Mindprint - Math - 7 bins

Felicia Zhang

2018-08-05

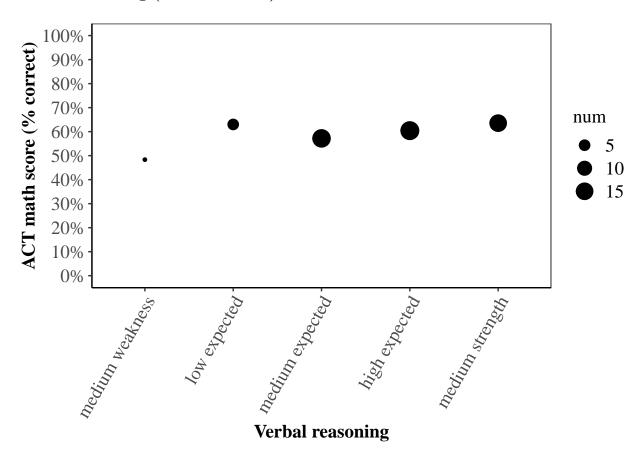
Contents

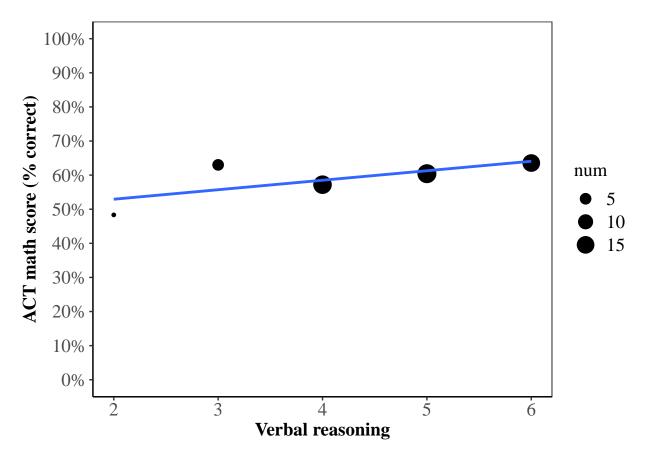
$ACT Math (n = 61) \mid 7 bins$
Overall score
Verbal reasoning (no correlation)
Spatial perception (p = 0.004 , r = 0.95)
EA/ Pre-Algebra/Elementary Algebra Subsection
Visual motor (no correlation)
Spatial perception (p = 0.001 , r = 0.97)
GT/ Plane Geometry/Trigonometry Subsection
Abstract reasoning (no correlation)
Spatial perception (p = 0.009 , r = 0.92)
AG/ Intermediate Algebra/Coordinate Geometry Subsection
Working memory (no correlation)
Spatial perception (p = 0.01, r = 0.92) \dots
Appleseed Suggested Analyses
EA - abstract reasoning model
EA - abstract reasoning broken down by difficulty of questions
GT - abstract reasoning & spatial perception
GT - abstract reasoning & spatial perception broken down by difficulty of
questions
AG - abstract reasoning & spatial perception
AG - abstract reasoning & spatial perception broken down by difficulty of
questions
AG - abstract reasoning & spatial perception & flexible thinking
AG - abstract reasoning & spatial perception & flexible thinking broken down
by difficulty of questions
Summary

ACT Math $(n = 61) \mid 7 \text{ bins}$

Overall score

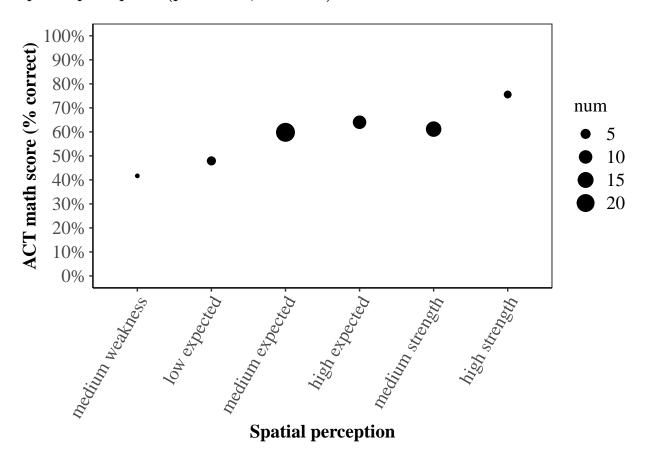
Verbal reasoning (no correlation)

