

X-RAY RESONANT RAMAN SCATTERING

SPECTRA SIMULATION FROM FIRST PRINCIPLES FOR COPPER BELLOW IONIZATION THRESHOLD USING HIGH-PERFORMANCE COMPUTING

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BSc in Physics Engineering

DOCTORATE IN PHYSICS ENGINEERING



DEPARTMENT OF PHYSICS

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X-ray resonant Raman scattering

Spectra simulation from first principles for Copper bellow ionization threshold using high-performance computing

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Acknowledgments are personal text and should be a free expression of the author.

However, without any intention of conditioning the form or content of this text, I would like to add that it usually starts with academic thanks (instructors, etc.); then institutional thanks (Research Center, Department, Faculty, University, FCT / MEC scholarships, etc.) and, finally, the personal ones (friends, family, etc.).

But I insist that there are no fixed rules for this text, and it must, above all, express what the author feels.

"Sometimes I'll start a sentence, and I don't even know where it's going.

I just hope I find it along the way.

Like an improv conversation."

An improversation."

— **Michael Scott**, The Office (Regional Manager of Dunder Mifflin Scranton)

"

"all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy all work and no play makes Jack a dull boy

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— Jack Torrance, The Shinning (Caretaker of the Overlook)

Abstract

The work performed on this thesis comes as part of the effort to further understand the highly convoluted structure present on Copper's X-ray emission spectra, where, as with many other transition metals, a skewness can be observed on the $K_{\alpha_{1,2}}$, K_{β} and L transition lines. These lines originate due to the radiative relaxation of the atom's electronic structure post-ionization of inner shell electrons. However, it is very likely that the observed skewness is due to copper's satellite states' transitions.

Throughout this thesis, a study will be performed for the satellite states formed by the excitation of the inner-shell electrons, where, as opposed to the ionization process, usually considered in X-ray calculations, a photoexcitation process occurs.

Multiple atomic structure calculations will be performed using the *ab initio* state of the art Multiconfiguration Dirac-Fock General Matrix Elements (*MCDFGME*) code for different excited states configurations.

The obtained results will then be used in the analysis of experimental data obtained from a High-Precision Double Crystal Spectrometer (DCS), using a synchrotron X-ray source.

Due to the complexity of the calculations, the process can become substantial in terms of computational power and time. Therefore, further similar and more complex studies will be performed by implementing and running a script in the *Oblivion* supercomputer located at the University of Évora.

Keywords: Atomic Excitation, X-ray lines, *MCDFGME*, DCS, High Performance Computing

Resumo

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Listings

Glossary

Feynman Diagram 2D diagram depicting various physical interactions between

elementary particles. Fermions are depectied as straight lines

and bosons as wavy lines. (p. 40)

four-vector Vector used in special relativity composed of 4 components,

one scalar time-like, and three vectorial space-like. These vectors behave in special way, such as their norm being Lorentz invariant. Can be written in covariant, X_{μ} , and contravariant form, X^{μ} , with the difference being the sign of the time-like components. Example of a contravariant four vector: X^{μ} =

 $(X^0, X^1, X^2, X^3) = (X^0, X) (pp. xiv, 9)$

Lorentz invariant A Lorentz invariant scalar, obtained, for example, from a

Minkowski norm, does not change when operated by a Lorentz

Transformation. (pp. xiv, 9)

Minkowski norm Yields the Lorentz Invariant norm for a four-vector: $p_{\mu}p^{\mu}$.

Equivalent to the dot product of a classical vector. (pp. xiv, 9)

self consistency method The electron wavefunctions go through a variational process

in order to reach convergence for an energetic minimum. (p. 7)

virtual photons While in reality, during a Coulomb interaction, 'real' particles

are not exchanged, the electromagnetic field is still mediated by photons. This way virtual photons are tools used in order

to better represent electromagnetic interactions. (p. 11)

Acronyms

Grasp2k General-purpose Relativistic Atomic Structure Package 2k (p. 13)

MCDFGME Multiconfiguration Dirac-Fock General Matrix Elements (pp. vi, viii, ix, 12–15,

18, 22)

MCDF Multiconfiguration Dirac-Fock (pp. viii, 11, 18)

MPI Message Passing Interface (pp. ix, 24)

ASC Atomic Structure Calculations (pp. ix, 32)

DCS Double Crystal Spectrometer (p. vi)

EMF Electromagnetic Field (pp. 6, 11, 17)

FAC Flexible Atomic Code (p. 13)

HF Hartree-Fock (p. 8)

HPC High Performance Computing (pp. ix, 32)

QED Quantum Electrodynamics (pp. viii, 2, 11, 14, 18)

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Theoretical Introduction

Falta introdução? Meter a conversa dos FP de 2008

Throughout this thesis, different topics regarding Quantum Mechanics, Atomic Physics and spectroscopy will be approached, hence why a theoretical introduction is needed. In it, themes such as the characteristic X-rays of elements, the relativistic Dirac equation and QED corrections and methods for solving the many-body problem will be discussed.

1.1 Characteristic X-rays

When subjected to a high energy beam of particles (usually photons or electrons), an element may go through the process of the ionization of inner-core electrons, which is followed by the emission of radiation of its own, in the form of X-rays and/or Auger electrons. The radiation emitted throughout this process presents well-defined energy values and thus provides a way to ascertain if an element is present in a sample under study. Due to this reason, these characteristic emissions are of an extremely high importance in a wide range of scientific areas.

When an atomic system is in a bound state, the electrons orbiting the nucleus are occupying fixed quantum states, defined by their principal atomic number, n, angular momentum, l, and spin, s. Electrons are also fermions, and thus must respect Pauli's exclusion principle, each occupying a single state, only occupied by that single electron. These quantum numbers provide information about each electron's wavefunction, and the collection of all the electrons' wavefunctions can be used in order to describe the whole system. When operating the Hamiltonian on this collection of wavefunctions, the atomic system's state's energy is obtained. Besides all the occupied states, an infinite more number of possible eigenfunctions will compose that system's base.

1.1.1 Ionization as a vacancy generator

As previously mentioned, X-ray fluorescence spectroscopy has many uses and applications in a wide range of scientific areas. In this form of spectroscopy, the element at study, composed of a nucleus and *N* orbiting electrons, is bombarded with radiation leading to the ionization of inner-shell electrons while leaving a vacancy in their place (Figure 1.1).

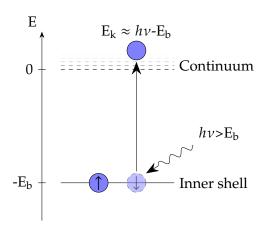


Figure 1.1: Photoionization.

The atomic structure, now composed of N-1 electrons, will be left in an energetically unstable state, due to there being other possible lower energy states. This will lead to various processes of atomic relaxation, where the system will rearrange itself in order to find a lower energy configuration.

The main processes for this rearrangement are two competing decay paths: radiative relaxation, and Auger electron emission.

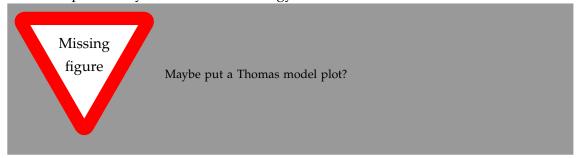


Figure 1.2: Principal atomic relaxation processes.

In the case of radiative relaxation, an upper shell electron will move and occupy the hole left in the inner shell. During this process, energy is released through the emission of photons with energy in the range of X-rays. The detection of these photons is what allows for an analysis and detection of the element at study.

On the other hand, an Auger emission occurs when in the process of an upper electron shifting to a shell hole, energy is released not in the form of photons, but by the atomic system going through the process of the ionization of a lesser bound electron.

