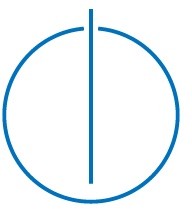
# Technische Universit¨at Mu¨nchen

**Fakult¨at fu¨r Informatik**

## Master’s Thesis in Informatik

An Email-Centered Approach to Intelligent Task Management Using Crowdsourcing and Natural Language Processing

John Doe



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## Master’s Thesis in Informatik

An Email-Centered Approach to Intelligent Task Management Using Crowdsourcing and Natural Language Processing

Ein Email-basierter Ansatz fu¨r intelligente Aufgabenverwaltung mit Hilfe von Crowdsourcing und Natural Language Processing

**Author:** John Doe

**Supervisor:** Prof. Dr. Johann Schlichter **Advisor:** Dr. Wolfgang W¨orndl **Submission:** DD.MM.YYYY

I assure the single handed composition of this master’s thesis only supported by declared resources.

Mu¨nchen, DD.MM.YYYY

*(John Doe)*

## Abstract

English abstract.

## Inhaltsangabe

Deutsches Abstract.

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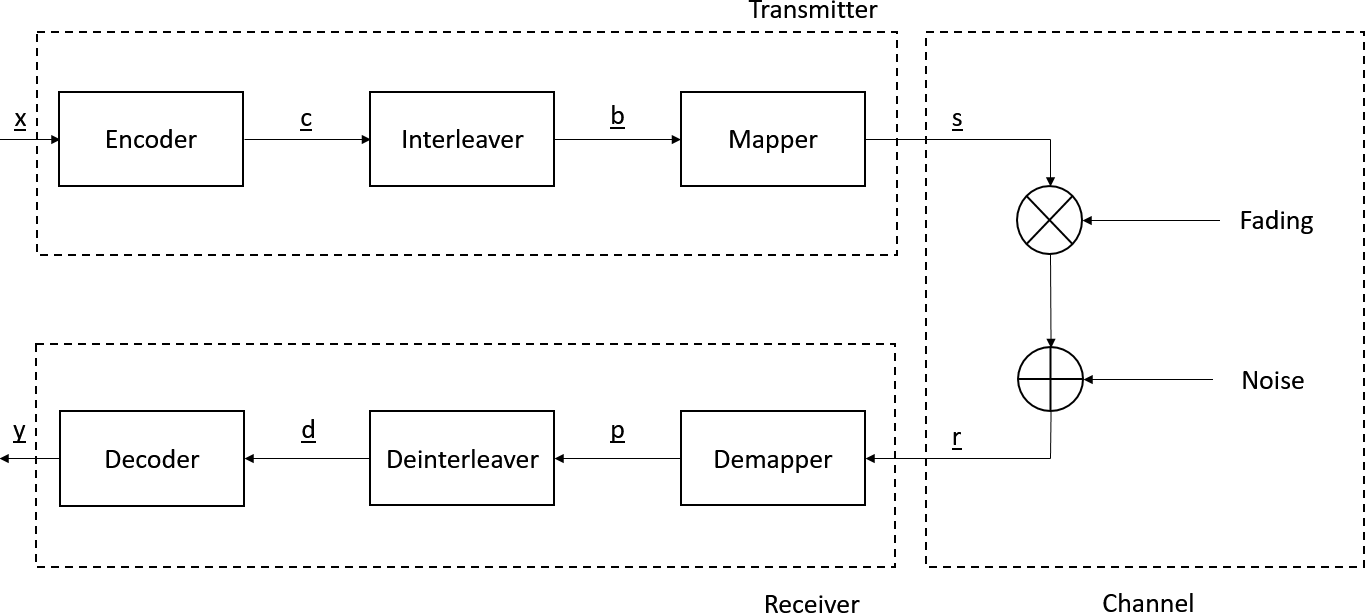
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# Chapter 1 Introduction

## 1.1Motivation 1.2Contributions

6

# Chapter 2 Channel model



**Figure 2.1:** Channel model for general Transmitter/Receiver Chain

First a short introduction of the system for all simulations will be given (Fig. [2.1).](#_bookmark6) A few crucial parts of channel blocks are needed for every communication link and a few blocks are added for improvement in performance. All the blocks were chosen in direct benefit to a LDPC transmission of codewords to make the simulations as simple and efficient as possible. The link is built up of three main blocks: The transmitter, the channel and the receiver. With the transmitter handling the creation of the random code words, coding with [low density parity check (LDPC)](#_bookmark0) and mapping in different modulation schemes. The channel will simulate any incoming and existing noise, e.g., [additive white gaussian noise](#_bookmark0) [(AWGN).](#_bookmark0) In the end the receiver will demap and decode our transmitted symbols and

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compare the decoded bitstream with the initially created codeword.