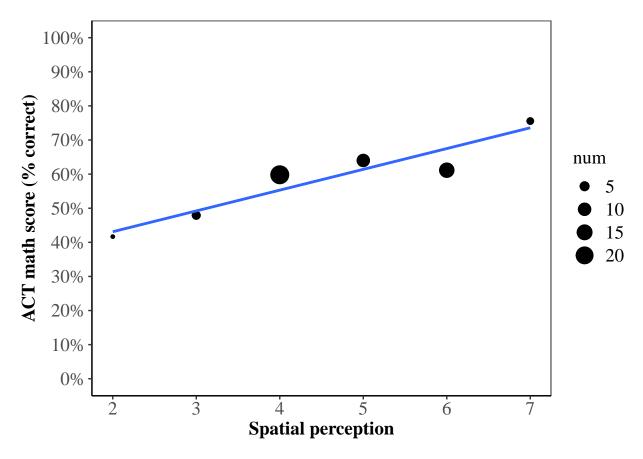




```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = 1.738, df = 3, p-value = 0.1806
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.4637769 0.9788659
## sample estimates:
## cor
## 0.7083136
```

Spatial perception (p = 0.004, r = 0.95)

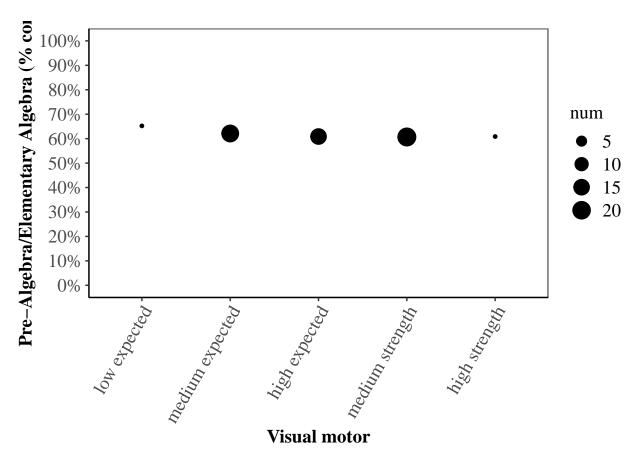


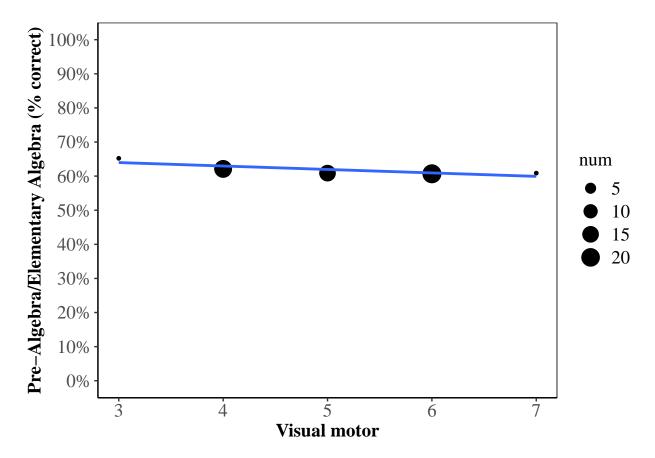


```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = 5.8891, df = 4, p-value = 0.004157
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.5844392 0.9943403
## sample estimates:
## cor
## 0.9468851
```

EA/ Pre-Algebra/Elementary Algebra Subsection

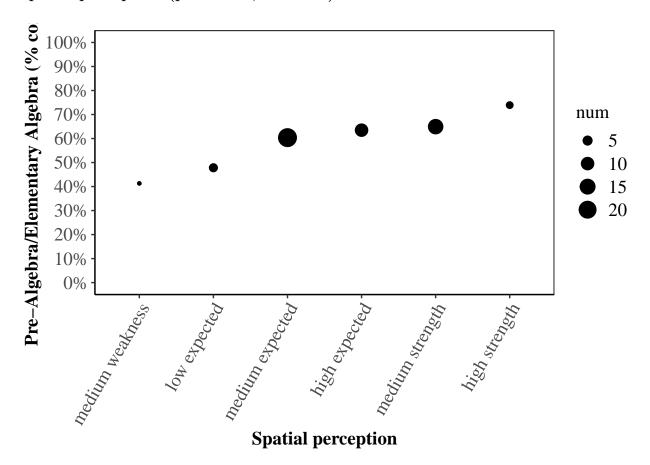
Visual motor (no correlation)

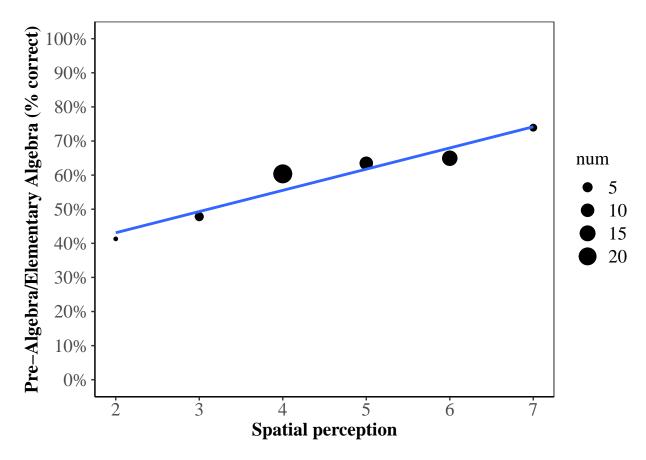




```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = -2.6465, df = 3, p-value = 0.07723
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.9889412 0.1739534
## sample estimates:
## cor
## -0.8367285
```

