Report of Entropy estimates based on NIST SP 800-90B non-IID track

 $2025\text{-Sep-}28\ 07\text{:}01\text{:}12.202025$

1 Identification information

1.1 Identification of acquisition data from entropy source

Table 1 Identification information of acquisition data from entropy source

| URL of the acquisition data | https://github.com/usnistgov/SP800-90B_EntropyAssessment/blob/master/bin/biased-random-bits.bin |
|--|---|
| SHA-256 hash value of the acqui- sition data [hex] | 481cdac6 e2d65d45 656c2123 4125eaf2 6df18a49 037f15ff d40002b3 5e547586 |

- Name of the submitter of the acquisition data :
- Brief explanation of the acquisition data (or entropy source) :

1.2 Identification of analysis environment

Table 2 Identification information of analysis environment

| Analysis tool | Name | Another entropy estimation tool with extensions |
|----------------------|------------------------|---|
| | Versioning information | 1.1.5 |
| | built as | 64-bit application |
| | built by | Intel C++ Compiler (INTEL_LLVM_COMPILER: 20250200) |
| | linked libraries | Boost C++ 1.89.0 |
| Analysis environment | Hostname | |
| | CPU information | Intel(R) Core(TM) i5- |
| | Physical memory size | MiB |
| | OS name | Microsoft Windows 11 Pro |
| | OS version | 10.0.26100 N/A Build 26100 |
| | System type | 64-bit |
| | Username | |

1.3 Identification of analysis conditions

Table 3 Identification information of analysis conditions

| Number of samples | 1000000 |
|---|---------|
| Bits per sample | 1 |
| Use Longest Common Prefix*1 for 6.3.5 and 6.3.6 | True |

^{*1} See [3] and [4]

1.4 Identification of analysis method

NIST SP 800-90B [1] 6.3 with corrections [2] is applied

2.1 Numerical results of min-entropy estimates based on non-IID track

Table 4 Numerical results

| Estimator | $H_{ m bitstring}{}^{ m a}$ | Notes to $H_{\text{bitstring}}$ |
|---|-----------------------------|---------------------------------|
| | [bit / 1 - bit] | |
| The Most Common Value Estimate | 0.0286331 | see 3.1 |
| The Collision Estimate | 0.0285138 | see 3.2 |
| The Markov Estimate | 0.029123 | see 3.3 |
| The Compression Estimate | 0.0177666 | see 3.4 |
| The t-Tuple Estimate | 0.0264893 | see 3.5 |
| The Longest Repeated Substring (LRS) Estimate | 0.0558814 | see 3.6 |
| Multi Most Common in Window Prediction Estimate | 0.0286349 | see 3.7 |
| The Lag Prediction Estimate | 0.0405998 | see 3.8 |
| The MultiMMC Prediction Estimate | 0.0286346 | see 3.9 |
| The LZ78Y Prediction Estimate | 0.028635 | see 3.10 |
| The intial entropy source estimate [bit / 1 -bit] | 0.0177666 | |
| $H_I = H_{ m bitstring}$ | $=H_{ m bitstring}$ | |
| ^a Entropy estimate of the sequential dataset [source: NIST SP 800-90B [1] 3.1.3] | | |