The single channel blocks will be explained shortly in the following sections.

## Encoder/Decoder

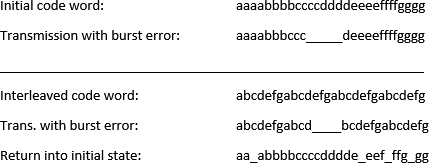
There are many ways to make our transmission more stable and less error prone. A major role in this protection plays the encoder and its counterpart the decoder. Encoder/decoder come in many different forms taking form in hardware coder and also as software coder. They reach from simple linear block codes to more complex convolutional coding and so called turbo codes. It is also important to note, that codes working well in a AWGN-channel will often not have the same performance in a fading channel. A further look will be taken into [LDPC](#_bookmark0) codes and the based on these, the WiMax code according to the standard IEEE 802.16e. **citation**. While [LDPC](#_bookmark0) was mainly ignored in the past, in the 1990’s the introduction of turbo codes and an sharp increase in computing power helped the recognition of these forms of decoding.

[LDPC-co](#_bookmark0)des are linear block codes with a particular structure for their parity check matrix **[H]**. In the case of [LDPC-co](#_bookmark0)des **H** has a small amount of nonzero entries, which means that there is a low density in the parity check matrix. Another important difference in LDPC to turbo codes is the complexity of encoding and decoding. While turbo codes have low complexity in encoding they have high complexity in decoding. The total opposite can be said about [LDPC](#_bookmark0) with high complexity in encoding and low complexity in decoding. Another advantage of [LDPC](#_bookmark0) is the ability of self correction after decoding with the help of the decoding algorithm and the parity check matrix.

WiMax IEEE 802.16e is a standard code model used in small and medium distances in urban areas, which fits the simulations quite well. With WiMax there are different given blocksizes ranging from 576 codewords up to 2304 codewords. The code rates are also set, which are the following: 1/2, 2/3, 3/4, and 5/6. While there are also two different classes of encoding (A/B), only encoding class A will be used in this setup.

## Bit interleave/Deinterleaver

While the above mentioned coder [LDPC](#_bookmark0) (Chapter [2.1)](#_bookmark7) works really well for an AWGN channel this is not always the case in a fading channel. This is where the next important channel block comes into play. To guarantee a stable performance the method of interleaving will be introduced. Interleaving will handle a major problem in fading channels, the appearance of burst errors mainly caused by deep fading over a set time. While [LDPC](#_bookmark0) has the ability to correct single code errors it is usually not able to correct a stream of errors. With the interleaver the codeword will be shuffled into a new random gaussian distributed code word, which will be passed through our channel. At the receiver a restoration of the shuffled codeword back into its intial state will take place.

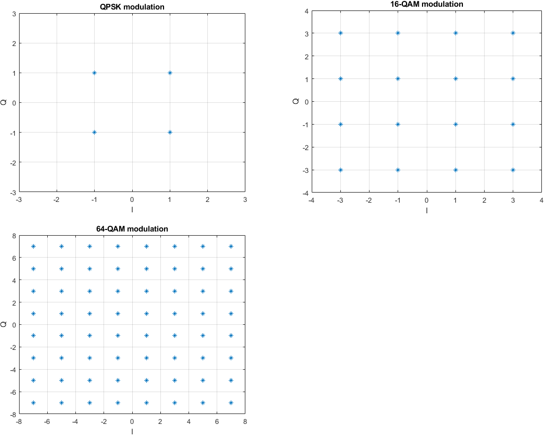


**Figure 2.2:** Example for interleaving

As clearly seen in figure [2.2](#_bookmark9) the interleaver will not remove any errors but will prevent or at least mitigate the presence of burst errors. Single errors can be corrected by the LDPC algorithm again. There are two main methods of interleaving today: [symbol-interleaved coded modulation (SICM)](#_bookmark0) will interleave our symbols after the modulator while [bit-interleaved coded modulation (BICM)](#_bookmark0) will interlave the single bits before the modulator, with [BICM](#_bookmark0) being the more dominant one of these two methods. BICM will also be used for this thesis for its more dominant position in pratical communcation systems. **cite**

