

Uniform Circular Motion

21. (b)

$$22. (a) \frac{a_R}{a_r} = \frac{\omega_R^2 \times R}{\omega_r^2 \times r} = \frac{T_r^2}{T_R^2} \times \frac{R}{r} = \frac{R}{r} \quad [\text{As } T_r = T_R]$$

$$23. (c) \omega = \frac{2\pi \text{ Rad}}{60 \text{ min}_{min}} \text{ and } \omega_{hr} = \frac{2\pi}{12 \times 60} \frac{\text{Rad}}{\text{min}}$$

$$\therefore \frac{\omega_{min}}{\omega_{hr} \frac{2\pi/60}{2\pi/12 \times 60}}$$

24. (d) The particle performing circular motion flies off tangentially.

$$25. (a) \text{ The angle of banking, } \tan \theta = \frac{v^2}{rg}$$

$$\Rightarrow \tan 12^\circ = \frac{(150)^2}{r \times 10} \Rightarrow r = 10.6 \times 10^3 \text{ m} = 10.6 \text{ km}$$

$$26. (c) \text{ K.E.} = \frac{1}{2}mv^2. \text{ Which is scalar, so it remains constant.}$$

$$27. (b) v = 72 \text{ km/hour} = 20 \text{ m/sec}$$

$$\theta = \tan^{-1} \left(\frac{v^2}{rg} \right) = \tan^{-1} \left(\frac{20 \times 20}{20 \times 10} \right) = \tan^{-1}(2)$$

28. (a)

$$29. (d) 120 \text{ rev/min} = 120 \times \frac{2\pi}{60} \text{ rad/sec} = 4\pi \text{ rad/sec}$$

30. (c) In uniform circular motion, acceleration causes due to change in direction and is directed radially towards centre.



31. (b) Reaction on inner wheel $R_1 = \frac{1}{2}M \left[g - \frac{v^2 h}{ra} \right]$

Reaction on outer wheel $R_2 = \frac{1}{2}M \left[g + \frac{v^2 h}{ra} \right]$

where, r = radius of circular path, $2a$ = distance between two wheels and h = height of centre of gravity of car.

32. (d) Maximum tension = $m\omega^2 r = m \times 4\pi^2 \times n^2 \times r$

By substituting the values we get $T_{\max} = 87.64N$

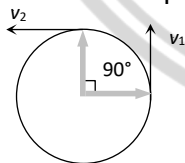
33. (d) $\frac{v^2}{rg} = \frac{h}{l} \Rightarrow v = \sqrt{\frac{rgh}{l}} = \sqrt{\frac{50 \times 1.5 \times 9.8}{10}} = 8.57m/s$

34. (b) $a = \omega^2 r = 4\pi^2 n^2 r = 4\pi^2 \times 1^2 \times 20 \times 10^3$
 $\therefore a = 8 \times 10^5 m/sec^2$

35. (c)

36. (d) In 15 second's hand rotate through 90° .

Change in velocity $|\Delta \vec{v}| = 2v \sin(\theta/2)$



$= 2(r\omega) \sin(90^\circ/2) = 2 \times 1 \times \frac{2\pi}{T} \times \frac{1}{\sqrt{2}}$

$= \frac{4\pi}{60\sqrt{2}} = \frac{\pi\sqrt{2}}{30} \frac{cm}{sec}$ [As $T = 60$ sec]

37. (c) Since $n = 2$, $\omega = 2\pi \times 2 = 4\pi rad/s^2$

So acceleration = $\omega^2 r = (4\pi)^2 \times \frac{25}{100} m/s^2 = 4\pi^2$





38. (b) $\omega^2 r = 4\pi^2 n^2 r = 4\pi^2 \left(\frac{1200}{60}\right)^3 \times 30 = 4740 \text{ m/s}^2$

39. (a)

40. (c) Particles of cream are lighter so they get deposited near the centre of circular path.