Spatial perception (p = 0.001, r = 0.97)

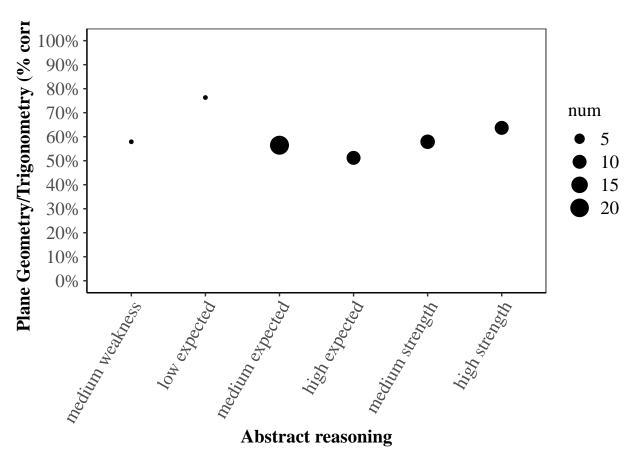


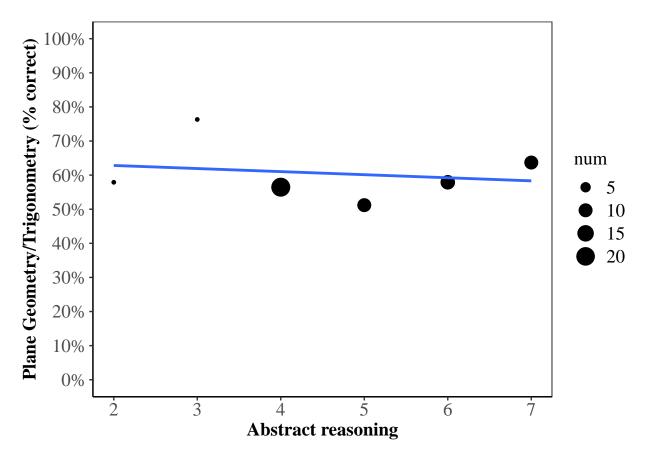


```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = 8.1198, df = 4, p-value = 0.001251
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.7520036 0.9969415
## sample estimates:
## cor
## 0.9709792
```

GT/ Plane Geometry/Trigonometry Subsection

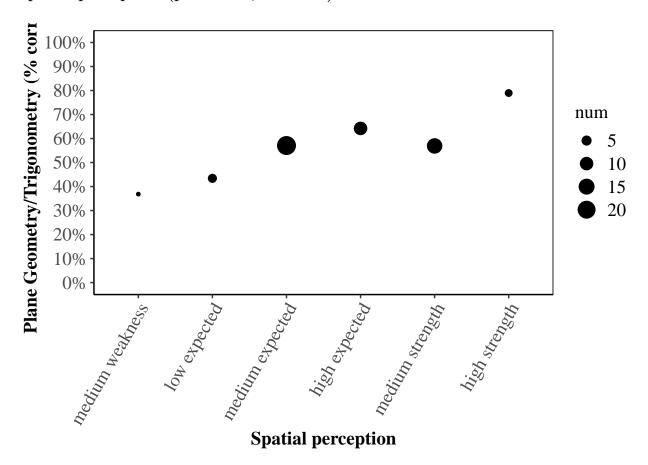
Abstract reasoning (no correlation)

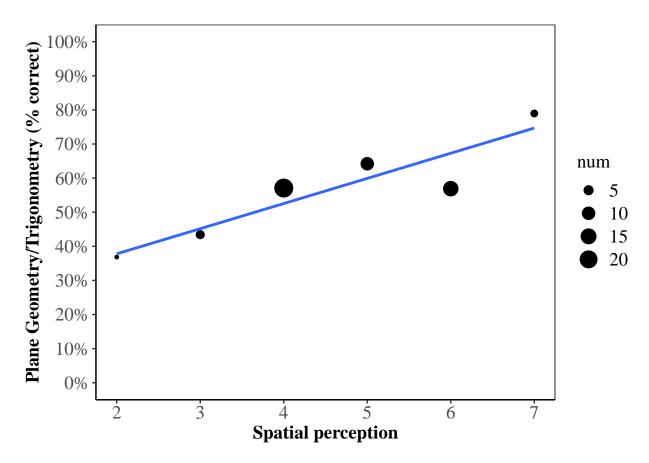




```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = -0.3965, df = 4, p-value = 0.712
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.8688973  0.7327361
## sample estimates:
## cor
## -0.194467
```

