world. To account for the
- 36 regional variation, we build a fixed-effect panel data regression model to capture the relationship
- between per capita urban land and GDP. This regression model was not applicable when
- 38 URBANMOD was developed, because only one year of global urban extents—the MODIS
- 39 global urban cover in 2000 was available.
- 40 The panel data regression is built on historical observations in 1975, 1990, and 2000:

$$ULC_{it} = \beta_0 + \beta_1 GDPC_{it} + \sum_{j=2}^{N} \gamma_j D_{ij} + \varepsilon_{it}$$

- 42 where β_0 is a constant, β_1 is the coefficient of GDPC and URB, γ_i is the coefficient of the
- regional dummies D_{ij} , ε_{it} is the error term, N is the number of regions, and t represents the year.
- 44 Supplementary Table 2 shows the estimates of coefficients in the regression. The panel
- regression ($R^2 = 0.94$) agrees better with observations than the simple linear regression ($R^2 = 0.94$)
- 46 0.34). The simple regression overestimates ULC for regions with less than 200 km² while
- 47 underestimates that for regions with more than 400 km², which are corrected in the panel data
- 48 regression. Applying this equation on the future GDPC in SSPs, we can estimate the future ULC
- by 2050. By multiplying per capita urban land with the urban population, we can forecast the
- 50 future urban land in each region under each scenario.
- Supplementary Table 4 shows the new urban lands forecasted here, from 2015 to 2050, and those
- 52 by Seto et al. 2012 (3), from 2000 to 2030. Although these two methods span across different
- 53 time periods and scenarios, we can still see that they forecast comparable amounts of urban lands
- 54 in America, Europe and Oceania, but URBANMOD-ZIPF forecasts much less in Africa and
- Asia. That is because the fixed-effect regression used in URBANMOD-ZIPF can account for
- regional differences: African and Asian countries tend to have denser cities, thus smaller urban
- 57 land per capita, than American, European and Oceanian countries. This is reflected in
- Supplementary Table 2, where Asian and African countries/regions have smaller coefficients (γ_i)
- of the regional dummies.

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1.3 Forecasting urban land locations

- The second improvement of URBANMOD-ZIPF over URBANMOD is the mechanism to
- preserve the Zipf's law of urban size distribution.
- In terms of allocating urban land spatially, URBANMOD uses a spatially explicit grid-based
- model, based on urban development suitability derived from slope, distance to roads, population
- density, and land cover. Here in URBANMOD-ZIPF, we modify the allocation process by
- preserving the Zipf's law of urban size distribution. Considering the observation that Zipf's law
- 67 is preserved because the expansion magnitude of an urban cluster is proportional to its size(4),
- we alter the probability of a grid converting to urban by multiplying the conversion probability
- by the size of the adjacent urban cluster. If multiple clusters are merged, the size of the new
- cluster will be used in the next iteration. Supplementary Figure 3 shows the rank-size
- 71 distributions of urban clusters forecasted by URBANMOD-ZIPF (black) and URBANMOD
- 72 (blue), and those from the GHSL datasets in 1975 (green), 1990 (yellow), 2000 (orange), and
- 73 2015 (red). As can be seen from the figure, URBANMOD-ZIPF is capable of preserving the
- historical rank-size distribution of urban clusters, while URBANMOD tends to underestimate the
- 75 sizes of larger clusters.

1.4 Validating and comparing urban expansion projections

- We use the observed urban land cover in 2015 to validate the accuracies of these two models. In
- 78 land use change modelling, accuracy should be measured as the comparison between predicted
- and observed changes(11). Therefore, we first run both models from 2000 to 2015, then overlap
- 80 the results with the new urban lands observed during the same period. If the model is more
- accurate in predicting land use changes, it should predict higher probabilities on the actual new
- 82 urban lands. Supplementary Table 3 shows the average probabilities predicted by two models on
- the new urban lands from 2000 to 2015. In terms of predicting higher probabilities on observed

- 84 new urban lands, URBANMOD-ZIPF outperforms URBANMOD by 72%. Supplementary
- 85 Figure 4 shows the predicted probabilities on urban clusters of various sizes. Regarding urban
- cluster sizes, URBANMOD-ZIPF outperforms URBANMOD in predicting clusters that are 86
- 87 larger than 130 km² but underperforms in predicting clusters smaller than 130 km².
- 88 Another commonly used metric to validate probabilistic forecasts is to calculate the root-mean-
- 89 square-error (RMSE) between the observed frequency and the predicted probabilities (12). First,
- 90 we divide the predicted probabilities into ten equal size intervals. Then, we estimate the
- 91 frequency of observed new urban lands from 2000 to 2015 within each interval. Finally, the
- 92 RMSE between observed frequencies and predicted probabilities of these intervals are
- 93 calculated. As shown in Supplementary Table 3, by this measure, URBANMOD-ZIPF achieves
- 94 about 20% smaller RMSE compared to URBANMOD.

Urban heat island intensification projections

- Two types of urban heat island (UHI) indicators are commonly used in urban climate studies: the 96
- 97 atmospheric UHI (AUHI) and surface UHI (SUHI). The AUHI is based on air temperature,
- 98 which can be measured by thermometers, which are installed sparsely in most cities worldwide;
- 99 while the SUHI is based on land surface temperature, which can be measured continuously
- across the space by radiometers onboard satellites or aircraft. Here, we build two models to 100
- 101 predict SUHI and AUHI respectively. Taking advantage of the spatially continuous
- 102 measurements, the first model links SUHI to urban cluster size, while controlling other UHI
- 103 determinants. The second model links air temperature to land surface temperature, in order to
- 104 convert the estimated SUHI to AUHI.