2.2 Visual comparison of min-entropy estimates from binary samples



Fig. 1 $\,$ Estimated Min-Entropy using $\S 6.3$ of NIST SP 800-90B $\,$

3 Detailed results of analysis from original samples

3.1 The Most Common Value Estimate (NIST SP 800-90B Section 6.3.1)

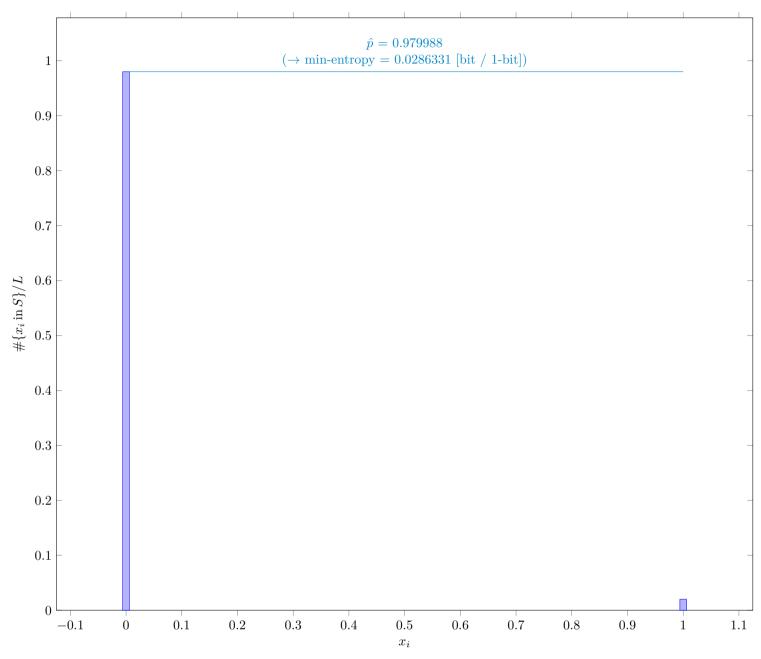


Fig. 2 Distribution of x_i

3.1.1 Supplemental information for traceability

Table 5 Supplemental information for traceability (NIST SP 800-90B Section 6.3.1)

| Symbol | Value |
|-----------|----------|
| mode | 979988 |
| \hat{p} | 0.979988 |
| p_u | 0.980349 |

3.2 The Collision Estimate (NIST SP 800-90B Section 6.3.2)

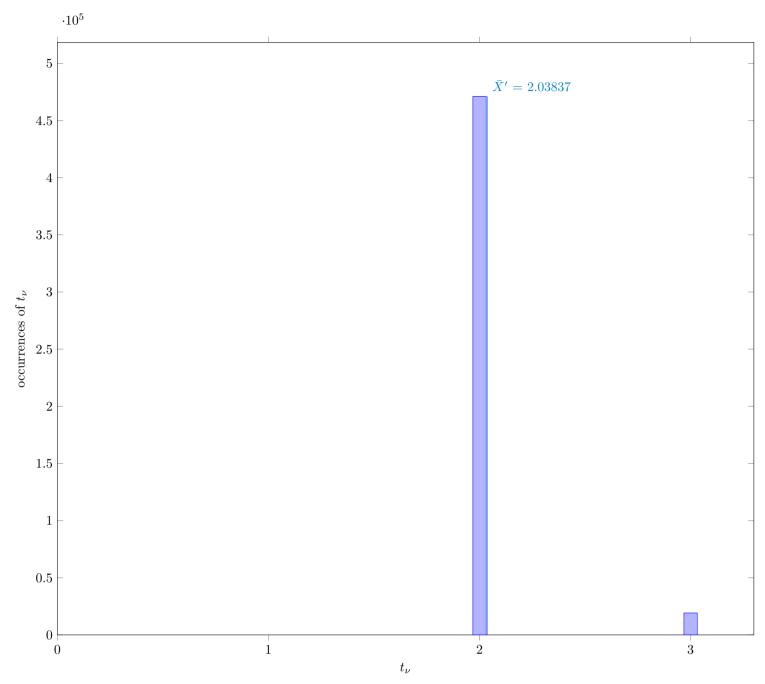


Fig. 3 Distribution of intermediate value t_{ν}



Fig. 4 Solution to the equation in step 7

3.2.1 Supplemental information for traceability

Table 6 Supplemental information for traceability (NIST SP 800-90B Section 6.3.2)

| Symbol | Value |
|----------------|----------|
| p | 0.98043 |
| $ar{X}$ | 2.03909 |
| $ar{X}'$ | 2.03837 |
| $\hat{\sigma}$ | 0.193803 |