In reality, when the initial vacancy is generated, two more processes can occur: shakeoff and shake-up. Due to a sudden change in the potential felt by the remaining electrons, whilst going through the ionization, one other electron may become unbound, leading to a second ionization, the shake-off process, or may be excited to an upper state, during shake-up. These processes' occurrence probabilities are related to the rate at which the electron leaves the system during the first ionization. For lower electron emission energies, where the ionization process is rather "slow", and there is not much energy for shake up/off to occur, the adiabatic regime reigns. In this regime, the shake probabilities are small, and increase with the beam's energy. For higher energies, the transition occurs in the sudden regime, where the electrons' exit can be considered instantaneous. Now, while the shake probabilities still increase with the energy of the beam, they quickly saturate for a maximum value of probability, which can be calculated by computing overlaps between the electrons' initial and final states. These processes, however, are out of scope for this thesis, but should the reader be interested, the model conceived by Thomas [1] predicts the shake probability as a function of energy.



1.1.2 Transition notation

The characteristic radiation measured from the radiative relaxation of a post-ionization unstable atomic system is one of the main ways of identifying an atomic element. This is due to the photons emitted possessing quantized values of energy, forming well-defined energy lines when observed in a spectrometer. In order to understand the change that occurred in the atomic system which lead to a specific emission, the spectral lines get labels based on a notation which usually takes into account the initial and final orbitals where the vacancy was present. A very illustrative diagram, exemplifying some transitions can be found in Appendix B.

Throughout this thesis, Siegbahn notation will be used, for the most part, but should the reader prefer IUPAC's, Table 1.1 has the conversion between notations.

1.1.3 Excitation as a vacancy generator

As previously mentioned, throughout this thesis, while the study is focused on the characteristic radiation emitted during an atomic relaxation process, the main vacancy generation method at study shall be the photoexcitation process (Figure 1.3), instead of ionization. The levels obtained after a photoexcitation of core shell electrons has occurred could be some of the many so-called satellite states, where the electronic configuration present during the relaxation process contains additional electrons or holes, or is simply not

Siegbahn	IUPAC	Siegbahn	IUPAC	Siegbahn	IUPAC
K_{α_1}	$K-L_3$	L_{α_1}	$L_3 - M_5$	L_{γ_1}	$L_2 - N_4$
K_{α_2}	$K-L_2$	L_{α_2}	$L_3 - M_4$	L_{γ_2}	$L_1 - N_1$
K_{eta_1}	$K-M_3$	L_{eta_1}	$L_2 - M_4$	L_{γ_3}	$L_1 - N_2$
$K^I_{eta_2}$	$K-N_3$	L_{β_2}	$L_3 - N_5$	L_{γ_4}	$L_1 - O_3$
$K^{'Iar{I}}_{eta_2}$	$K-N_2$	L_{eta_3}	$L_1 - M_3$	$L_{\gamma'_{4}}$	$L_1 - O_2$
K_{β_3}	$K-M_2$	L_{β_4}	$L_1 - M_2$	L_{γ_5}	$L_2 - N_1$
$K_{eta_4}^{I}$	$K-N_5$	L_{eta_5}	$L_3 - O_{4,5}$	L_{γ_5}	$L_2 - O_4$
$K_{eta_4}^{'II}$	$K-N_4$	L_{eta_6}	$L_3 - N_1$	L_{γ_8}	$L_2 - O_1$
$K^{x}_{\beta_4}$	$K-N_4$	L_{β_7}	$L_3 - O_1$	$L_{\gamma_8'}$	$L_2 - N_{5,6}$
$K_{\beta_5}^{I}$	$K-M_5$	L_{β_8}	$L_3 - N_{6,7}$	L_{η}	$L_2 - M_1$
$K_{eta_4}^{II}$	$K-M_4$	L_{β_9}	$L_1 - M_5$	L_l	$L_3 - M_1$
,		L_{β_9}	$L_1 - M_4$	L_s	$L_3 - M_3$
		L_{β_9}	$L_3 - N_4$	L_t	$L_3 - M_2$
		L_{β_9}	$L_2 - M_3$	L_u	$L_3 - N_{6,7}$
				L_v	$L_2 - N_{6,7}$

Table 1.1: Siegbahn VS IUPAC notation. Adapted from [2].

the standard configuration when talking about characteristic emissions. The characteristic radiation from transitions that originated from these states are one of the keys needed to fully comprehend and deconvolute an element's emission spectra.

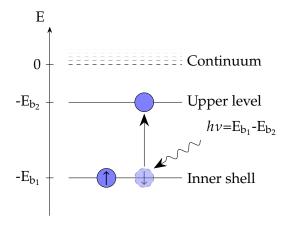


Figure 1.3: Resonant Photoexcitation

1.2 Radiative transitions

In terms of quantum mechanics, the properties of a system's change of state can be derived using perturbation theory, where a change in energy can be treated as perturbation, and takes into account the conservation laws physical properties, such as the angular momentum of the system as basis for the selection rules.

The transition's radiation type can be of two main flavors, Electric, E_k , or Magnetic, M_k ,

with k representing its multiplicity. These labels indicate which of the Electromagnetic Field (EMF) component had the strongest influence on the transition's occurrence. For both these types of transitions, the system's total angular momentum is allowed a change of $\Delta J = 0, \pm k$, and so does its projection, M_J . However, different transitions lead to different changes of parity in the system and to different selection rules.

It should also be of note that, usually, for the same multiplicity, an *E* transition is more intense than an *M*, and that it is also possible for rare 2-photon transitions to take place, where a combination of different transition types can occur.

The intensity of a transition is proportional to the squared norm of the perturbation's matrix element involving the initial and final state $\left(\Gamma_{if} \propto \left|\left\langle \psi_i \middle| H' \middle| \psi_f \right\rangle \right|^2\right)$. It should also be noted that the electron's initial state population will serve as a scaling factor for the transitions' rate. For example, while the transition rate for a $2p_{1/2} \to 1s$ and $2p_{3/2} \to 1s$ should be about the same, the orbital $2p_{3/2}$ has double the population $2p_{1/2}$ has, hence why the K_{α_2} line has about half the K_{α_1} line's intensity.

One should also mention that monochromatic transitions do not exist. While the transition might have a well-defined energy, calculated by the difference in energy between the initial and final levels, due to Heisenberg's uncertainty principle, $\Delta E \Delta t > \frac{\hbar}{2}$, there will exist a natural energy broadening, the transition's natural width. The shapes representing these transitions are given by a Lorentzian distribution.

1.3 Solving the atomic many-body problem

When studying a system composed of multiple charged bodies, one must consider all the existing interactions. Whilst there are known analytical solutions for 2-bodies Hydrogenoid systems, with the presence of more non spatially-bound particles, the Coulomb interaction pairs lead to the impossibility of finding a set of analytical wavefunctions which are a part of the Hamiltonian's eigenset. Consecutively, the need for a numerical method that is able to compute solutions for these complex systems arose.

1.3.1 The non-relativistic Hamiltonian

The first approach used in order to solve the many-bodies problem used a non-relativistic consideration. This way, the Hamiltonian consists on the sum of the system's non-relativistic momentum-related energies and the energy of Coulomb interactions between all the bodies in the system, while considering the nucleus as fixed in space, due to it being thousands of times more massive than the orbiting electrons.

Essentially, and in atomic units:

$$\sum_{i}^{N} \underbrace{\frac{1}{2} \nabla_{i}^{2} - \frac{Z}{r_{i}}}_{Individual Hamiltonian} + \underbrace{\sum_{i < j}^{j} \underbrace{\frac{1}{r_{ij}}}_{Pair repulsion}}_{Pair repulsion},$$

$$E_1 \rightarrow$$
 Momentum $E_2 \rightarrow$ e⁻nuc. Coulomb attraction $E_3 \rightarrow$ e⁻e⁻ Coulomb repulsion (1.1)

1.3.2 The Hartree-Fock Method

This numerical method is one of the staple and most enduring procedures for solving the problem associated with a many-body system. As a side note, an in-depth explanation on all the intricacies of this method can be found in many of the literature, but as for the writing of this thesis, the works [3–6] were the ones consulted.

