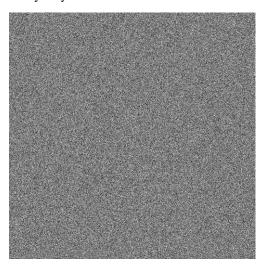
## Colors of image noise

## 1 White Gaussian noise

Everybody knows about white Gaussian noise



White Gaussian noise is famous because it has very nice properties:

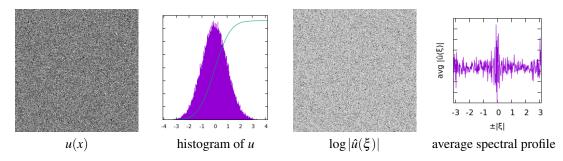
- 1. It is easy to generate using pseudorandom numbers
- 2. Each pixel is an independent, identically distributed Normal variable
- 3. The discrete Fourier, Hartley and Cosine transforms are also white Gaussian noise (except for the obvious symmetries)
- 4. In particular, the power spectrum is mostly flat
- 5. Applying a linear filter renders the pixel values non-independent, but they are still Normal and identically distributed.

Some properties of dubious convenience:

1. The mean is zero, thus it cannot be directly represented as a positive-valued image

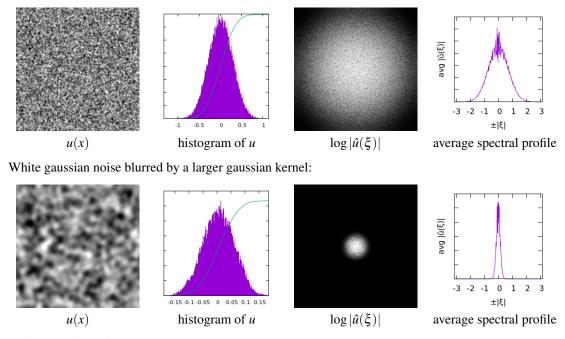
- 2. Worse, the pixel values are not bounded, thus it has a-priori infinite dynamic range.
- 3. When you see it from far away (zooming-out), it disappears.

Statistics of white gaussian noise and its DFT:

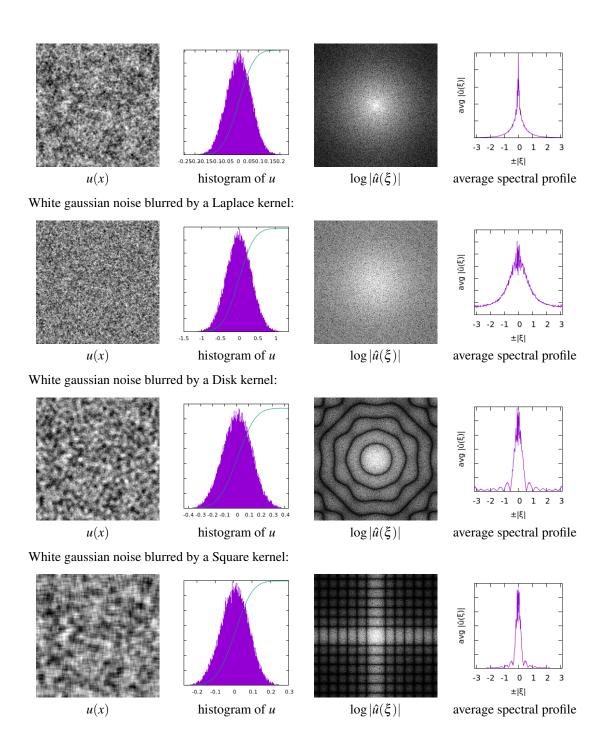


## 2 Blurred white Gaussian noise

White gaussian noise blurred by a small gaussian kernel:

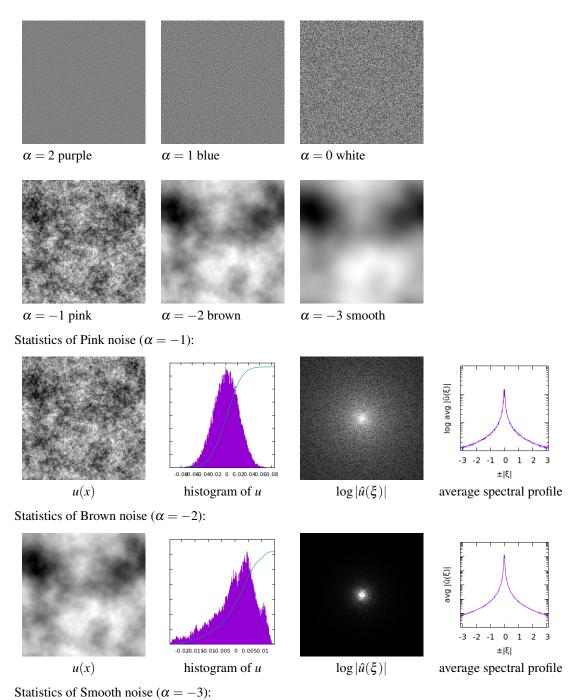


White gaussian noise blurred by a Cauchy kernel:



## 3 Colored gaussian noise

When the spectrum of noise decays as a power-law, we say that it is "colored" noise. The exponent  $\alpha$  of the power law determines its color. The particular case of  $\alpha=0$  corresponds to white noise (a flat spectrum).



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