Machine Design ME-4403

Ch. 3, 4, & 5

J. Alejandro Martinez C.

Exam #1

Name:	Gabe Morr	is		
Date:_	06/15/2022			

Jabe Morris

Signature

"As a Mississippi State University student, I will conduct myself with honor and integrity at all times. I will not lie, cheat, or steal, nor will I accept the actions of those who do."

Honor Code, Mississippi State University

Instructions:

Complete all your work in a MathCAD file following the homework format.

Any graphs/figures can be pasted in MathCAD.

Show all your work and box your answers.

Problems:

Ch 3: 6, 17a&d, 72, 82, 91.

Ch 4: 46.

Ch 5: 1d, 12, 19a, 49

Machine Design Test 1

June 15, 2022

Gabe Morris

```
[1]: # Notebook Preamble
import sympy as sp
import numpy as np
import matplotlib.pyplot as plt
from IPython.display import display, Markdown

plt.style.use('maroon_ipynb.mplstyle')
```

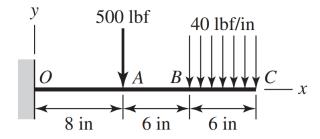
Contents

1	Problem 3-6	4								
	1.1 Given	. 4								
	1.2 Find	. 4								
	1.3 Solution	. 4								
	1.3.1 Reaction Forces	. 4								
	1.3.2 Bending and Moment Diagram	. 5								
2	Problem 3-17	8								
_	2.1 Given									
	2.2 Find	_								
	2.3 Solution									
	2.3.1 Part A									
	2.3.2 Part D									
3	Problem 3-72	11								
	3.1 Given									
	3.2 Find									
	3.3 Solution	. 11								
4	Problem 3-82									
	4.1 Given	. 12								
	4.2 Find	. 12								
	4.3 Solution	. 13								
	4.3.1 Part A	. 13								
	4.3.2 Part B	. 14								
	4.3.3 Part C	. 14								
	4.3.4 Part D	. 15								
	4.3.5 Part E	. 16								
5	Problem 3-91 17									
0	5.1 Given									
	5.2 Find									
	5.3 Solution									
	5.3.1 Part A									
	5.3.2 Part B									
	5.3.3 Part C									
c	D. 11 4.40	90								
6	Problem 4-46 6.1 Given	20 . 20								
	6.2 Find									
	6.3.1 Uniform Diameter									
	0.0.2 Maximum Defiction	. 41								
7	Problem 5-1									
	7.1 Given									
	7.2 Find	. 23								

	7.3	$\operatorname{Solution}$	23
		7.3.1 Maximum Shear Stress Method	24
		7.3.2 Distortion Energy Method	24
8 Pro		lem 5-12	25
	8.1	Given	25
	8.2	Find	25
	8.3	$\operatorname{Solution}$	25
		8.3.1 Part A	25
		8.3.2 Part B	26
		8.3.3 Part C	26
		8.3.4 Part D	26
		8.3.5 Part E	
9	Pro	lem 5-19	27
	9.1	Given	27
	9.2	Find	
	9.3	$\operatorname{Solution}$	
		0.3.1 Brittle Coulomb-Mohr	
		0.3.2 Modified-Mohr	
10) Pro	lem 5-49	28
		Given	28
		Find	
		Solution	
	20.0	.0.3.1 Maximum Shear Stress Method	
			-0 29

1 Problem 3-6

1.1 Given

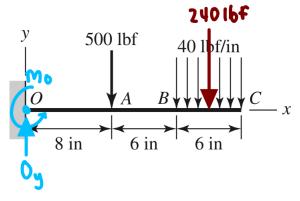


1.2 Find

Find the reaction forces and plot the shear and bending diagram.