Hartree developed an iterative method, further enhanced by Fock and Slater, based on the field's self consistency method. In this approach, when studying a multi-electronic system, such as an atom, each electron's wavefuction is composed as a product of a spacial part, ψ , and one related to the electron's spin, χ , as to be able to account for Pauli's exclusion principle and, if so desired, relativistic effects.

$$u = \psi \chi, \tag{1.2}$$

The wavefuction capable of describing the whole system, Ψ , should be somewhat of a product of all the wavefunctions describing each individual electron. However, one must not forget the need for this wavefunction to respect the antisymmetry principle, due to the electron's fermionic nature. In order to achieve this, Ψ is to be composed of a Slater determinant:

Explain antisymmetry and put it in the glossary

Explain in the glossary

$$\Psi = \frac{1}{\sqrt{N!}} \begin{vmatrix} u_1(x_1) & u_2(x_1) & \cdots & u_N(x_1) \\ u_1(x_2) & u_2(x_2) & \cdots & u_N(x_2) \\ \vdots & \vdots & \ddots & \vdots \\ u_1(x_N) & u_2(x_N) & \cdots & u_N(x_N) \end{vmatrix},$$
(1.3)

It is of high importance that the set of basis wavefunctions respects orthonormality. These are to be initialized as trial wavefunctions for the numerical method.

The main goal for this algorithm is to, as per the self consistency method, follow the variational principle with the goal of minimize a functional, as a way of reaching an energetic minimum. This optimal, yet unknown energy, E_0 (calculated by operating the Hamiltonian on the system's optimal wavefunctions), will attempt to be reached by the variation of the trial wavefunctions that provide a non-minimized solution. Whilst the optimal wavefunctions will never be reached, the purpose of this method is to reach a

solution that yields an energetic value as close as possible to E_0 , while always yielding $\langle \Psi | H | \Psi \rangle \geq E_0$, due to the numerical nature of the method.

The computational method consists on starting with the previously mentioned trial wavefunctions and employing them in the Hartree-Fock's potential calculation through the Hartree-Fock (HF) equations.

Finish the explanation

In an over-simplistic scheme, the self-consistent Hartree-Fock computational method can be represented by the block diagram in Figure 1.4.

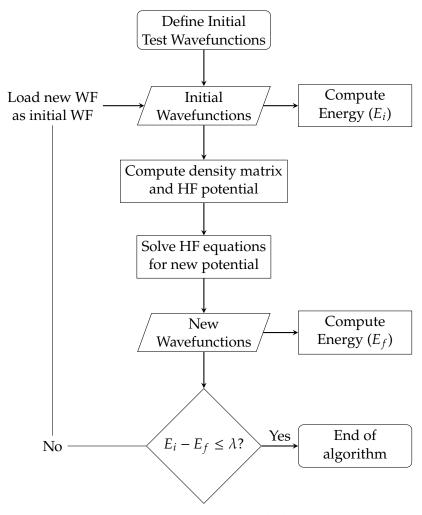


Figure 1.4: HF method's block diagram.

1.3.3 The Dirac Equation

While Schrödinger's equation may be one of the most significant and impactful equations in Modern Physics, it is also not free of its of limitations. The fact that it does not account for the existence of the electron's spin and the lack of consideration of relativistic effects are some of the most impactful setbacks. Consulting the works in [7–10], this work will follow an exploration of different approaches that followed in order to solve the aforementioned problem.

Many scientists, such as Klein, Gordon and later Fock, had already conceived a relativistic correction to Schrödinger's equation, where the free-particle energy makes use of the relativistic momentum-energy relation, as displayed in equation (1.4).

$$E = \sqrt{c^2 p^2 + m^2 c^4},\tag{1.4}$$

This notable definition can be derived from the Lorentz invariant scalar produced by Minkowski norm of the momentum four-vector (1.5).

$$p^{\mu}p_{\mu} = m^2c^2 \Leftrightarrow \frac{E^2}{c^2} - p^2 = m^2c^2 \Leftrightarrow \frac{E^2}{c^2} = p^2 + m^2c^2,$$
 (1.5)

Now, inputting this new energy operator into Schrödinger's equation, yields the Klein-Gordon equation (1.6), allowing for Schrödinger's equation to now be Lorentz-invariant (proof can be found in Strickland's book [11]).

$$-\hbar^2 \frac{\partial^2}{\partial t^2} \psi = \left(-c^2 \hbar^2 \nabla^2 + m^2 c^4 \right) \psi, \tag{1.6}$$

This new approach was, however, still limited, as it only described spin 0 particles (e.g., some mesons), and made use of a second order derivative in the time-like component.___

Came 1928 and a new equation was developed by Paul Dirac [12], one taking now into account not the classical 3 dimensional space components, but the relativistic four components.

Try to explain why this might be a problem

Dirac started by rewriting the energy-momentum relation, ending up with an equivalent equation (1.7), employing 4×4 matrices, due to the 4 relativistic dimensions at play, and incorporating spins into the equation by making use of the Pauli matrices (1.9).

$$E = c\alpha \cdot p + \beta mc^2, \quad \alpha = (\alpha_1, \alpha_2, \alpha_3), \tag{1.7}$$

$$\alpha_i = \begin{pmatrix} 0 & \sigma_i \\ \sigma_i & 0 \end{pmatrix} \qquad \beta = \begin{pmatrix} I_2 & 0 \\ 0 & -I_2 \end{pmatrix} \qquad I_2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \tag{1.8}$$

$$\sigma_1 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \qquad \qquad \sigma_2 = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \qquad \qquad \sigma_3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}, \tag{1.9}$$

In order to fully comprehend this shift of notation, one should equate the square of the two equations, (1.4) and (1.7), and confirm its validity.

$$c^{2} p^{2} + m^{2} c^{4} = c^{2} \alpha^{2} p^{2} + 2mc^{3} \alpha \cdot p \cdot \beta + \beta^{2} m^{2} c^{4}, \tag{1.10}$$

In order for this equation to make sense, the following conditions must be true (which in fact, they are):

do the demonstration, dummy

$$\begin{cases} c^{2} \mathbf{p}^{2} = c^{2} \alpha^{2} p^{2} & \Leftrightarrow \alpha^{2} = 1 \\ 0 = 2mc^{3} p \alpha \beta & \Leftrightarrow \alpha \beta = 0 , \\ m^{2} c^{4} = \beta^{2} m^{2} c^{4} & \Leftrightarrow \beta^{2} = 1 \end{cases}$$

$$(1.11)$$

Taking the previous considerations into account, one can now construct Dirac's free-particle equation (1.12):

$$i\hbar \frac{\partial}{\partial t} \boldsymbol{\psi} = \left(c \boldsymbol{\alpha} \cdot \boldsymbol{p} + \beta m c^2 \right) \boldsymbol{\psi} = \begin{pmatrix} m c^2 I_2 & -i\hbar c \boldsymbol{\sigma} \cdot \boldsymbol{\nabla} \\ -i\hbar c \boldsymbol{\sigma} \cdot \boldsymbol{\nabla} & -m c^2 I_2 \end{pmatrix} \cdot \begin{pmatrix} \psi_1 \\ \vdots \\ \psi_4 \end{pmatrix}, \tag{1.12}$$

This equation, however, as mentioned above, can only describe a single particle present in a field-free region. In order to account for the existence of a field, such as the electromagnetic field, derived from the four-potential A^{μ} , composed by the electric scalar potential field, $A^0 = \phi$, and the vector potential, $(A^1, A^2, A^3) = A$, the following change on the momentum four-vector must be made:

$$p^{\mu} \to p^{\mu} - eA^{\mu}, \quad A^{\mu} = (\phi, A),$$
 (1.13)

The Hamiltonian can now be rewritten as to account for the presence of the electromagnetic field (1.14). This way it is possible to include, for example, the electron-nucleus Coulomb attraction.

$$H_D = -e\phi + \beta mc^2 + \alpha(cp + eA), \qquad (1.14)$$

For a central fixed potential, as is the one generated by the nuclear charge, the 3 space-like components from the four-potential are null, and the time-like component, $\phi = \frac{Ze}{r}$. The Hamiltonian gains now a more recognizable form:

$$H_D = -\frac{e^2 Z}{r} + \beta m c^2 + \alpha \cdot p c, \qquad (1.15)$$

A very interesting fact about Dirac's equation is that it yields, in fact, two sets of solutions: the large component (positive energy values), for particles, and the small component (negative energy values), for antiparticles.

