

Names: \_\_\_\_\_

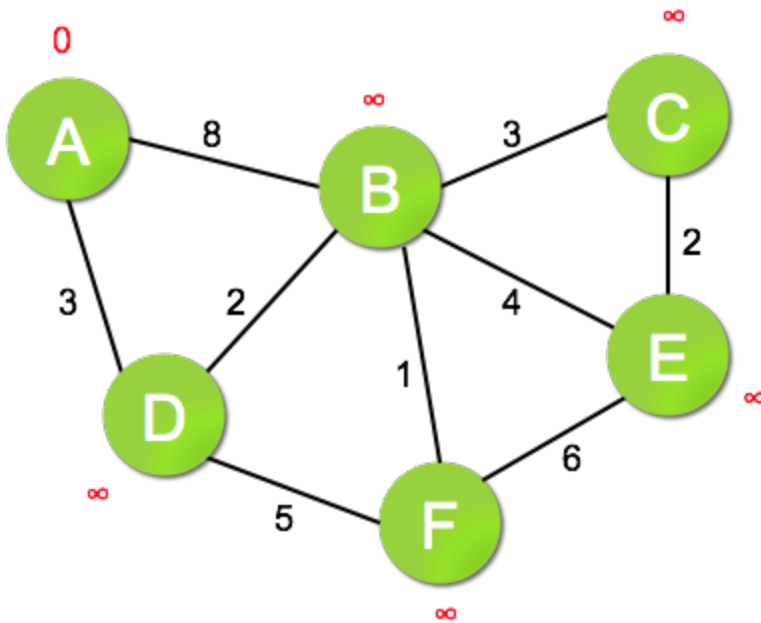
CS Logins: \_\_\_\_\_

Worksheet #15

MSTs: Prim's and Kruskal's

*As always, sit with a partner and work through these together.*

### Activity 1: Prim-Jarnik



while PQ not empty:

N = removeMin and circle it  
connect N to MST (except start node)

for each neighbor M of N:  
update distance to M **if smaller**

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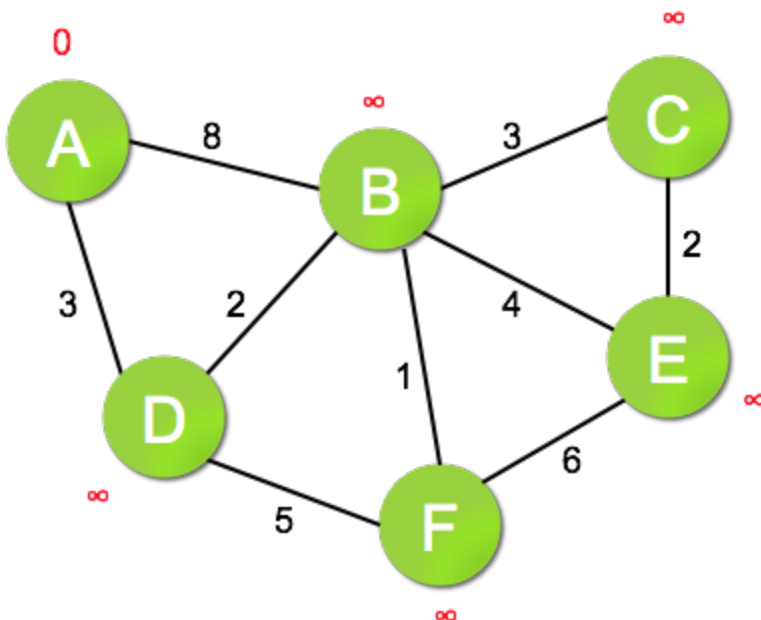
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## Activity 2: Runtime of Prim-Jarnik's

Find the runtime of Prim-Jarnik's Algorithm based on the following pseudocode by filling in the runtime for each appropriate line of code.

```
function prim(G):
  for all v in V:----- 1. O(_____)
    v.cost = ∞
    v.prev = null
  source = a random v in V
  source.cost = 0
  MST = []
  PQ = PriorityQueue(V) ----- 2. O(_____)
  while PQ is not empty:----- 3. O(_____)
    v = PQ.removeMin()----- 4. O(_____)
    if v.prev != null:
      MST.append((v, v.prev))
    for all incident edges (v,u) of v: ----- 5. O(_____)
      if u.cost > (v,u).weight:
        u.cost = (v,u).weight
        u.prev = v
        PQ.replaceKey(u, u.cost) ----- 6. O(_____)
  return MST
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Runtime of Prim-Jarnik's: \_\_\_\_\_

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