3.3 The Markov Estimate (NIST SP 800-90B Section 6.3.3)

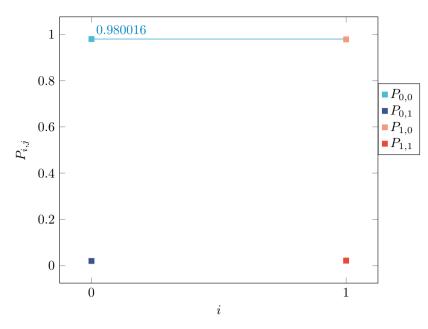


Fig. 5 Transition probability $P_{i,j}$ of §6.3.3 of NIST SP 800-90B

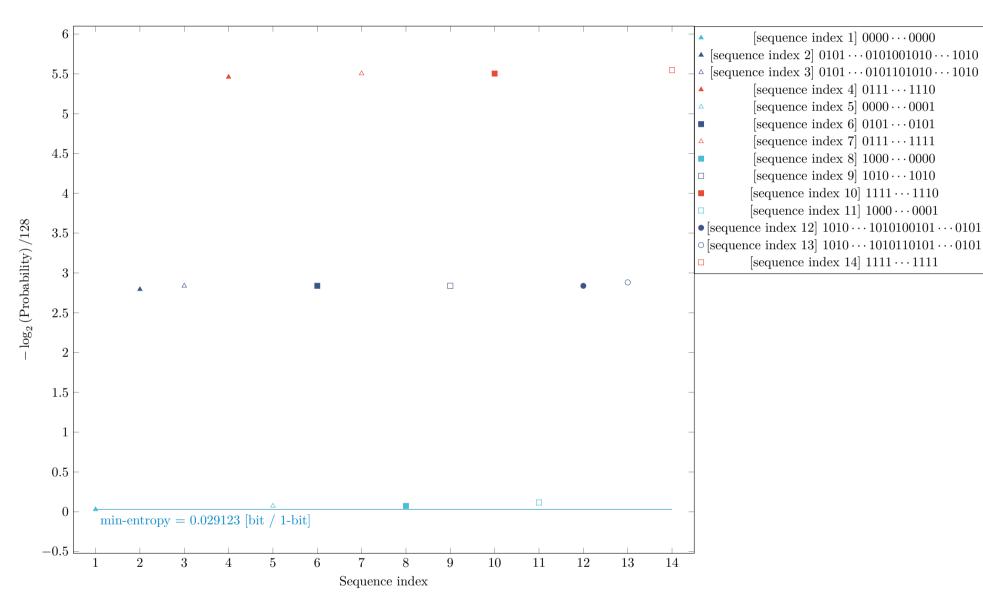


Fig. 6 Estimated Min-Entropy using $\S 6.3.3$ of NIST SP 800-90B

3.4 The Compression Estimate (NIST SP 800-90B Section 6.3.4)

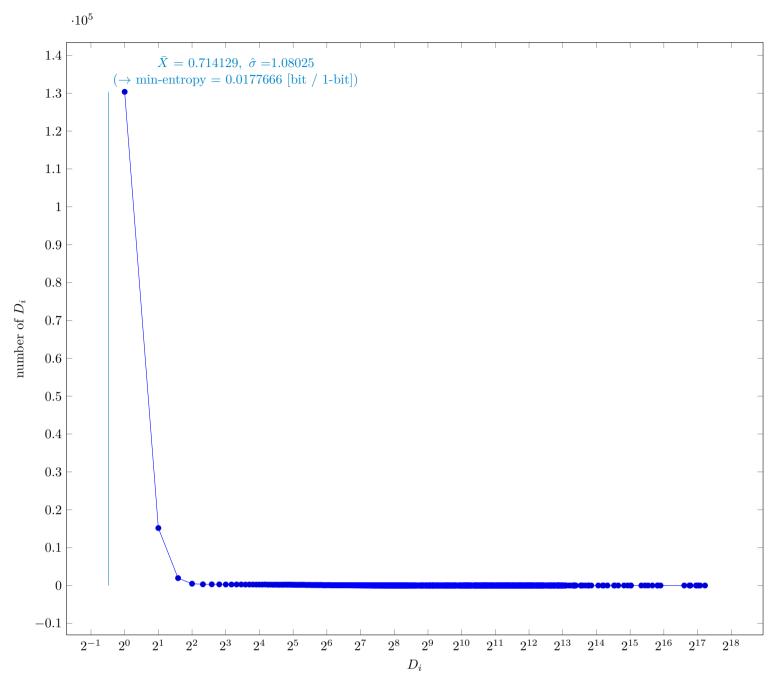


Fig. 7 Distribution of intermediate value D_i

3.4.1 Supplemental information for traceability

Table 7 Supplemental information for traceability (NIST SP 800-90B Section 6.3.4)

| Symbol | Value |
|----------------|----------|
| p | 0.928775 |
| \bar{X} | 0.714129 |
| $\hat{\sigma}$ | 1.08025 |
| \bar{X}' | 0.707292 |

