

Report of Entropy estimates based on NIST SP 800-90B non-IID track

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1 Identification information

1.1 Identification of acquisition data from entropy source

Table 1 Identification information of acquisition data from entropy source

|  |  |
|--|--|
| URL of the acquisition data                      | https://github.com/usnistgov/SP800-90B_EntropyAssessment/blob/master/bin/rand1_short.bin |
| SHA-256 hash value of the acquisition data [hex] | 38144044 97a3b912 f8d3db6b c05a9933 8f0986cd 75fe54af 2a5f1bdb 0a12a583                  |

- Name of the submitter of the acquisition data :
- Brief explanation of the acquisition data (or entropy source) :

1.2 Identification of analysis environment

Table 2 Identification information of analysis environment

|                      |                        |  |
|----------------------|------------------------|--|
| Analysis tool        | Name                   | Another entropy estimation tool with extensions        |
|                      | Versioning information | 1.0.49   |
|                      | built as               | 64-bit application                                     |
|                      | built by               | Intel C++ Compiler ( __INTEL_LLVM_COMPILER: 20230200 ) |
|                      | linked libraries       | Boost C++ 1.82.0                                       |
| Analysis environment | Hostname               | TIGER140A  |
|                      | CPU information        | AMD Ryzen 5 PRO 5650U with Radeon Graphics             |
|                      | Physical memory size   | 47950 MiB  |
|                      | OS information         | Windows 10 or greater 64-bit                           |
|                      | Username               | genya  |

1.3 Identification of analysis conditions

Table 3 Identification information of analysis conditions

|                   |       |
|-------------------|-------|
| Number of samples | 10000 |
| Bits per sample   | 1     |

1.4 Identification of analysis method

NIST SP 800-90B [1] 6.3 with corrections [2] is applied

## 2 Executive summary

### 2.1 Numerical results of min-entropy estimates based on non-IID track

Table 4 Numerical results

| Estimator   | $H_{\text{bitstring}}^a$<br>[bit / 1 - bit] |
|---|---|
| The Most Common Value Estimate  | 0.961059                                    |
| The Collision Estimate  | 0.691464                                    |
| The Markov Estimate   | 0.987596                                    |
| The Compression Estimate  | 0.611716                                    |
| The t-Tuple Estimate  | 0.867624                                    |
| The Longest Repeated Substring (LRS) Estimate   | 0.962626                                    |
| Multi Most Common in Window Prediction Estimate   | 0.952618                                    |
| The Lag Prediction Estimate   | 0.943334                                    |
| The MultiMMC Prediction Estimate  | 0.961617                                    |
| The LZ78Y Prediction Estimate   | 0.961446                                    |
| The initial entropy source estimate [bit / 1 -bit]<br>$H_I = H_{\text{bitstring}}$          | 0.611716                                    |
| <sup>a</sup> Entropy estimate of the sequential dataset [source: NIST SP 800-90B [1] 3.1.3] |   |