## Mapper/Demapper

In the mapper, also called modulator, it is possible to compress the codeword into a set sequence of symbols. Group of bits are taken from the bit stream to combine them to specific constellation points. The symbols are located in a real/imaginary plane, also called Inphase/Quadrature Planes (I/Q-Planes). With the distance from the nullpoint of the axis giving the magnitude of the signal and the angle to the real axis the phase shift. There are many forms of modulation schemes, with the most common ones being M-phase shift keying (PSK), M-frequency shift keying (FSK), M-amplitude modulation (AM) and [M-quadrature amplitude modulation (QAM).](#_bookmark0) For the simulation a further look will be taken at [quadrature phase shift keying (QPSK),](#_bookmark0) 16-[QAM](#_bookmark0) and [64-QAM,](#_bookmark0) which are depicted below (Fig. [3.1).](#_bookmark25) All three modulations share the common fact of being differential, which means that the symbols are located in both the real and imaginary plane. One important aspect of differential modulation is the requirement of coherent demodulation, which means that the transmitter and receiver must have matched phase *φ*. In the simulation it will be assumed that perfect phase match is guaranteed between those two. If not, a phase recovery has to be done.



**Figure 2.3:** Modulation in I/Q planes for QPSK, 16-QAM and 64-QAM

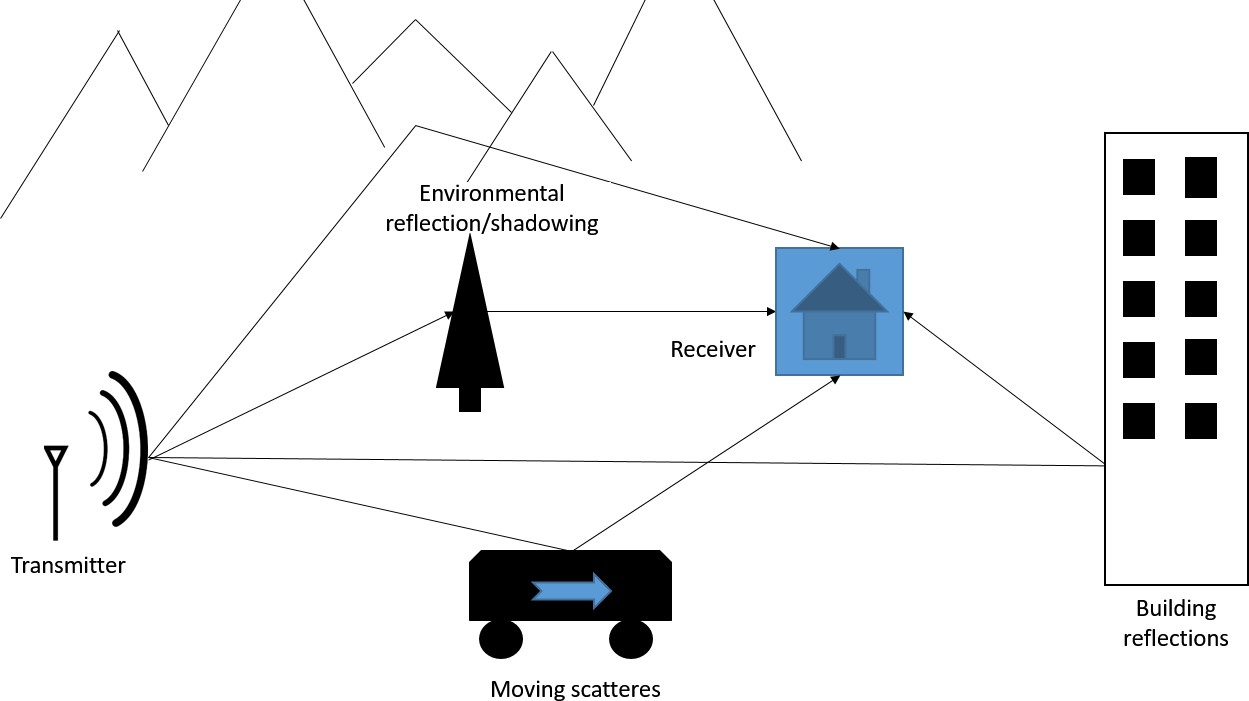
With [QPSK](#_bookmark0) the symbols all share the same amplitude and only differ in their respective phase angle. With the information entropy *S* = *log*2(*M* )**cite** the maximum number of bits can be identified which are assigned in every symbol, with M being the number of symbols in the modulation scheme. So for [QPSK](#_bookmark0) the number of bits per symbol amounts to 2.