3.5 The t-tuple Estimate (NIST SP 800-90B Section 6.3.5)

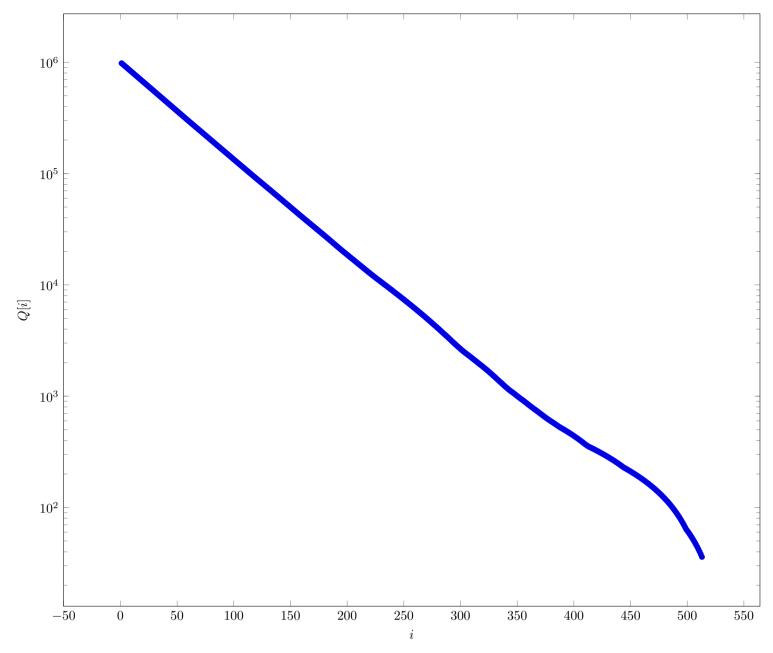


Fig. 8 Intermediate value Q[i] ~ in $\S 6.3.5$ of NIST SP 800-90B

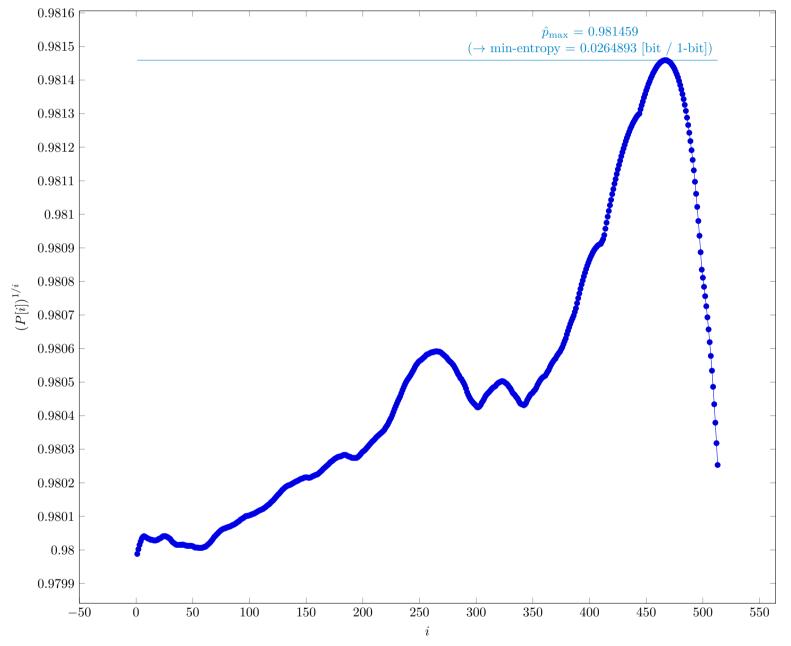


Fig. 9 $P[i]^{1/i}$ in $\S 6.3.5$ of NIST SP 800-90B

3.5.1 Supplemental information for traceability

