



# MULTI-STATE CHURN ANALYSIS

WITH A SUBSCRIPTION PRODUCT

GRADIENT

DEVELOPING INTELLIGENCE POWERED BY DATA

# ***WHO IS THIS GUY?***

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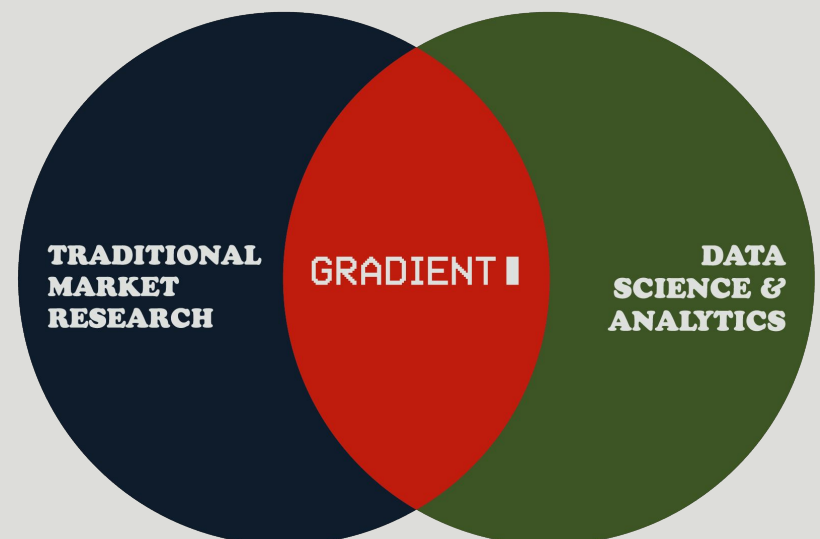
***Nice to  
meet you!***



## WE'RE GRADIENT:

A crew of quantitative marketers and technologists that gather hard data and build robust statistical models to guide organizations through their most difficult decisions.

We're confirmed data geeks, but word on the street is that we're easy to work with and pretty fun, too.





# ***SURVIVAL ANALYSIS***

## ***DEFINITION & EXAMPLES***

### ***LET'S START TALKING***

A branch of statistics for analyzing the **expected duration of time until** one or more **events** happen.

#### Examples

1. A death of the patient.
2. A deactivation of the service.
3. An accident on the road.
4. The device failure.
5. An employee leaving the company.
6. A customer cancelling subscription.



# ***SURVIVAL ANALYSIS***

## ***QUESTIONS IT (MIGHT) ANSWER***

### ***LET'S START ASKING***

What's the probability an event will (not) occur after a specific period of time?

Which characteristics indicate a reduced or increased risk of occurrence of an event?

What periods of time are most (or least) exposed to the risk of an event?