1.3 Solution

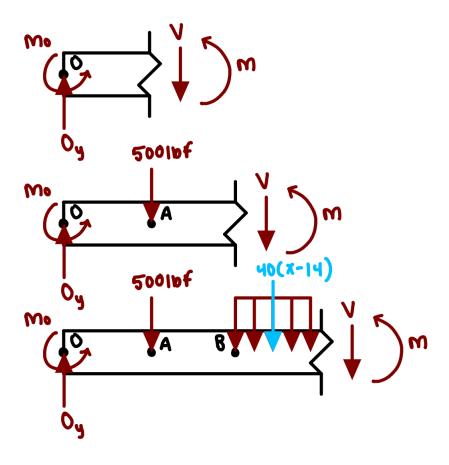
1.3.1 Reaction Forces



```
[2]: # Getting the reaction forces
Oy_sym, Mo_sym = sp.symbols('O_y M_o')
Oy = 240 + 500
Mo = 500*8 + 240*17
display(sp.Eq(Oy_sym, Oy), sp.Eq(Mo_sym, Mo)) # lbf and lbf*in
```

 $O_y = 740$ $M_o = 8080$

1.3.2 Bending and Moment Diagram



The equation may be described as the piecewise relationship coded below.

```
[3]: V, M, x = sp.symbols('V M x')

# From 0 to A

V1 = 0y

M1 = -Mo + 0y*x

# From A to B

V2 = 0y - 500

M2 = -Mo + 0y*x - 500*(x - 8)

# From B to C

V3 = 0y - 500 - 40*(x - 14)

M3 = -Mo + 0y*x - 500*(x - 8) - 40*(x - 14)*(x - 14)/2

eq1 = sp.Eq(V, sp.Piecewise((V1, (x >= 0) & (x < 8)), (V2, (x >= 8) & (x <= 0.00)))

eq2 = sp.Eq(M, sp.Piecewise((M1, (x >= 0) & (x < 8)), (M2, (x >= 8) & (x <= 0.00)))

eq2 = sp.Eq(M, sp.Piecewise((M1, (x >= 0) & (x < 8)), (M2, (x >= 8) & (x <= 0.00)))
```

```
display(eq1, eq2)
```

```
V = \begin{cases} 740 & \text{for } x \ge 0 \land x < 8 \\ 240 & \text{for } x \ge 8 \land x < 14 \\ 800 - 40x & \text{for } x \ge 14 \land x \le 20 \end{cases} M = \begin{cases} 740x - 8080 & \text{for } x \ge 0 \land x < 8 \\ 240x - 4080 & \text{for } x \ge 8 \land x < 14 \\ 240x - \frac{(x - 14)(40x - 560)}{2} - 4080 & \text{for } x \ge 14 \land x \le 20 \end{cases}
```

The important key points for shear are shown in the piecewise function expression above. The key points for the bending moment are,

```
[4]: points = ['0', 'A', 'B', 'C']
values = [0, 8, 14, 20]
for p, v in zip(points, values):
    display(sp.Eq(sp.Symbol(f'M_{p}'), eq2.rhs.subs(x, v))) # in lbf*in
```

```
M_O = -8080
```

$$M_A = -2160$$

$$M_B = -720$$

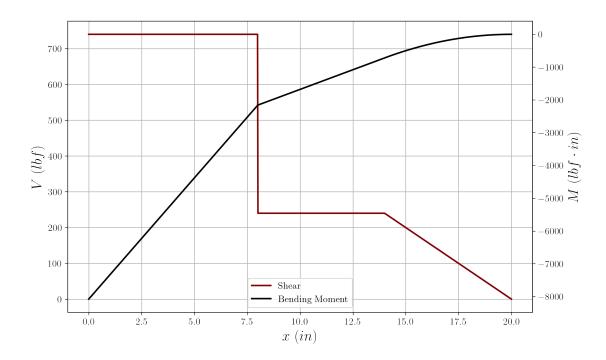
$$M_C = 0$$

```
[5]: # Getting shear and bending diagram
    x_ = np.linspace(0, 20, 1000)
    V_ = sp.lambdify(x, eq1.rhs, modules='numpy')
    M_ = sp.lambdify(x, eq2.rhs, modules='numpy')
    fig, ax = plt.subplots()
    ax2 = ax.twinx()

ax.plot(x_, V_(x_), label='Shear')
    ax2.plot(x_, M_(x_), label='Bending Moment', color='black')

ax2.grid(visible=False)
    ax.legend(handles=[ax.lines[0], ax2.lines[0]], loc='lower center')

ax.set_xlabel('$x$ ($in$)')
    ax.set_ylabel('$V$ ($lbf$)')
    ax2.set_ylabel(r'$M$ ($lbf$cdot in$)')
    plt.show()
```



Notice that the graph has a duel y-axis.