Table 8 Supplemental information for traceability (NIST SP 800-90B Section 6.3.5)

| Value |
|----------|
| 513 |
| 0.981459 |
| 0.981807 |
| |

3.6 The LRS Estimate (NIST SP 800-90B Section 6.3.6)

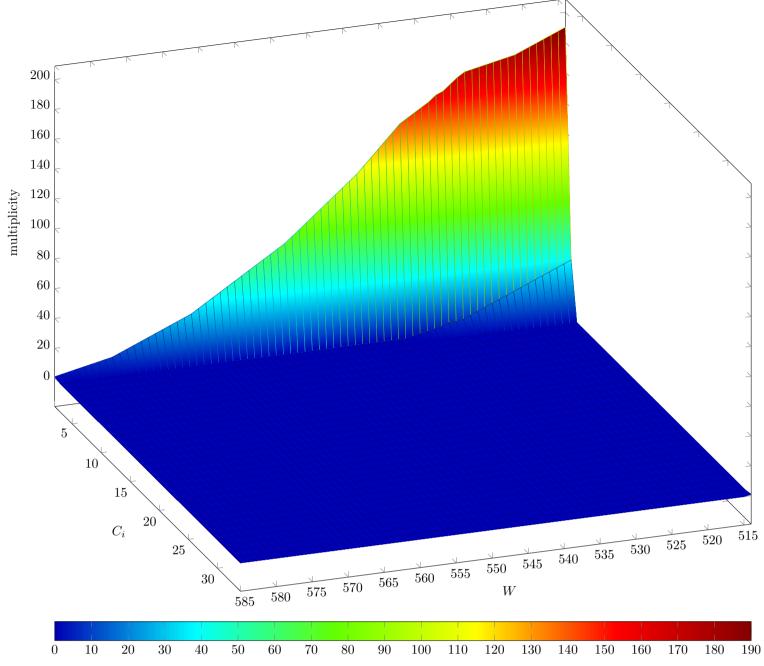


Fig. 10 Estimated W-tuple collision probability in Step 3 of $\S 6.3.6$ of NIST SP 800-90B

