

APC 524 - Homework #1

7)

a)

$$\begin{aligned}
 a_{20} &= 1 \\
 a_{19} &= -210 \\
 a_{18} &= 20615 \\
 a_{17} &= -1256850 \\
 a_{16} &= 53327946 \\
 a_{15} &= -1672280820 \\
 a_{14} &= 40171771630 \\
 a_{13} &= -756111184500 \\
 a_{12} &= 11310276995381 \\
 a_{11} &= -135585182899530 \\
 a_{10} &= 1307535010540395 \\
 a_9 &= -10142299865511450 \\
 a_8 &= 63030812099294896 \\
 a_7 &= -311333643161390640 \\
 a_6 &= 1206647803780373360 \\
 a_5 &= -3599979517947607200 \\
 a_4 &= 8037811822645051776 \\
 a_3 &= -128709 \\
 a_2 &= \\
 a_1 &=
 \end{aligned}$$

b)

using the Newton-Raphson method

root = 20.000083722 ..., which is close but not equal to 20.

using np.roots()

root = 19.999809 ..., which is also close but not exact

c)

δ	largest root
10^{-8}	$20.64758 \dots + 1.189 \dots i$
10^{-6}	$23.14901 \dots + 2.74 \dots i$
10^{-4}	$28.4002 \dots + 6.51 \dots i$
10^{-2}	$38.478 \dots + 20.834 \dots i$

the estimate for the largest root changes dramatically even with small perturbations

d)