1.3.3.1 The Dirac-Breit Equation

Once again, when considering a system composed of many bodies, one must consider all the present interactions, namely, the electron-electron repulsion in an atom. Breit, in 1929, had created a relativistic approach to treat the electron-electron interactions, consisting on a set of equations building upon the classical non-relativistic Hamiltonian from equation (1.1), which can be consulted in Appendix A. Breit's equations are able to

account for angular momenta couplings and estimate level energy splittings, the change of a particle's apparent mass as a function of velocity, and even include the interaction of an applied external magnetic field [10].

It is quite obvious Breit's equations introduce a great complexity in the search of the new Hamiltonian's eigenfunctions. Nonetheless, when trying to include an approximation of Breit's considerations into Dirac's equation, one must add the following operator to the one present in equation (1.15):

$$H_B = \sum_{i>j} \frac{e^2}{r_{ij}} - e^2 \left(\frac{\alpha_i \alpha_j}{r_{ij}} + \frac{(\alpha_i \nabla_i) (\alpha_j \nabla_j) r_{ij}}{2} \right), \tag{1.16}$$

This set of terms will account for the fact that Coulomb interactions, mediated by the electric field, and therefore, virtual photons, cannot occur at instantaneous velocities, but at the speed of light.

1.4 QED considerations

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Should the atomic system be subjected to an external EMF, the level structure would change due to Zeeman's and Stark's effects, allowing for the probing of the atom's hyperfine structure.

1.4.1 The *MCDF* Method

As previously mentioned in section 1.3.2, there is a need for a numerical method in order to compute and find the eigenfunctions for a many-body Hamiltonian. While the Hartree-Fock method was able to reasonably solve the non-relativistic problem, now,

Falar aqui sobre as contribuições. Não tem que ser extensivo

Ler bem o manual e explicar bem o método e todas as coisas diferentes que se podem fazer

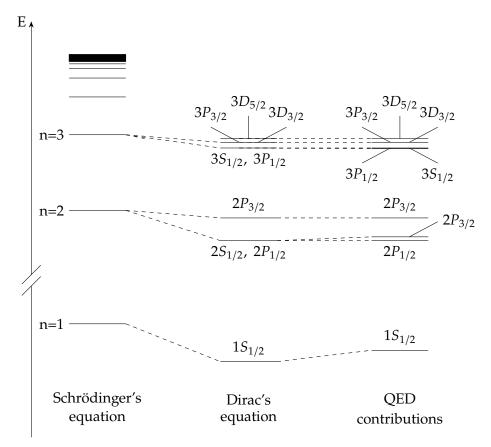


Figure 1.5: Comparison of Hydrogen level diagrams. Adapted from [13]

while considering the Dirac-Breit Hamiltonian from equations (1.15) and (1.16), there is a need for a new method.

Hence, the state of the art *MCDFGME* arises. This self-consistent iterative method, based on the same method present in section 1.3.2, is able to solve and find eigenfunctions for a multielectronic system, now taking into account the Dirac-Breit Hamiltonian. Moreover, it is also capable of incorporating electron correlation and many QED effects not yet considered in the relativistic equation, such as the Lamb-shift, vacuum polarization, and the electron's self energy. A brief description of these contributions can be found in appendix C

1.5 State of the Art

This really needs a re-do

1.5.1 Copper's characteristic X-rays

Copper is a dominant element in today's society. While most of its uses are day-to-day related, it also has a high prevalence in many physical areas, namely, copper's K_{α} transitions [14]. While these radiative transitions have been measured countless times, with very well recorded energy values [15–19]. It is also common knowledge Copper's K_{α}

lines do not have a symmetric distribution, since both K_{α_1} and K_{α_2} line display a negative (left-tailed) skewness. Due to this fact, most of the fitting models used in order to analyze both Copper's K_{α_1} and K_{α_2} transitions involve the usage of a Lorentzian doublet, for each line [20, 21]. While many associate these asymmetries due to satellite states formed by shake processes [14, 22], with some theoretical studies having been performed [23], some authors note it could be due to X-ray resonant Raman scattering [22]. This effect occurs when a sample is exposed to energies under to near the ionization threshold, when a bound electron is excited to an upper state [24]. While there are some studies exploring this topic, most are focused on the cascade of low energy transitions that follow the post-scattering excitation [25]. Nonetheless, a previous experimental study has been able to show that for Copper exposed to synchrotron radiation tuned to energies near K-shell's ionization energy, some K_{α_1} transitions demonstrated to be narrower than expected [26].

1.5.2 MCDFGME capabilities

It has been noted multiple times that *MCDFGME* code excels in atomic structure calculations of super-heavy elements and highly-charged ions, where relativistic and QED effects are in prevalence [27–29]. However, it has also been proven to be an excellent tool for the calculation of less ionized and lighter atomic systems [30].

In addition, the *MCDFGME* code is able to calculate radiative and auger transition rates for the calculated configurations, which can be used in the simulation of theoretical spectra, due to being able to compute the transition's intensity and natural width. Since it is able to perform calculations, even for exotic atoms, it can be used to further understand many QED phenomena, further exploring the limits of our theory, and it's comparison to experimental data [31].

It should also be of note that there are many other code alternatives. While *MCDFGME*, which is a close-source project, provides a very high precision in the performed calculations at a high computational cost, Flexible Atomic Code (FAC), is an open source code which requires less computational time for the calculations, however, it lacks *MCDFGME*'s precision, since it only is able to consider all the spin-orb couplings, but does not mix the possible configurations originating them. It can, however, calculate other collisional processes, such as electronic impact excitation cross-sections [32]. General-purpose Relativistic Atomic Structure Package 2k (*Grasp2k*) [33], and *AUTOSTRUCTURE* [34] are other codes with some of the same capabilities.

Atomic Structure Calculations

In this chapter, the procedure that follows a standard atomic structure calculation will be discussed and explained in detail. Topics ranging from the usage of the *MCDFGME* code to compute quantities such as energy levels, orbital wavefunctions and transition rates, to the manner in which these parameters can be used in order to simulate a theoretical spectrum will be explored. All the information present in this chapter was obtained after a thorough study of *MCDFGME*'s manual [35].

2.1 The *MCDFGME* code's capabilities

As previously stated, *MCDFGME* is a program that allows for not only solving the many-body problem for an atomic system while making the proper QED energy corrections, but also for the computation of a great deal of atomic parameters. Consulting [36], one can see that these include, but are not limited to:

- Energy level calculations.
- Multipole radiative transition probabilities.
- Auger transition probabilities.
- Photoionization cross-sections.
- Electronic impact excitation cross-sections.
- Orbital wavefunction overlaps between same and different atomic systems.

meter mais cenas

2.2 The atomic system at study

Before proceeding to the explanation behind every step of the calculations performed, a previous discussion on the reason behind them should be had.