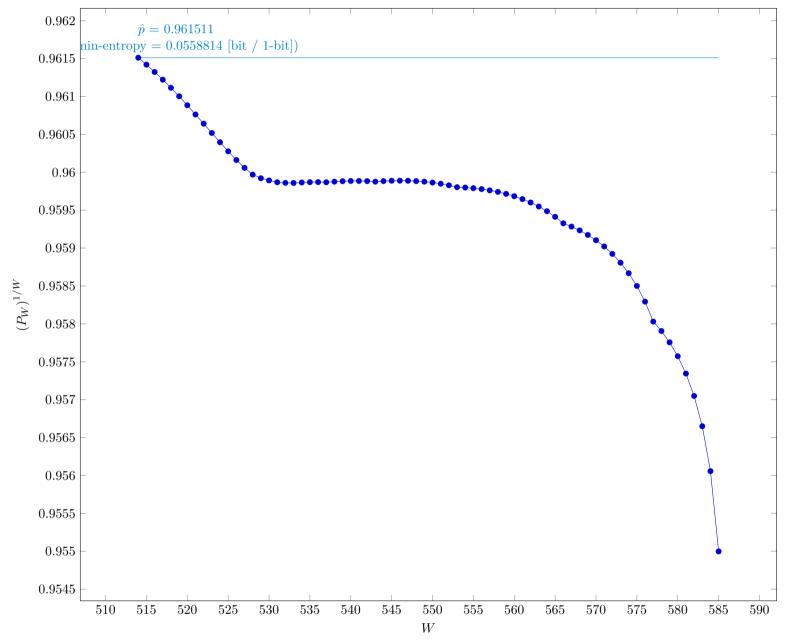


Fig. 11 Estimated average collision probability per string symbol in Step 3 of $\S 6.3.6$ of NIST SP 800-90B

3.6.1 Supplemental information for traceability

Table 9 Supplemental information for traceability (NIST SP 800-90B Section 6.3.6)

| Symbol | Value |
|-----------|----------|
| u | 514 |
| v | 585 |
| \hat{p} | 0.961511 |
| p_u | 0.962007 |

3.7 Multi Most Common in Window Prediction Estimate (NIST SP 800-90B Section 6.3.7)

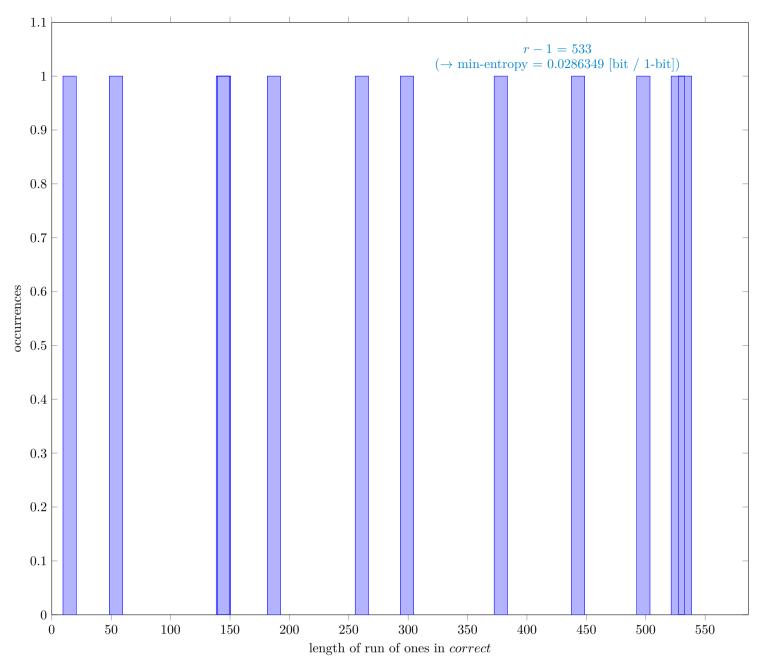


Fig. 12 Distribution of correct

3.7.1 Supplemental information for traceability

Table 10 Supplemental information for traceability (NIST SP 800-90B Section 6.3.7)

| Symbol | Value |
|-----------------------|----------|
| N | 999937 |
| C | 979925 |
| P_{global} | 0.979987 |
| $P'_{ m global}$ | 0.980347 |
| r | 534 |
| P_{local} | 0.972635 |