# ***SURVIVAL ANALYSIS***

## ***CHALLENGES IT FACES***

### ***DEPENDENDING ON THE SCENARIO***

#### Data

1. Censoring.
2. Interval data.
3. Observations may not be independent.
4. Time varying features.

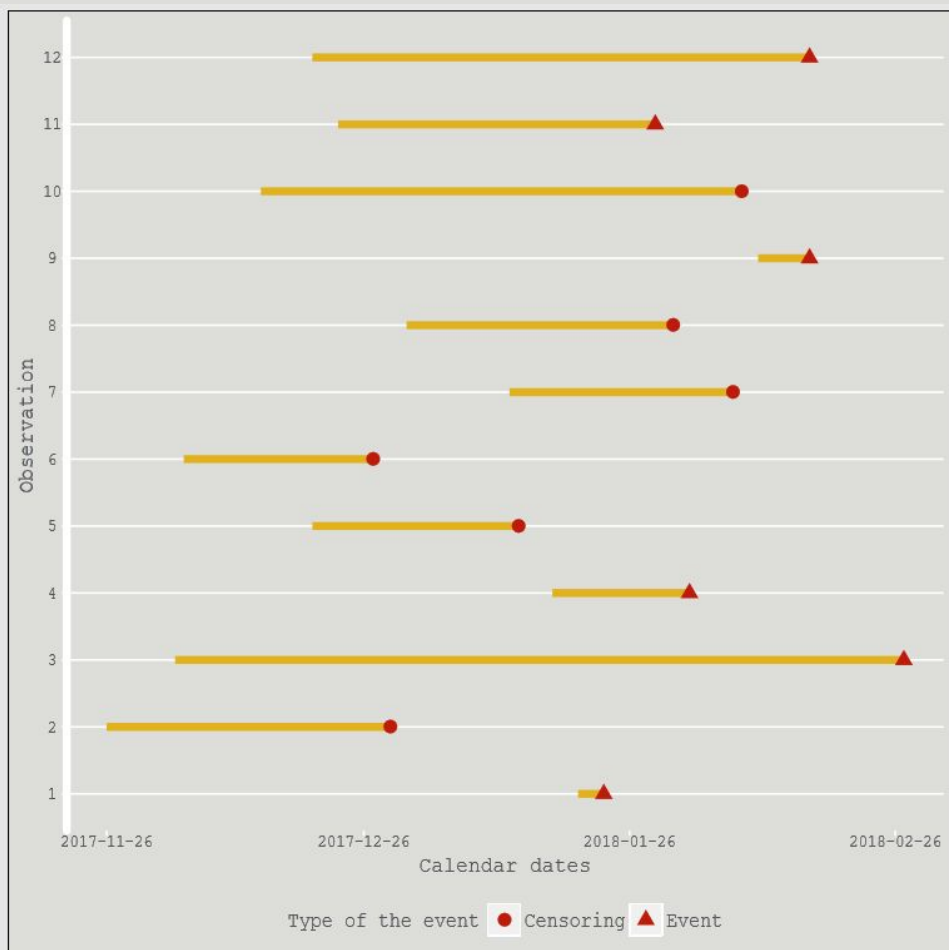
#### Events

1. Recurring events - one event might occur multiple times.
2. Competing risks - one of multiple events might occur.
3. A multi-state (cyclic/acyclic) nature of the process.



# ***DATA STRUCTURE***

## ***SIMPLE CASE***



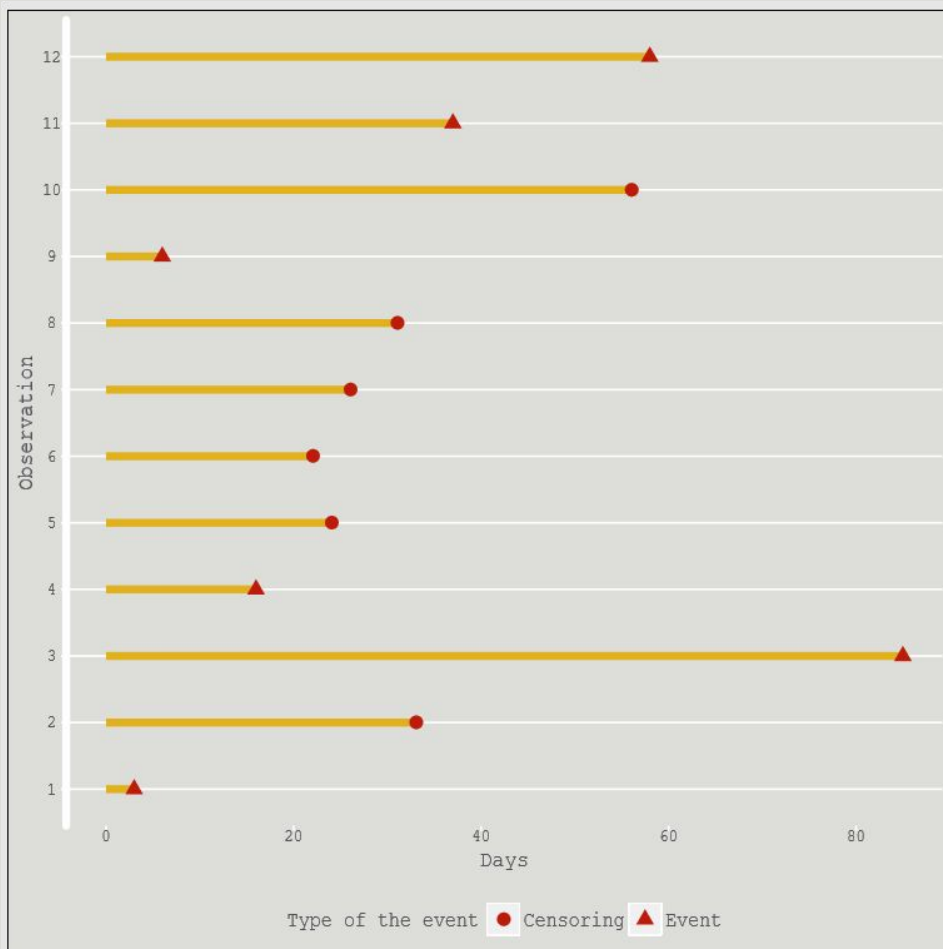
### HEAD OF THE DATA

ID	Start Date	End Date	Status
1	2018-01-28	2018-02-22	Censoring
2	2017-12-16	2018-01-08	Event
3	2017-12-09	2018-01-06	Censoring
4	2018-01-16	2018-02-23	Censoring
5	2017-12-16	2018-02-11	Event
6	2018-02-18	2018-03-01	Event

Data **do not** correspond to the plot.

# ***DATA STRUCTURE***

## ***SIMPLE CASE***



### HEAD OF THE DATA

ID	Time	Status
1	3 days	Event
2	33 days	Censoring
3	85 days	Event
4	16 days	Event
5	24 days	Censoring
6	22 days	Censoring

Data **do** correspond to the plot.