The main purpose of this thesis is that of simulating a theoretical spectrum for Copper's x-ray emission lines when subjected to a near ionization threshold x-ray source.

At this energy range, two main processes will be responsible for an electron moving out of a core-shell: Resonant photoexcitation, and ionization.

While the simulation of the theoretical spectra for ionized Copper would be quite straightforward (due to the low shake probabilities at near ionization threshold energies, transitions for satellite states were not incorporated in the simulation), the more extensive calculation is that of resonant photoexcitation.

Aside from ionized Copper, multiple atomic structure calculations were performed for many of Copper's first excited state configurations in order to consistently account for all possible decays from excited states.

In total, and in addition to ionized Copper, 18 different standalone calculations were performed for the case in which the atomic system has undergone the process of an excitation of any one of the constituent electrons to one of the following orbitals:

- 4s, 4p, 4d, 4f
- 5s, 5p, 5d, 5f, 5g
- 6s, 6p, 6d, 6f, 6g, 6h
- 7p, 8p, 9p

2.2.1 Selecting all possible orbital configurations

As to perform an atomic structure calculation, by making use of the *MCDFGME* code, the system's electronic configuration is needed, hence why, for each calculation, all the possible one-hole and two-holes ¹ configurations need to be provided, along with their respective labels which are used as identifiers of the orbital where the hole is present during the calculations. For example, in the case of ground state Copper that went through the process of the excitation of one of its electrons to the orbital 4p, there are many possibilities for the original orbital from where the electron came from. For this case, an example of all possible 1-hole and 2-holes configurations can be found in Annex I. These are obtained by running a single hole, or two holes by all the orbitals present in the ground state configuration.

2.3 Level Calculations

Now that all configurations have been selected, the calculations can proceed.

The first and most influential, step needed in order to simulate theoretical spectra is the calculation of the level structure for all given configurations.

¹These need to be considered due to describing the final state of the system after an Auger transition or Shake-off process. The Auger transition rates will be needed in order to compute the full width of the initial 1-hole level and diagram transitions.

This, however, is no simple task. Besides the given configuration, an atomic level is described by two other quantum numbers.

2.3.1 The level manifold

Prior to proceeding with the discussion, it is important to establish some of the notation that will be used throughout this thesis. In this work, where hyperfine splitting is not accounted for, an atomic level will be described by three sets of quantum numbers. These will be the parameters that will influence the system's energy levels.

Hole orbital labels $(n l_j)$ - This quantum number set is related to the system's electronic configuration and can be composed of one or more labels, indicators of the orbitals where electrons are missing. These labels may have no physical meaning on their own and are used in conjunction with files such as the one in Annex I in order to retrieve the system's electronic configuration. For demonstrative purposes, assuming an initial Copper's ground state configuration as a starting point, before any hole-generating processes, to be $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^1$, the quantum number set in question can be used to describe various possible ionization configurations:

- $1s^1 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^1 \rightarrow (1s)$
- $1s^1 2s^1 2p^6 3s^2 3p^6 3d^{10} 4s^1 \rightarrow (1s, 2s)$

Total angular momentum number *J* - This number is the indicator of the total angular momentum of the atomic system, resulting from the couplings between the electrons' orbital angular momenta and spin. A single configuration can result in many coupling possibilities and, in turn, different values for *J*.

As an example, let's take that of Copper that underwent the excitation process of an electron from the 2p orbital to 4p, with an electron configuration of $1s^2 2s^2 2p^5 3s^2 3p^6 3d^{10} 4s^1 4p^1$. One can now easily observe there are three open orbitals, each with an uncoupled electron. The different coupling possibilities between these three electrons will generate four different possible total angular momentum values: J = 1/2, 3/2, 5/2, 7/2. In table 2.1, a coupling example will be given for each of them.

Table 2.1: Total angular momentum generated by different couplings

2p		4s		4p		Total/ <i>J</i>	
m_l	m_s	m_l	m_s	m_l	m_s	$m_l + m_s$	
1	-1/2	0	-1/2	1	-1/2	1/2	
1	$1/_{2}$	0	-1/2	1	-1/2	$^{3}/_{2}$	
1	$^{1}/_{2}$	0	$^{1}/_{2}$	1	-1/2	5/2	
1	1/2	0	1/2	1	$^{1}/_{2}$	7/2	

Lagrange multiplier ϵ - Indicator of the eigenvalue for the state on which the calculation will be performed on. The need for this quantum number arises from the fact that, even for the same configuration and the same total angular momentum, there are many possible arrangements that yield these quantum numbers. As an example, for the same configuration used previously, and assuming a total angular momentum J = 5/2, there are three different possible couplings that generate that value of angular momentum, as can be seen in table 2.2.

$J = \frac{5}{2}$								
2	<u>2</u> p	4s		4p				
m_l	m_s	m_l	m_s	m_l	m_s			
1	-1/2	0	1/2	1	1/2			
1	$^{1}/_{2}$	0	-1/2	1	$^{1}/_{2}$			
1	1 /	0	1 /	-1	1 /			

Table 2.2: Same total angular momentum generated by different configurations

This splitting of quantum numbers for a given configuration gives origin to the level manifold (Figure 2.1), reason why, even for a simple calculation, hundreds to thousands of levels need to be calculated. It is also of note that, for a given Total angular momentum value, J, there are 2J + 1 states associated to it due to the angular momentum projection. In the presence of an external EMF, the hyperfine level structure would be observed, due to Zeeman and Stark's effects. However, for the purpose of this thesis, no external field was considered, and calculations were only done for the maximum total angular momentum projection value, with a 2J + 1 degeneracy taken into account in the following calculations.

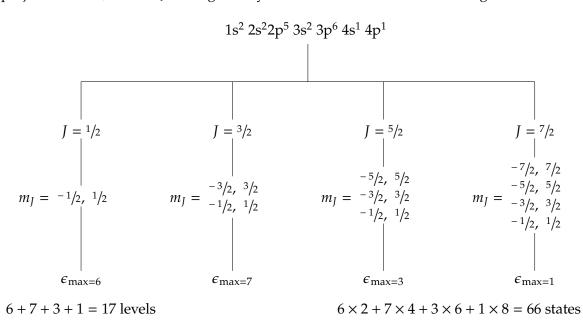


Figure 2.1: Splitting of quantum numbers for a given configuration.

In conclusion, an atomic level can be defined by the set of these three quantum numbers.

In the notation used throughout this thesis, a level will be identified by:

$$i \equiv [(n \ l_j)_i; \ J_i; \ \epsilon_i], \tag{2.1}$$

And the energy of the level:

$$E_i \equiv E[(n l_j)_i; J_i; \epsilon_i], \qquad (2.2)$$

2.3.2 Level calculation with MCDFGME

A typical level calculation begins with the formatting of the input . £05 file. This file contains the necessary information and instructions the program needs for the computation that follows when the executable mcdfgme2019.exe is called.

The input file has a certain input structure in which certain calculation parameters are defined. A previously tailored template input file is used, where, by default, the full Breit interaction is considered, with the magnetic and retardation parts, as well as vacuum polarization included in the self-consistent process. Retardation is also applied to Lorentz's and Coulomb's gauges.

The template is now formatted in order to perform the calculation for the desired level. The element's atomic number and the electron configuration are selected with the former having the same format as in Annex I. The double of the value of the total angular momentum is then indicated (as not to work with non-integer values) and so is the Lagrange multiplier/eigenvalue.

