Box #_____

Math 60

HW 11

Due May 32, 2016

Problems: 6.2.{R10, 13, 15}, 6.3.{1, 3, 4, R7, 25, R26, 33}

Problem 6.2.13

Evaluate $\oint_C (x^4y^5 - 2y)\,dx + (3x + x^5y^4)\,dy$, where C is the oriented curve pictured in Figure 6.29

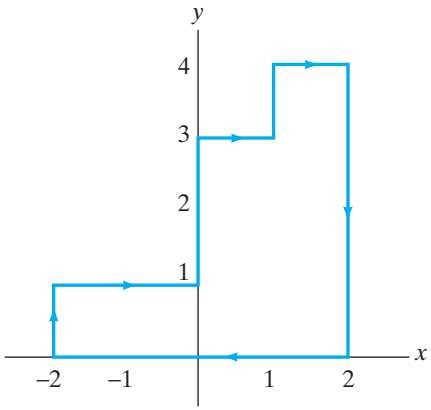

FIGURE 6.29. The oriented curve C of Exercise 13.

Problem 6.2.15

(a) Sketch the curve given parametrically by $x(t) = (1 - t^2, t^3 - t)$.

(b) Find the area inside the closed loop of the curve.

Problem 6.3.1

Consider the line integral $\int_C z^2\,\mathrm{d}x + 2y\,\mathrm{d}y + xz\,\mathrm{d}z$.

(a) Evaluate this integral, where C is the line segment from $(0,0,0)$ to $(1,1,1)$.

(b) Evaluate this integral, where C is the path from $(0,0,0)$ to $(1,1,1)$ parametrized by $\mathbf{x}(t) = (t, t^2, t^3)$, $0 \le t \le 1$.

(c) Is the vector field $\mathbf{F} = \begin{bmatrix} z^2, & 2y, & xz \end{bmatrix}$ conservative? Why or why not?

Problem 6.3.3
Determine whether the vector field $\mathbf{F} = \left[e^{x+y}, \quad e^{xy}\right]$ conservative. If it is, find a scalar potential function for $\mathbf{F}$.

Problem 6.3.4

Determine whether the vector field $\mathbf{F} = \left[2x\sin y, \quad x^2\cos y\right]$ conservative. If it is, find a scalar potential function for $\mathbf{F}$.

Problem 6.3.25

Let $\mathbf{F} = \left[x^2, \quad \cos y \sin z, \quad \sin y \cos z\right]$.

(a) Show that $\mathbf{F}$ is conservative and find a scalar potential function f for $\mathbf{F}$.

(b) Evaluate $\int_{\mathbf{x}} \mathbf{F} \cdot d\mathbf{s}$ along the path $\mathbf{x}[0,1] \to \mathbb{R}^3$, $\mathbf{x}(t) = (t^2 + 1, e^t, e^{2t})$.

Problem 6.3.33

(a) Determine where the vector field

$$\mathbf{F} = \begin{bmatrix} \dfrac{x + xy^2}{y^2} & \dfrac{x^2 + 1}{y^3} \end{bmatrix}$$

is conservative.

(b) Determine a scalar potential for $\mathbf{F}$.

(c) Find the work done by $\mathbf{F}$ in moving a particle along the parabolic curve $y = 1 + x - x^2$ from $(0, 1)$ to $(1, 1)$.