# KAPLAN-MEIER ESTIMATES

$$\hat{S}(t) = \prod_{t_i < t} \frac{n_i - d_i}{n_i}$$

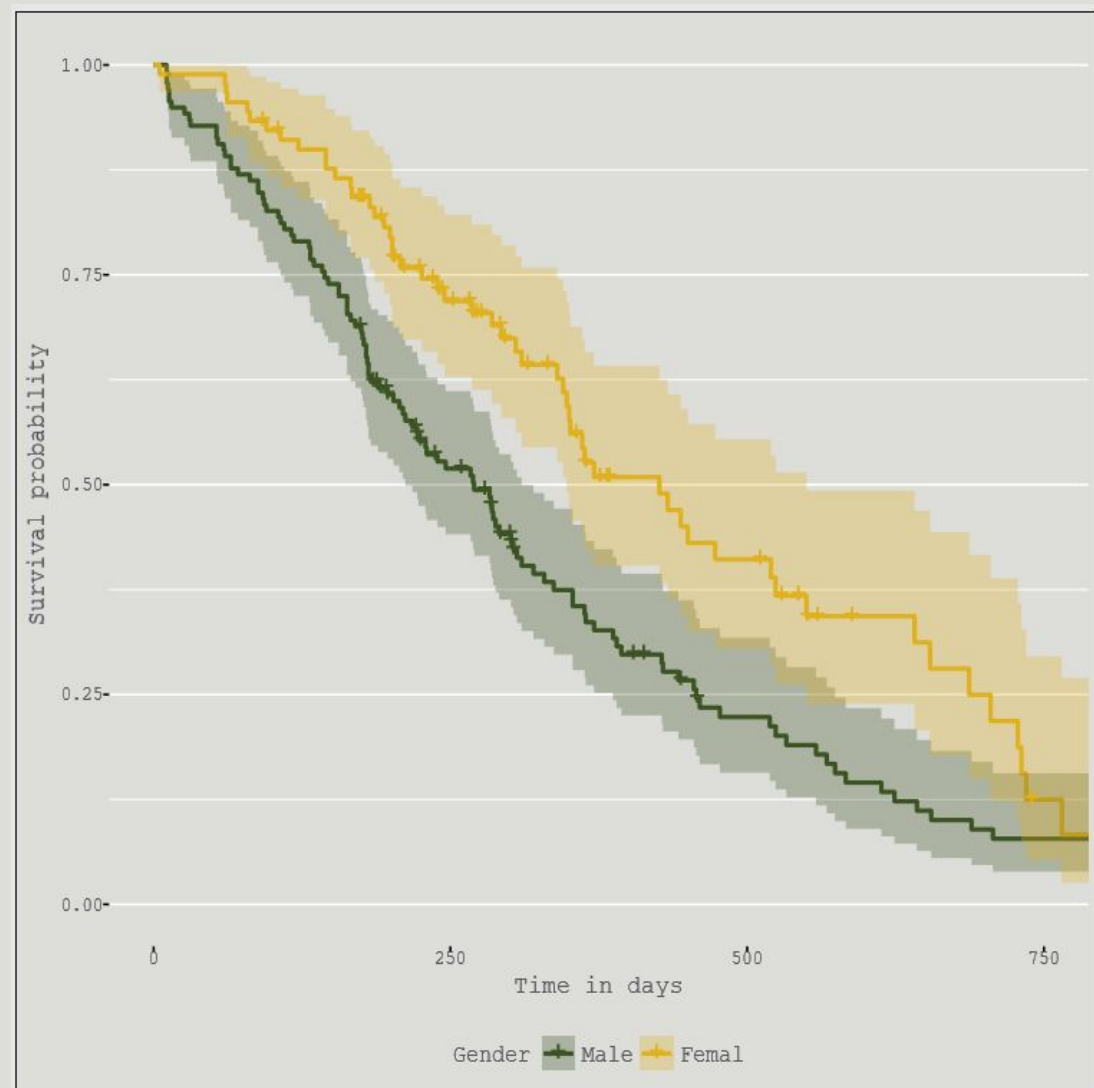
where

$t_i$  - time of i-th event

$n_i$  - number of observations  
in a risk set at time  $t_i$

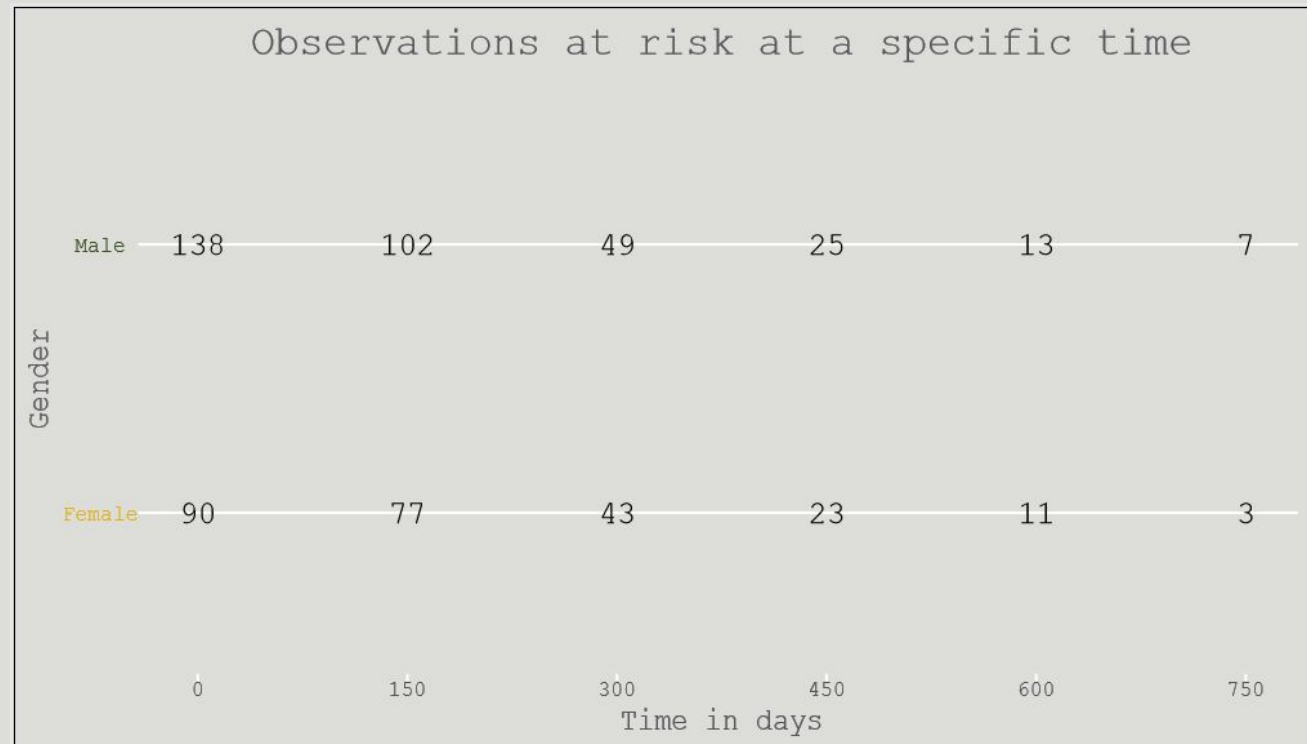
$d_i$  - number of events at  $t_i$