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2.1 Measuring surface urban heat island and its determinants

- 106 We measure SUHIs with the MOD11A2 land surface temperature (LST) 8-day product derived
- 107 from the images obtained by the Moderate Resolution Imaging Spectroradiometer (MODIS)
- 108 instrument on board the Terra satellite. The approach by (13) is used to fill the gaps in these
- 109 images due to cloud coverage. Following (6, 8, 14, 15), we measure the SUHI as the difference
- 110 between the mean LST of an urban cluster and its equal-area buffer zone. Before calculating
- SUHI, water pixels are removed from both the urban clusters and the buffer zones, and urban 111
- 112 pixels are removed from the buffer zones.
- 113 To account for the diurnal, seasonal and intra-urban variations of urban heat islands, we define
- 114 different types of SUHIs and build separate models respectively. For diurnal variation, we
- 115 measure SUHIs with the daytime and nighttime LSTs from MOD11A2, which are obtained by
- 116 Terra satellite at ~10:30 and at ~22:30 local solar time. We choose MOD11A2 from Terra rather
- 117 than MYD11A2 from Aqua, because the former shows a better correlation with daily maximum
- 118 and minimum air temperature (see session 2.3 for more details). For seasonal variation, we
- 119 measure the summer and winter SUHIs with LSTs in Jun to August and December to February in
- 120 the northern hemisphere (opposite months in the southern hemisphere). For intra-urban variation,
- we first classify the LSTs in an urban cluster into four quantiles (0-25th, 25-50th, 50-75th and 75-121
- 122 100th percentiles) and then measure SUHI of each quantile as the difference between its mean
- 123 LST from that of the buffer zone. These LST quantiles each represent zones within an urban
- 124 cluster that have different UHI intensities, usually ranging from the hottest center zone (75th–
- 100th) to the coolest outskirt (0th-25th). In total, there are 16 types of SUHIs as listed in 125
- Supplementary Table 5. 126

- We use other remote sensing products to measure the known determinants of SUHI in the existing large-scale studies:
 - 1) Urban cluster size(6–8, 14, 16, 17): measured as the area of urban clusters delineated from GHSL using the City Clustering Algorithm(18);
 - 2) Urban cluster compactness(14, 19): measured as the ratio between areas of the cluster and its minimum circumcised circle;
 - 3) Vegetation abundance(15, 19): approximated by the difference of the mean Enhanced Vegetation Index (EVI) between the cluster and its buffer zone, using the MYD13A1 product;
 - 4) Surface albedo(15, 16, 20): approximated by the difference of mean white sky albedo between the cluster and its buffer zone, using the MCD43B3 product;
 - 5) Surface roughness(20): approximated by the mean difference of backscattering between the cluster and its buffer zone, using the VV and VH composites of Sentinel-1 SAR data;
 - 6) Anthropogenic heat(15, 16): approximated by the VIIRS Stray Light Corrected Nighttime product.

All variables are measured in 2015, because this is the only year when both GHSL and MODIS datasets are available. Among these determinants, anthropogenic heat has a stronger influence over AUHI than SUHI, and its diurnal and seasonal profiles vary in different regions across the world, which cannot be adequately captured here. The anthropogenic heat release depends on energy, transportation, built infrastructures and human activities, whose future changes are not explicitly modeled in the projections of urban land expansion. Therefore, we leave out the influences of changing anthropogenic heat in our models and only focus on the effects of urban expansion.

2.2 Modeling surface urban heat island

We build a sigmoid-based regression model to predict how SUHIs will intensify as urban clusters grow larger in size, while other determinants stay constant. We first transform urban cluster size with sigmoid functions then use multiple linear regression to model the SUHI as a function of sigmoid-transformed size and other determinants.

function of sigmoid-transformed size and other determinants.

Although previous studies suggest positive relationships between SUHI and urban cluster size, there is a considerable discrepancy in the literature. While Li et al. (2017) (8) and Tan & Li (2015) (7) found linear relationships between SUHI and logarithmic urban cluster size in the continental U.S. and North China, Zhou et al. (2013) (6) found a non-linear, sigmoid relationship in Europe. Here, we replicate the analysis at the global scale by binning urban clusters according to their logarithmic sizes and calculating the average SUHIs of each bin. Replicating the analysis at the global scale allows sufficient sample sizes to more reliably test the underlying relationship

- between urban size and UHI. Supplementary Figure 5 shows the results for the 75-100th
- percentiles SUHIs during daytime and nighttime, in summer and winter. The binning analysis
- suggests non-linear sigmoid relations at the global scale across different seasons and time of day.
- 165 The binning analyses for all four quantiles are shown in Supplementary Figure 6, where only the
- SUHIs of 0-25th percentiles do not increase with logarithmic size. After fitting the sigmoid functions S(*):

$$SUHI = S(log_{10}(size)) = \frac{a}{1 + (log_{10}(size)/b)^{-c}}$$

with the binning average on different types of SUHIs, we apply these functions to the logarithmic urban sizes, in order to obtain sigmoid size indices that are linearly correlated to