### 2.2 Visual comparison of min-entropy estimates from binary samples

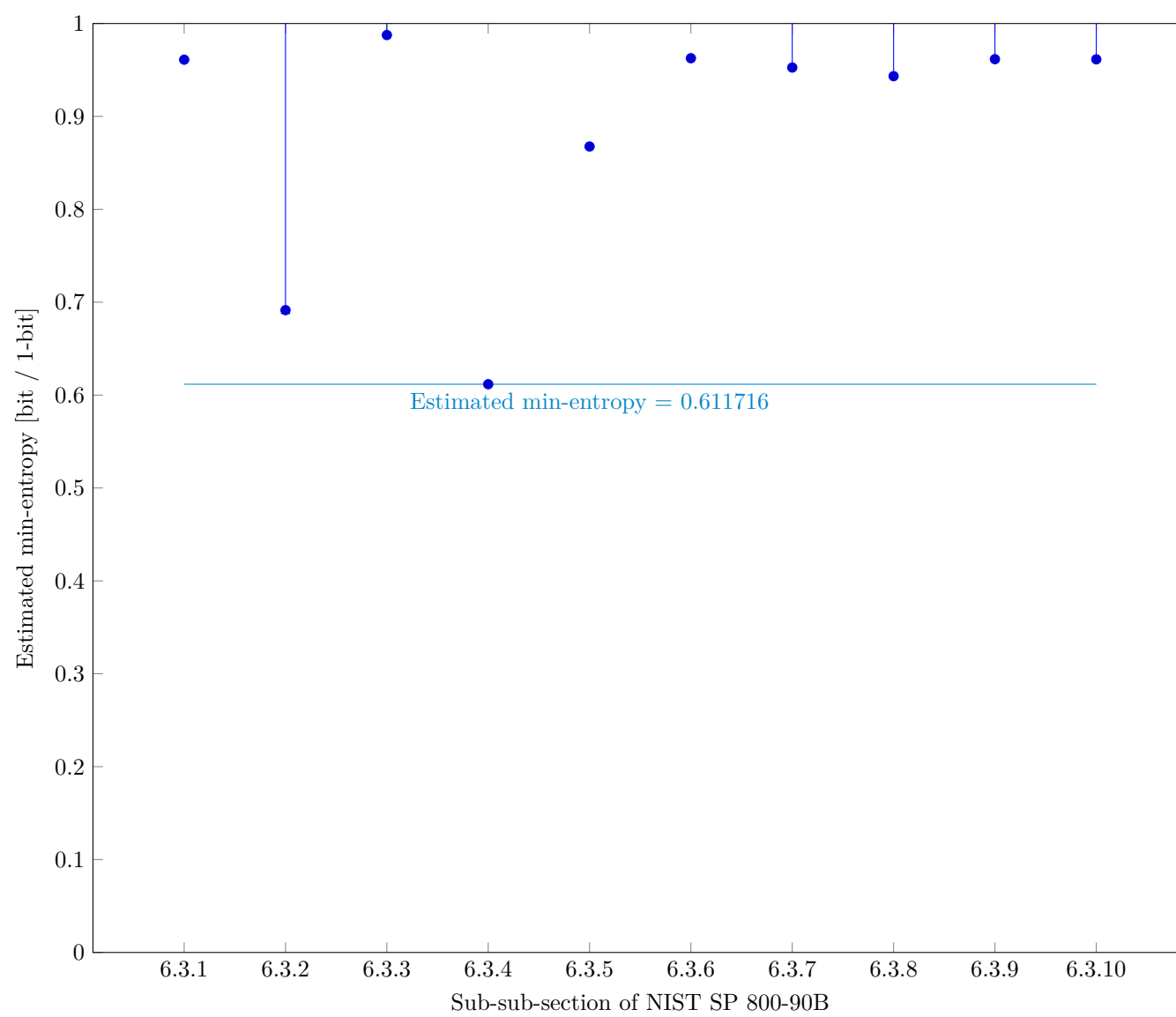


Fig. 1 Estimated Min-Entropy using §6.3 of NIST SP 800-90B

### 3 Detailed results of analysis from original samples

#### 3.1 The Most Common Value Estimate (NIST SP 800-90B Section 6.3.1)

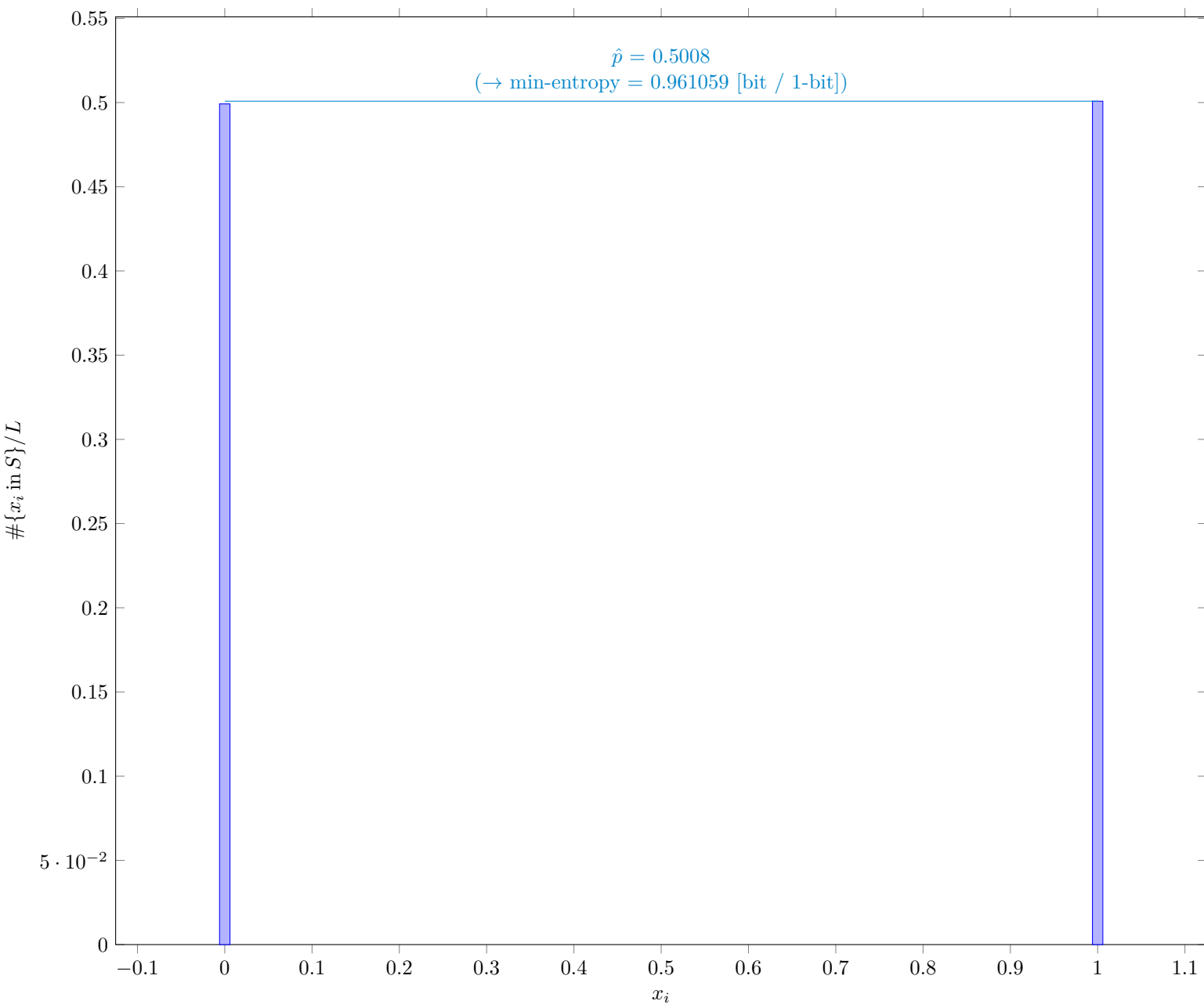


Fig. 2 Distribution of  $x_i$

##### 3.1.1 Supplemental information for traceability

Table 5 Supplemental information for traceability (NIST SP 800-90B Section 6.3.1)

| Symbol    | Value   |
|-----------|---------|
| mode      | 5008    |
| $\hat{p}$ | 0.5008  |
| $p_u$     | 0.51368 |