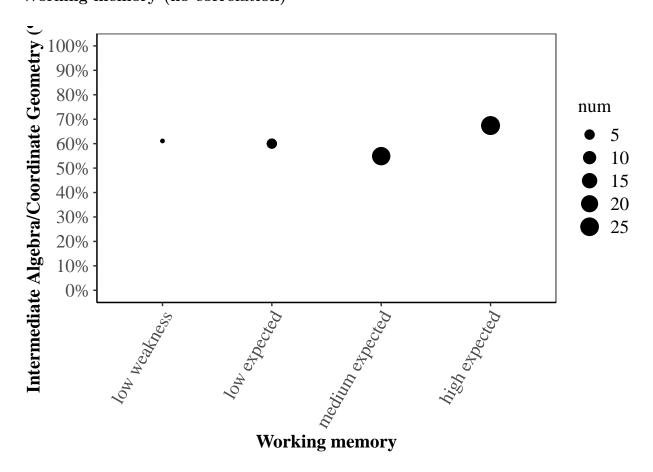
Spatial perception (p = 0.009, r = 0.92)

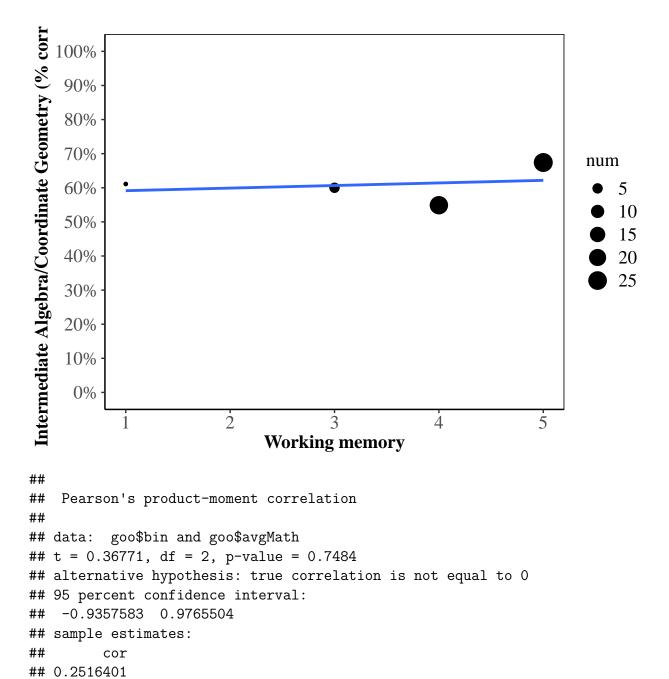




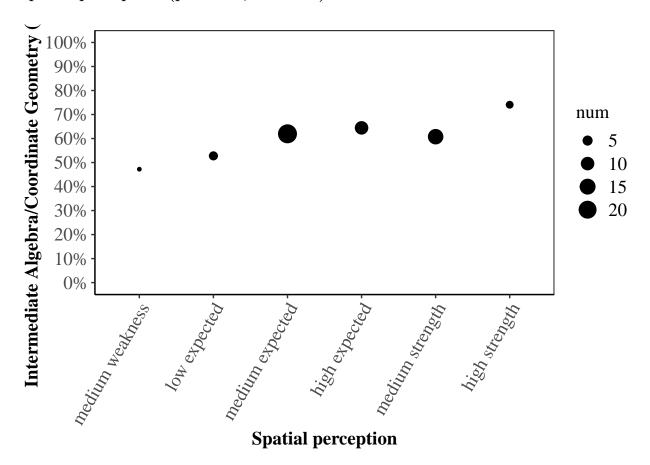
```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = 4.7437, df = 4, p-value = 0.009012
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.4357562 0.9915315
## sample estimates:
## cor
## 0.9214524
```

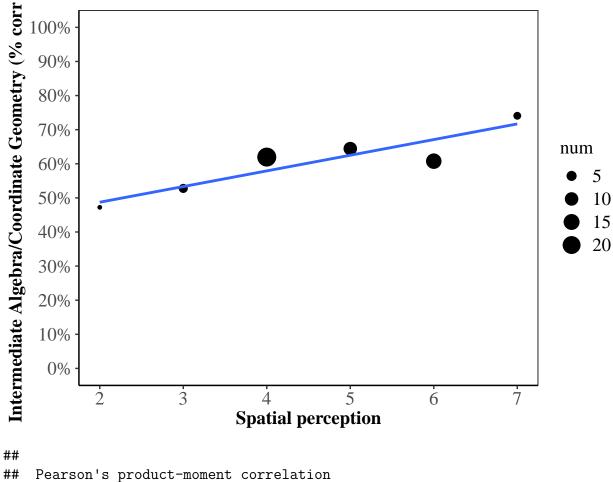
AG/ Intermediate Algebra/Coordinate Geometry Subsection Working memory (no correlation)





Spatial perception (p = 0.01, r = 0.92)





```
##
## Pearson's product-moment correlation
##
## data: goo$bin and goo$avgMath
## t = 4.6397, df = 4, p-value = 0.009737
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.4190758 0.9911802
## sample estimates:
## cor
## 0.9183135
```

