

Uniform Circular Motion

81. (c)

82. (a)
$$T = m\omega^2 r \Rightarrow \omega \propto \sqrt{T}$$
 : $\frac{\omega_2}{\omega_1} = \sqrt{\frac{1}{4}} \Rightarrow \omega_2 = \frac{\omega_1}{2} = 5rpm$

83. (d)
$$\theta = tan^{-1} \left(\frac{v^2}{rg} \right) = tan^{-1} \left[\frac{(14\sqrt{3})^2}{20\sqrt{3} \times 9.8} \right] = tan^{-1} \left[\sqrt{3} \right] = 60^{\circ}$$

- **84.** (c) Centripetal acceleration= $4\pi^2 n^2 r = 4\pi^2 \left(\frac{1}{2}\right)^2 \times 4 = 4\pi^2$
- 85. (b) Centripetal force = breaking force $\Rightarrow m\omega^2 r = \text{breaking stress} \times \text{cross sectional area}$ $\frac{1}{p \times A} \sqrt{\frac{4.8 \times 10^7 \times 10^{-6}}{4.8 \times 10^7 \times 10^{-6}}}$

$$\Rightarrow m\omega^2 r = p \times A \Rightarrow \omega = \sqrt{\frac{p \times A}{mr}} = \sqrt{\frac{4.8 \times 10^7 \times 10^{-6}}{10 \times 0.3}}$$

$$\omega = 4rad/sec$$

- 86. (a) Because velocity is always tangential and centripetal acceleration is radial.
- 87. (c) T = tension, W = weight and F = centrifugal force

88. (c)
$$\mu = \frac{v^2}{rg} = \frac{(4.9)^2}{4 \times 9.8} = 0.61$$

89. (d) As body covers equal angle in equal time intervals. its angular velocity and hence magnitude of linear velocity is constant.

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90. (b)
$$\omega = \frac{v}{r} = \frac{10}{100} = 0.1 rad/s$$

91. (a)
$$F = \frac{mv^2}{r} \Rightarrow v = \sqrt{\frac{rF}{m}}$$





92. (d) Electrostatic force provides necessary centripetal force for circular motion of electron.

93. (a) Acceleration=
$$\omega^2 r = \frac{v^2}{r} = \omega v = \frac{2\pi}{T} v$$

94. (b)
$$v = \sqrt{\mu rg} = \sqrt{0.6 \times 150 \times 10} = 30 m/s$$

96. (c)
$$F = \frac{mv^2}{r} \Rightarrow F \propto v^2$$
 i.e. force will become 4 times.

97. (d)
$$v = \sqrt{\mu rg} = \sqrt{0.25 \times 40 \times 10} = 10 m/s$$

No. of revolution=
$$\frac{\text{Total time}}{\text{Time period}} = \frac{140sec}{40sec=3.5Rev}$$
.

So, distance=
$$3.5 \times 2\pi R = 3.5 \times 2\pi \times 10 = 220m$$
.

99. (a)
$$m4\pi^2 n^2 r = 4 \times 10^{-13} \Rightarrow n = 0.08 \times 10^8 cycles/sec$$
.

100. (b) Momentum changes by 2mv but kinetic energy remains same.