### 3.2 The Collision Estimate (NIST SP 800-90B Section 6.3.2)

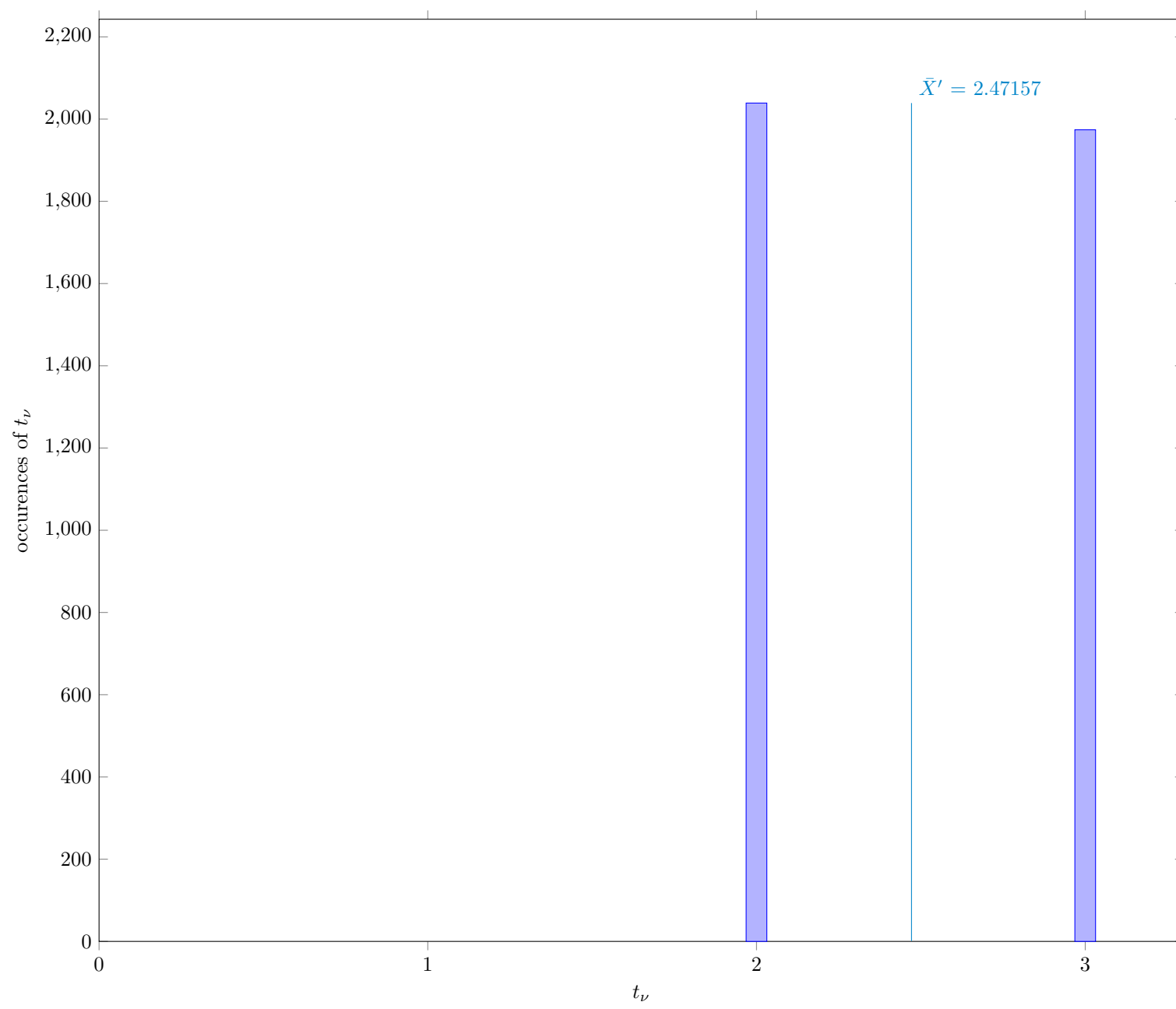


Fig. 3 Distribution of intermediate value  $t_\nu$

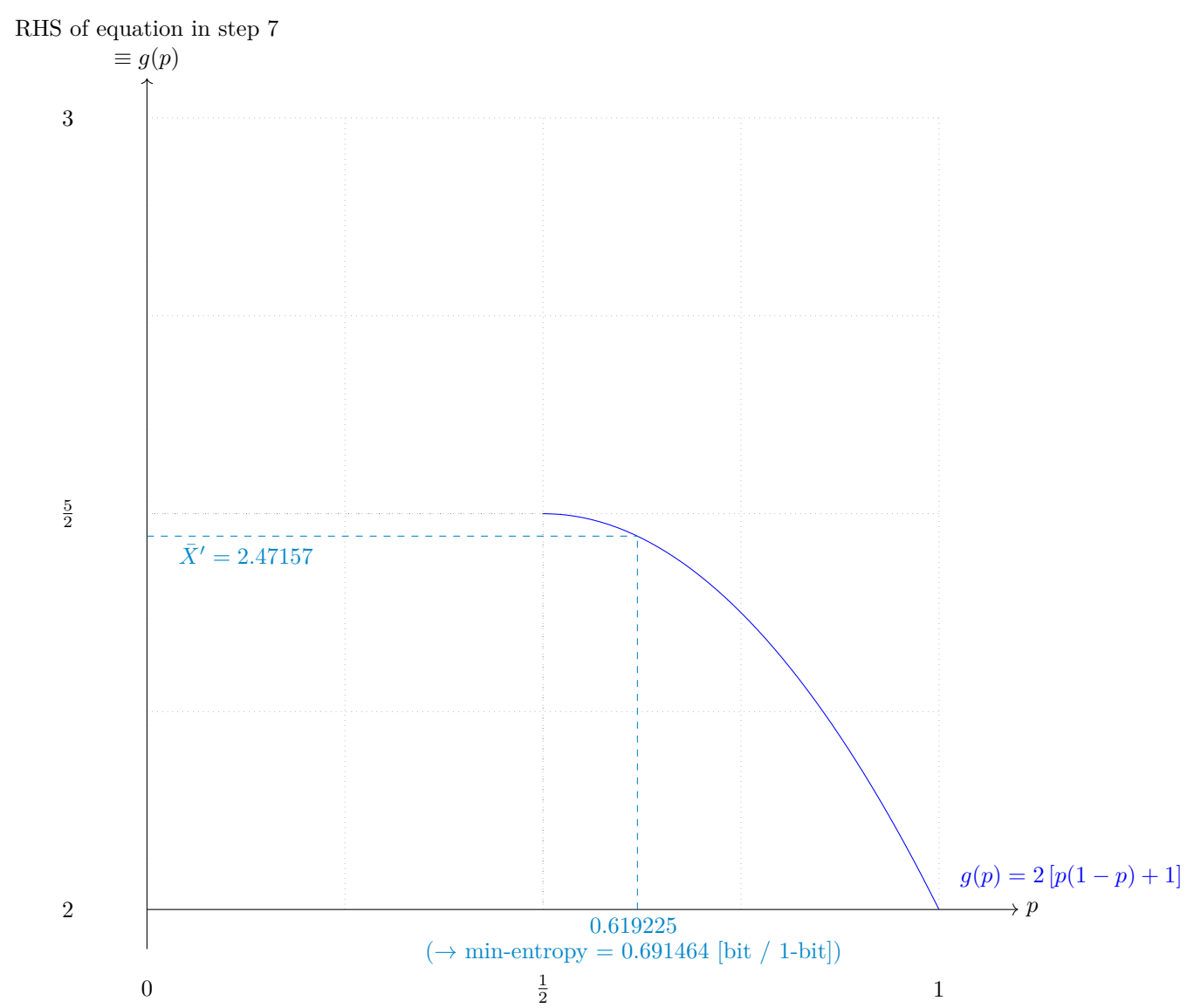


Fig. 4 Solution to the equation in step 7

3.2.1 Supplemental information for traceability

Table 6 Supplemental information for traceability (NIST SP 800-90B Section 6.3.2)

| Symbol         | Value    |
|----------------|----------|
| $p$            | 0.619225 |
| $\bar{X}$      | 2.4919   |
| $\bar{X}'$     | 2.47157  |
| $\hat{\sigma}$ | 0.499997 |