3.8 Lag Prediction Estimate (NIST SP 800-90B Section 6.3.8)

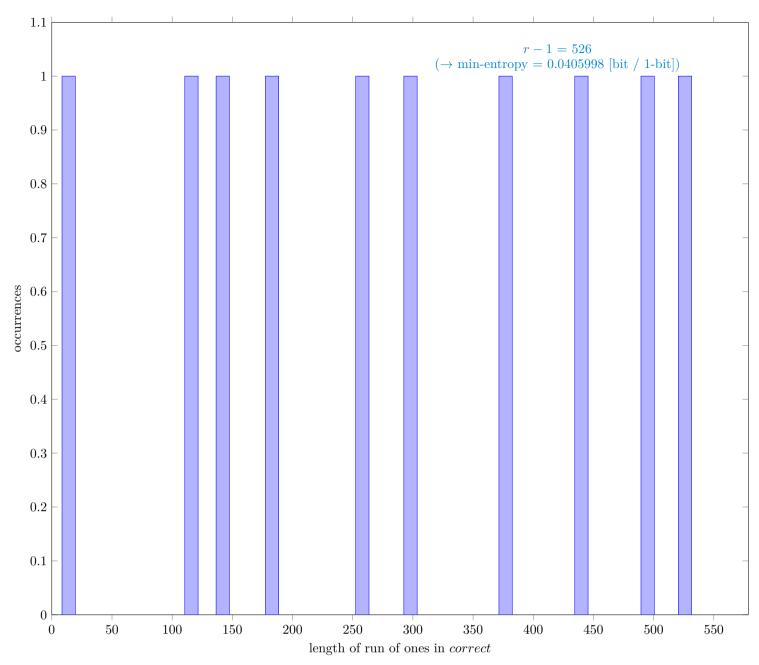


Fig. 13 Distribution of correct

3.8.1 Supplemental information for traceability

 $\begin{tabular}{ll} Table 11 & Supplemental information for traceability (NIST SP 800-90B Section 6.3.8) \\ \end{tabular}$

| Symbol | Value |
|----------------------|----------|
| N | 999999 |
| C | 959838 |
| $P_{ m global}$ | 0.959839 |
| $P'_{ m global}$ | 0.960345 |
| r | 527 |
| P_{local} | 0.972251 |

3.9 The MultiMMC Prediction Estimate (NIST SP 800-90B Section 6.3.9)

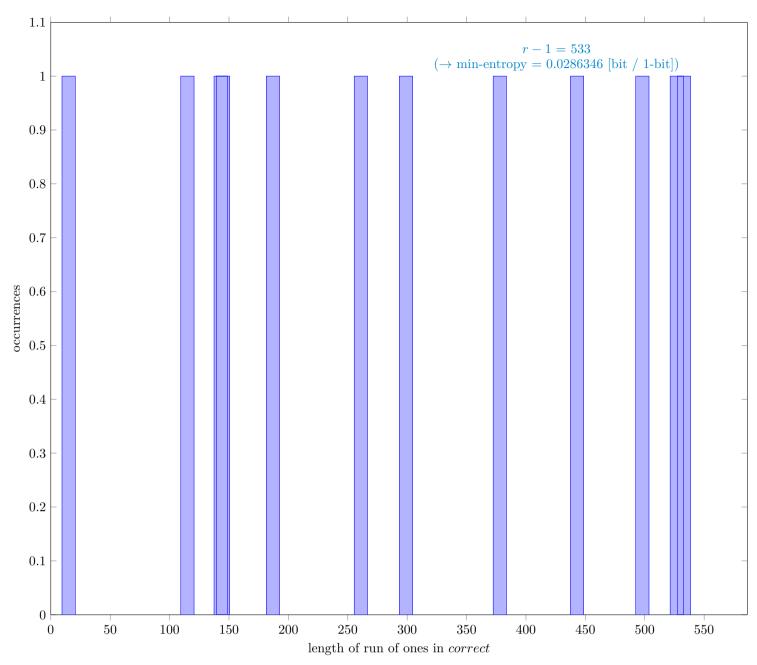


Fig. 14 Distribution of correct

3.9.1 Supplemental information for traceability

Table 12 Supplemental information for traceability (NIST SP 800-90B Section 6.3.9)

| Symbol | Value |
|-----------------------|----------|
| N | 999998 |
| C | 979985 |
| P_{global} | 0.979987 |
| $P'_{ m global}$ | 0.980348 |
| r | 534 |
| $P_{ m local}$ | 0.972635 |

