# Machine Design Homework 4

June 17, 2022

# Gabe Morris

# Contents

1	Problem 6-1	3
	1.1 Given	 3
	1.2 Find	
	1.3 Solution	 3
<b>2</b>	Problem 6-3	5
	Problem 6-3           2.1 Given	 5
	2.2 Find	 5
	2.3 Solution	 5
3	Problem 6-17	7
	3.1 Given	 7
	3.2 Find	 7
	3.3 Solution	7

# ME 4403 Homework 4 Gabe Morris gnm54

#### 1 Problem 6-1

#### 1.1 Given

A 10-mm steel drill rod was heat treated and ground. The measured hardness was found to be 300 Brinell.

#### 1.2 Find

Estimate the endurance strength in MPa if the rod is used in rotating bending.

### 1.3 Solution

Eq. 6-10 on p. 305,

$$S_e' = \begin{cases} 0.5S_{ut} & S_{ut} \leq 200 \; ksi \; (1400 \; MPa) \\ 100 & S_{ut} > 200 \; ksi \\ 700 \; MPa & S_{ut} > 1400 \; MPa \end{cases}$$

The ultimate strength of steel comes from Eq. 2-36,

$$S_{ut} = 3.4H_B$$

[2]: 510.0

This value is not the final value. The relationship for the refined value is,

$$S_e = k_a k_b k_c k_d k_e S'_e$$

The only necessary k values used for this analysis is  $k_a$  and  $k_b$ , whose equations are at 6-18 and 6-19 respectfully.

```
k_b = sp.S('1.24')*d**-(sp.S('0.107'))

# display(k_a, k_b)

S_e = k_a*k_b*S_e_prime

S_e # MPa
```

[3]: <sub>428.839455736079</sub>

# 2 Problem 6-3

#### 2.1 Given

A steel rotating beam test specimen has an ultimate strength of 120 ksi.

#### 2.2 Find

Estimate the life of the specimen if it is tested at completely reversed stress amplitude of 70 ksi.

#### 2.3 Solution

Find  $S_e$  first.

[4]: 60.0

The  $S'_e$  value will be used in place of  $S_e$  from Figure 6-23 description. We can use the following relationships to determine N.

$$\begin{split} N &= \left(\frac{\sigma_{ar}}{a}\right)^{1/b} \\ a &= \frac{(fS_{ut})^2}{S_e} \\ b &= -\frac{1}{3}\log\left(\frac{fS_{ut}}{Se}\right) \end{split}$$

The value of f is 0.82 from Figure 6-23. The  $S_{ut}$  value is  $2(S_e) = 120 \ ksi$ .

```
[5]: def log10(x_):
    return sp.log(x_)/sp.log(10)

f = sp.S('0.82')
a = (f*S_ut)**2/S_e_prime
b = -sp.Rational(1, 3)*log10(f*S_ut/S_e_prime)

display(sp.Eq(sp.Symbol('a'), a.n()),
    sp.Eq(sp.Symbol('b'), b.n()))
```

```
sig_ar = 70
N = ((sig_ar/a)**(1/b)).n()
N # cycles
```

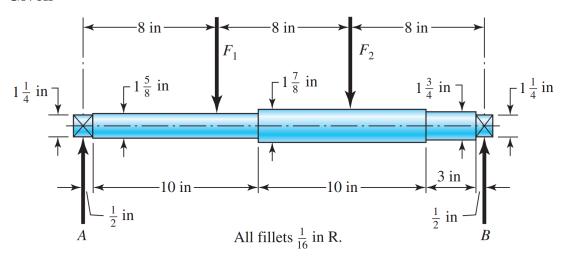
a = 161.376

b = -0.0716146160158993

[5]: <sub>116192.956004683</sub>

# 3 Problem 6-17

#### 3.1 Given



The shaft shown in the figure above is machined from AISI 1040 CD steel. The shaft rotates at 1600 rpm and is supported in roller bearings at A and B. The applied forces are  $F_1 = 2500 \ lbf$  and  $F_2 = 1000 \ lbf$ .

# **3.2** Find

Determine the minimum fatigue factor of safety based on achieving infinite life. If infinite life is not predicted, estimate the number of cycles to failure. Also check for yielding.

#### 3.3 Solution

The reaction forces need to be solved first.

```
[6]: A, B = sp.symbols('A B')
F1, F2 = 2500, 1000

eq1 = sp.Eq(A + B, F1 + F2)
eq2 = sp.Eq(B*24 - F1*8 - F2*16, 0)

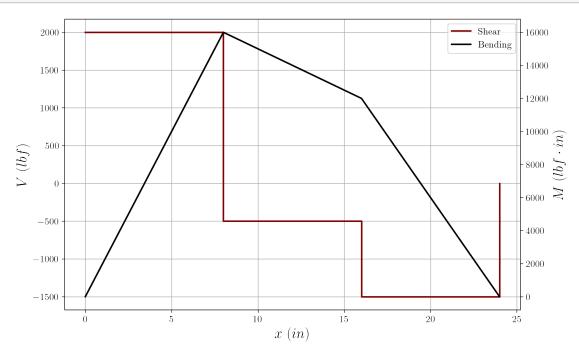
sol = sp.solve([eq1, eq2], dict=True)[0]

display(eq1, eq2, Markdown('---'))
for key, value in sol.items():
    display(sp.Eq(key, value))
```

$$A + B = 3500$$
  
 $24B - 36000 = 0$ 

```
A = 2000B = 1500
```

```
[7]: # Plotting Shear and Bending Moment Diagram
    x = [0, 8, 16, 24]
    x_{shear} = [0, 8, 8, 16, 16, 24, 24]
    ⇔sol[B]]
    V = [V1, V1, V2, V2, V3, V3, V4]
    M = M1, M2, M3, M4 = [0, V1*8, V1*8 + V2*8, V1*8 + V2*8 + V3*8]
    fig, ax = plt.subplots()
    ax2 = ax.twinx()
    ax.plot(x_shear, V, label='Shear')
    ax2.plot(x, M, color='black', label='Bending')
    ax2.grid(visible=False)
    ax.legend(handles=[ax.lines[0], ax2.lines[0]])
    ax.set_xlabel('$x$ ($in$)')
    ax.set_ylabel('$V$ ($lbf$)')
    ax2.set_ylabel(r'$M$ ($lbf\cdot in$)')
    plt.show()
```



We are interested in the stress at the fillet radius in which the smaller diameter is used.

```
[8]: M_{mid} = (M3 - M2)/8*(sp.S('10.5') - 8) + M2
M_{mid} # in lbf*in
```

[8]: <sub>14750.0</sub>

```
[9]: c = sp.S('1.625')/2

I = sp.pi.n()/4*c**4

sig = M_mid*c/I

sig # in psi
```

# [9]: 35013.218176932

The yield strength is 71 ksi, and this stress is far below this value. The ultimate strength is  $S_{ut}=0.5(H_B)=0.5(170)=85\ ksi$ .