Appleseed Suggested Analyses

EA - abstract reasoning model

```
##
## Call:
## lm(formula = EAscore ~ bin, data = EA_AbsRea)
##
## Residuals:
##
                   1Q
                         Median
                                       3Q
                                                Max
## -0.41489 -0.08703 0.01989 0.10330
                                          0.26080
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                             0.07323
                                        6.998 2.72e-09 ***
                 0.51250
## (Intercept)
## bin
                 0.01996
                             0.01409
                                        1.416
                                                  0.162
## ---
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.1423 on 59 degrees of freedom
## Multiple R-squared: 0.03289,
                                       Adjusted R-squared:
## F-statistic: 2.006 on 1 and 59 DF, p-value: 0.1619
Pre–Algebra/Elementary Algebra (% correct)
   100%
    90%
    80%
    70%
                                                                          num
    60%
    50%
                                                                              10
                                                                              15
    40%
                                                                              20
    30%
    20%
    10%
     0%
      medium weallowesexportedium explicitle dexportedium strengthstrength
```

Normed accuracy score for abstract reasoning

Elementary algebra is not predicted by abstract reasoning accuracy (p=0.645).

EA - abstract reasoning broken down by difficulty of questions

```
Level 1 EA
##
## Call:
## lm(formula = EA1 ~ bin_absrea, data = finalDF3)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    3Q
                                           Max
## -0.43567 -0.02729 -0.00710 0.12903 0.14922
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.837316
                         0.080758 10.368 6.52e-15 ***
## bin absrea 0.006732
                         0.015542
                                    0.433
                                             0.667
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1569 on 59 degrees of freedom
## Multiple R-squared: 0.00317,
                                   Adjusted R-squared:
## F-statistic: 0.1876 on 1 and 59 DF, p-value: 0.6665
Level 2 EA
##
## Call:
## lm(formula = EA2 ~ bin absrea, data = finalDF3)
## Residuals:
##
                      Median
                                    3Q
                  1Q
                                           Max
## -0.65521 -0.11392 0.05237 0.13608 0.28172
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
               0.65634
                          0.10850
                                    6.049 1.07e-07 ***
## bin absrea
               0.02065
                          0.02088
                                    0.989
                                             0.327
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2108 on 59 degrees of freedom
## Multiple R-squared: 0.0163, Adjusted R-squared: -0.0003722
## F-statistic: 0.9777 on 1 and 59 DF, p-value: 0.3268
```

```
Level 3 EA
##
## Call:
## lm(formula = EA3 ~ bin_absrea, data = finalDF3)
## Residuals:
##
       Min
                 10
                      Median
                                   30
                                           Max
## -0.55661 -0.28321 -0.03321 0.21679 0.46679
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
               0.43961
                          0.14593
                                    3.013 0.00381 **
## bin absrea
               0.02340
                          0.02808
                                    0.833 0.40809
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2835 on 59 degrees of freedom
## Multiple R-squared: 0.01163,
                                  Adjusted R-squared:
                                                        -0.005122
## F-statistic: 0.6942 on 1 and 59 DF, p-value: 0.4081
Level 4 EA
##
## Call:
## lm(formula = EA4 ~ bin_absrea, data = finalDF3)
##
## Residuals:
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -0.39938 -0.31864 -0.06604 0.26729 0.68136
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.50702
                          0.16341
                                    3.103 0.00294 **
## bin absrea -0.02691
                          0.03145 -0.856 0.39561
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3175 on 59 degrees of freedom
## Multiple R-squared: 0.01226,
                                  Adjusted R-squared:
## F-statistic: 0.7323 on 1 and 59 DF, p-value: 0.3956
Level 5 EA
##
## Call:
## lm(formula = EA5 ~ bin_absrea, data = finalDF3)
```

```
##
## Residuals:
##
      Min
                1Q Median
                               ЗQ
                                      Max
## -0.1737 -0.1673 -0.1640 -0.1576 0.8424
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.180122
                                     0.930
                                              0.356
                          0.193726
## bin_absrea -0.003216
                          0.037283 -0.086
                                              0.932
##
## Residual standard error: 0.3764 on 59 degrees of freedom
## Multiple R-squared: 0.0001261, Adjusted R-squared: -0.01682
## F-statistic: 0.007443 on 1 and 59 DF, p-value: 0.9315
```

Elementary algebra is not predicted by abstract reasoning accuracy.

