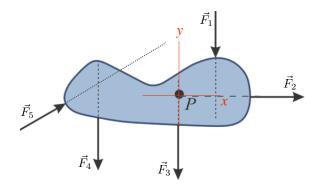
## **Solving Rotational Equilibrium Problems:**

Setup Stage: Sketch a Free-Body Diagram.

Because distances, either r (from pivot to force) or  $r_{\perp}$  ( $\perp$  from pivot to line of action), are essential for calculating torques, you should provide some idea of the geometry of the object of interest.

Do <u>not</u> simply represent the object as a dot at the origin of a coordinate system for torque problems.



Analysis Stage: Apply Newton's Laws for Rotations (i.e. "Read" the free-body diagrams).

- ► Similar to translational motion problems, **EACH STEP IS GRADED**.
- **Physics Principle:** write Newton's First Law for Rotational Motion (corollary of Newton's 1<sup>st</sup> Law). i.e.  $\Sigma \tau = 0$  and indicate the point used as pivot.

example: 
$$\sum \vec{\tau} = 0 \qquad \text{(about point P)}$$

 Application: Write the explicit sum of torque vectors; include a torque term for every force in the FBD.
 Recall: If the line of action of a force crosses the pivot, it exerts no torque.

$$\vec{\tau}_1 + \vec{y}_2 + \vec{y}_3 + \vec{\tau}_4 + \vec{\tau}_5 = 0$$

• Sign Convention: Separate magnitude and direction. Use the right-hand rule to determine direction of torque terms about pivot; represent it with +/- signs. Note: the  $\tau$  terms are now magnitudes, so no arrow caps; the direction is described by the +/- signs.

$$-\tau_1 + \tau_4 - \tau_5 = 0$$

• Using the torque definition and either method of visualizing it, express <u>each</u> torque term as a function of r or  $r_{\perp}$ , and F.

$$\tau_1 = r_1 F_1 \sin \phi_1 \quad \text{or} \quad \tau_1 = r_{\perp 1} F_1$$
 $\tau_4 = r_4 F_4 \sin \phi_4 \quad \text{or} \quad \tau_4 = r_{\perp 4} F_4$ 

· Identify and solve for the desired quantity.