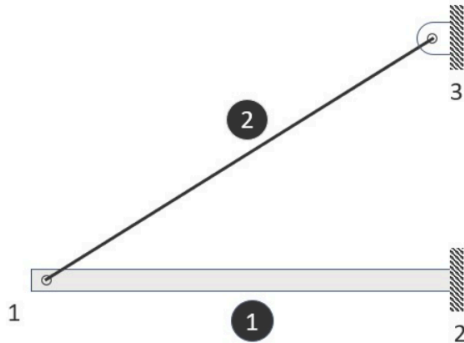


In the mesh shown below, element 1 is a beam element about which we will learn later. It has 3 dofs per node and two nodes. The three dofs are two translations and one rotation. On the other hand, element 2 is a truss element with two dofs per node (two translations) and two nodes. The stiffness matrices in the global coordinate system are given as  $K_1, K_2$ . The element connectivities are

element 1 1,2

element 2 1,3

Assemble the global stiffness  $K_{global}$ . Form the destination arrays  $dest1, dest2$ .



```
% problem 2b: assembly, nodes with different dofs from different
elements
nelem=2;
nnode=3;
Kglobal=zeros(8 ,8);
%for element 1
K1=250000*[10 0 0 -10 0 0;0 0.835 5 0 -0.0835 5;0 5 400 0 -5 200;...
    -10 0 0 10 0 0;0 -0.0835 -5 0 0.0835 -5;0 5 200 0 -5 400];
dest1=[1 2 3 4 5 6];
%for element 1
k=3.15e04;
theta=pi/4;
c=cos(theta);s=sin(theta);
K2=k*[c*c c*s -c*c -c*s;c*s s*s -c*s -s*s;c*s s*s c*c c*s;-c*s -s*s c*s
s*s];
dest2=[1 2 7 8];
for ii=1:nelem
    if ii == 1
        Klocal=K1;
        dest=dest1;
    end
    if ii == 2
        Klocal=K2;
```

```

        dest=dest2;
    end
    %Assemble Kglobal here
    c=dest;
    l=Klocal;
    Kglobal(c,c)=Kglobal(c,c)+l ;
end

function Ke = axisymmetric_quad4_stiffness(R_nodes, z_nodes, E, nu)
% R_nodes, z_nodes: 4x1 vectors [node1..node4]
% DOF order per node: [u (radial), w (axial)]
% returns Ke (8x8)

% material D (4x4) as given
coef = E / ((1+nu)*(1-2*nu));
D = coef * [1-nu, nu,    nu,    0;
            nu,    1-nu, nu,    0;
            nu,    nu,    1-nu, 0;
            0,     0,     0,     (1-2*nu)/2];

% initialize
Ke = zeros(8,8);
gp = 1/sqrt(3);
rGP = [-gp, gp];
sGP = [-gp, gp];
w = [1, 1];

for i = 1:2
    for j = 1:2
        r = rGP(i); s = sGP(j);
        weight = w(i)*w(j);

        % shape functions and their parametric derivatives (dr, ds)
        N = 0.25 * [(1-r)*(1-s);
                    (1+r)*(1-s);
                    (1+r)*(1+s);
                    (1-r)*(1+s)];
        dNdr = 0.25 * [ -(1-s);
                       (1-s);
                       (1+s);
                       -(1+s)];
    end
end

```

```

            (1+s);
            -(1+s) ];
dNds = 0.25 * [ -(1-r);
                -(1+r);
                (1+r);
                (1-r) ];

% Jacobian J = [dR/dr dR/ds; dz/dr dz/ds]
dRdr = dNdr' * R_nodes;
dRds = dNds' * R_nodes;
dzdr = dNdr' * z_nodes;
dzds = dNds' * z_nodes;
J = [dRdr, dRds; dzdr, dzds];
detJ = det(J);
invJ = inv(J);

% physical derivatives dNi/dR and dNi/dz
dN = invJ * [dNdr'; dNds']; % 2 x 4 matrix
dN_dR = dN(1,:)' ; % 4x1
dN_dz = dN(2,:)' ; % 4x1

% radial coordinate at gauss point
Rgp = N' * R_nodes; % scalar

% assemble B (4x8)
B = zeros(4,8);
for a = 1:4
    col_u = 2*(a-1) + 1; % radial DOF index
    col_w = col_u + 1; % axial DOF index
    B(1, col_u) = dN_dR(a);
    B(2, col_w) = dN_dz(a);
    B(3, col_u) = dN_dz(a);
    B(3, col_w) = dN_dR(a);
    B(4, col_u) = N(a) / Rgp;
end

% integrand: B' * D * B * (2*pi*Rgp) * detJ * weight
Ke = Ke + (B' * D * B) * (2*pi * Rgp) * detJ * weight;
end
end

end

```