### 3.3 The Markov Estimate (NIST SP 800-90B Section 6.3.3)

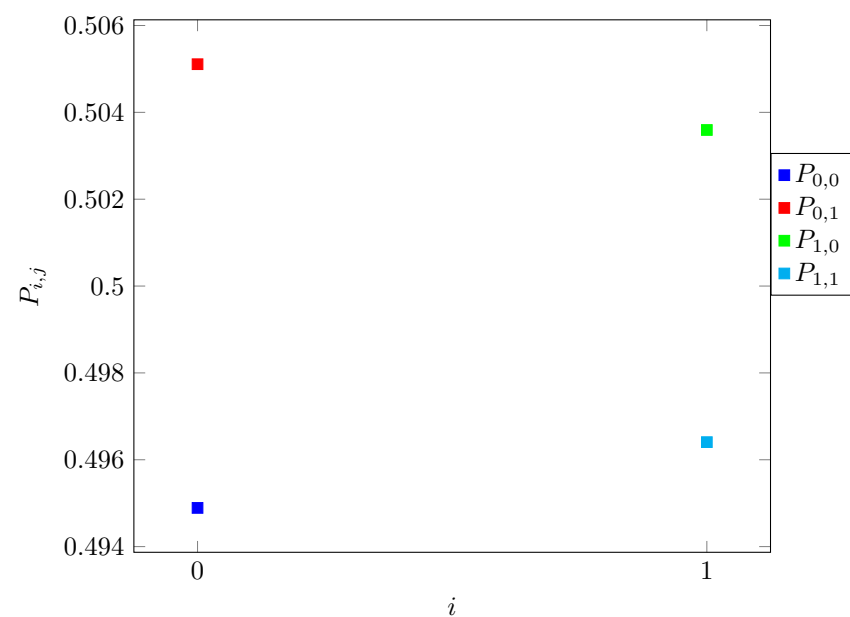


Fig. 5 Transition probability  $P_{i,j}$  of §6.3.3 of NIST SP 800-90B

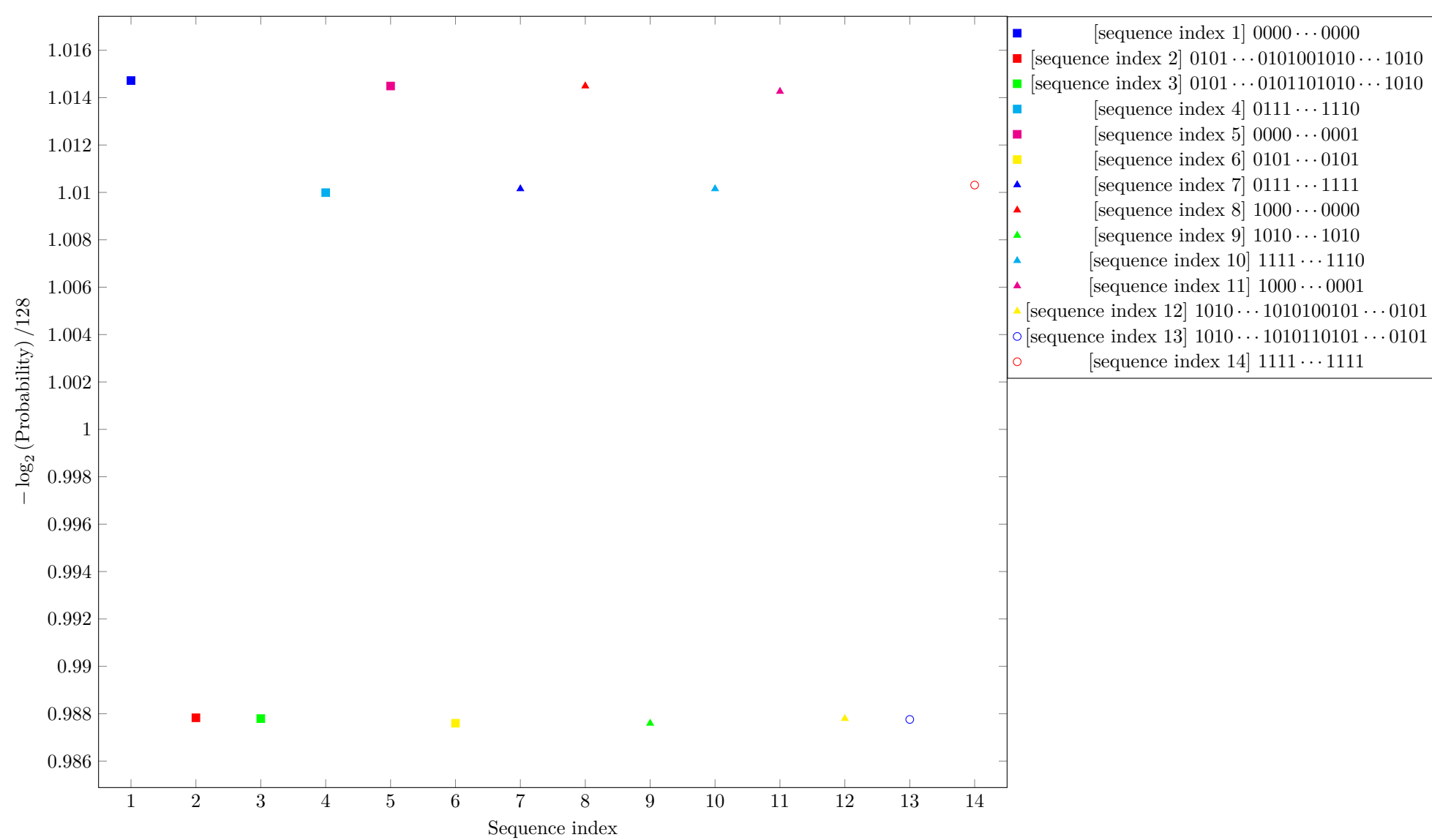


Fig. 6 Estimated Min-Entropy using §6.3.3 of NIST SP 800-90B

### 3.4 The Compression Estimate (NIST SP 800-90B Section 6.3.4)



Fig. 7 Distribution of intermediate value  $D_i$

#### 3.4.1 Supplemental information for traceability

Table 7 Supplemental information for traceability (NIST SP 800-90B Section 6.3.4)

| Symbol         | Value     |
|----------------|-----------|
| $p$            | 0.0785472 |
| $\bar{X}$      | 5.23228   |
| $\hat{\sigma}$ | 1.02952   |
| $\bar{X}'$     | 5.12953   |



### 3.5 The t-tuple Estimate (NIST SP 800-90B Section 6.3.5)



Fig. 8 Intermediate value  $Q[i]$  in §6.3.5 of NIST SP 800-90B



Fig. 9  $P[i]^{1/i}$  in §6.3.5 of NIST SP 800-90B

3.5.1 Supplemental information for traceability

Table 8 Supplemental information for traceability (NIST SP 800-90B Section 6.3.5)

| Symbol           | Value    |
|------------------|----------|
| $t$              | 9        |
| $\hat{p}_{\max}$ | 0.535201 |
| $p_u$            | 0.548049 |