- SUHIs. We create the sigmoid size indices for all types of SUHIs except those of 0-25th
- percentiles, because they are not correlated with size. Supplementary Table 5 shows the
- 173 correlations between urban cluster $log_{10}(size)$, sigmoid size indices $S(log_{10}(size))$, and SUHIs. As
- shown in the table, the sigmoid size indices have stronger linear correlations with SUHIs. This
- transformation allows for the multiple regression that assumes linearity.
- 176 To demonstrate the significance of urban cluster size in determining SUHIs, we run the best
- subsets regressions(21) between SUHIs of 75-100th percentiles and the determinants listed in 2.1.
- 178 The best subsets regression compares all possible combinations of independent variables, in
- order to find the best subset of variables that yields the highest coefficient of determination (R^2) .
- Supplementary Table 6 shows the summary of the best subsets sorted by the resulting R². Our
- analyses show that, compared to other determinants, the sigmoid size indices ($S(log_{10}(size))$) of
- urban clusters contribute the most to correlations (from 79% to 94%) with all types of SUHIs and
- therefore they are the suitable variables in predicting future SUHIs.
- Previous studies(8, 20, 22) suggest that SUHIs are influenced by the climatic-ecological
- contexts, which are accounted for by building conditional linear regressions. Specifically, we
- build separate models for urban clusters within different Köppen-Geiger climate zones(23): the
- arid, cold, temperate and tropical. The summaries of these regression models are shown in
- Supplementary Table 7, where the coefficients of determination (R^2) are higher than 0.7 except
- for winter nighttime. Note that in the arid climate, only the SUHIs of 75-100th percentiles
- increase with size while those of the other two quantiles decrease. In arid climate, although dense
- development in the urban cores increases the temperature, the urban green spaces introduced in
- the less dense areas actually cool down the surface. This is consistent with previous studies that
- found urban cool islands(24, 25) in the arid zones.

194 2.3 Predicting air temperature with the land surface temperature

- Although it is possible to measure and model SUHI at the global scale, predicting future SUHI
- intensification is less useful because the impacts of warming on human health and energy
- 197 consumption are more relevant to air temperature. Here, we build a model to predict daily
- maximum and minimum air temperature (AT) from daytime and nighttime LST, based on a
- series of methods developed and tested in diverse regions such as the U.S.(26–29), China(30–
- 200 32), Europe(33, 34), the Middle East(35) and Africa(36). The daily maximum and minimum air
- temperatures used here are obtained from the Global Historical Climatology Network-Daily
- 202 (GHCN-D) dataset version-3 (37), which include over 80,000 weather stations in 180 countries
- and territories. To avoid the influences of rural stations, we spatially overlay the GHCN stations
- with GHSL urban extent in 2015, to identify 1,074 urban stations to be used in the regression
- 205 (Supplementary Figure 7).

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The air temperature (AT) is modeled as:

$$AT = (\beta_0 + \beta_1 \times LST + \beta_2 \times elev + \beta_3 \times d_{water}|c_i)$$

- where *elev* is the elevation, d_{water} is the distance to the closest water body, and c_i denotes the climatic zone.
- In the previous regional AT-LST modeling studies, both LSTs of MOD11A1/2 (measured by
- 211 Terra at ~11:30 and ~22:30) and MYD11A1/2 (measured by Aqua at ~13:30 and ~1:30) have
- been used. In order to assess which LST products are more suitable in predicting
- 213 maximum/minimum air temperatures at the global scale, we built two sets of models using both
- products and compared their performances. As shown in Supplementary Table 9, the regression
- 215 model built with MOD11A2 outperforms that with MYD11A2, which is consistent with the

- previous study by Zhu et al. (32) that also compared the performances of these two products in
- predicting daily maximum/minimum air temperatures. These performance differences can be
- explained by observation times and diurnal temperature fluctuations. While the observations of
- 219 MYD11A are close to maximum/minimum LSTs, the earlier observation times of MOD11A
- result in daytime LSTs lower than the maximum values and nighttime LSTs higher than the
- minimum values, resulting in smaller diurnal fluctuations observed by MOD11A than those by
- MYD11A. Therefore, the fluctuations observed by MOD11A are closer to the fluctuations of
- ATs, which are usually smaller than LSTs.
- Supplementary Figure 8 and Supplementary Figure 9 show the relationships between the
- observed air temperature and land surface temperature (1st columns), and the predicted air
- temperature (2nd columns), in summer and winter respectively. Compared to LSTs, the air
- 227 temperatures predicted by the AT-LST model show stronger correlations with the observed
- values, with no bias (slope = 1 and intercept = 0).

2.4 Assessing uncertainty propagation

- In the SUHI and AT-LST models established above, estimations of coefficients involve ranges of
- uncertainty (the standard deviations in parentheses in Supplementary Table 7 and Supplementary
- Table 8). When used in predicting the future intensification of UHI, the uncertainties will
- propagate through the two models. Since the projected AUHIs are the products of multiplying
- increases in urban cluster size with the slope in SUHI model (Supplementary Table 7) and then
- with the slope in AT-LST model (Supplementary Table 8), we can use the multiplication error
- propagation formula (38) to measure the standard deviation of AUHI increases:

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$$\sigma_{\Delta AUHI} \approx |\Delta AUHI| \cdot \sqrt{\left(\frac{\sigma_{slope1}}{slope1}\right)^2 + \left(\frac{\sigma_{slope2}}{slope2}\right)^2}$$

- where σ denotes standard deviation, *slope1* is the slope in the SUHI model, and *slope2* is that in
- the AT-LST model.