2 Problem 3-17

2.1 Given

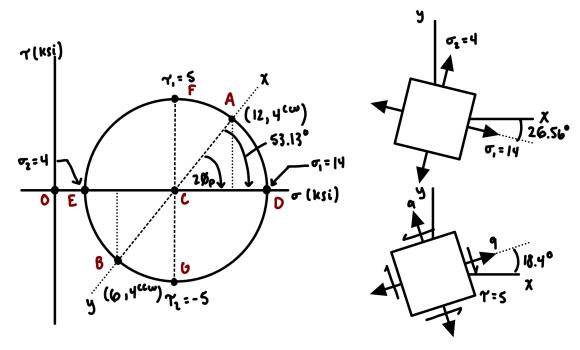
a.
$$\sigma_x=12~ksi,~\sigma_y=6~ksi,~\tau_{xy}=4~ksi~cw$$
b. $\sigma_x=9~ksi,~\sigma_y=19~ksi,~\tau_{xy}=8~ksi~cw$

2.2 Find

Draw the plane stress element as seen in Figure 3-11c and d. Also draw Mohr's circle fully labeled.

2.3 Solution

2.3.1 Part A



Center and Radius:

$$C = \frac{\sigma_x}{2} + \frac{\sigma_y}{2} = 9.0$$

$$R = \sqrt{\tau_{xy}^2 + \left(\frac{\sigma_x}{2} - \frac{\sigma_y}{2}\right)^2} = 5.0$$

Principle Stresses:

$$\sigma_1 = C + R = 14.0$$

$$\sigma_2 = C - R = 4.0$$

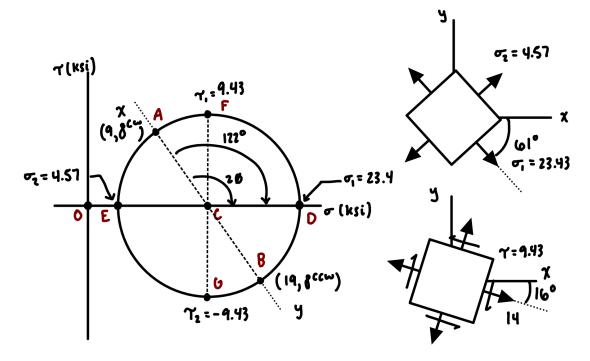
$$\tau_1 = R = 5.0$$

$$\tau_2=-R=-5.0$$

Angle of Occurrence:

$$2\phi_p = \mathrm{atan}\left(\frac{2\tau_{xy}}{\sigma_x - \sigma_y}\right) = 53.130102354156$$

2.3.2 Part D



Center and Radius:

$$C = \frac{\sigma_x}{2} + \frac{\sigma_y}{2} = 14.0$$

$$R = \sqrt{\tau_{xy}^2 + \left(\frac{\sigma_x}{2} - \frac{\sigma_y}{2}\right)^2} = 9.4339811320566$$

Principle Stresses:

$$\sigma_1 = C + R = 23.4339811320566$$

$$\sigma_2 = C - R = 4.5660188679434$$

$$\tau_1 = R = 9.4339811320566$$

$$\tau_2 = -R = -9.4339811320566$$

Angle of Occurrence:

$$2\phi_p = \mathrm{atan}\left(\frac{2\tau_{xy}}{\sigma_x - \sigma_y}\right) = 122.005383208084$$

ME 4403 Test 1 Gabe Morris gnm54

3 Problem 3-72

3.1 Given

A 2-foot-long steel bar with a $\frac{3}{4}$ in diameter is to be used as a torsion spring. The torsional stress in the bar is not to exceed 30 ksi.

3.2 Find

What is the maximum angle of twist of the bar?