There are many other parameters to chose in order to have the .f05 ready for the computation. These parameters, however, are not always the same, since occasionally different methods will have to be employed in order to reach convergence. Before these methods are discussed, it is necessary to provide an explanation as to how to evaluate the numerical convergence of the calculation:

2.3.3 Level calculation with *MCDFGME* - Alternative

For a given set of quantum numbers, a relativistic *MCDF* was performed using the *MCDFGME* script. The code executes an iterative self-consistent field calculation, accounting for both Coulomb and Breit's interactions, including the magnetic and retardation parts for the latter. For QED corrections, the formation of local potentials due to vacuum polarization was included in the self-consistent part of the calculation, while corrections due to self-energy were treated as perturbation. Furthermore, electron correlation was also accounted for by composing the antisymmetric wavefunction as a linear combination of state wavefunctions with mixing coefficients.

For executing the calculation, a previously tailored .f05 input file is prepared. In it, a calculation with all the previously mentioned interactions is set up, with the option of changing the initial trial wavefunctions and the parameters of the self-consistent calculation

Mention that the program works by the means of an input f05 file

Breit can be used as self consistent or perturbative

Talk about Lorentz and Coulomb gauges cycles. Throughout the calculation these wavefunctions will go through a variational process, changing until the optimal solution is reached, as can be observed in Figure 2.2.

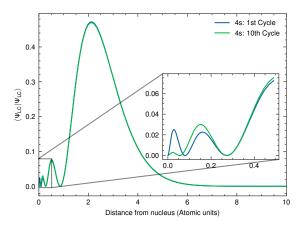


Figure 2.2: 4s Large component wavefunction after one and ten cycles of the self-consistent iterative process.

2.3.3.1 Evaluating the convergence

After launching the mcdfgme2019.exe executable, the computation will start, generating an output file with the .f06 extension, where the output will be written while the program is actively running.

One of the convergence benchmarks can already be evaluated while the calculation is being processed. Actively monitoring the output file with, as an example, the UNIX command tail, one can observe the output from the self-consistent cycles. Should the numerical method be diverging, warnings concerning sudden shifts in the wavefunction derivative may be displayed.

The calculation can also be aborted due to a numerical error. In this case, if the error occurred while running calculations for a certain orbital(s), this/these will be displayed in the output.

The three other parameters used when evaluating if the convergence was successful can be checked only after the calculation is over:

- Each cycle, a component of the level's energy is calculated through two different methods. These two values should be consulted for the last cycle and the absolute energy difference should be below a certain stipulated benchmark value (1 eV).
- The wavefunction overlaps between each orbital sharing the same l_j value are displayed, since these cases are the most probable of having a convergence error leading them not to be orthogonal. The convergence is considered acceptable if every value is lower than 10^{-6} .
- For every orbital, the effective charge is calculated and displayed. This parameter is related to the shielding effect the charge of the electrons in other orbitals exert

Olha lá se não tens que fazer o quadrado disso Meter aqui ref de como calcular on the nuclear charge. If the calculation converged correctly, these values should never be equal to the extreme possible values: 1 or N, where N is the total number of electrons. For each orbital, this value should be close to an expected value .

2.3.3.2 Level convergence methods

Some text here. Mention the Optimize orbital method.

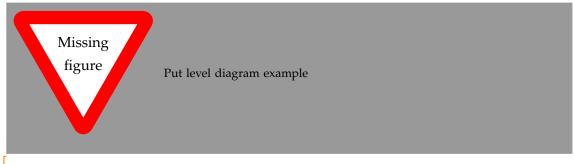
First attempt at numerical convergence For the first calculation, by default, a simpler template file (Annex II) is used and a calculation of five self-consistent cycles is performed. All trial orbital wavefunctions are initialized by wavefunctions calculated using the Thomas Fermi potential [37].

Second attempt at numerical convergence Should the first attempt have failed to reach convergence, a similar calculation is performed, keeping the previous parameters, but increasing the number of self-consistent cycles to 10, enforcing for each, an increasingly more precise accuracy and higher number of iterations. The template can be found in Annex III.

Third attempt at numerical convergence Should the previous two attempts have been made, and no convergence was reached, a new calculation needs to be made. In addition to the change cycle parameters, the parameters for some orbitals are to be altered. This can be done by altering the initial wavefunction to hydrogenics, or to a previously computed one. The method for solving the Dirac equation can also be changed for each chosen orbital. This final attempt can be quite time-consuming due to the many possibilities and combinations of methods to be employed for each orbital.

Since for every calculation thousands of levels need to be computed, a parallelized automation script was used. In total two scripts were used: a first one, previously written in bash by one of the advisors, Jorge Machado, which used GNU's parallel command for parallelization, was used for the first calculations performed; and for most of the calculations, a new script, developed in the scope of this thesis, written in Python and employing an MPI approach for the purpose of parallelization. This last one will be discussed further in the thesis.

In the total number of calculated 1-hole and 2-holes levels is displayed in Table 2.3.



Maybe put a plot of the calculated wavefunctions

Atomic	Nun	nber of lev	vels	Number of hand-converged levels				
System	1-hole	2-holes	Total	1-hole		Total		
Cu ¹⁺	19	183	202	0	1	1		
4s	10			!		'		
4p	83	1001	1084	17	118	135		
4d	107			'		'		
4f	114		,					
5s	33							
5p	83							
5d	107							
5f	114							
5g	115							
6s	33							
6p	83							
6d	107							
6f	114							
6g	115							
6h		•						
7p	83							
8p	83							
9p	83							
Total	1							

Table 2.3: Total number of levels calculated. For all but the first row, the indicated orbital is the one where an electron was excited to.

2.4 Transition computations

After all level computations have been performed, the next step towards the spectra simulation should be that of calculating level transitions. Any level that is not ground state will eventually decay into a more stable and less energetic one. This process is what eventually allows for the emission of x-ray radiation and Auger electrons.

When considering transitions between a given set of states, the transition energy and transition rate matrices are two 2D matrices of the greatest importance on spectra simulation, since their matrix elements contain the mentioned properties for all possible transitions across the set.

For an initial state denoted by i and a final one by j (using the notation from equation (2.1)), the matrix elements are as follows:

For the energy matrix:

$$E_{i,j} = E_i - E_j, (2.3)$$

And now for the rate matrix:

$$R_{i,j} = R[(n,l_j)_i, J_i, \epsilon_i; (n,l_j)_f, J_f, \epsilon_f], \tag{2.4}$$

2.4.1 Diagram transitions

Diagram transitions are associated with radiative transitions between two 1-hole states. For ionized systems, this kind of transitions are associated to the characteristic radiation from principal spectral lines such as K_{α} , K_{β} , L, etc. For this reason, they are the focal point of study for the work performed on this thesis.

Given a set of all $n_{1-\text{hole}}$ 1-hole levels, one must consider only transitions from higher to lower energetic states. Therefore, the total number of diagram transitions, not taking account level degeneracy, N_{diag} can be simply calculated by the number of combinations of two 1-hole states:

$$N_{\text{diag}} = \frac{n_{1-\text{hole}}!}{2 \cdot (n_{1-\text{hole}} - 2)!},$$
(2.5)

For the rate calculation, the same approach was taken as in the works of Guerra [30] and Pinheiro [38], where the lack of orthogonality in the initial and final state due to numerical convergence is treated by the formalism present in Löwdin's work [39] and full orbital relaxation is allowed.

While *MCDFGME* calculates transition rates for both Coulomb (length) and Lorentz (velocity) gauges, only the length gauge calculated ones were used in this work. Rates are calculated for both Electric and Magnetic transitions and their many components (poles).

needs to be checked

2.4.2 Auger transitions

As previous mentioned, these type of transitions are characterized by the transition's energy release coming in the form of an ejected electron, as opposed to x-ray radiation.

The set of initial and final states is now composed of the 1-hole and 2-hole sets. While for diagram transitions the total number of transitions could be calculated just by the number of elements in the set, in this case is not as simple, as the energy for every level has to be taken into account. The maximum number of possible transitions could be calculated by the product of the total number of 1-hole and 2-hole levels. The real number of transitions is, however, far away from this value.