### 3.6 The LRS Estimate (NIST SP 800-90B Section 6.3.6)

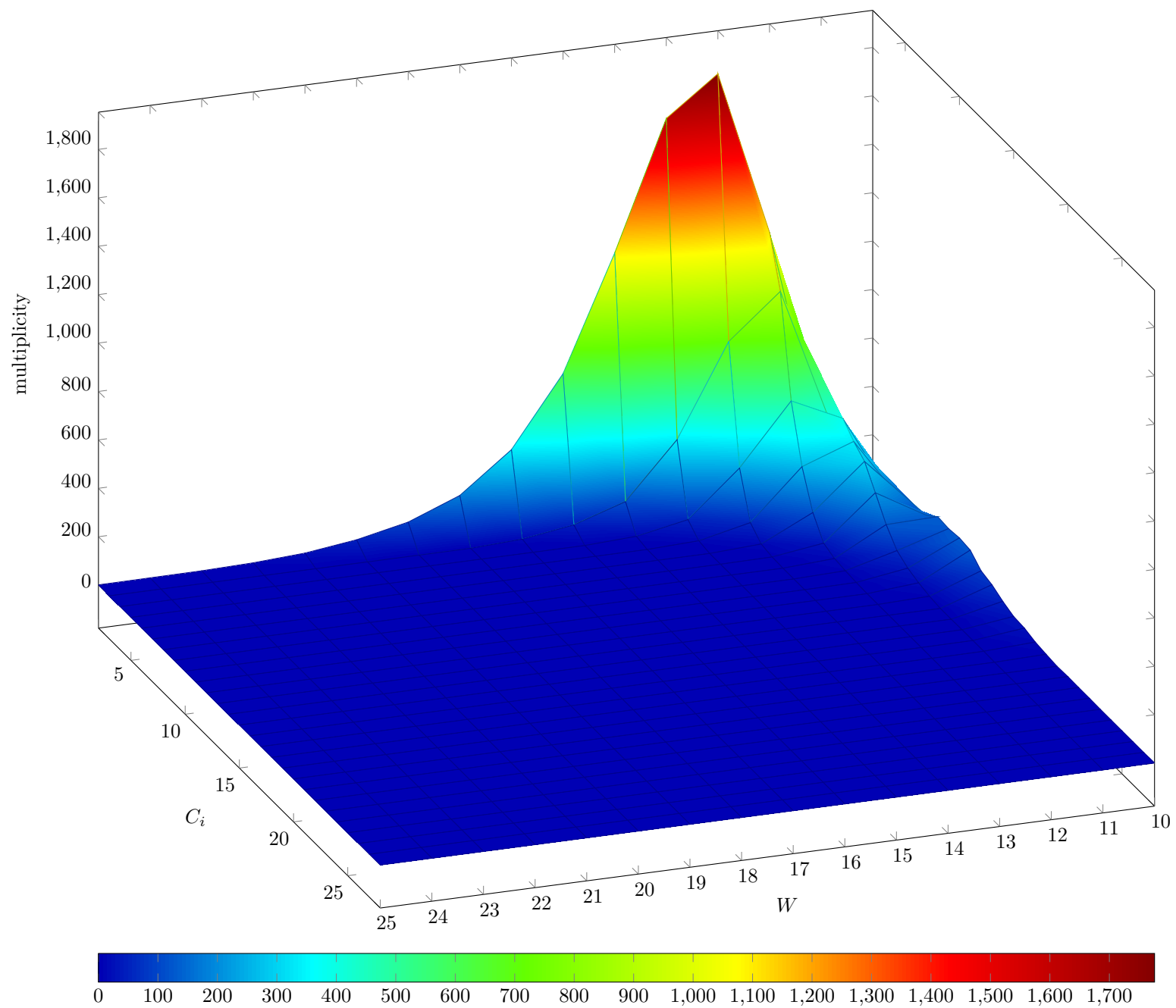


Fig. 10 Estimated  $W$ -tuple collision probability in Step 3 of §6.3.6 of NIST SP 800-90B