3.3 Solution

Use the following relationship to determine the torque,

$$\tau = \frac{Tc}{J}$$

The angle of twist is,

$$\phi = \frac{TL}{JG}$$

```
[8]: # Find torque
c = sp.S('0.75')/2
J = sp.pi/2*c**4
tau = 30_000
T = tau*J/c
T.n() # torque in lbf*in
```

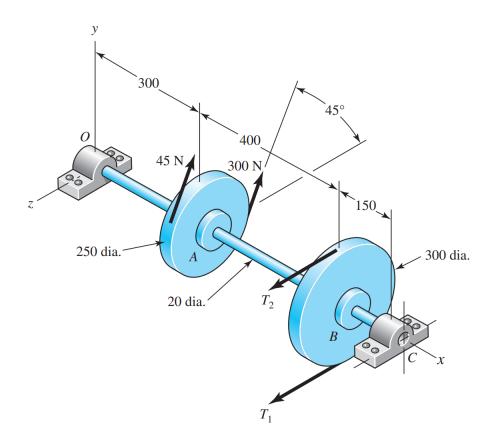
[8]: _{2485.04887637474}

```
[9]: # Find angle of twist
G = sp.S('11.5e6') # from Table A-5
L = 24
phi = (T*L/(J*G))
(phi*180/sp.pi).n() # angle of twist in degrees
```

[9]: 9.56590405783635

4 Problem 3-82

4.1 Given



A counter shaft carrying two V-belt pulleys is shown in the figure. Pulley A receives power from a motor through a belt with the belt tensions shown. The power is transmitted through the shaft and delivered to the belt on pulley B. Assume the belt tension on the loose side at B is 15 percent of the tension on the tight side.

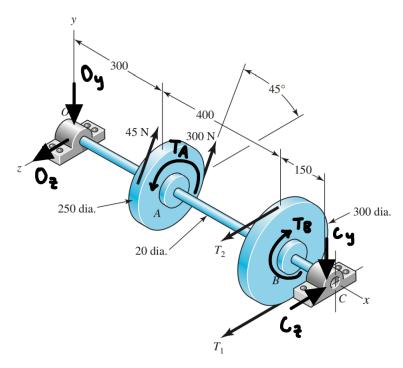
4.2 Find

- a. Determine the tensions in the belt on pulley B, assuming the shaft is running at a constant speed.
- b. Find the magnitudes of the bearing reaction forces, assuming the bearings act as simple supports.
- c. Draw shear-force and bending-moment diagrams for the shaft. If needed, make one set for the horizontal plane and another set for the vertical plane.
- d. At the point of maximum bending moment, determine the bending stress and the torsional shear stress.
- e. At the point of maximum bending moment, determine the principal stresses and the maximum shear stress.

4.3 Solution

4.3.1 Part A

The directions of the torques about A and B are,



Since the shaft has no angular acceleration, $T_A = T_B$ (with directions shown above). It should also be noted that T_1 must be greater than T_2 because the torque shows that the pulley is more tensile at the bottom.

```
[10]: # Solving for T1 and T2

T1, T2 = sp.symbols('T_1 T_2')

T_A = \text{sp.S}('0.125')*(300 - 45)
eq1 = sp.Eq(sp.S('0.15')*(T1 - T2), T_A)
eq2 = sp.Eq(T2, sp.S(0.15)*T1)

[display(eq) for eq in [eq1, eq2, Markdown('---')]]

sol = sp.solve([eq1, eq2], dict=True)[0]
_ = [display(sp.Eq(key, value)) for key, value in sol.items()]

0.15T_1 - 0.15T_2 = 31.875

T_2 = 0.15T_1
```

