Evaluate  $\oint_C (x^4y^5 - 2y) dx + (3x + x^5y^4) dy$ , where *C* is the oriented curve pictured in Figure 6.29

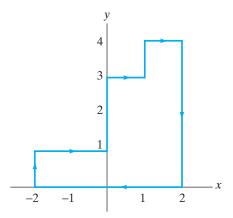


FIGURE 6.29. The oriented curve *C* of Exercise 13.

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(a) Sketch the curve given parametrically by  $x(t) = (1 - t^2, t^3 - t)$ .

(b) Find the area inside the closed loop of the curve.

Consider the line integral  $\int_C z^2 dx + 2y dy + xz dz$ .

(a) Evaluate this integral, where C is the line segment from (0,0,0) to (1,1,1).

(b) Evaluate this integral, where *C* is the path from (0,0,0) to (1,1,1) parametrized by  $\mathbf{x}(t) = (t,t^2,t^3), \ 0 \le t \le 1.$ 

(c) Is the vector field  $\mathbf{F} = \begin{bmatrix} z^2, & 2y, & xz \end{bmatrix}$  conservative? Why or why not?

Determine whether the vector field  $\mathbf{F} = \begin{bmatrix} e^{x+y}, & e^{xy} \end{bmatrix}$  conservative. If it is, find a scalar potential function for  $\mathbf{F}$ .

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Determine whether the vector field  $\mathbf{F} = \left[2x\sin y, \ x^2\cos y\right]$  conservative. If it is, find a scalar potential function for  $\mathbf{F}$ .

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Let  $\mathbf{F} = [x^2, \cos y \sin z, \sin y \cos z].$ 

(a) Show that F is conservative and find a scalar potential function f for F.

(b) Evaluate  $\int_{\mathbf{x}} \mathbf{F} \cdot d\mathbf{s}$  along the path  $\mathbf{x}[0,1] \to \mathbb{R}^3$ ,  $\mathbf{x}(t) = (t^2 + 1, e^t, e^{2t})$ .

(a) Determine where the vector field

$$\mathbf{F} = \begin{bmatrix} \frac{x + xy^2}{y^2} & \frac{x^2 + 1}{y^3} \end{bmatrix}$$

is conservative.

(b) Determine a scalar potential for F.

(c) Find the work done by **F** in moving a particle along the parabolic curve  $y = 1+x-x^2$  from (0,1) to (1,1).