Once again, the same procedure as in [30, 38] was followed. Given the energy of the transition, the free electron wavefunction is calculated for the same potential as the initial state. This time, no relaxation is included, as to only account for the ionization, and orthogonality between the free wave and the bound orbitals is enforced.

2.4.3 Satellite transitions

This type of transitions are related to radiative relaxation between two 2-hole states. They are, therefore processed the same as Diagram transitions.

While they might not be of great relevance for this thesis, some were still calculated as they can be useful for other works due to being equivalent to some diagram transitions for Copper following shake-up. 2.4.3.1 Rate Matrices as a calculation evaluating comparison tool

A new High-Performance Computing code for the parallelization of atomic structure calculations

- 3.1 A brief introduction on MPI
- 3.2 Program advantages
- 3.3 Program limitations

Blocking communication CPU overheat No buffering for now

CHAPTER 4

Fundamental atomic parameters calculation

asdas

Spectra simulation

asdas

CHAPTER 6

Spectra analysis

- 6.1 Photoexcitation cross-section estimation
- 6.2 Photoionization cross-section computation

Comparison with experimental data

CHAPTER 8

Next Steps

Final remarks and Conclusion

Usar o Denitions aqui

- 9.1 Quantum states and properties
- 9.2 State transitions
- 9.2.1 Transition rates and widths
- 9.2.2 Branching Ratios and Fluorescence Yields
- 9.3 Spectra simulation

CHAPTER 10

Spectra Analysis

Development of a HPC script for the parallelization of ASC

- 11.1 blablabla
- 11.2 Speedup

Compare with Amdahl's law or Gustafson's law.

Comparação com o do Jorge

Bibliography

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The Breit Hamiltonian Operators

Note: This operators are valid for the electrons in an atom.

The free particle energy:

$$H_0 = \sum_{i}^{N} \frac{p^2}{2m_e} \tag{A.1}$$

The electron-nucleus Coulomb attraction:

$$H_1 = \sum_{i}^{N} -\frac{e^2 Z}{r_i}$$
 (A.2)

The electron-electron Coulomb repulsion:

$$H_2 = \sum_{i < j} \frac{e^2}{r_{ij}} \tag{A.3}$$

Incorporates the relativistic apparent mass - velocity dependance:

$$H_3 = -\frac{1}{8m_e^3 c^2} \sum_{i}^{N} p_i^4 \tag{A.4}$$

Electric field retardation and magnetic dipole interaction:

$$H_4 = -\frac{e^2}{2m_e^2 c^2} \sum_{i < j} \left[\frac{\boldsymbol{p}_i \cdot \boldsymbol{p}_j}{r_{ij}} + \frac{(\boldsymbol{r}_{ij} \cdot \boldsymbol{p}_{ij})(\boldsymbol{r}_{ij} \cdot \boldsymbol{p}_j)}{r_{ij}^3} \right]$$
(A.5)

Darwin's term, accounts for the electron's quantum fluctuation motion:

$$H_5 = \frac{\pi e \hbar^2}{2m_e^2 c^2} \sum_{i < j} \frac{Z}{2} \left[\delta(\mathbf{r}_i) + \delta(\mathbf{r}_j) \right] + \delta(\mathbf{r}_{ij})$$
(A.6)

And the last two operators, for the consideration of spin orbit interactions:

$$H_{6} = \frac{e^{2}\hbar^{2}}{2m_{e}^{2}c^{2}} \sum_{i < j} \left(Z \frac{\mathbf{r}_{i} \times \mathbf{p}_{i}}{r_{i}^{3}} - \frac{\mathbf{r}_{ij} \times \mathbf{p}_{i}}{r_{ij}^{3}} + 2 \frac{\mathbf{r}_{ij} \times \mathbf{p}_{j}}{r_{ij}^{3}} \right) \mathbf{s}_{i} + \left(Z \frac{\mathbf{r}_{j} \times \mathbf{p}_{j}}{r_{j}^{3}} - \frac{\mathbf{r}_{ji} \times \mathbf{p}_{j}}{r_{ij}^{3}} + 2 \frac{\mathbf{r}_{ji} \times \mathbf{p}_{i}}{r_{ij}^{3}} \right) \mathbf{s}_{j}$$
(A.7)

$$H_7 = \frac{e^2 \hbar^2}{m_e^2 c^2} \sum_{i < j} \left(-\frac{8\pi}{3} \mathbf{s}_i \cdot \mathbf{s}_j \, \delta(\mathbf{r}_{ij}) + \frac{1}{\mathbf{r}_{ij}^3} \left[\mathbf{s}_i \cdot \mathbf{s}_j - \frac{3(\mathbf{s}_i \cdot \mathbf{r}_{ij})(\mathbf{s}_j \cdot \mathbf{r}_{ij})}{\mathbf{r}_{ij}^2} \right] \right) \tag{A.8}$$

Transition Diagram

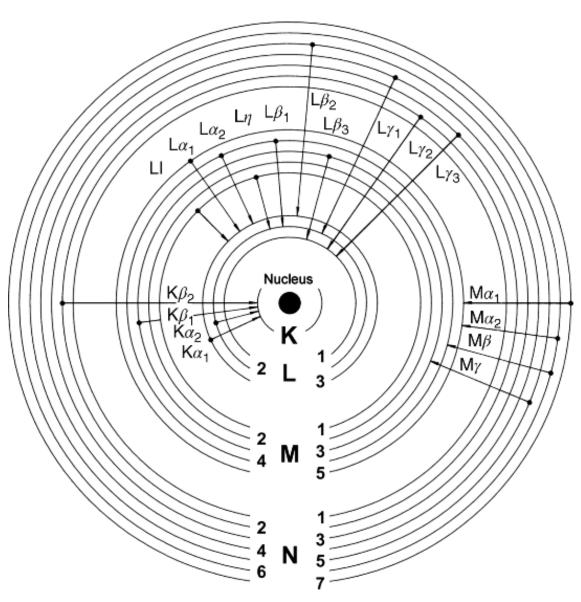


Figure B.1: Transition notation scheme. Adapted from [2]

QED considerations

It should be apparent by now that studying Atomic systems call not only for relativistic effects and corrections, but also for QED ones.

One of the most famous cases where QED came to light was the discovery of the Lamb Shift [40], when it was discovered Hydrogen's $2s_{1/2}$ and $2p_{1/2}$ levels were in fact, not degenerate (did not have the same energy), contrary to what was expected from solving Dirac's equation. This difference in energy came to be known as the Lamb Shift, only explained by QED effects.

C.1 Self-Energy

The self-energy represents a particle's emission and reabsorption of virtual photon, present in the particle's own generated field. This interaction has the most impact in the Lamb Shift effect and when performing energy corrections. One of its Feynman Diagrams can be seen in Figure C.1a.

C.2 Vacuum Polarization

As previously stated, electromagnetic fields, such as the Coulomb field generated by the nucleus, are mediated by virtual photons. These photons can lead to the creation of electron-positron pairs which create screening effects. Pair annihilation will follow, leading to the production of another virtual photon (Figure C.1b).