$$T_1 = 250.0$$

$$T_2 = 37.5$$

4.3.2 Part B

```
[11]: # Solving for the reactions

Oy, Oz, Cy, Cz = sp.symbols('O_y O_z C_y C_z')

eq1 = sp.Eq((300 + 45)*sp.sin(sp.pi/4) - Oy - Cy, 0) # Forces in y direction
eq2 = sp.Eq(sol[T1] + sol[T2] + Oz - Cz - (45 + 300)*sp.cos(sp.pi/4), 0) #__

Forces in z direction

eq3 = sp.Eq(sp.S('0.3')*(45 + 300)*sp.sin(sp.pi/4) - Cy*sp.S('0.85'), 0) #__

Moments about z-axis

eq4 = sp.Eq(sp.S('0.3')*(45 + 300)*sp.cos(sp.pi/4) - sp.S('0.7')*(sol[T1] +__

sol[T2]) + Cz*sp.S('0.85'), 0) # Moments about the y-axis

sol2 = sp.solve([eq1, eq2, eq3, eq4], dict=True)[0]
[display(eq) for eq in [eq1, eq2, eq3, eq4, Markdown('---')]]

= [display(sp.Eq(key, value)) for key, value in sol2.items()]
```

$$\begin{split} -C_y - O_y + \frac{345\sqrt{2}}{2} &= 0 \\ -C_z + O_z - \frac{345\sqrt{2}}{2} + 287.5 &= 0 \\ -0.85C_y + 51.75\sqrt{2} &= 0 \\ 0.85C_z - 201.25 + 51.75\sqrt{2} &= 0 \end{split}$$

 $C_y = 86.1006492385973$

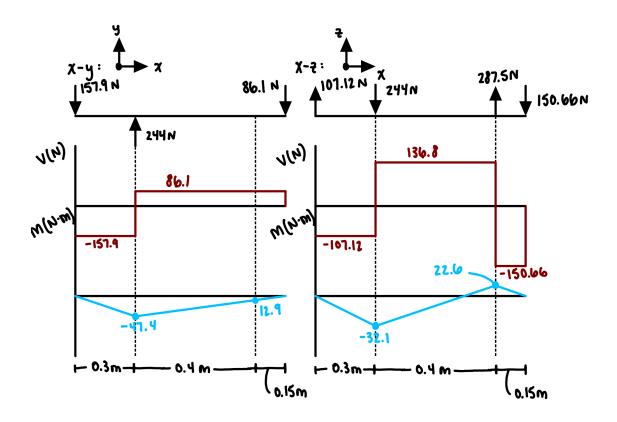
 $O_y = 157.851190270762$

 $C_z = 150.664056643756$

 $O_z = 107.115896153115$

4.3.3 Part C

The shear and bending moment diagram for the two planes is,



4.3.4 Part D

```
[12]: # Getting max bending moment
M_A = sp.sqrt(47.35535708**2 + 32.13476885**2)
M_B = sp.sqrt(12.91509739**2 + 22.59960847**2)
sp.Matrix([M_A, M_B])
```

[12]: [57.2291290621938] 26.0296377921492]

The maximum bending moment occurs at point A.

```
[13]: # Getting the bending stress
c = sp.S('0.01')
sig_x = (M_A*c/(sp.pi/4*c**4)).n()
sig_x # in Pa
```

[13]: 72866390.2327375

```
[14]:  # Getting the torsional stress

t_xz = (31.875*c/(sp.pi/2*c**4)).n()

t_xz # in Pa
```

[14]: 20292255.2442167

4.3.5 Part E

[15]: mohr(sig_x, 0, t_xz)

Center and Radius:

$$C = \frac{\sigma_x}{2} + \frac{\sigma_y}{2} = 36433195.1163688$$

$$R = \sqrt{\tau_{xy}^2 + \left(\frac{\sigma_x}{2} - \frac{\sigma_y}{2}\right)^2} = 41703157.3059383$$

