

## Review Guide 3: Database Theory

1. Given:  $\alpha, \beta, \gamma, \delta$  refer to distinct sets of attributes in  $R$ . For each of the following inference rules, show it is either sound through derivation using only **Armstrong's Axioms**, or unsound by providing a counterexample.

(a)  $\alpha \rightarrow \beta \xRightarrow{?} \alpha \cup \gamma \rightarrow \beta$

(b)  $\alpha \rightarrow \beta \xRightarrow{?} \beta \subseteq \alpha$

(c)  $\alpha \rightarrow \beta, \beta \rightarrow \gamma \xRightarrow{?} \alpha \cup \delta \rightarrow \gamma \cup \delta$

(d)  $** \alpha \rightarrow \beta, \beta \cup \gamma \rightarrow \delta \xRightarrow{?} \alpha \cup \gamma \rightarrow \beta \cup \delta$

2. \*\* Consider the relation  $U(W, X, Y, Z)$  with a set of functional dependencies

$$FD(U) = \{ \\ XZ \rightarrow YZ, \\ Y \rightarrow Z \}$$

- (a) List all of  $U$ 's superkeys with respect to  $FD(U)$ .
- (b) Is  $U$  in BCNF with respect to  $FD(U)$ ? If so, show that every functional dependency  $\alpha \rightarrow \beta$  is either trivial or that  $\alpha$  is a superkey in  $U$ . Otherwise, decompose  $U$  into a set of BCNF relations with respect to  $FD(U)$ . Show your work.
- (c) Find  $FD_c(U)$ , a canonical cover of  $FD(U)$ .
- (d) List all of  $U$ 's superkeys with respect to  $FD_c(U)$ .
- (e) Is  $U$  in BCNF with respect to  $FD_c(U)$ ? If so, show that every functional dependency  $\alpha \rightarrow \beta$  is either trivial or that  $\alpha$  is a superkey in  $U$ . Otherwise, decompose  $U$  into a set of BCNF relations with respect to  $FD_c(U)$ . Show your work.