GT - abstract reasoning & spatial perception

```
##
## Call:
## lm(formula = GTscore ~ bin_absrea + bin_spaper, data = GT_DF2)
##
## Residuals:
                      Median
                                   3Q
##
       Min
                 1Q
                                          Max
## -0.52936 -0.16284 0.03439 0.14535 0.40091
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.3701409 0.1291859
                                     2.865
                                             0.0058 **
## bin absrea -0.0009498 0.0195707 -0.049
                                             0.9615
## bin_spaper
               0.0450297 0.0217292
                                     2.072
                                             0.0427 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1935 on 58 degrees of freedom
## Multiple R-squared: 0.07108,
                                 Adjusted R-squared:
## F-statistic: 2.219 on 2 and 58 DF, p-value: 0.1179
```

Plane geometry/trigonometry is predicted by spatial perception accuracy (p=0.042).

GT - abstract reasoning & spatial perception broken down by difficulty of questions

```
Level 1 GT
##
## Call:
## lm(formula = GT1 ~ bin_absrea + bin_spaper, data = finalDF3)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   ЗQ
                                           Max
## -0.55801 -0.11771 0.09919 0.16928 0.23936
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                    5.677 4.62e-07 ***
## (Intercept) 0.78141
                          0.13765
## bin absrea -0.02271
                          0.02085 - 1.089
                                             0.281
## bin spaper
               0.03504
                          0.02315
                                    1.514
                                             0.136
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2062 on 58 degrees of freedom
## Multiple R-squared: 0.04808,
                                   Adjusted R-squared:
## F-statistic: 1.465 on 2 and 58 DF, p-value: 0.2395
Level 2 GT
##
## Call:
## lm(formula = GT2 ~ bin_absrea + bin_spaper, data = finalDF3)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -0.4940 -0.2071 0.0496 0.2146 0.3365
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.546035
                          0.158602
                                     3.443 0.00107 **
## bin absrea -0.002242
                          0.024027 -0.093 0.92598
## bin spaper
                                   1.552 0.12618
               0.041394
                          0.026677
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2376 on 58 degrees of freedom
## Multiple R-squared: 0.04067, Adjusted R-squared: 0.007585
## F-statistic: 1.229 on 2 and 58 DF, p-value: 0.3
```

```
Level 3 GT
##
## Call:
## lm(formula = GT3 ~ bin_absrea + bin_spaper, data = finalDF3)
## Residuals:
##
       Min
                  10
                      Median
                                    30
                                            Max
## -0.63073 -0.22101 0.00768 0.18847 0.48637
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.08762
                          0.17620
                                    0.497
                                              0.621
## bin absrea
               0.02131
                           0.02669
                                     0.798
                                              0.428
                                    2.335
## bin spaper
               0.06921
                          0.02964
                                             0.023 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2639 on 58 degrees of freedom
## Multiple R-squared: 0.1096, Adjusted R-squared: 0.07888
## F-statistic: 3.569 on 2 and 58 DF, p-value: 0.03453
Level 4 GT
##
## Call:
## lm(formula = GT4 ~ bin absrea + bin spaper, data = finalDF3)
##
## Residuals:
       Min
                  1Q
                      Median
                                    3Q
## -0.43989 -0.23576 -0.06781 0.18219 0.56011
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.14581
                           0.18459 - 0.790
                                            0.4328
## bin absrea
                                            0.6351
               0.01334
                           0.02796
                                    0.477
## bin spaper
               0.08205
                                     2.643
                                            0.0106 *
                          0.03105
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2765 on 58 degrees of freedom
## Multiple R-squared: 0.1219, Adjusted R-squared: 0.09163
## F-statistic: 4.026 on 2 and 58 DF, p-value: 0.02305
Level 5 GT
##
```

```
## Call:
## lm(formula = GT5 ~ bin_absrea + bin_spaper, data = finalDF3)
##
## Residuals:
       Min
                      Median
                                   3Q
                 1Q
                                          Max
## -0.33351 -0.16541 0.01778 0.15160 0.50125
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -0.18381
                          0.13745 -1.337 0.18634
## bin_absrea
               0.01632
                          0.02082
                                   0.784 0.43646
## bin spaper
               0.06691
                          0.02312
                                   2.894 0.00535 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2059 on 58 degrees of freedom
## Multiple R-squared: 0.1512, Adjusted R-squared: 0.1219
## F-statistic: 5.166 on 2 and 58 DF, p-value: 0.008614
```

Difficult questions level 3-5 of plane geometry/trigonometry is predicted by spatial perception accuracy.

AG - abstract reasoning & spatial perception

```
##
## Call:
## lm(formula = AGscore ~ bin_absrea + bin_spaper, data = AG_DF2)
##
## Residuals:
                      Median
                                   3Q
##
       Min
                 1Q
                                          Max
## -0.37201 -0.15112 0.01555 0.12378 0.29466
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                   4.305 6.51e-05 ***
## (Intercept) 0.480461
                         0.111596
## bin absrea 0.004212
                         0.016906
                                   0.249
                                            0.804
                                            0.202
## bin_spaper 0.024232
                         0.018771 1.291
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1672 on 58 degrees of freedom
## Multiple R-squared: 0.03234,
                                  Adjusted R-squared:
                                                       -0.00103
## F-statistic: 0.9691 on 2 and 58 DF, p-value: 0.3855
```

Algebra/coordinate geometry is not predicted by abstract reasoning or spatial perception.