Principle Stresses:

$$\sigma_1 = C + R = \boxed{78136352.422307}$$

$$\sigma_2 = C - R = \frac{-5269962.18956954}{}$$

$$\tau_1 = R = 41703157.3059383$$

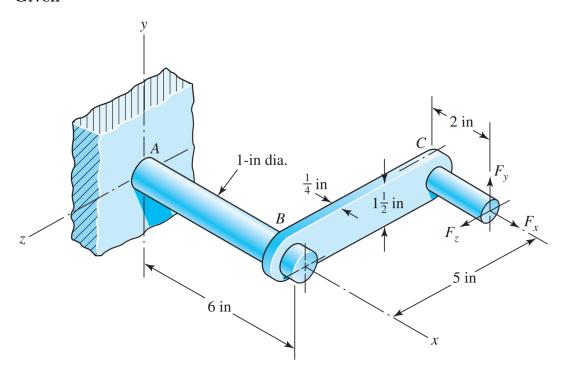
$$\tau_2 = -R = -41703157.3059383$$

Angle of Occurrence:

$$2\phi_p = \mathrm{atan}\left(\frac{2\tau_{xy}}{\sigma_x - \sigma_y}\right) = 29.1165652891492$$

5 Problem 3-91

5.1 Given



The cantilevered bar in the figure is made from a ductile material and is statically loaded with $F_y=200\ lbf$ and $F_x=F_z=0$.

5.2 Find

Analyze the stress situation on rod AB by obtaining the following:

- a. Determine the precise location of the critical stress element.
- b. Sketch the critical stress element and determine magnitudes and directions for all stresses acting on it. (Transverse shear may only be neglected if you can justify this decision.)
- c. For the critical stress element, determine the principal stresses and the maximum shear stress.

5.3 Solution

5.3.1 Part A

The critical stress element will be at the top or bottom $(y = \pm 0.5 \ in)$ because both the bending stress and shear stress are maximized at the farthest distance away from the neutral axis.

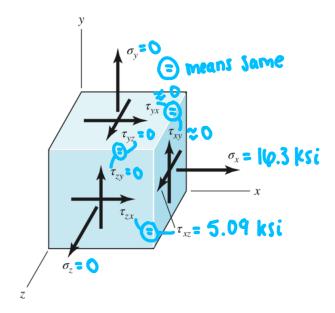
5.3.2 Part B

[16]: # Acquiring shear stress
T = 5*200
c = sp.S('0.5')
J = sp.pi/2*c**4
t_xz = (T*c/J).n()
t_xz # in psi

[16]: 5092.95817894065

[17]: # Acquiring the bending stress
M = 8*200
I = sp.pi/4*c**4
sig_x = (M*c/I).n()
sig_x # in psi

[17]: 16297.4661726101



The transverse shear, τ_{xy} , is being neglected because the rod is a magnitude longer than its diameter.

5.3.3 Part C

Center and Radius:

$$C = \frac{\sigma_x}{2} + \frac{\sigma_y}{2} = 8148.73308630504$$

$$R = \sqrt{\tau_{xy}^2 + \left(\frac{\sigma_x}{2} - \frac{\sigma_y}{2}\right)^2} = 9609.37427329589$$

Principle Stresses:

$$\sigma_1 = C + R = \boxed{17758.1073596009}$$

$$\tau_1 = R = 9609.37427329589$$

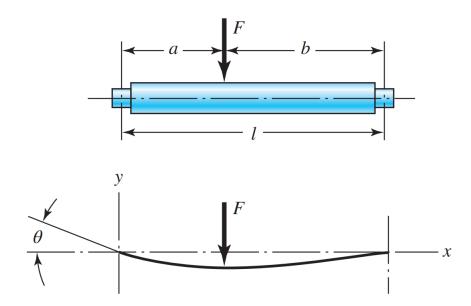
$$\tau_2 = -R = -9609.37427329589$$

Angle of Occurrence:

$$2\phi_p = \mathrm{atan}\left(\frac{2\tau_{xy}}{\sigma_x - \sigma_y}\right) = 32.0053832080835$$

6 Problem 4-46

6.1 Given



The diameter is uniform with $l = 300 \ mm$, $a = 100 \ mm$, and $F = 3 \ kN$. The allowable slope ath the bearings is $0.001 \ mm/mm$ and the design factor is 1.28. The shaft is steel with $E = 207 \ GPa$. The relationship for the diameter is,

$$d = \left| \frac{32Fb(l^2 - b^2)}{3\pi E l \xi} \right|^{1/4}$$

6.2 Find

What uniform diameter will the shaft support? Determine the maximum deflection of the shaft.

