

## Problem I – Inversion Insight

In MathemIsland, the wildlife is very diverse. There are roots, trees, leaves, pigeons – everything you’d find in a math book. And everywhere you look, there is a permutation.

ICPC University has devised a systematic way to catalog these permutations. Specifically, because inversions are of utmost importance in studying wildlife genetics, ICPC University has decided to sort all  $N!$  permutations of the integers from 1 to  $N$ : first by the number of inversions and, in the case of a tie, by lexicographic order. This approach uniquely identifies each permutation by an integer from 1 to  $N!$ , indicating its position in the sorted list of all  $N!$  permutations.

Thus, the identity permutation  $(1, 2, \dots, N)$ , which is the only permutation with zero inversions, is assigned the identifier 1, while the reverse identity permutation  $(N, N - 1, \dots, 1)$ , which is the only one with the maximum number of inversions, is assigned the identifier  $N!$ .

As part of the team implementing the ICPC University database, your task is to retrieve a specific permutation based on its identifier. Write a program that, given two integers  $N$  and  $K$ , outputs the permutation of the integers from 1 to  $N$  corresponding to identifier  $K$ .

Remember that the number of inversions in a permutation is the number of pairs of elements that are out of their natural order. That is, for a permutation  $\pi$  with  $N$  elements, its number of inversions  $\text{inv}(\pi)$  is defined as

$$\text{inv}(\pi) = |\{(i, j) : 1 \leq i < j \leq N \wedge \pi(i) > \pi(j)\}|$$

### Input

The input consists of a single line that contains two integers  $N$  ( $1 \leq N \leq 2 \cdot 10^5$ ) and  $K$  ( $1 \leq K \leq \min(N!, 4 \cdot 10^{18})$ ).

### Output

Output a single line with  $N$  integers, describing the  $K$ -th permutation of the integers from 1 to  $N$ , considering permutations sorted according to the university’s criteria.

<b>Sample input 1</b> 4 10	<b>Sample output 1</b> 1 4 3 2
<b>Sample input 2</b> 5 120	<b>Sample output 2</b> 5 4 3 2 1
<b>Sample input 3</b> 16 12345678901234	<b>Sample output 3</b> 2 13 8 10 3 15 16 5 11 12 1 9 7 6 14 4