With [M-QAM](#_bookmark0) the phase shift already implemented in [QPSK](#_bookmark0) will be used and also a differentiation by magnitude of the signal will be added. So for [QAM,](#_bookmark0) signals which differ in their phase shift and also their amplitude, will be send. For [16-QAM](#_bookmark0) a maximum of 4 bits per symbols and for [64-QAM](#_bookmark0) 6 bits per symbol can be achievied.

The modulation schemes make it possible to increase the rate/speed of transmission and are used for any kind of practical communication link. In a practical case modulation will protect the signal from outside noise and interferences, e.g., other mobile handheld devices, GPS-signals or wifi signals. It can also increase the range of communication by transmitting over higher carrier frequencies.

## Channel

The channel can be modified in many different ways. Different sources of noise or fading can be applied, which relate to real world interferences. Some interferences experienced in real life transmission are, e.g., thermal noise, distance fading, doppler effect and reflection of signals. To approach those kind of interferences there are many different channel models in simulations, like an [AW](#_bookmark0)GN-Channel or Rayleigh/Rician fading. A further look into the [AW](#_bookmark0)GN-Channel and the Rayleigh fading will be given. A small graphic will further illustrate the usual culprits for degradation of signal power and resulting loss in communication performance (Fig. [2.4](#_bookmark13)).



**Figure 2.4:** Interferences in a normal transmission between two devices

**Ausfu¨hren, beispiele, bilder**

### AWGN-Channel

**Lookup math**

The easiest kind of channel manipulation is to add random gaussian noise to the channel, also commonly known as an [AW](#_bookmark0)GN-Channel. Like the name says we will add noise, which is a random gaussian distribution with flat spectral density, to an existing transmitted signal. Our channel will receive a signal like this:

*Y* = *X* + *N,* (2.1)

with Y being the received signal, X the send codeword and N the AWGN noise. The probability density function is defined as follows:

*f* (*x*|*µ, σ*

2

1

) = ~~√~~2*πσ*2 ∗ *e*

(*x−µ*)2

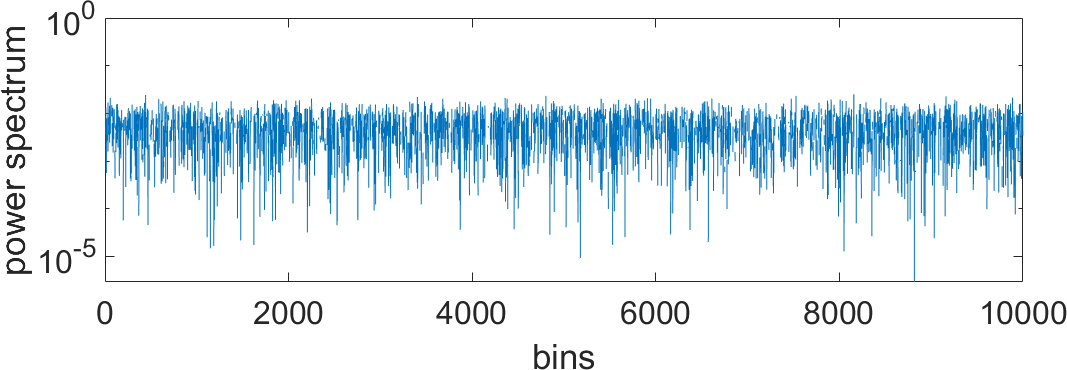
2*µ ,* (2.2)

*−*

with x being the acquired point, *µ* being the mean or expectation of the distribution and

*σ*2 the variance of the distribution.