**Log-rank** test seeks for statistically significant differences between curves.

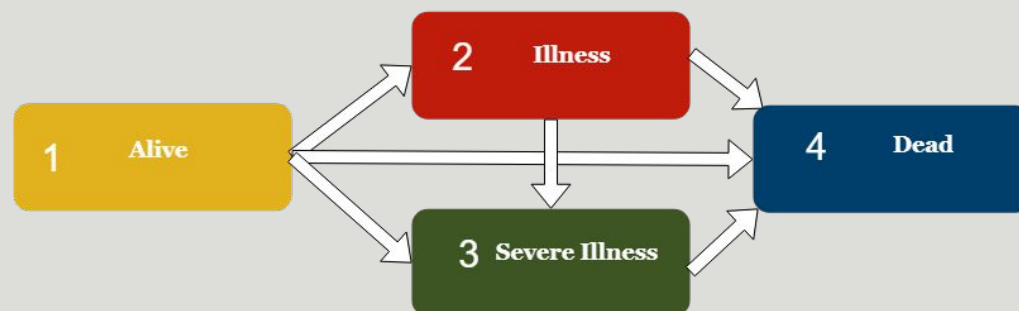
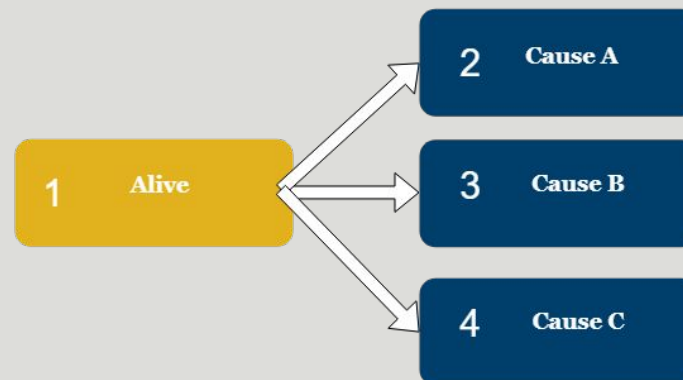
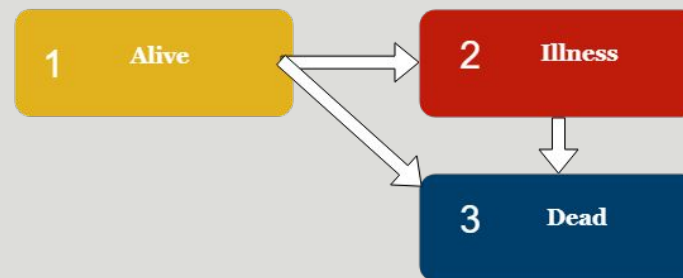
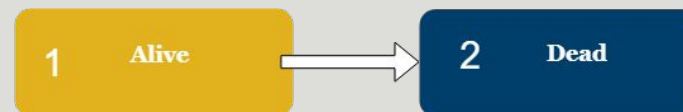
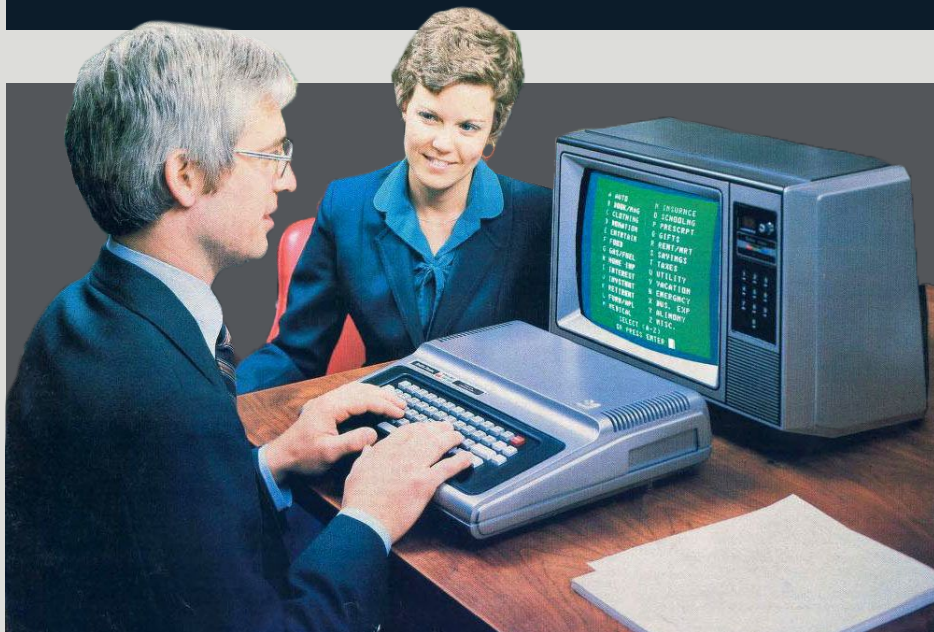