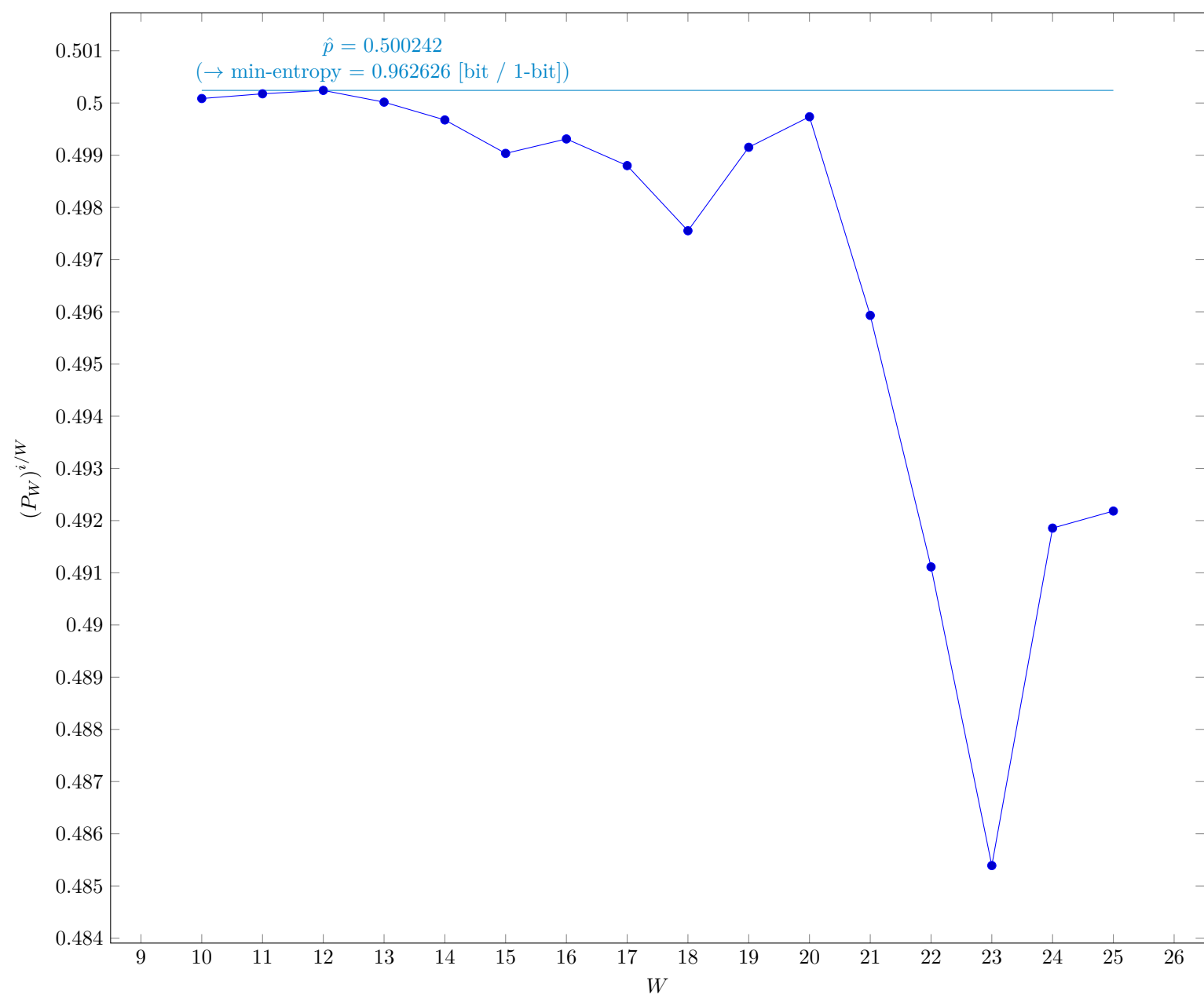


Fig. 11 Estimated average collision probability per string symbol in Step 3 of §6.3.6 of NIST SP 800-90B

3.6.1 Supplemental information for traceability

Table 9 Supplemental information for traceability (NIST SP 800-90B Section 6.3.6)

| Symbol    | Value    |
|-----------|----------|
| $u$       | 10       |
| $v$       | 25       |
| $\hat{p}$ | 0.500242 |
| $p_u$     | 0.513122 |

3.7 Multi Most Common in Window Prediction Estimate (NIST SP 800-90B Section 6.3.7)

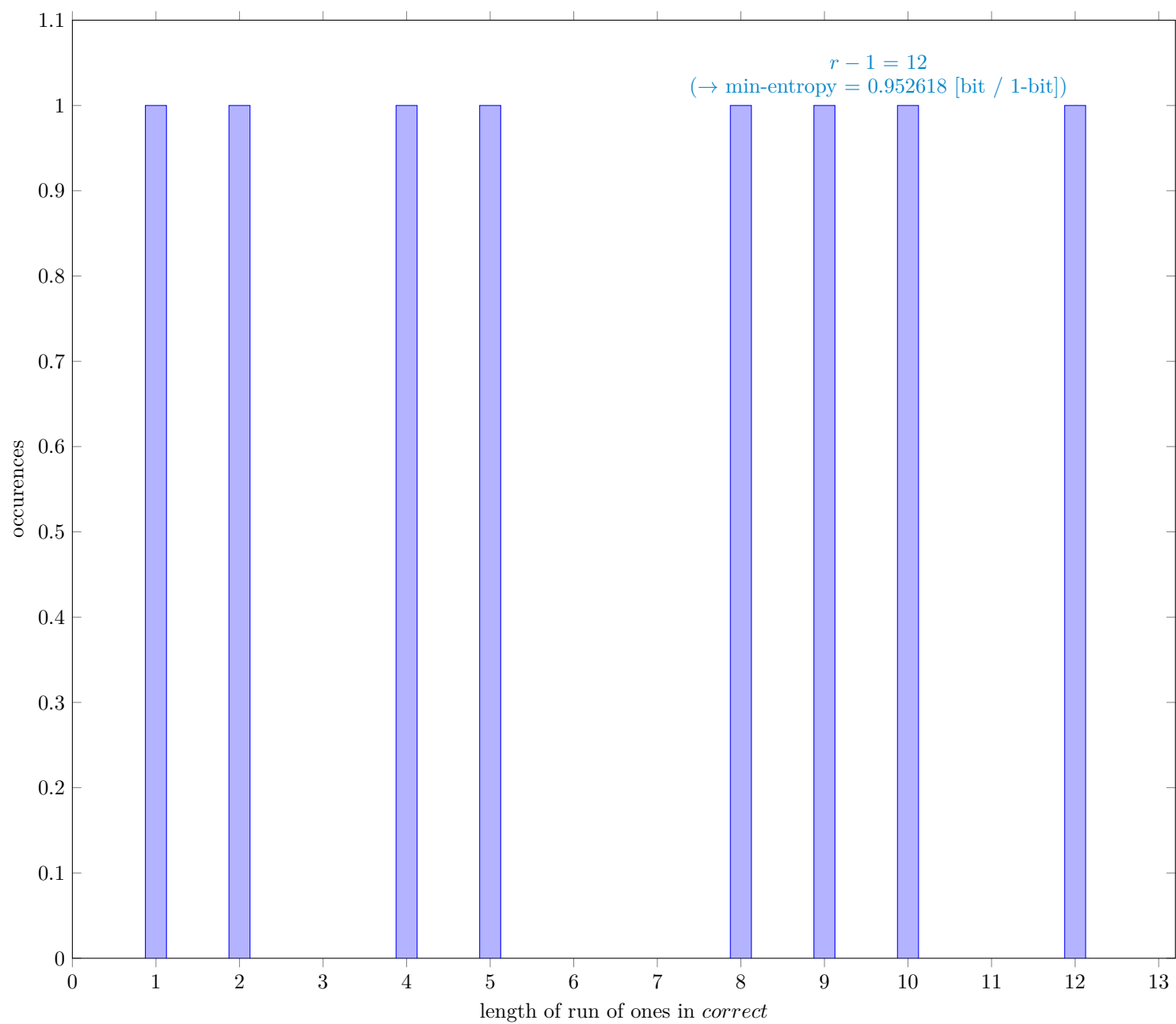


Fig. 12 Distribution of *correct*

3.7.1 Supplemental information for traceability

Table 10 Supplemental information for traceability (NIST SP 800-90B Section 6.3.7)

| Symbol               | Value    |
|----------------------|----------|
| $N$                  | 9937     |
| $C$                  | 5006     |
| $P_{\text{global}}$  | 0.503774 |
| $P'_{\text{global}}$ | 0.516694 |
| $r$                  | 13       |
| $P_{\text{local}}$   | 0.357828 |