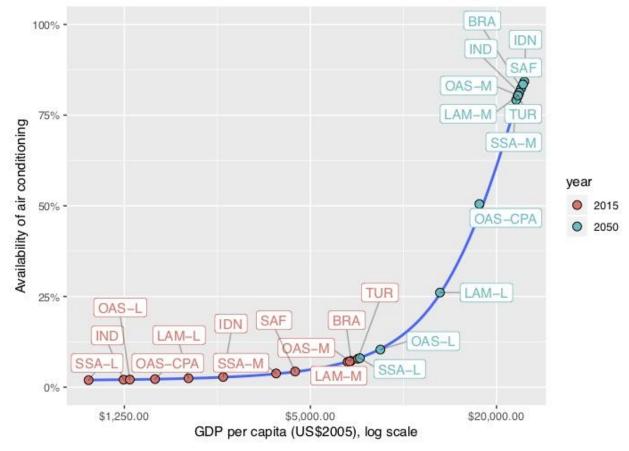
240 2.5 Predicting urban heat island intensification and population exposure

- The increased sizes of urban clusters from 2015 to 2050 forecasted in the urban expansion
- 242 model, are used in the above SUHI model to predict the future increased LST. Apart from urban
- cluster size, other SUHI determinants stay constant. Within an urban cluster, we allocate the
- intensification results according to the observed pattern that LST generally decreases from the
- core to the outer boundary(22). We first divide the cluster into four equal-area concentric rings,
- then allocate the predicted 75-100th percentiles SUHI to the inner most ring, 50-75th to the
- second ring, 25-50th to the third, and 0-25th to the outer most one. We then apply the AT-LST
- 248 model to the resulting increased SUHI to predict future intensification of AUHI.

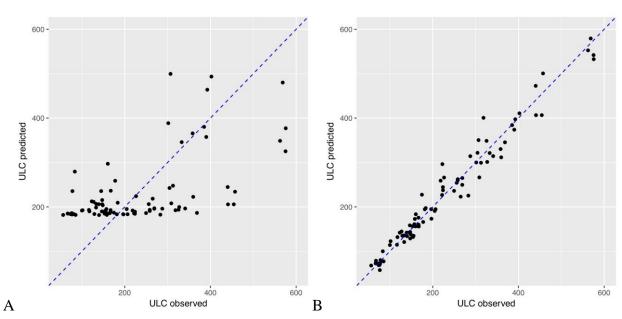
2.6 Affordability of indoor cooling

- 250 The proportion of households with air conditioners (AC) installed depends on climate and on
- income. While climates determine the needs for AC, incomes determine whether the household
- can afford to install, maintain, and operate AC. Following a global-scale study(39), we model
- affordability of indoor cooling as a logistic function of GDP per capita, using the same
- coefficients listed in the reference.

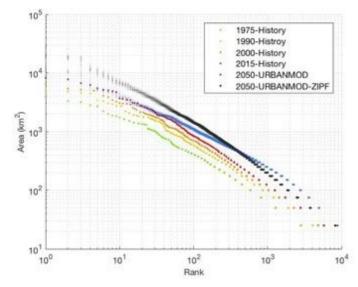
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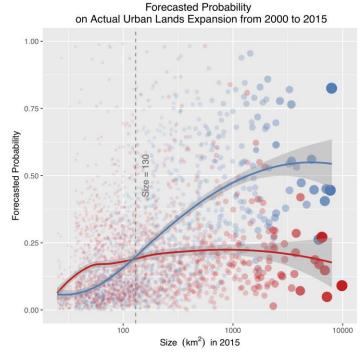
Supplementary Figure 1 Growth of availability of air conditioning from 2015 (red) to 2050 (blue), in the SSP5 scenario. See Supplementary Table 1 for regions definition.



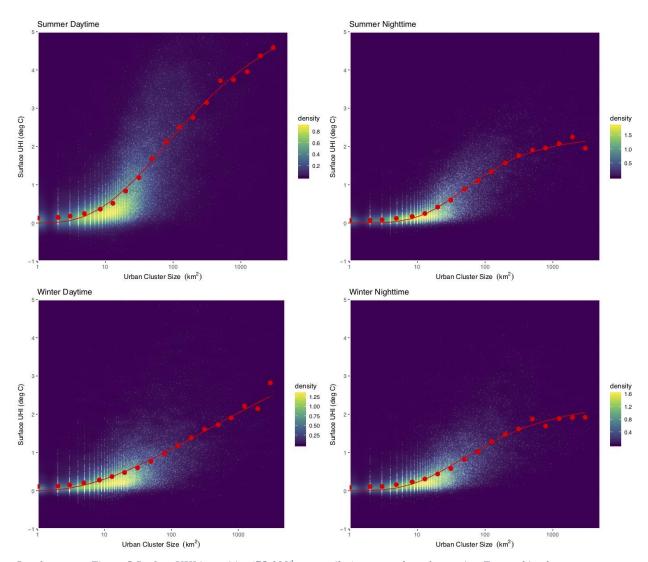
Supplementary Figure 2 Observed versus predicted urban land per capita (ULC) in km^2 per million persons of 32 regions defined in SSP database. A) Predicted by linear regression. B) Predicted by panel data regression. The y = x reference line is dashed blue.