AG - abstract reasoning & spatial perception broken down by difficulty of questions

```
Level 1 AG
##
## Call:
## lm(formula = AG1 ~ bin_absrea + bin_spaper, data = finalDF3)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   30
                                           Max
## -0.93163 -0.18262 0.09455 0.23438 0.42655
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.35510
                          0.21392
                                    1.660
## bin absrea
               0.01309
                          0.03241
                                    0.404
                                            0.6878
## bin spaper
               0.08300
                          0.03598
                                    2.307
                                            0.0247 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3204 on 58 degrees of freedom
## Multiple R-squared: 0.09534,
                                   Adjusted R-squared:
## F-statistic: 3.056 on 2 and 58 DF, p-value: 0.05472
Level 2 AG
##
## Call:
## lm(formula = AG2 ~ bin_absrea + bin_spaper, data = finalDF3)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -0.8110 -0.2023 0.1890 0.2714 0.3556
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.84088
                                    3.886 0.000264 ***
                          0.21637
## bin absrea
               0.01315
                          0.03278
                                    0.401 0.689846
## bin spaper -0.04122
                          0.03639 -1.133 0.262042
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3241 on 58 degrees of freedom
## Multiple R-squared: 0.02215, Adjusted R-squared:
                                                       -0.01157
## F-statistic: 0.6568 on 2 and 58 DF, p-value: 0.5223
```

```
Level 3 AG
##
## Call:
## lm(formula = AG3 ~ bin_absrea + bin_spaper, data = finalDF3)
## Residuals:
##
       Min
                 10
                      Median
                                   30
                                           Max
## -0.51651 -0.14286 0.03434 0.17586 0.37119
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.30137
                          0.15033
                                    2.005
                                            0.0497 *
## bin absrea
               0.02690
                          0.02277 1.181
                                            0.2424
## bin spaper
               0.04151
                          0.02529
                                   1.642
                                            0.1061
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2252 on 58 degrees of freedom
                                   Adjusted R-squared:
## Multiple R-squared: 0.08059,
## F-statistic: 2.542 on 2 and 58 DF, p-value: 0.08746
Level 4 AG
##
## Call:
## lm(formula = AG4 ~ bin absrea + bin spaper, data = finalDF3)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -0.4777 -0.1073 -0.0331 0.2141 0.6091
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.35318
                          0.19593
                                    1.803
                                            0.0767 .
## bin absrea -0.02451
                          0.02968 -0.826
                                            0.4123
## bin spaper
               0.03710
                          0.03296
                                    1.126
                                            0.2649
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2935 on 58 degrees of freedom
## Multiple R-squared: 0.0275, Adjusted R-squared: -0.006039
## F-statistic: 0.8199 on 2 and 58 DF, p-value: 0.4455
Level 5 AG
##
```

```
## Call:
## lm(formula = AG5 ~ bin absrea + bin spaper, data = finalDF3)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -0.2829 -0.1594 -0.1083 0.2682 0.8118
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.340451
                          0.177155
                                     1.922
                                             0.0596 .
## bin_absrea -0.043652
                          0.026838 -1.627
                                             0.1093
## bin spaper
               0.007435
                          0.029798
                                     0.250
                                             0.8038
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2653 on 58 degrees of freedom
## Multiple R-squared: 0.04373,
                                   Adjusted R-squared:
## F-statistic: 1.326 on 2 and 58 DF, p-value: 0.2734
```

Overall algebra/coordinate geometry is not predicted by abstract reasoning or spatial perception. But level 1 algebra/coordinate geometry is predicted by spatial perception.

AG - abstract reasoning & spatial perception & flexible thinking

```
##
## Call:
## lm(formula = AGscore ~ bin_absrea + bin_spaper + bin_flexthin,
##
      data = AG_DF2)
##
## Residuals:
##
       Min
                1Q
                    Median
                                3Q
                                       Max
## -0.39426 -0.14305 0.01244 0.12100 0.31039
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.436758
                       ## bin_absrea 0.005031
                       0.016976 0.296 0.768024
## bin spaper 0.020910
                       0.019225 1.088 0.281344
## bin flexthin 0.012660
                       ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1676 on 57 degrees of freedom
## Multiple R-squared: 0.04426,
                             Adjusted R-squared: -0.006041
## F-statistic: 0.8799 on 3 and 57 DF, p-value: 0.457
```

Algebra/coordinate geometry is not predicted by abstract reasoning, spatial perception or flexible thinking.