More or less every communication link will have some kind of gaussian noise interference, so the AWGN-channel will be added to every simulation run. Below (Fig. [2.5)](#_bookmark15) a depiction of the spectral power distribution of AWGN. It can be clearly seen that it is flat and spread evenly over the whole spectrum.



**Figure 2.5:** Power spectral density for a AWGN channel

**Add picture of AWGN, pdf or distribution**

### Rayleigh-Channel

**Lookup math**

Another common channel model used in communication theory is Rayleigh fading. Rayleigh fading is used to simulate multipath reception, which means that for a receiver antenna in a wireless link there are many reflected and scattered signals reaching it (Fig. [2.4).](#_bookmark13) These kind of reflections are common for high density urban areas. This results into construction or destruction of waves. Rayleigh distribution can be defined like this:

*H* = √*X*2 + *Y* 2*,* (2.3)

with X and Y being two independent gaussian distributed random variables. This leads our channel to look like this:

*Y* = *H* ∗ *X* + *N,* (2.4)

with the newly added fading coefficient H. Further calculations will lead to the following pdf:

*f* (*xσ*) =

2

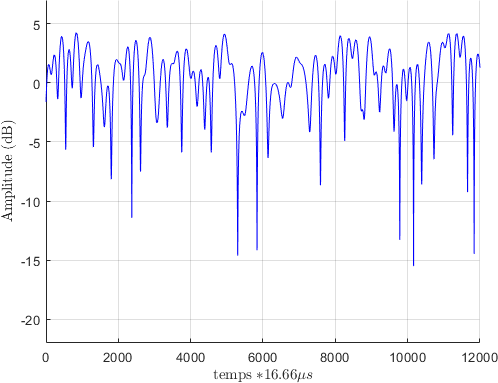
*e−*2*σ*2 *,* (2.5)

*x*

1

*σ*2

this time only with sigma being the variance of the pdf. The graphic (Fig. [2.6)](#_bookmark17) shows the power distribution over 12000 samples. Being gaussian randomly distributed there are now these so called ”deep fadings” where the power of the fading drops, which will also decrease the signal power of the received signal drop significantly. This results in the so called burst errors, which was mentioned in chapter [2.2.](#_bookmark8)



**Figure 2.6:** Power spectral density for a rayleigh channel

**Add pictures, spreading, reflection...**

**Chapter 3**

**Capacity in an AWGN channel**

We will now look into the maximum capacity we can achieve for our communication model in Chapter 2 with added AWGN noise.

## Capacity and Monte-Carlo-Simulation

In general capacity *C* can be defined as the rate *R* at which information can be reliably transmitted over a channel, which means as long *R* ≤ C we can achieve a transmission without errors even with noise. All the capacities we will be looking at will be for complex channel models.

For a [AW](#_bookmark0)GN-Channel we will have a simple channel model defined by Y = X + N with X

∼ *N* (0,*σ*T2) and N ∼ *N* (0,1). With this our received signal Y will have a distribution of Y ∼ *N* (0,*sigma*2+1) under the condition that X and N being independently distributed. We will calculate the capacity as the maximum of mutual information I between X and Y:

*C* = *max*(*I*(*X*; *Y* )) (3.1)

with X and Y being to independent randomly normal distributed variables. With the maximum mutual information we calculate the maximum information we can achieve with the given parameters, like modulation, encoding, channel.

For the mutual information we can further part it into the differential entropy:

*I*(*X*; *Y* ) = *h*(*Y* ) − *h*(*Y* |*X*) (3.2)

With differential entropy being defined as:

*h*(*Y* ) = ∫ *p*(*y*) ∗ [−*log*(*p*(*y*)]d*x* (3.3)

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We will now apply the simulation of monte carlo to turn our integral into an addition. The Monte-Carlo-Simulation will be further explained in the following chapters.