### 3.8 Lag Prediction Estimate (NIST SP 800-90B Section 6.3.8)

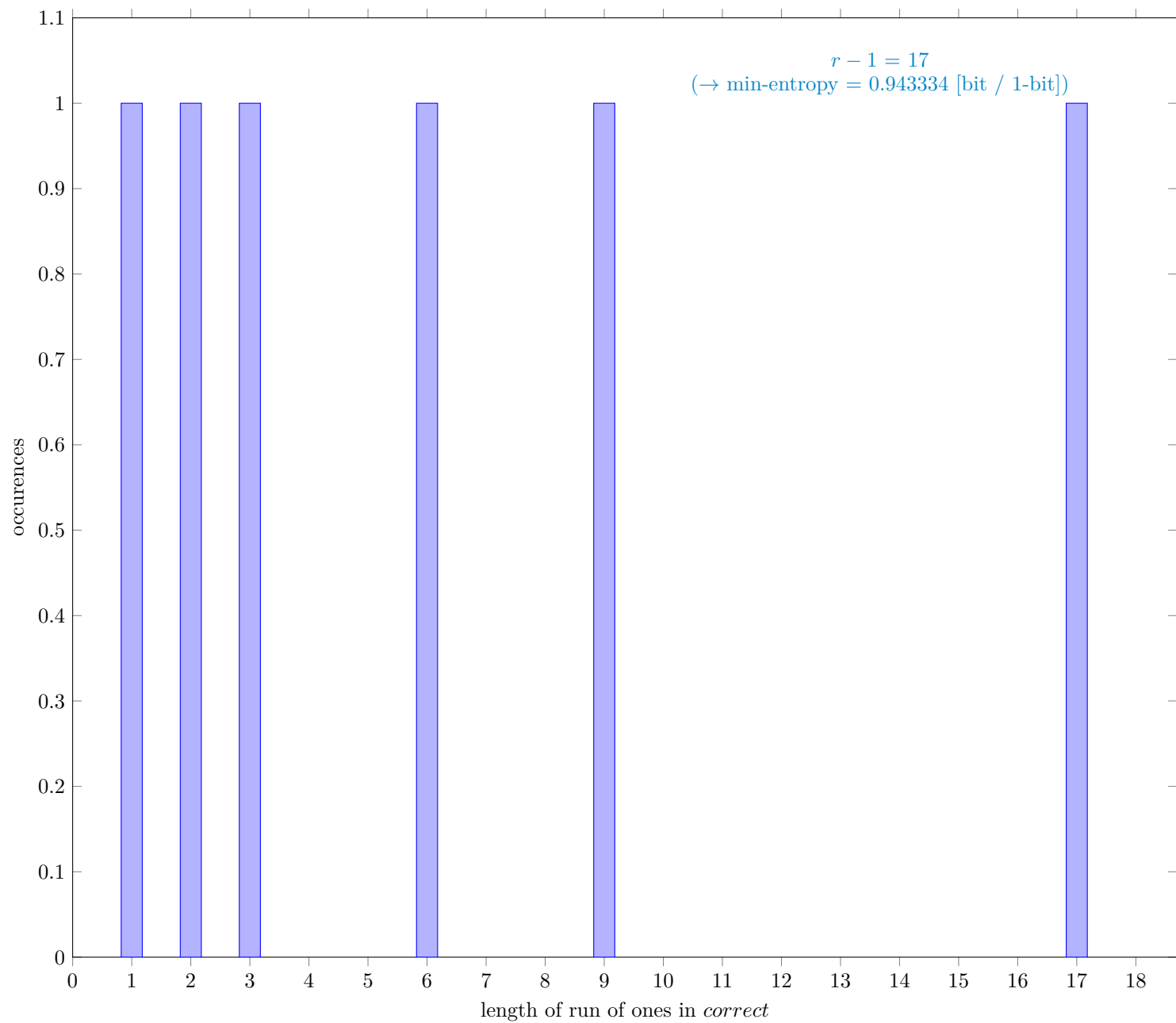


Fig. 13 Distribution of *correct*

#### 3.8.1 Supplemental information for traceability

Table 11 Supplemental information for traceability (NIST SP 800-90B Section 6.3.8)

| Symbol               | Value    |
|----------------------|----------|
| $N$                  | 9999     |
| $C$                  | 5071     |
| $P_{\text{global}}$  | 0.507151 |
| $P'_{\text{global}}$ | 0.52003  |
| $r$                  | 18       |
| $P_{\text{local}}$   | 0.481593 |