## ***SURVIVORS AT A TIME***

Useful when considering whether results at a specific time point are significant due to the sample size.

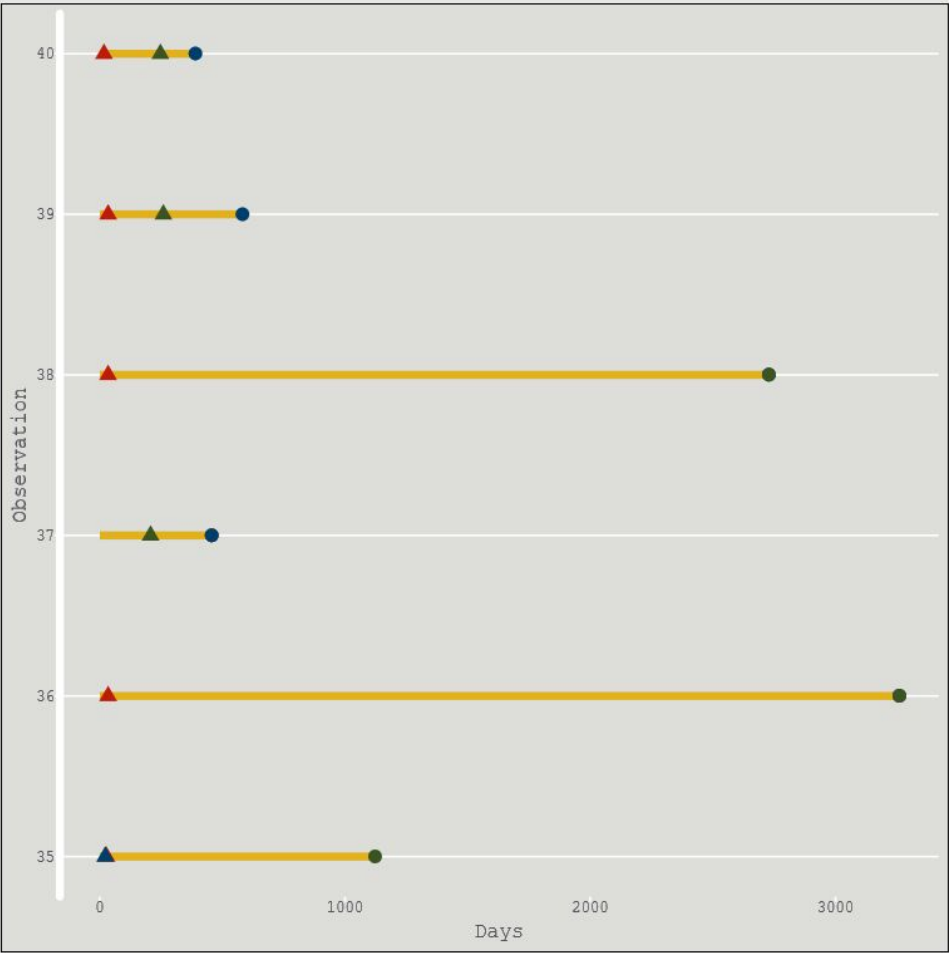


# MULTI-STATE MODELS



# DATA STRUCTURE

## MULTI-STATE CASE



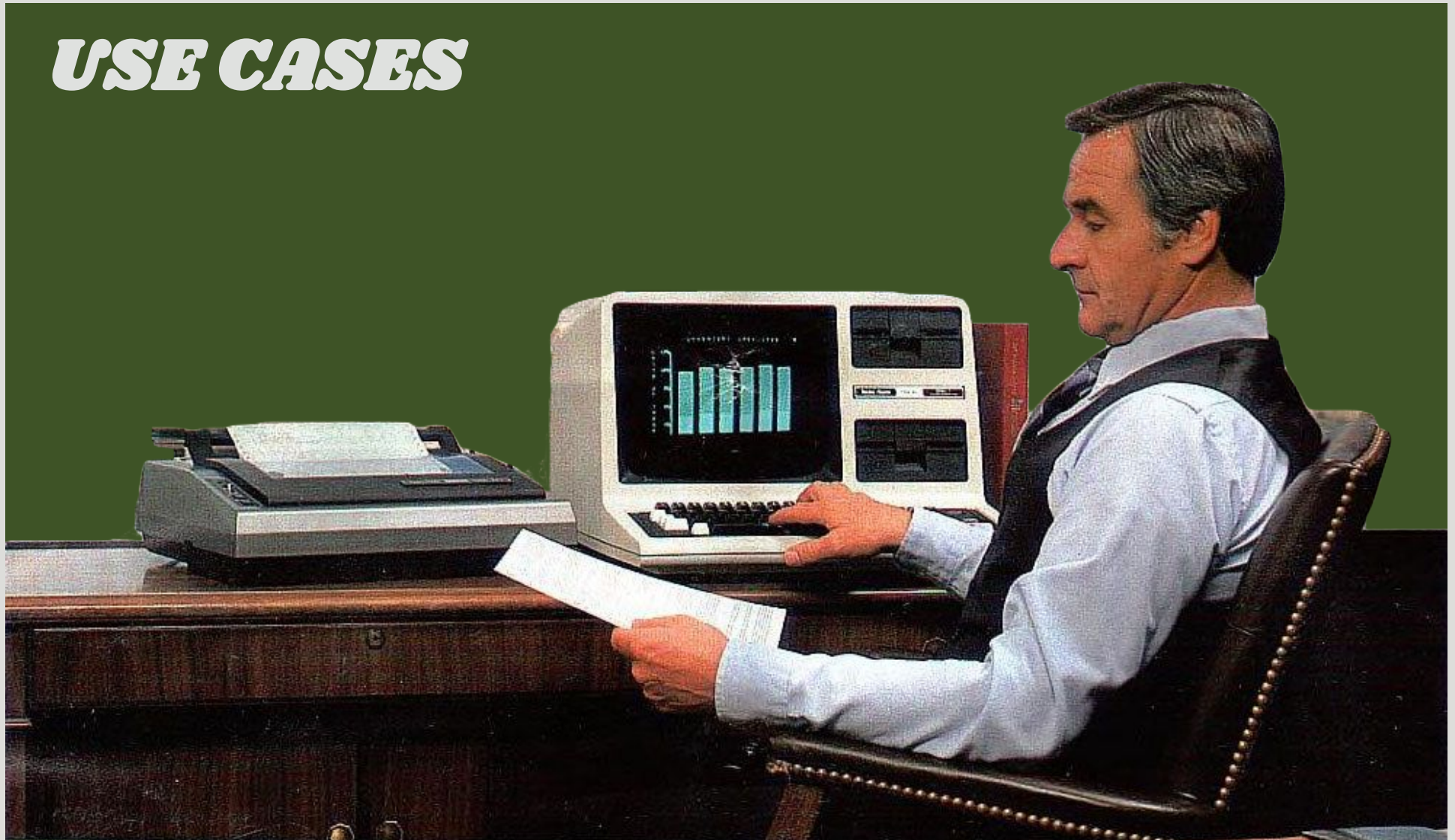
### HEAD OF THE DATA

ID	Time 1	Event 1	Time 2	Event 2	Time 3	Event 3
1	22	1	995	0	995	0
2	29	1	12	1	422	1
3	1264	0	27	1	1264	0
4	50	1	42	1	84	1
5	22	1	1133	0	114	1
6	33	1	27	1	1427	0

Demonstrational data.



# ***USE CASES***



# 1 EVENT / COX PROPORTIONAL HAZARDS

## COX METHODOLOGY OVERVIEW

1. Proportional hazards assumptions.