*h*(*Y* ) = *h*(*X* + *N* ) = *log*(*π* ∗ *eσ*2+1) and *h*(*Y* |*X*) = *h*(*N* ) = *log*(*π* ∗ *e*1) (3.4)

Further calculations will lead us to the final equation for the capacity in an AWGN-channel:

*C* = *log*(1 +

*σ*2

) (3.5)

*N*

With this approach we have good approximation values for further calculations with added modulation schemes. It is given that for only AWGN the capacity is at his maximum, there should be no capacity value over the calculated ones here.

### Approach in Matlab

The above mentioned formula 2.4 will be simply implemented in MATLAB. With our noise being randomly distributed around 1 our formula simplifies even more into:

*C*AWGN = *log*(1 + *SN R*) (3.6)

The SNR here must be transformed into power and not in decibel.

### Monte-Carlo-Simulation

Monte Carlo Simulation is widely used in stochastic to get solutions for random experiments. It is used to solve analytical unsolvable problems numerically. MC is based upon the law of large numbers, which says that a large number of performing the same experiment will lead the average of the results close to the expected value. We take this as our bases to get reliable results. The Monte Carlo simulations will be used for two calculations, once already used above for calculating the differential entropy and later once to calculate our theoetical Rayleigh fading curve out of AWGN.

## Capacity for QPSK and M-QAM

Now we will look into different modulation schemes, which were already mentioned in Chapter [section 2.3.](#_bookmark10) We will implement these modulation schemes into our capacity calculations in an AWGN channel.

### QPSK

For QPSK we will have 4 symbols and resulting 2 bits per symbol. Before any simulation or calculation were run we can already be sure that we will not pass the upper bound of 2 bits/Symbol. So the plot will approach the 2 bits/Symbol for high SNR. After creating a random codeword modulated with the fitting modulation scheme. Noise is added to the signal, which is than received as the bit array Y. The next step to calculate the capacity differs from above. While

We know that our signal is normal random distributed variables and we have to calculate the differential entropy for h(Y), which is:

*N*

Σ

*h*(*Y* ) = (−*log*(*p*(*y*n

*n*=0

1

))) ∗ *N*

(3.7)

with p(y) being the probability of y for a normal distributed variable and N the codelength.

*p*(*y*) = 1 ∗ Σ(*ey−x*i ) (3.8)

*i*=1

*i*=1

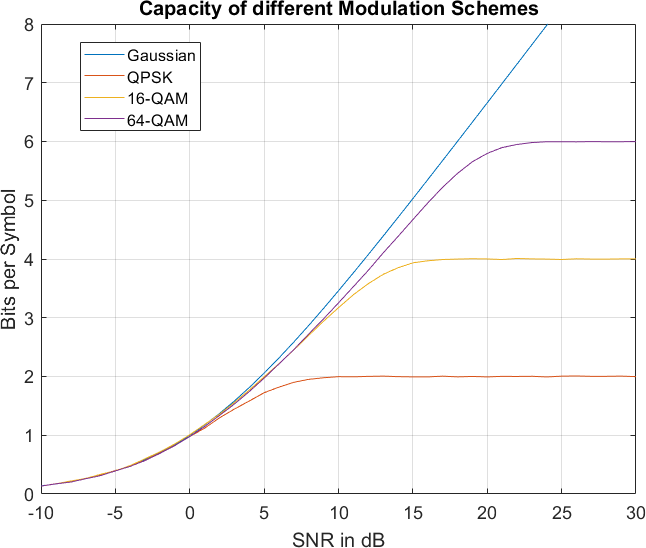
*n*

*n* ∗ *π*

Here we only need to watch out for the number of symbols in the modulation scheme. For QPSK we have a n = 4, 16-QAM n = 16 and 64-QAM n = 64.

For the QAM modulation only the above mentioned parameter n must be changed.

### Results



**Figure 3.1:** Capacity plot for general AWGN-channel, QPSK, 16-QAM and 64-QAM

The results of the calculation in MATLAB can be seen above. We can clearly see the modulated channels approach the desired bit/symbol in a good SNR to bit/symbol rate. The gaussian channel clearly outperforms the modulated channels, clearly seen after 0 dB SNR.