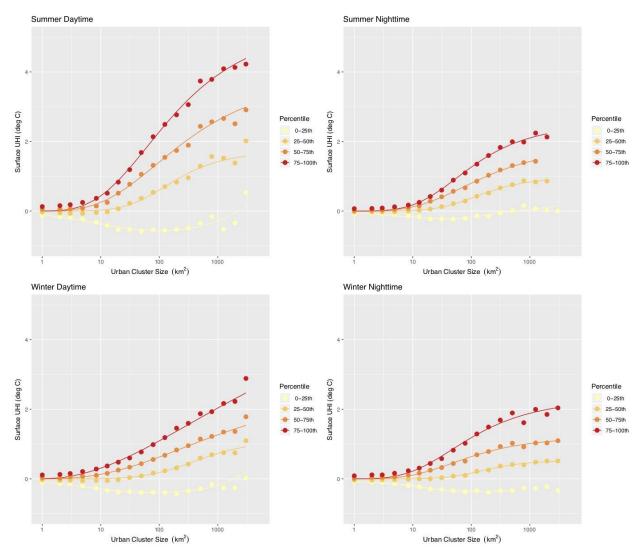
Supplementary Figure 3 Rank-Size distributions of global urban areas in 1975 (green), 1990 (yellow), 2000 (orange), and 2015 (red) obtained from Global Human Settlement Layer (GHSL) and those in 2050 under the SSP5 scenario, forecasted by the new model (URBANMOD-ZIFP, black) and the previous model (URBANMOD, blue). Both ranks and sizes are on the logarithmic scale.



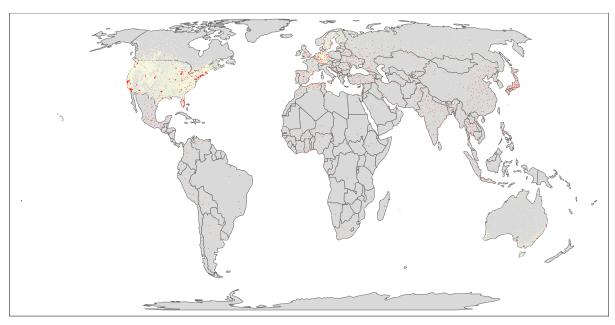
Supplementary Figure 4 Forecasted probabilities of urbanization preditected by URBANMOD-ZIPF (blue) and URBANMOD (red) on the observed new urban lands from 2000 to 2015. Each dot is one urban cluster in 2015.



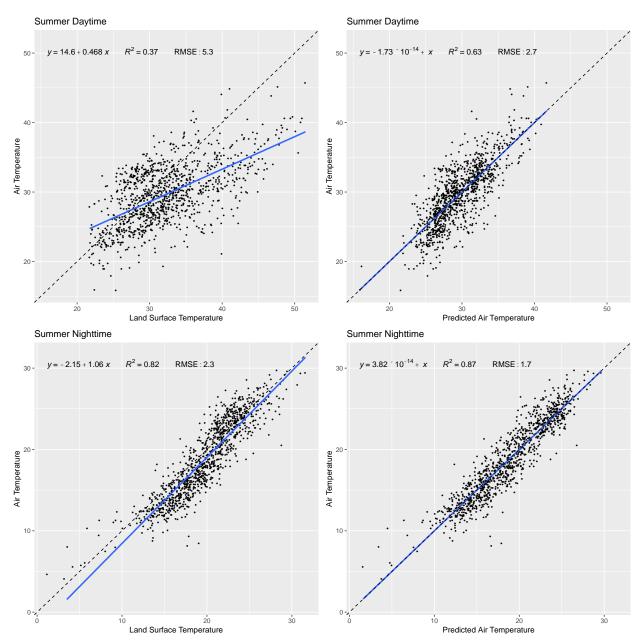
Supplementary Figure 5 Surface UHI intensities (75-100th percentiles) versus urban cluster size. Every white dot represents one urban cluster, and the background colors (dark blue to yellow) represents the density of dots. Red dots present the mean of each bin and the red lines are the fitted Sigmoid functions.



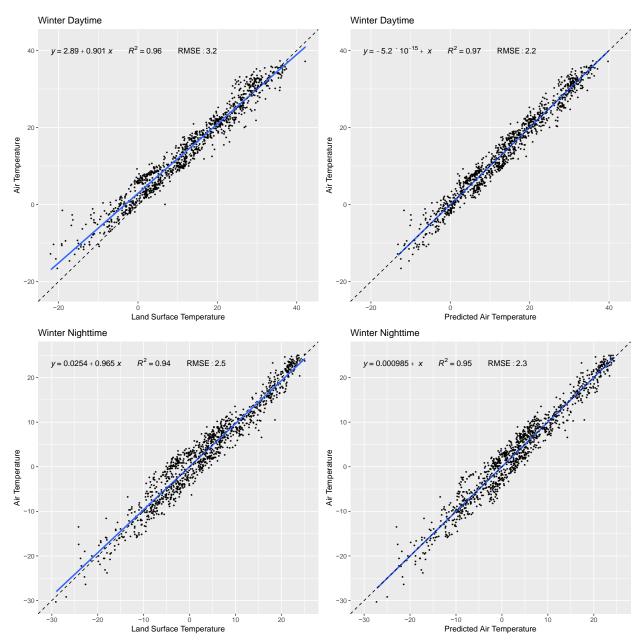
Supplementary Figure 6 The mean SUHIs and cluster sizes of each bin and the fitted curves. Colors present different percentiles of SUHIs



