Find the first- and second-order Taylor polynomials for

$$f(x,y) = \frac{1}{x^2 + y^2 + 1}$$

at 
$$a = (1, -1)$$
.

Find the first- and second-order Taylor polynomials for

$$f(x,y) = e^{2x+y}$$

at 
$$\mathbf{a} = (0, 0)$$
.

Find the Hessian matrix  $Hf(\mathbf{a})$  for

$$f(x,y,z) = e^{2x-3y}\sin(5z)$$

at 
$$\mathbf{a} = (0, 0, 0)$$
.

Determine the total differential of

$$f(x,y) = x^2 y^3$$

Near the point (1,-2,1), is the function  $g(x,y,z) = x^3 - 2xy + x^2z + 7z$  is most sensitive to changes in x, y, or z?

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Identify and determine the nature of the critical points of

$$f(x,y) = y^4 - 2xy^2 + x^3 - x$$

Identify and determine the nature of the critical points of

$$f(x,y) = e^{-x}(x^2 + 3y^2)$$

Under what conditions on the constant k will the function

$$f(x,y) = kx^2 - 2xy + ky^2$$

have a nondegenerate local minimum at (0,0)? What about a local maximum?

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