2. Functional form of continuous variables.
3. Independent observations.
4. Independent censoring from the mechanism that rules of event's times.
5. Non informative censoring  
- does not give an information on parameters of the time distribution of events because it does not depend on them

```
coxph(Surv(futime, fustat) ~ age + ecog.ps + rx, data=ovarian)
```

## NOTE

One can use accelerated failure time (AFT) models.

## EXAMPLE COEFFICIENTS

variable	coef	exp(coef)
age	0.15	1.16
ecog.ps	0.10	1.11
rx	-0.81	0.44

## DIAGNOSTIC PLOTS

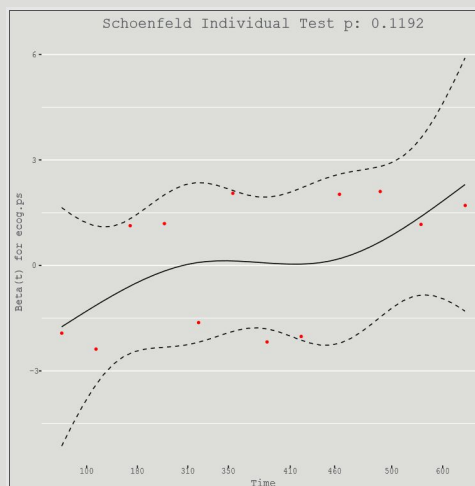
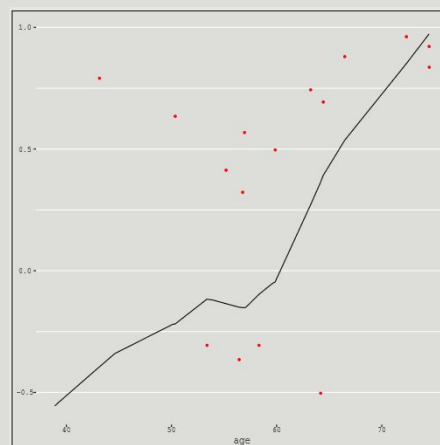


Fig. 1: Shoenfeld residuals.



