

Let's say that:  $n$  - no of elements in  $A$ ,

$A$  - the list of elements,

sum - the sum of elements from  $A$ .

The problem is: divide  $A$  into 2 subsets ( $B$  and  $C$ ) such that:  $B \subset A$ ,  $C \subset A$ ,  $B \cap C = \emptyset$ ,  $B \cup C = A$  (if  $A$  has

$[1, 2, 2, 3]$ , the first 2 "differs" from the second one), and

$$\frac{\sum B}{\text{card}(B)} = \frac{\sum C}{\text{card}(C)} = \frac{\sum A}{n} = \frac{\text{sum}}{n}$$

~~( $A \subset \mathbb{Z}$ )~~  $A \subset \mathbb{Z}$  - only integers!  $\Rightarrow \sum B \in \mathbb{Z}$

$$\sum C \in \mathbb{Z}$$

$$\text{sum} \in \mathbb{Z}$$

$$\Rightarrow \sum B = \frac{\text{sum} \cdot \text{card}(B)}{n} \in \mathbb{Z} \Rightarrow \text{the nr of elements in } B \text{ times the sum of } A \text{ must be divisible with } n$$

$$\Rightarrow \underline{\text{sum} \cdot \text{card}(B) : n}!!!$$

analog pentru  $C$

$$i) \text{ sum} \cdot \text{card}(C) : n$$

$\Rightarrow$  if we cannot find a subset  $B$  such that  $i)$  is satisfied  $\Rightarrow$  there is no such arrangement for the problem

$\Rightarrow$  return false.

if we can find such number, proceed.

~~We have to check~~ the nr. of  
we suppose that  $B$  has elements in range  $(1 - n/2)$  because  
if  $B$  has  $n/2 + 5$  elem, then  $C$  will have  $n/2 - 5$  elem  
and will be in the same range. So we have to check only  
that range.

This problem requires dynamic approach. So we create  
a vector of ~~sum~~ sets, call it sums (`set<int> sums[n/2+1]`),  
which has  $n/2 + 1$  elements.

The first "row" contains only value 0, the second row  
will contain (in the end) every element in  $A$ , the third  
will contain <sup>every</sup> ~~the~~ sum possible between pairs of elements in  $A$   
and so on.

0	0
1	---
2	---
3	---
$\vdots$	
$n/2$	---

Let's say that  $A$  is  $[1, 2, 3, 4, 5, 6, 7, 8]$ .

$$n = 8$$

$$\text{sum} = 36.$$

⇒ return true

2     3     4     5     6     7     8     (9)

3   6   7   8   9   10   11   12

4      10      11      12      13      14

invest

Print <sup>index</sup> and the element 1 in ~~first~~ second row

insert ~~add~~ the second element in the record column, but in the

third add it with every element found in the ~~prev~~ record <sup>at</sup> row

insert the third element in the second, add it with every element from the second list and insert in the third, then sum it

with every element in the third ~~network~~ and insert in fourth.

(The order is exactly the opposite, so add it with every element in the second to last ~~row~~ row and insert it in the last row, then work all the way up to top row)

We use sets because if the num was already inserted,

that means it can be activated and we don't use anymore.

Every time we add a num, check if that element

is equal with the index of the row \* sum / n AND

if (index \* sum) is divisible by n. if it is, return true.

if no such element was not found, return false.