OR4030

Projects

2021 December

Each group is required to write a report which should include the following parts.

- 1. State the problem;
- 2. Formulate the problem as an optimization model with necessary specification and explanation;
- 3. Explain the methodology and algorithm for solving your model;
- 4. Write a Matlab (or C or Python) code and run the program. Attach a copy of your code and running record;
- 5. Give your solution;
- 6. Make a short discussion or extension if necessary.

Upload your report and source code (one zip file including report and code)via ispace by the Due Date – 23:59 Jan 2nd, 2022 (one for each group).

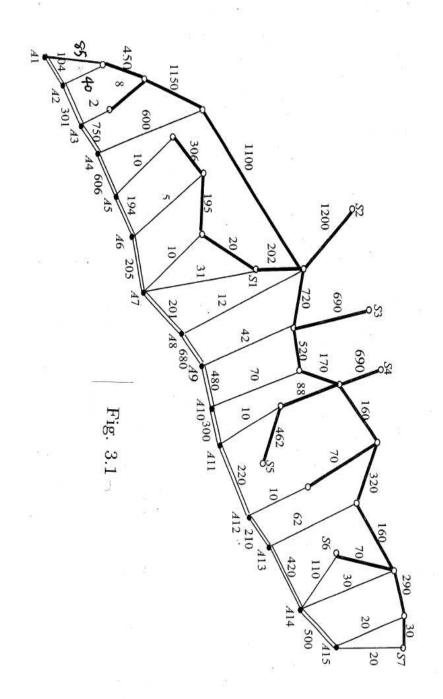
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Project 1

A pipeline is about to be built in order to deliver natural gas. The pipeline should link location points $A_1 \to A_2 \to \ldots \to A_{15}$ as shown by the double lines in Fig. 3.1. Seven steel factories S_1, S_2, \ldots , and S_7 are able to provide the required pipes. The production capacity and selling price of each steel factory S_i are listed in Table 3.1, where K_i is the maximum production capacity (in km of length), and P_i is the price for 1 km (i.e. 1 unit) of pipes (the money unit used is 10,000 Yuan) for the product of factory S_i . It is requested that if pipes are bought from factory i, then at least a total of 500 km of pipes should be purchased from it (regardless of which location the pipes are purchased for).

Table 3.1: Production Capacity and Sell Price

Factory S_i	S1	S2	S3	S4	S5	S6	S7
Capacity K_i	800	800	1000	2000	2000	2000	3000
Price P_i	160	155	155	160	155	150	160



The pipes are shipped from factories S_i (i = 1, 2, ..., 7) via railway or highway to the location points A_j (j = 1, 2, ..., 15), where pipes are unloaded and paved towards either A_{j-1} direction or A_{j+1} direction. In Fig. 3.1, the dark solid lines represent railways and the thin lines represent highways. Their lengths (in km) are shown beside these lines. The highway transportation cost is 0.1 (money unit) per km for per unit of pipes, and the railway transportation cost is 0.065 (money unit) per km for per unit of pipes.

It is assumed that the pipes shipped to location point A_j can only be used to pave the interval between A_{j-1} and A_{j+1} , and the interval must contain A_j , that is, such pipes can be paved towards A_{j-1} , but cannot exceed A_{j-1} , or similarly, towards A_{j+1} , but cannot exceed A_{j+1} , or towards both directions. For such movement of pipes, the transportation cost is 0.1 per km for per unit of pipes, and for a moving distance shorter than 1km, the cost is counted as 1km, i.e., 0.1 per unit. For simplicity, we further assume that during the construction process, no pipes shall be wasted and hence the total amount of pipes required is equal to the length of the entire pipeline $A_1 \rightarrow A_2 \rightarrow \ldots \rightarrow A_{15}$. Also, all required pipes are of the same size.

Consider a pipe purchasing and shipping plan so that the total cost for buying and moving pipes (from factories to location points, and between location points) can be minimized.