## OVARIAN DATA

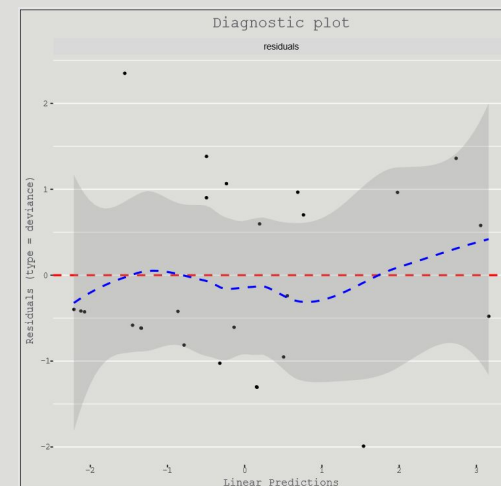


Fig. 2: Deviance residuals.

## FUNCTIONS (survminer)

1. `ggcoxzph`
2. `ggcoxdiagnostics`
3. `ggcoxfunctional`

Fig. 3: Martingale residuals.

# NEVENTS (ACYCLIC) MULTI-STATE MODEL

TRANSITION MATRIX

to

from	1	2	3	4	5
1	NA	1	2	NA	3
2	NA	NA	NA	4	5
3	NA	NA	NA	6	7
4	NA	NA	NA	NA	8
5	NA	NA	NA	NA	NA

NA = transition not possible

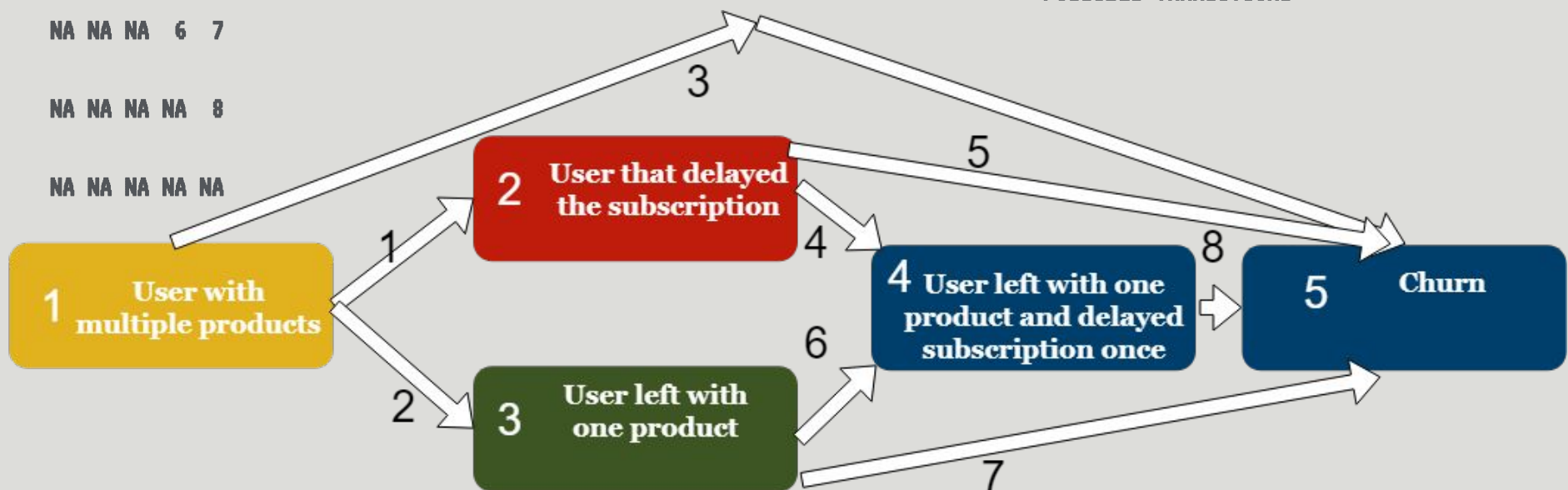
numbers in cells

=

names of transitions

The most complicated part is the proper data coding for the model's input.

POSSIBLE TRANSITIONS



# ***NEVENTS (ACYCLIC) MULTI-STATE MODEL***

## SOME COEFFICIENTS

transition	age=>40	age=20-40	discount=yes	gender=female	year=2008-2012	year=2013-2017
1	-1.15	-0.77	-0.26	-0.72	0.80	0.94
2	-1.34	-0.72	-0.15	-0.58	0.39	0.31
3	-0.43	-0.04	0.08	-0.53	0.02	-0.11
4	-0.86	-0.66	-0.09	-0.22	0.13	0.23
5	0.14	-0.64	0.14	-0.24	-0.54	-0.63
6	-1.65	-1.23	0.24	-0.35	0.88	1.33
7	-0.82	-0.57	0.39	-0.57	-0.35	0.09

Reference level for

- age - below 20
- year - 2002-2007



# NEVENTS (ACYCLIC) MULTI-STATE MODEL

## PREDICTIONS OF THE STATE

Depending on the customer features, the predictions of being in a state after particular time are different.