### 3.9 The MultiMMC Prediction Estimate (NIST SP 800-90B Section 6.3.9)

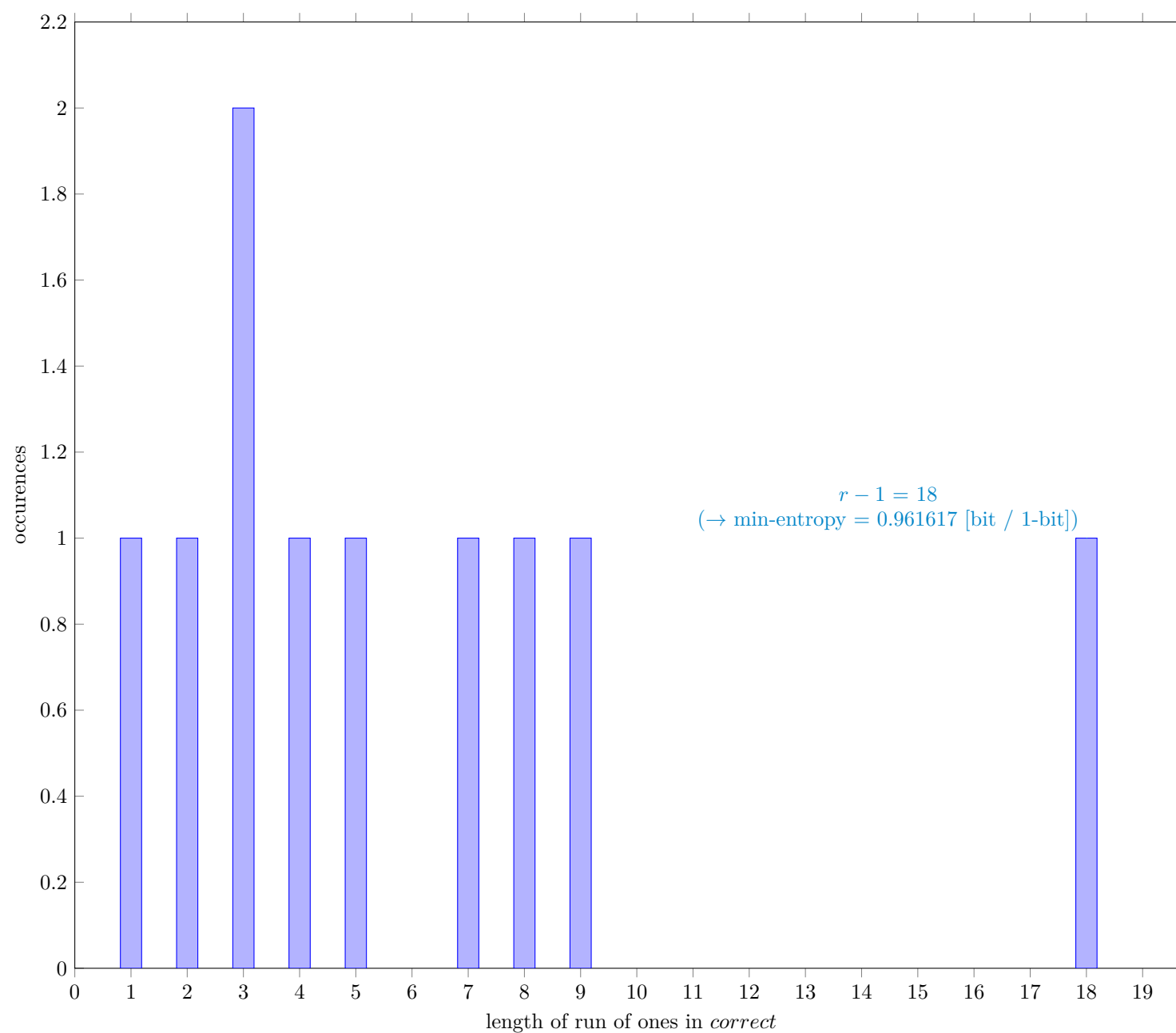


Fig. 14 Distribution of *correct*

#### 3.9.1 Supplemental information for traceability

Table 12 Supplemental information for traceability (NIST SP 800-90B Section 6.3.9)

| Symbol               | Value    |
|----------------------|----------|
| $N$                  | 9998     |
| $C$                  | 5005     |
| $P_{\text{global}}$  | 0.5006   |
| $P'_{\text{global}}$ | 0.513481 |
| $r$                  | 19       |
| $P_{\text{local}}$   | 0.501512 |

3.10 The LZ78Y Prediction Estimate (NIST SP 800-90B Section 6.3.10)

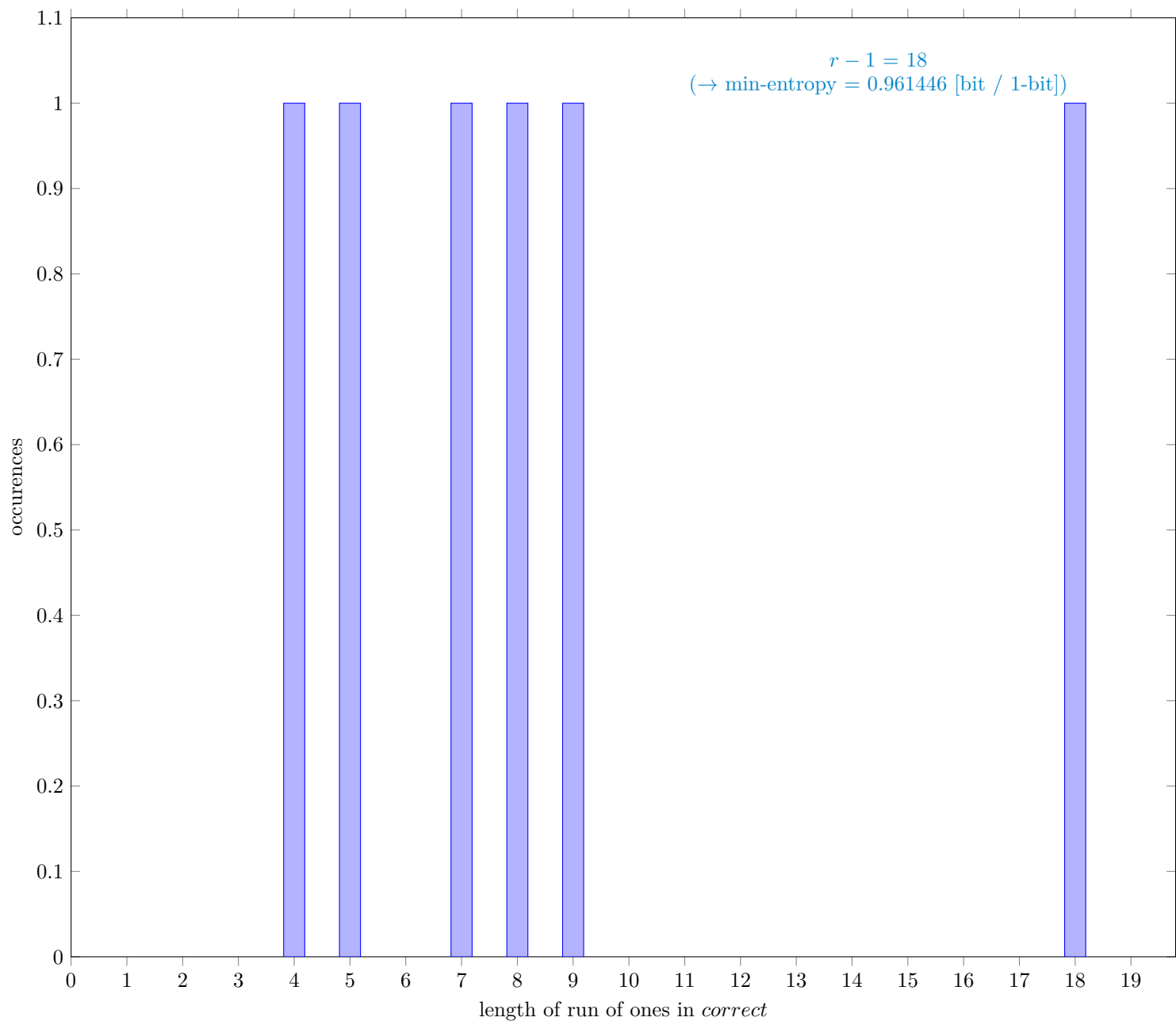


Fig. 15 Distribution of *correct*

3.10.1 Supplemental information for traceability

Table 13 Supplemental information for traceability (NIST SP 800-90B Section 6.3.10)

| Symbol               | Value    |
|----------------------|----------|
| $N$                  | 9983     |
| $C$                  | 4998     |
| $P_{\text{global}}$  | 0.500651 |
| $P'_{\text{global}}$ | 0.513542 |
| $r$                  | 19       |
| $P_{\text{local}}$   | 0.501554 |

3 References

[1] Meltem Sönmez Turan, Elaine Barker, John Kelsey, Kerry A. McKay, Mary L. Baish, Mike Boyle *Recommendation for the Entropy Sources Used for Random Bit Generation*, NIST Special Publication 800-90B, Jan. 2018 <https://nvlpubs.nist.gov/nistpubs/SpecialPublications/NIST.SP.800-90B.pdf>

[2] G. Sakurai, *Proposed list of corrections for NIST SP 800-90B 6.3 Estimators*, Dec. 2022 [https://github.com/g-g-sakura/AnotherEntropyEstimationTool/blob/main/documentation/ProposedListOfCorrections\\_SP800-90B.pdf](https://github.com/g-g-sakura/AnotherEntropyEstimationTool/blob/main/documentation/ProposedListOfCorrections_SP800-90B.pdf)