

Problem Of The Day 2022

1. **(27 Jun)** If y varies inversely as x and can be represented by the equation $y = (m - 1)x^{m^2-2}$, find the value of constant m .

Solution:

$$\begin{aligned} y &= (m - 1)x^{m^2-2} = \frac{k}{x} \\ k &= (m - 1)x^{m^2-1} \\ &= (m - 1)x^{(m+1)(m-1)} \quad (x \neq 0) \end{aligned}$$

By definition, $y \neq 0$ as well, hence

$$\begin{aligned} (m - 1)x^{(m+1)(m-1)} &\neq 0 \\ \therefore m &\neq 1 \end{aligned}$$

2. **(28 Jun)** Which of the following is a possible plot of $y = x + m$ and $y = \frac{m}{x}$ on the same axes? (The graphs are not drawn to scale.)

Solution: B.

- The straight line should be increasing, since the coefficient of x is positive. **C** and **D** are eliminated.
- If $m > 0$, the y-intercept of the straight line could not be negative. **A** is eliminated, since the hyperbola in the same graph shows that $m > 0$.

3. **(29 Jun)** Given that points $A(-2, y_1)$, $B(-1, y_2)$, $C(1, y_3)$ are all on the graph of $y = -\frac{1}{x}$, arrange y_1 , y_2 and y_3 in ascending order.

Solution: $y_3 < y_1 < y_2$.

Subst. $x = -2$ into $y = -\frac{1}{x}$:

$$\begin{aligned} y_1 &= -\frac{1}{-2} \\ &= \frac{1}{2} \end{aligned}$$

Subst. $x = -1$ into $y = -\frac{1}{x}$:

$$\begin{aligned}y_2 &= -\frac{1}{-1} \\&= 1\end{aligned}$$

Subst $x = 1$ into $y = -\frac{1}{x}$:

$$\begin{aligned}y_3 &= -\frac{1}{1} \\&= -1\end{aligned}$$

4. **(30 Jun)** Given that points (x_1, y_1) , (x_2, y_2) and (x_3, y_3) are all on the graph of $y = \frac{3}{x}$, also $x_1 < x_2 < 0 < x_3$, arrange y_1 , y_2 and y_3 in ascending order.

Solution: $y_2 < y_1 < y_3$.

- $y_3 > 0$ since $x_3 > 0$. Hence, y_3 is the greatest.
- $0 > x_2 > x_1$, hence $y_2 < y_1 < 0$.