Credits for modeling:

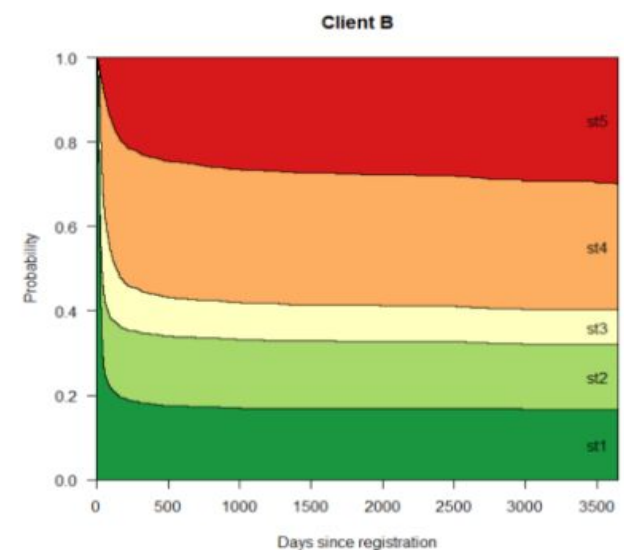
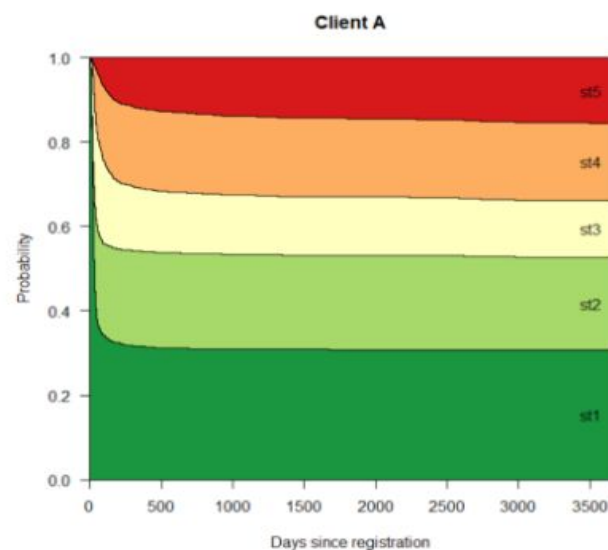
[cran.r-project.org/package=mstate](https://cran.r-project.org/package=mstate)

### Customer A

- Discount: Yes
- Gender: Female
- Joined: 2013-2017
- Age: Younger than 20

### Customer B

- Discount: No
- Gender: Male
- Joined: 2002-2007
- Age: 20-40



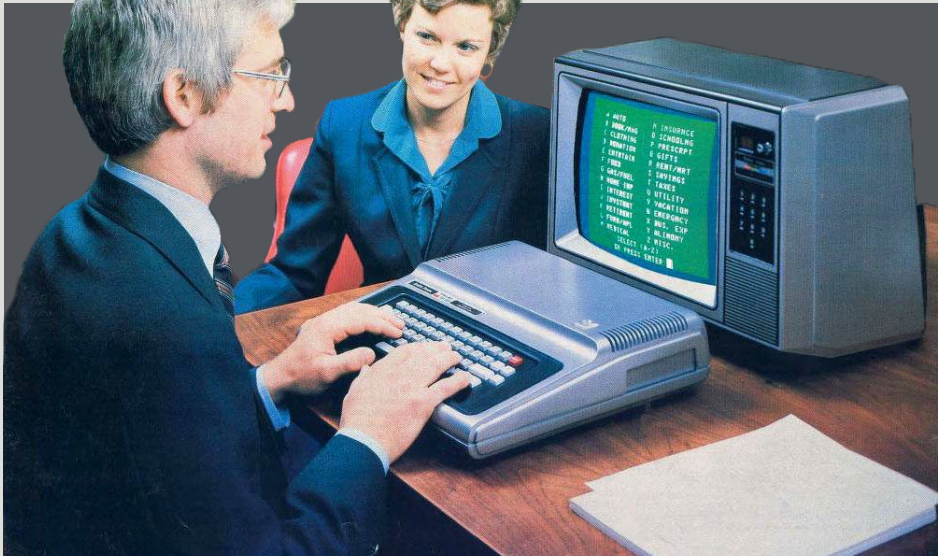
# NOTES



Model assumptions should be considered for every possible transition.

Time varying variables can be taken into the account when handling subscription based data.

Playing with cyclic models requires domain knowledge in (sub) Markov Chain field. ■



cran.r-project.org/package=survminer

[www.ggplot2-exts.org/gallery/](http://www.ggplot2-exts.org/gallery/)

[stdha.com/english/rpks/survminer](http://stdha.com/english/rpks/survminer)



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Presentation and codes

[github.com/g6t/mchurn](https://github.com/g6t/mchurn) ■

THANK YOU FOR THE ATTENTION