Figure C.1: QED Feynman Diagrams

4p excited Copper configurations

I.1 1-hole configurations

```
1 (1s)1 (2s)2 (2p)6 (3s)2 (3p)6 (4s)1 (3d)10 (4p)1 ,1s

2 (1s)2 (2s)1 (2p)6 (3s)2 (3p)6 (4s)1 (3d)10 (4p)1 ,2s

3 (1s)2 (2s)2 (2p)5 (3s)2 (3p)6 (4s)1 (3d)10 (4p)1 ,2p

4 (1s)2 (2s)2 (2p)6 (3s)1 (3p)6 (4s)1 (3d)10 (4p)1 ,3s

5 (1s)2 (2s)2 (2p)6 (3s)2 (3p)5 (4s)1 (3d)10 (4p)1 ,3p

6 (1s)2 (2s)2 (2p)6 (3s)2 (3p)6 (4s)1 (3d)9 (4p)1 ,3d

7 (1s)2 (2s)2 (2p)6 (3s)2 (3p)6 (3d)10 (4p)1 ,4s

8 (1s)2 (2s)2 (2p)6 (3s)2 (3p)6 (4s)1 (3d)10 ,4p
```

I.2 2-holes configurations

```
(2s)2 (2p)6 (3s)2 (3p)6 (3d)10 (4s)1 (4p)1
      (1s)1 (2s)1 (2p)6 (3s)2 (3p)6 (3d)10 (4s)1 (4p)1 ,1s_2s
      (1s)1 (2s)2 (2p)5 (3s)2 (3p)6 (3d)10 (4s)1 (4p)1 ,1s_2p
      (1s)1 (2s)2 (2p)6 (3s)1 (3p)6 (3d)10 (4s)1 (4p)1 ,1s_3s
      (1s)1 (2s)2 (2p)6 (3s)2 (3p)5 (3d)10 (4s)1 (4p)1 ,1s_3p
      (1s)1 (2s)2 (2p)6 (3s)2 (3p)6 (3d)9 (4s)1 (4p)1
      (1s)1 (2s)2 (2p)6 (3s)2 (3p)6 (3d)10 (4p)1
                                                         ,1s_4s
      (1s)1 (2s)2 (2p)6 (3s)2 (3p)6 (3d)10 (4s)1
                                                         ,1s_4p
      (1s)2 (2p)6 (3s)2 (3p)6 (3d)10 (4s)1 (4p)1
                                                         ,2s_2s
      (1s)2 (2s)1 (2p)5 (3s)2 (3p)6 (3d)10 (4s)1 (4p)1 ,2s_2p
11
      (1s)2 (2s)1 (2p)6 (3s)1 (3p)6 (3d)10 (4s)1 (4p)1 ,2s_3s
      (1s)2 (2s)1 (2p)6 (3s)2 (3p)5 (3d)10 (4s)1 (4p)1 ,2s_3p
13
      (1s)2 (2s)1 (2p)6 (3s)2 (3p)6 (3d)9 (4s)1 (4p)1
      (1s)2 (2s)1 (2p)6 (3s)2 (3p)6 (3d)10 (4p)1
                                                         ,2s_4s
15
      (1s)2 (2s)1 (2p)6 (3s)2 (3p)6 (3d)10 (4s)1
                                                         ,2s_4p
      (1s)2 (2s)2 (2p)4 (3s)2 (3p)6 (3d)10 (4s)1 (4p)1 ,2p_2p
      (1s)2 (2s)2 (2p)5 (3s)1 (3p)6 (3d)10 (4s)1 (4p)1 ,2p_3s
      (1s)2 (2s)2 (2p)5 (3s)2 (3p)5 (3d)10 (4s)1 (4p)1 ,2p_3p
18
      (1s)2 (2s)2 (2p)5 (3s)2 (3p)6 (3d)9 (4s)1 (4p)1 ,2p_3d
      (1s)2 (2s)2 (2p)5 (3s)2 (3p)6 (3d)10 (4p)1
                                                         ,2p_4s
      (1s)2 (2s)2 (2p)5 (3s)2 (3p)6 (3d)10 (4s)1
                                                         ,2p_4p
```

ANNEX I. 4P EXCITED COPPER CONFIGURATIONS

22	(1s)2	(2s)2	(2p)6	(3p)6	(3d)10	(4s)1	(4p)1		,3s_3s
23	(1s)2	(2s)2	(2p)6	(3s)1	(3p)5	(3d)10	(4s)1	(4p)1	,3s_3p

First cycle template

```
program_year=2019 program_version=1
          1 mcdfgmelabel
          scfmdf max :
          mod_lightspeed=n
          nz=mcdfgmeatomicnumber
          mdf opt_ener=todo modfilname_ener=n modfilname_wf=n do_scf=y
          Breit=full mag_scf=y ret_scf=y
          qedstpg_n4=n
          vacpol_scf=y
10
          energy
11
          use_mcdfener=y
           opt_relax=y
12
          ret_Lorentz=y
13
          opt_qedel=y :
14
      # ":" above is for ilams taken to be the default value
          mod_mesh=n
16
          hx=0.012 r(1)=0.001 amesh=0.01:
17
18
          exotic=n
          use_nms=y
19
          mod_nuc=n
20
          project=n
21
           cgt_order_vint=y order=6
23
          cgt_order_vint=n
          def_config=given
24
          nbel=mcdfgmeelectronnb jjt=mcdfgmejj :
25
      c 1 mcdfgmeconfiguration:
27
      end
      # initial state parameters
28
          neigv=mcdfgmeneigv icmul=0
                                          iprfgr=0
          norbsc=00 ndep=0 nlec=0 nec=1 :
          nstep=0
31
          lregul=n modtest=n
32
33
          modsolv_orb=n
          mod_odlm=n
      # data for uwfrdf
```

ANNEX II. FIRST CYCLE TEMPLATE

36		:				
37	**					

Input File .f05 Example

```
program_year=2019 program_version=1
          1 mcdfgmelabel
          scfmdf max :
          mod_lightspeed=n
          nz=mcdfgmeatomicnumber
          mdf opt_ener=todo modfilname_ener=n modfilname_wf=n do_scf=y
          Breit=full mag_scf=y ret_scf=y
          qedstpg_n4=n
          vacpol_scf=y
10
          energy
11
           use_mcdfener=y
           opt_relax=y
12
          ret_Lorentz=y
13
          opt_qedel=y :
14
      # ":" above is for ilams taken to be the default value
          mod_mesh=n
16
17
          hx=0.012 r(1)=0.001 amesh=0.01:
18
          exotic=n
          use_nms=y
19
          mod_nuc=n
20
          project=n
21
           cgt_order_vint=y order=6
23
          cgt_order_vint=n
          def_config=given
24
          nbel=mcdfgmeelectronnb jjt=mcdfgmejj :
25
      c 1 mcdfgmeconfiguration:
27
      end
      # initial state parameters
28
          neigv=mcdfgmeneigv
                               icmul=0
                                          iprfgr=0
          norbsc=00 ndep=0
30
                              nlec=0
                                        nec=1 :
          nstep=10
31
          n y y 50
                     z=mcdfgmeatomicnumber 1.D-2
                                                    0.2 1.
32
33
          n y y 50 z=mcdfgmeatomicnumber 3.D-3
                50
                     z=mcdfgmeatomicnumber 1.D-3
                                                    0.3 1.
          n y y 50 z=mcdfgmeatomicnumber 3.D-4 0.3 1.
```

```
n y y 50 z=mcdfgmeatomicnumber 1.D-4 0.5 1. 1.
36
          n y y 50 z=mcdfgmeatomicnumber 3.D-5 0.5
37
          n y y 50 z=mcdfgmeatomicnumber 1.D-5 0.5
38
                                                     1.
                                                          1.
          n y y 100 z=mcdfgmeatomicnumber 4.D-6 1. 1.
                                                          1.
39
          n y y 100 z=mcdfgmeatomicnumber 2.D-6 1. 1. 1.
40
          n y y 200 z=mcdfgmeatomicnumber 1.D-6 1. 1.
41
          lregul=n modtest=n
42
          {\tt modsolv\_orb=n}
43
44
          mod\_odlm=n
      # data for uwfrdf
45
46
47
```



Lion t First principles for ctra simula 2 AV resonan Z

2023