**Compare with book capactiy!**

**Chapter 4**

**Transmitter Receiver Chain in MATLAB**

We will now focus in creating a functioning Transmitter-Receiver chain to simulate a wireless communication as real as possible. The blocks for the communication link were shortly introduced in the beginning, but will be explained further in the following chapters. With LDPC WiMax we use a common communication protocol, which simulates a real channel quite well. Furthermore we will use soft mapping to reconstruct our symbols not hard decoding. Later on I will explain my reasoning behind it.

## LDPC and the CML Library

With a given codeword *x* of length *n* and a generator matrix *G* = [*IT* |*P* ]. The parity check matrix **H** can now be derived as **H** = [−*P T* |*I*n-k]. With the parity check matrix **H** and a code **C** = *xG* the condition for *c***H** = 0 must be fulfilled for the codeword to be valid.

*T*

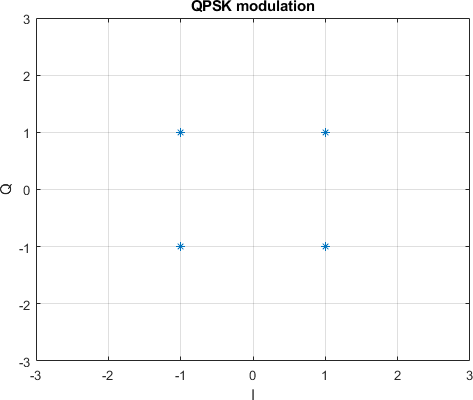
Also with a parity check matrix error correction can be done, that means for single errors we get in our codeword the parity check matrix can selfcorrect our code. This whole process in MATLAB can be computed with the help of the Coded Modulation Library (CML). For this we have the given function ”*InitializeWiMaxLDPC* ” to create the parity-check.matrix, ”*LdpcEncode*” and ”*MpDecode*” to encode and decode our codeword. We decided on a length of 2304, the maximum length that can be send, and self correcting for 50 iterations to be sure to correct as many errors as possible that we receive at the end of our communication chain.

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## Soft-demapping vs. Hard-demapping

These two approaches will result in rather different result in any kind of simulation. We will have a look in both approaches and will compare their unique advantages and disadvantages. For hard-demapping a received symbol is compared to a given fixed threshhold. At every sampling instant the receiver will decide the state of the bit, either ”0” or ”1”. Hard-demapping uses the minumum Hamming distance to make a decision, which means that bitrow from our receiver is compared to every available constellation point. For every bitdifference between bitrow and constellation point will add to the Hamming distance. In the end the receiver will make a decision by taking the constellation symbol which compared to the created bitrow resembles the most, that means the one with the lowest Hamming distance.

Major difference to hard-demapping the soft-demapping will use the euclidean distance to make a decision. It will use additional informations supplied by us to make a decision. While hard demapping has no info about the reliability of the receivers decision, soft demapping will gives us exactly this. With the eucladian distance we calculate the distance between received symbol to every constellation point. Furthermore we will use the loglikelihood ratio to calculate the reliability with the euclidian distance. While hard-demapping is fast and easy to implement in a system it gives us no reliability and as good of performance as soft demapping. In the end it is a decision based on a balance of computing complexity and performance gain. With many modern systems achieving great computing capability and our desire to create a channel as good as possible we will decide to use soft-demapping. In the next section we will have a further look into soft-demapping and LLR based on a QPSK example.



**Figure 4.1:** Capacity plot for general AWGN-channel, QPSK, 16-QAM and 64-QAM

With QPSK we have 4 different symbol constellation also depicted above: (0,0),(0,1),(1,1) and (1,0). The loglikelihood ratio is defined as below

*Ln* = *log P* (*Y* |*B*1 = 0) = *log P* (*Y* |*X*1) + *P* (*Y* |*X*2)

(4.1)

*P* (*Y*|*B*1 = 1) *P* (*Y* |*X*3) + *P* (*Y* |*X*4)

