## Machine Design Homework 3

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```
[1]: # Notebook Preamble
import sympy as sp
import matplotlib.pyplot as plt
from IPython.display import display

plt.style.use('maroon_ipynb.mplstyle')
```

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#### 1 Problem 5-3

#### 1.1 Given

A ductile AISI 1030 hot-rolled steel bar has a minimum yield strength in tension and compression of  $37.5 \ ksi$ .

#### 1.2 Find

Use the distortion energy and maximum shear stress theories to determine the factors of safety for the following plane stress states:

```
a. \sigma_x = 25 \ ksi, \ \sigma_y = 15 \ ksi
b. \sigma_x = -12 \ ksi, \ \sigma_y = 15 \ ksi, \ \tau_{xy} = -9 \ ksi
c. \sigma_x = -24 \ ksi, \ \sigma_y = -24 \ ksi, \ \tau_{xy} = -15 \ ksi
```

#### 1.3 Solution

The relationship comes from Eq. 5-3 (maximum shear stress theory) and Eq. 5-19 (distortion energy theory),

$$\sigma_1 - \sigma_3 = \frac{S_y}{n}$$
$$\sigma' = \frac{S_y}{n}$$

#### 1.3.1 Part A

```
for i, j in zip((sig1, sig2, sig3), roots_):
                                                                      display(sp.Eq(i, j))
                                               return roots_
                           def von_mises(s1_, s2_, s3_):
                                               return (1/sp.sqrt(2)*sp.sqrt((s1_ - s2_)**2 + (s2_ - s3_)**2 + (s3_ -_
                               ⇒s1_)**2)).n()
                          s1, s2, s3 = get_principal(25, 15, 0, 0, 0, 0)
                      \sigma^3 - \sigma^2 \left(\sigma_x + \sigma_y + \sigma_z\right) + \sigma \left(\sigma_x \sigma_y + \sigma_x \sigma_z + \sigma_y \sigma_z - \tau_{xy}^2 - \tau_{yz}^2 - \tau_{zx}^2\right) - \sigma_x \sigma_y \sigma_z + \sigma_x \tau_{yz}^2 + \sigma_y \tau_{zx}^2 + \sigma_z \tau_{xy}^2 - \tau_{xy}^2 + \sigma_z \tau_{xy}^2 
                       2\tau_{xy}\tau_{yz}\tau_{zx} = 0
                      \sigma_1 = 25.0
                      \sigma_2 = 15.0
                      \sigma_3 = 0
[3]: # Maximum shear stress theory
                           Sy/(s1 - s3)
[3]:
1.5
[4]: # Distortion energy method
                           s_vm = von_mises(s1, s2, s3)
                           Sy/s_vm
[4]:
1.72061800402921
                       1.3.2 Part D
[5]: s1, s2, s3 = get_principal(-12, 15, 0, -9, 0, 0)
                           # Maximum shear stress
                          Sy/(s1 - s3)
                      \sigma_1 = 17.724980739588
                      \sigma_2 = 0
                      \sigma_3 = -14.724980739588
[5]:
1.15562540880256
[6]: # Distortion
                           s_vm = von_mises(s1, s2, s3)
                           Sy/s_vm
[6]:
1.33250447722257
```

## 1.3.3 Part E

```
[7]: s1, s2, s3 = get\_principal(-24, -24, 0, -15, 0, 0)

# Maximum shear stress
sy/(s1 - s3)

\sigma_1 = 0

\sigma_2 = -9.0

\sigma_3 = -39.0
```

## $[7]: \underbrace{0.961538461538462}$

```
[8]: # Distortion
s_vm = von_mises(s1, s2, s3)
Sy/s_vm
```

[8]: 1.06023616209996

## 2 Problem 5-17

#### 2.1 Given

An AISI 4142 steel Q&T at 800°F exhibits  $S_{yt}=235~ksi,~S_{yc}=285~ksi,$  and  $\epsilon_f=0.07.$   $\sigma_x=-80~ksi,~\sigma_y=-125~ksi,~\tau_{xy}=50~ksi$ 

Determine the factor of safety.

#### 2.3 Solution

The strain at failure is above 0.05, which means that the material is considered ductile. We can apply Eq. 5-22,

$$\frac{\sigma_1}{S_t} - \frac{\sigma_3}{S_c} = \frac{1}{n}$$

$$\sigma_1 = 0$$

 $\sigma_2 = -47.6707195013467$ 

 $\sigma_3 = -157.329280498653$ 

## [9]: 1.81148734105118

This answer lines up with the answer in tha back of the book.

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## 3 Problem 5-19

#### 3.1 Given

A brittle material has properties  $S_{ut}=30\ ksi$  and  $S_{uc}=90\ ksi.$ 

$$\sigma_x = 20~ksi,~\tau_{xy} = -10~ksi$$

## **3.2** Find

Using only the modified-Mohr theories, determine the factor of safety.

#### 3.3 Solution

Start by computing the principal stresses.

$$\sigma_1 = 24.142135623731$$

$$\sigma_2 = 0$$

$$\sigma_3 = -4.14213562373095$$

For this case, we can use Eq. 5-32a on p. 264,

$$\sigma_1 = \frac{S_{ut}}{n}$$

[11]: Sut/s1

[11]: 1.24264068711929

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## 4 Problem 5-24

## 4.1 Given

ASTM 30 cast iron.

$$\sigma_x = -10~ksi,\, \sigma_y = -25~ksi,\, {\rm and}~ \tau_{xy} = -10~ksi$$

## 4.2 Find

Determine the factor of safety using the modified-Mohr method.

$$\sigma_1 = 0$$

$$\sigma_2 = -5.0$$

$$\sigma_3 = -30.0$$

Use Eq. 5-32c,

$$n = \frac{-S_{uc}}{\sigma_3}$$

-Suc/s3

## 5 Problem 5-98

### 5.1 Given

A cylinder subjected to internal pressure  $p_i$  has an outer diameter of 14 in and a 1-in wall thickness. For the cylinder material,  $K_{IC}=72~ksi\sqrt{in},~S_y=170~ksi,$  and  $S_{ut}=192~ksi.$ 

#### **5.2** Find

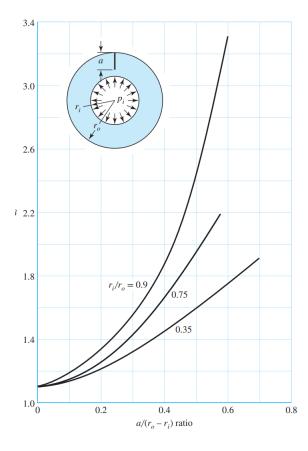
If the cylinder contains a radial crack in the longitudinal direction of depth 0.5 in determine the pressure that will cause uncontrollable crack growth.

## 5.3 Solution

We use the following relationship,

$$K_I = \beta \sigma \sqrt{\pi a}$$

 $\beta$  may be found from,



```
[14]: a = sp.S('0.5')
    ro, ri = sp.S(7), 6
    a/(ro - ri)

[14]: 0.5
    The correct line to use depends on \(\frac{r_i}{r_o}\).

[15]: \(\frac{ri}{ro.n()}\)

[15]: 0.857142857142857

[16]: \(\text{beta} = sp.S(2.35) \) # from the above figure
    K_IC = 72
    sig = K_IC/(beta*sp.sqrt(sp.pi*a))
    sig.n() # ksi

[16]: 24.4458248416197
```