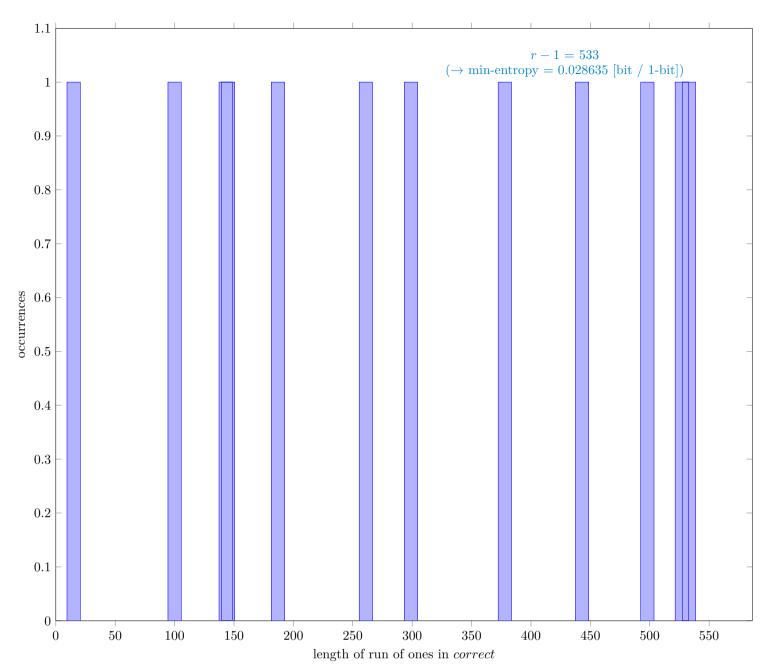


Fig. 15 Distribution of correct

3.10.1 Supplemental information for traceability

Table 13 Supplemental information for traceability (NIST SP 800-90B Section 6.3.10)

| Symbol | Value |
|------------------|----------|
| N | 999983 |
| C | 979970 |
| $P_{ m global}$ | 0.979987 |
| $P'_{ m global}$ | 0.980347 |
| r | 534 |
| $P_{ m local}$ | 0.972635 |

3 References

- [1] Meltem Sönmez Turan, Elaine Barker, John Kelsey, Kerry A. McKay, Mary L. Baish, Mike Boyle, Recommendation for the Entropy Sources Used for Random Bit Generation, NIST Special Publication 800-90B, Jan. 2018 https://nvlpubs.nist.gov/nistpubs/SpecialPublications/NIST.SP.800-90B.pdf
- [2] G. Sakurai, Proposed list of corrections for NIST SP 800-90B 6.3 Estimators, Dec. 2022 https://github.com/g-g-sakura/AnotherEntropyEstimationTool/blob/main/documentation/ProposedListOfCorrections_SP800-90B.pdf
- [3] Thomas H. Cormen, Charles E. Leiserson, Ronald L. Rivest and Clifford Stein, *Introduction to Algorithms (fourth edition)*, The MIT Press. https://mitpress.mit.edu/9780262046305/introduction-to-algorithms/
- [4] G. Sakurai, ImplementationNotes for entropy estimation based on NIST SP800-90B non-IID track, Sep. 2025 https://github.com/g-g-sakura/AnotherEntropyEstimationTool/blob/main/documentation/SP800-90B_EntropyEstimate_ImplementationNotes.pdf