 $Supplementary\ Figure\ 7\ Locations\ of\ Global\ Historical\ Climate\ Network\ (GHCN)\ weather\ stations\ (yellow\ dot),\ where\ urban\ stations\ are\ shown\ as\ red\ dots.$



Supplementary Figure 8 Observed air temperature versus land surface temperature and the predicted air temperature in summer. The first column shows the air temperature (y-axis) versus land surface temperature (x-axis), and the second column shows that versus the predicted air temperature (x-axis). The first row shows the summer daytime temperatures, and the second row shows the summer nighttime temperatures. The blue solid lines are linear regression fits. The y=x reference lines are dashed black.



Supplementary Figure 9 Observed air temperature versus land surface temperature and the predicted air temperature in summer. Same as Supplementary Figure 8 but for winter.

Regions	Countries and territories included
ANUZ	Australia, New Zealand
CAN	Canada
EEU	Eastern Europe (excl. former Soviet Union and EU member states): Albania, Bosnia and Herzegovina, Croatia,
	Montenegro, Serbia, The former Yugoslav Republic of Macedonia
EFTA	Iceland, Norway, Switzerland
EU12-H	New EU member states that joined as of 2004 - high income: Cyprus, Czech Republic, Estonia, Hungary, Malta,
	Poland, Slovakia, Slovenia
EU12-M	New EU member states that joined as of 2004 - medium income: Bulgaria, Latvia, Lithuania, Romania
EU15	European Union member states that joined prior to 2004: Austria, Belgium, Denmark, Finland, France,
	Germany, Greece, Ireland, Italy, Luxembourg, Netherlands, Portugal, Spain, Sweden, United Kingdom
JPN	Japan
TUR	Turkey
USA	United States of America, including Puerto Rico, United States Virgin Islands
CAS	Countries of Central Asia: Armenia, Azerbaijan, Georgia, Kazakhstan, Kyrgyzstan, Tajikistan, Turkmenistan,
	Uzbekistan
EEU-FSU	Eastern Europe, former Soviet Union (excl. Russia and EU members): Belarus, Republic of Moldova, Ukraine
RUS	Russian Federation
CHN	China (Mainland, Hong Kong, Macao; excl. Taiwan)
IDN	Indonesia
IND	India
KOR	Republic of Korea
OAS-CPA	Countries of Other Asia - former Centrally Planned Asia: Cambodia, Lao People's Democratic Republic,
	Mongolia, Viet Nam
OAS-L	Countries of Other Asia - low income: Bangladesh, Democratic People's Republic of Korea, Fiji, Micronesia
	(Fed. States of), Myanmar, Nepal, Papua New Guinea, Philippines, Samoa, Solomon Islands, Timor-Leste,
	Tonga, Vanuatu
OAS-M	Countries of Other Asia - medium and high income: Bhutan, Brunei Darussalam, French Polynesia, Guam,
	Malaysia, Maldives, New Caledonia, Singapore, Sri Lanka, Thailand
TWN	Taiwan
MEA-H	Countries of Middle East Asia - high income: Bahrain, Israel, Kuwait, Oman, Qatar, Saudi Arabia, United Arab
	Emirates
MEA-M	Countries of Middle East Asia - low and medium income: Iran (Islamic Republic of), Iraq, Jordan, Lebanon,
	Occupied Palestinian Territory, Syrian Arab Republic, Yemen
NAF	Countries of North Africa: Algeria, Egypt, Libyan Arab Jamahiriya, Morocco, Tunisia, Western Sahara
PAK	Pakistan, Afghanistan
SAF	South Africa
SSA-L	Countries of Subsahara Africa (excl. South Africa) - low income: Benin, Burkina Faso, Burundi, Cameroon,
	Cape Verde, Central African Republic, Chad, Comoros, Congo, Côte d'Ivoire, Democratic Republic of the
	Congo, Djibouti, Eritrea, Ethiopia, Gambia, Ghana, Guinea, Guinea-Bissau, Kenya, Lesotho, Liberia,
	Madagascar, Malawi, Mali, Mauritania, Mozambique, Niger, Nigeria, Rwanda, Sao Tome and Principe,
	Senegal, Sierra Leone, Somalia, South Sudan, Sudan, Swaziland, Togo, Uganda, United Republic of Tanzania,
	Zambia, Zimbabwe
SSA-M	Countries of Subsahara Africa (excl. South Africa) - medium and high income: Angola, Botswana, Equatorial
	Guinea, Gabon, Mauritius, Mayotte, Namibia, Réunion, Seychelles
BRA	Brazil
LAM-L	Countries of Latin America (excl. Brazil, Mexico) - low income: Belize, Guatemala, Haiti, Honduras, Nicaragua
LAM-M	Countries of Latin America (excl. Brazil, Mexico) - medium and high income: Antigua and Barbuda, Argentina,
	Bahamas, Barbados, Bermuda, Bolivia (Plurinational State of), Chile, Colombia, Costa Rica, Cuba, Dominica,
	Dominican Republic, Ecuador, El Salvador, French Guiana, Grenada, Guadeloupe, Guyana, Jamaica,
	Martinique, Netherlands Antilles, Panama, Paraguay, Peru, Saint Kitts and Nevis, Saint Lucia, Saint Vincent and
MEN	the Grenadines, Suriname, Trinidad and Tobago, Uruguay, Venezuela (Bolivarian Republic of)
MEX	Mexico