### 4.2.1Results

After receiving our demodulated symbols we can compare those to our codeword we initially send. With this we will determine the frame errors we got for the whole transmission. A frame is defined as a whole codeword length, that means for us it is 2304 bits sent. We have to simulate at least 100000 of those codewords to receive a reliable error rate. Our error rate = frame errors . With 100 errors being a reliable number we can also prematurely interrupt our simulation after 100 errors to save simulation time.

number of frames sent

## 4.3FER and comparison with capacity plots

**Add FER points with respective capacity plots**

**Chapter 5**

**Communication link for Rayleigh fading channels**

**Mention slowfading** We will do the same as before but also add the fading coefficient *H* to our channel. The fading coefficient is represented by rayleigh fading, which was introduced in chapter 2.1... For fading our received signal changes in this way:

*Y* = √*σ*2 ∗ *H* ∗ *X* + *N* (5.1)

With the fading being unknown to our receiver we need a way to extract or estimate the fading coefficient in the channel. An efficient and easy approach to this it to insert a pilot symbol Xp before the transmission. We also will divide our whole codeword in single blocks T which will range for blocksize equal to one symbol up to the whole codeword being one codeword. For every block we will insert one pilot symbol at the beginning.

**Graphic for block + pilot**

Our pilot symbol will have the default value of 1, which is also known at the receiver side. This means to estimate the fading we will do this:

*Yp* = √*σ*2 ∗ *H* ∗ *Xp* + *N* (5.2)

which leads to:

*Yp* + *N*

*H*est = √*σ*2 ∗ *X*

*p*

(5.3)

With this we get a proper estimation for the fading coefficient, but its estimation is highly dependable of the strength of fading and SNR. With higher SNR we receive better estimation not disturbed by the noise as much. And with lesser fading, close to 1, we do not receive a weakened signal, which is hard to distinguish from the noise.

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**Maybe add graphics which shows the single scenarios**

With the estimated fading coefficient the symbols can be reconstructed.

*Y* est

*H*

=

*H*est

√*σ*2 *X* + *N*

*H*est

∗ ∗

(5.4)

and with Hest being close to H we get

*Y* est

= √*σ*2 *X* + *N*

*H*

∗

(5.5)

est

which can be used to calculate the log likelihood ratio.

**Maybe add the scatterplot with and w/ rayleigh fading**

## Theoratical rayleigh fading FER constructed out of AWGN-Channel

For a proper simulation we will need a reference to compare our simulation results to. For this we will construct a theoratical FER plot for rayleigh fading out of the AWGN-channel. First step is the simulate the AWGN channel with the desired codelength over our SNR. In the previous chapters we have already proven that our simulations are match the theoratical curves. With the simulation for AWGN finished we can now start creating many random value (here n = 10000) rayleigh fading coeffiecients. For every single step of SNR, one step being one SNR, we will compute the SNR after rayleigh fading is created, that means SNR= SNR \* H. The SNR for the fading has a corresponding FER-value which we will be add up and divide by the number of fading coefficients.

*n*

Σ

*F ER* − *with* − *SN Ri* = *F ER*(*SN Ri* ∗ *H*(*k*)) (5.6)

*k*=0

**Add plot from AWGN**

It can seen that for the AWGN channel we will reach the error floor really fast at around 3 SNR. For any snr-value which was not simulated for, here only for 0 - 5 SNR, we will add virtual value. While the frame error rate of the AWGN channel reaches a minumum value for high SNR it will never reach 0. In our case we will calculate the theoratical rayleigh FER with error floor 0 and once with error floor 10*−*6, just to show the drastic difference in performance with different error floors. Later on we will also prove that the assumend error floor of 10*−*6 comes close to the real error floor.

**Plot for FER with error floor 0 and** 10*−*6

## Rayleigh fading FER with AWGN channel

**Add different plots 1. Simulation with perfect channel knowledge 2. Simulation with estimated coefficient 3. Different blocksizes T=N/2, T=N/16Explain difference and why?** We can clearly see a distinct performance difference between the two error floors. OH WOW! SURPRISE!

## Increase power of pilot symbol 5.4Increase of pilot symbols in one block

## 5.5Results and comparison with AWGN channel

**Chapter 6 Conclusion**

**6.1Comparison between fading and AWGN channel** **6.2Fazit**

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