AG - abstract reasoning & spatial perception & flexible thinking broken down by difficulty of questions

```
Level 1 AG
##
## Call:
## lm(formula = AG1 ~ bin_absrea + bin_spaper + bin_flexthin, data = finalDF3)
##
## Residuals:
##
      Min
                1Q Median
                               3Q
                                      Max
## -0.9241 -0.1735 0.0918 0.2357
                                   0.4232
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                0.31438
                           0.23747
                                     1.324
                                             0.1908
## bin absrea
                0.01385
                           0.03270
                                     0.424
                                             0.6734
## bin spaper
                0.07991
                           0.03703
                                     2.158
                                             0.0352 *
## bin flexthin 0.01179
                           0.02892
                                     0.408
                                             0.6849
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3227 on 57 degrees of freedom
## Multiple R-squared: 0.09797,
                                 Adjusted R-squared: 0.05049
## F-statistic: 2.064 on 3 and 57 DF, p-value: 0.1152
Level 2 AG
##
## Call:
## lm(formula = AG2 ~ bin_absrea + bin_spaper + bin_flexthin, data = finalDF3)
##
## Residuals:
##
      Min
               10 Median
                               3Q
                                      Max
## -0.8171 -0.2163 0.1577 0.2766 0.3589
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                0.76666
                           0.23940
                                     3.202 0.00223 **
## bin absrea
                0.01454
                           0.03296
                                     0.441 0.66084
## bin spaper
               -0.04686
                           0.03733 -1.255 0.21448
## bin flexthin 0.02150
                           0.02915
                                     0.738 0.46375
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.3254 on 57 degrees of freedom
```

```
Adjusted R-squared:
## Multiple R-squared: 0.03139,
                                                        -0.01959
## F-statistic: 0.6158 on 3 and 57 DF, p-value: 0.6076
Level 3 AG
##
## Call:
## lm(formula = AG3 ~ bin_absrea + bin_spaper + bin_flexthin, data = finalDF3)
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -0.47846 -0.14512 0.00586 0.17897 0.39066
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                0.24098
                           0.16604 1.451
                                               0.152
## bin absrea
                 0.02803
                            0.02286
                                     1.226
                                               0.225
## bin spaper
                           0.02589
                 0.03692
                                     1.426
                                               0.159
## bin flexthin 0.01749
                           0.02022
                                     0.865
                                               0.391
##
## Residual standard error: 0.2257 on 57 degrees of freedom
## Multiple R-squared: 0.09251,
                                   Adjusted R-squared:
## F-statistic: 1.937 on 3 and 57 DF, p-value: 0.1339
Level 4 AG
##
## Call:
## lm(formula = AG4 ~ bin_absrea + bin_spaper + bin_flexthin, data = finalDF3)
##
## Residuals:
       Min
                  1Q
                       Median
                                    3Q
## -0.47793 -0.10717 -0.03335 0.21325
                                      0.60956
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                                       1.625
## (Intercept)
                0.3540621 0.2178221
                                                 0.110
## bin absrea
                           0.0299909 -0.818
               -0.0245267
                                                 0.417
                0.0371663 0.0339647
                                       1.094
                                                 0.278
## bin spaper
## bin flexthin -0.0002563
                           0.0265232
                                      -0.010
                                                 0.992
##
## Residual standard error: 0.296 on 57 degrees of freedom
## Multiple R-squared: 0.0275, Adjusted R-squared: -0.02369
## F-statistic: 0.5372 on 3 and 57 DF, p-value: 0.6587
Level 5 AG
```

##

```
## Call:
## lm(formula = AG5 ~ bin absrea + bin spaper + bin flexthin, data = finalDF3)
##
## Residuals:
      Min
                1Q Median
##
                                3Q
                                       Max
## -0.3070 -0.1712 -0.1101 0.2392 0.8412
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 0.289291
                            0.196285
                                       1.474
                                                0.146
## bin_absrea
                -0.042693
                            0.027026
                                      -1.580
                                                 0.120
## bin spaper
                 0.003547
                            0.030606
                                       0.116
                                                0.908
## bin flexthin 0.014820
                            0.023901
                                       0.620
                                                0.538
##
## Residual standard error: 0.2668 on 57 degrees of freedom
## Multiple R-squared: 0.05014,
                                    Adjusted R-squared:
                                                          0.0001434
## F-statistic: 1.003 on 3 and 57 DF, p-value: 0.3983
```

Algebra/coordinate geometry is not predicted by abstract reasoning, spatial perception or flexible thinking. But level 1 algebra/coordinate geometry is predicted by spatial perception.

Summary

- 1. Overall math score is predicted by spatial perception.
- 2. Elementary algebra score is predicted by spatial perception. It is not predicted by abstract reasoning even when broken down by question difficulty.
- 3. Plane geometry/trigonometry score is predicted by spatial perception. Specifically, level 3-5 difficulty, of plane geometry/trigonometry is predicted by spatial perception.
- 4. Intermediate algebra/coordinate geometry is predicted by spatial perception (univariate analysis).
 - Intermediate algebra/coordinate geometry is not predicted by abstract reasoning, spatial perception or flexible thinking (multivariate analysis).
 - But level 1 algebra/coordinate geometry is predicted by spatial perception.