Variable	Estimate	Std. Error	t value	Pr (> t)
GDPC	0.0037516	0.0011784	3.2	< 0.01
dummy: ANUZ (baseline)	476.3	21.0	13.4	< 0.001
dummy: BRA	-345.6	20.1	-9.5	< 0.001
dummy: CAN	-182.6	21.1	-5.9	< 0.001
dummy: CAS	-242.6	20.6	-6.1	< 0.001
dummy: CHN	-304.1	21.2	-8.0	< 0.001
dummy: EEU	-218.6	19.7	-6.3	< 0.001
dummy: EEU-FSU	-133.6	19.2	-2.8	< 0.01
dummy: EFTA	-207.4	19.3	-6.4	< 0.001
dummy: EU12-H	-183.7	25.5	-3.2	< 0.01
dummy: EU12-M	-169.1	19.0	-3.3	< 0.01
dummy: EU15	-229.9	18.0	-5.9	< 0.001
dummy: IDN	-251.7	21.2	-4.8	< 0.001
dummy: IND	-408.9	22.0	-11.3	< 0.001
dummy: JPN	-270.4	18.9	-5.6	< 0.001
dummy: KOR	-421.0	18.5	-12.3	< 0.001
dummy: LAM-L	-322.1	20.1	-9.0	< 0.001
dummy: LAM-M	-348.7	19.0	-9.4	< 0.001
dummy: MEA-H	-345.6	21.5	-10.4	< 0.001
dummy: MEA-M	-367.2	22.8	-10.3	< 0.001
dummy: MEX	-358.9	19.9	-10.0	< 0.001
dummy: NAF	-321.9	22.8	-9.2	< 0.001
dummy: OAS-CPA	-342.7	22.2	-9.4	< 0.001
dummy: OAS-L	-405.4	22.0	-11.4	< 0.001
dummy: OAS-M	-233.6	20.6	-6.3	< 0.001
dummy: PAK	-399.5	21.3	-11.1	< 0.001
dummy: RUS	-292.1	18.7	-7.5	< 0.001
dummy: SAF	-81.1	21.0	-1.3	0.19
dummy: SSA-L	-282.8	21.8	-7.8	< 0.001
dummy: SSA-M	-222.3	31.5	-4.9	< 0.001
dummy: TUR	-348.6	19.3	-10.0	< 0.001
dummy: USA	-32.7	28.6	-0.8	0.44

Model	Mean Predicted Probability	Root Mean Squared Errors of Probability
URBANMOD	0.18	0.50
URBANMOD-ZIPF	0.31	0.41

Supplementary Table 4 Urban land (km²) forecasted by this work and that by Seto et al. 2012 (grey shaded).

	Urban land	Urban Expansion	Urban land	Uı	rban Expa	nsion from	2015 to 20	50
	in 2000	from 2000 to 2030	in 2015	SSP1	SSP2	SSP3	SSP4	SSP5
Africa	41,450	303,813	84,853	198,402	169,889	131,724	240,323	206,042
America	224,025	356,323	218,285	208,998	199,791	145,461	168,746	274,447
Asia	225,825	903,529	249,256	545,259	431,489	285,207	436,483	612,774
Europe	151,075	115,118	198,952	136,113	110,462	25,931	90,861	189,509
Oceania	10,450	12,871	12,663	18,591	17,808	8,336	16,283	26,526
World	652,825	1,691,654	764,009	1,107,363	929,440	596,658	952,696	1,309,297

Supplementary Table 5 Correlations between urban cluster size, its sigmoid index, and different types of SUHIs.

Time of day	Season	SUHIs by percentiles	\mathbf{R}^2 with $log_{1\theta}(\mathbf{size})$	\mathbf{R}^2 with $S(log_{I\theta}(\mathbf{size}))$	Improvement of R ²
Daytime	Summer	75-100 th	0.46	0.51	10.8%
		50-75 th	0.32	0.36	12.5%
		25-50 th	0.15	0.18	20.0%
	Winter	75-100 th	0.30	0.34	13.3%
		50-75 th	0.19	0.22	15.8%
		25-50 th	0.07	0.10	42.9%
Nighttime	Summer	75-100 th	0.49	0.56	14.3%
		50-75 th	0.38	0.43	13.2%
		25-50 th	0.21	0.26	23.8%
	Winter	75-100 th	0.42	0.47	11.9%
		50-75 th	0.26	0.28	8.7%
		25-50 th	0.06	0.08	33.3%

Supplementary Table 6 Summary of the best subset regressions between SUHIs (75-100th percentiles) and the determinants. The sign 'X' denotes that the determinant is included in the regressions, and the percentage in the parenthesis is the marginal contribution to the final coefficients of determination (R^2).

Time of day	Season	$S(log_{1\theta}(size))$	EVI	Elevation	Albedo	Compactness	Roughness	NTL	\mathbb{R}^2
Daytime	Summer	X (80%)							0.51
		X	X (14%)						0.60
		X	X	X (3%)					0.62
		X	X	X	X (2%)				0.63
		X	X	X	X			X (2%)	0.64
		X	X	X	X	X (<1%)		X	0.64
	Winter	X (79%)							0.34
		X		X (14%)					0.40
		X	X (2%)	X					0.41
		X	X	X	X (2%)				0.42
		X	X	X	X		X (2%)		0.43
		X	X	X	X	X (<1%)	X		0.43
Nighttime	Summer	X (88%)							0.56
		X						X (5%)	0.59
		X		X (3%)				X	0.61
		X	X (3%)	X				X	0.63
		X	X	X			X (2%)	X	0.64
		X	X	X		X (<1%)	X	X	0.64
	Winter	X (94%)							0.47
		X					X (2%)		0.48
		X			X (2%)		X		0.49
		X		X (2%)	X		X		0.50
		X		X	X	X (<1%)	X		0.50

Supplementary Table 7 Summary of the conditional linear regressions of SUHIs of different percentile ranges (75-100th, 50-75th, and 25-50th). The regressions are conditioned on the background climates (arid, cold, temperate and tropical). The standard errors of the coefficient estimations are shown in the parentheses.

Time of day	Season	Percentiles	\mathbb{R}^2	Slope of sigmoid size index $S(log_{10}(size))$				
				Arid	Cold	Temperate	Tropical	
Daytime	Summer	75-100 th	0.76***	0.34 (±0.02) ***	0.91 (±0.04) ***	0.68 (±0.02) *	0.57 (±0.03) ***	
		50-75 th	0.74***	-0.12 (±0.03) ***	0.97 (±0.05) ***	0.63 (±0.04) ***	0.44 (±0.04) ***	
		25-50 th	0.70***	-0.54 (±0.04) ***	1.15 (±0.07) ***	0.60 (±0.04) ***	0.51 (±0.05) ***	
	Winter	75-100 th	0.76***	0.28 (±0.03) ***	0.25 (±0.05) *	0.65 (±0.04) ***	0.96 (±0.04) ***	
		50-75 th	0.73***	-0.08 (±0.04) ***	0.31 (±0.06) ***	0.59 (±0.04) ***	0.68 (±0.05) ***	
		2550^{th}	0.71***	-0.31 (±0.04) ***	0.51 (±0.07) ***	0.46 (±0.05) ***	0.64 (±0.05) ***	
Nighttime	Summer	75-100 th	0.73***	0.28 (±0.03) ***	0.25 (±0.05) *	0.65 (±0.04) ***	0.96 (±0.04) ***	
		50-75 th	0.71***	-0.08 (±0.04) *	0.31 (±0.06) ***	0.59 (±0.04) ***	0.68 (±0.05) ***	
		2550^{th}	0.69***	-0.31 (±0.04) ***	0.51 (±0.07) ***	0.46 (±0.05) ***	0.64 (±0.05) ***	
	Winter	75-100 th	0.54***	1.10 (±0.03) ***	0.95 (±0.06) ***	0.86 (±0.04) ***	0.79 (±0.04) ***	
		50-75 th	0.47***	0.73 (±0.04) ***	0.94 (±0.08) **	0.74 (±0.05) *	0.55 (±0.06) ***	
		$25-50^{th}$	0.42***	0.46 (±0.06) ***	1.07 (±0.10) ***	0.61 (±0.07) *	0.29 (±0.08) *	

 $P \le 0.05$ *, $P \le 0.01$ **, $P \le 0.001$ ***

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Supplementary Table 8 Summary of the conditional linear regression models of air temperature. The regressions are conditioned on the background climates (arid, cold, temperate and tropical). The standard errors of the coefficients are shown in the parentheses.

Time of day	Season	\mathbb{R}^2	Slope of LST			
			Arid	Cold	Temperate	Tropical
Daytime	Summer	0.63***	0.43 (±0.04) ***	0.44 (±0.07) ***	0.44 (±0.05) **	0.30 (±0.08) ***
	Winter	0.87***	0.88 (±0.02) ***	0.69 (±0.03) *	0.69 (±0.06) *	0.85 (±0.02) ***
Nighttime	Summer	0.97***	0.84 (±0.04) ***	0.80 (±0.07) *	0.49 (±0.10) ***	1.04 (±0.05) ***
	Winter	0.95***	0.98 (±0.02) ***	0.88 (±0.04) ***	1.25 (±0.08) ***	0.84 (±0.03) ***

 $P \le 0.05^*, P \le 0.01^{**}, P \le 0.001^{***}$

Supplementary Table 9 Summary of the linear regression models of air temperature, with MOD11A2 and MYD11A2 land surface temperature as independent variables.

MODIS data	Time of day	Season	\mathbb{R}^2
MYD11A2	Daytime	Summer	0.46***
		Winter	0.54***
	Nighttime	Summer	0.82***
		Winter	0.81***
MOD11A2	Daytime	Summer	0.63***
		Winter	0.87***
	Nighttime	Summer	0.97***
		Winter	0.95***

 $P \le 0.05^*$, $P \le 0.01^{**}$, $P \le 0.001^{***}$

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