6.3 Solution

6.3.1 Uniform Diameter

We can use the given relationship to determine the diameter.

```
[19]: E = sp.S('207e9')
1, a = sp.S('0.3'), sp.S('0.1')
xi = sp.S('0.001')
b = 1 - a
n = sp.S('1.28')
F = n*3_000

d = (sp.Abs(32*F*b*(1**2 - b**2)/(3*sp.pi*E*l*xi))**sp.S('0.25')).n()
```

```
d # in meters
```

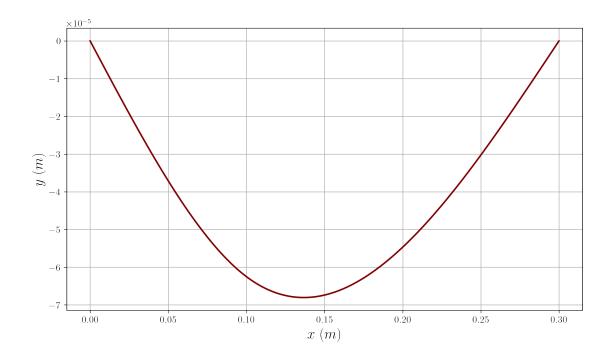
$[19]: \underbrace{0.0380653317176321}_{}$

plt.show()

6.3.2 Maximum Deflection

The maximum deflection equation may be found from Table A-9. The deflection may be graphed like so,

```
[20]: x = sp.Symbol('x')
       I = sp.pi/4*(d/2)**4
       F = 3_000
       y_AB = F*b*x/(6*E*I*1)*(x**2 + b**2 - 1**2)
       y_BC = F*a*(1 - x)/(6*E*I*1)*(x**2 + a**2 - 2*1*x)
       y = sp.Piecewise((y_AB, (x >= 0) & (x < a)), (y_BC, (x >= a) & (x <= 1)))
[20]: \int 0.0490873852123405x(x^2-0.05)
                                                     for x \ge 0 \land x < 0.1
        \substack{\pi \\ 8.18123086872342 \cdot 10^{-5} \cdot (90.0 - 300.0x)(x^2 - 0.6x + 0.01)}
                                                    for x \ge 0.1 \land x \le 0.3
[21]: x_ = np.linspace(0, 0.3, 10_000)
       y_lamb = sp.lambdify(x, y, modules='numpy')
       fig, ax = plt.subplots()
       ax.plot(x_, y_lamb(x_))
       ax.set_xlabel('$x$ ($m$)')
       ax.set_ylabel('$y$ ($m$)')
```



With access to numerical tools, the maximum deflection may be obtained by simply calculating the maximum value from a discritized data set rather than taking the derivative symbolically.

```
[22]: # Getting the maximum magnitude
y_max = np.max(np.abs(y_lamb(x_)))
y_max*1_000 # in mm
```

[22]: 0.06804138155566049

This answer is not rounded, but the one in the back of the book is rounded.

7 Problem 5-1

7.1 Given

A ductile hot-rolled steel bar has a minimum yield strength in tension and compression of 350 MPa.

$$\sigma_x = -50~MPa, \, \sigma_y = -75~MPa, \, {\rm and} \, \, \tau_{xy} = -50~MPa$$

7.2 Find

Use the distortion-energy and maximum shear stress methods to determine the factor of safety.

7.3 Solution

Begin by getting the principal stresses.

```
[23]: sig_x, sig_y, sig_z, tau_xy, tau_xx, tau_yz = sp.symbols(r'\sigma_x \sigma_y_

¬\sigma_z \tau_{xy} \tau_{zx} \tau_{yz}')
                       sig = sp.Symbol(r'\sigma')
                       sig1, sig2, sig3 = sp.symbols(r'\sigma_1 \sigma_2 \sigma_3')
                       poly = sig**3 - (sig_x + sig_y + sig_z)*sig**2 + (sig_x*sig_y + sig_x*sig_z + u)
                            ⇒sig_y*sig_z - tau_xy**2 - tau_yz**2 - tau_zx**2)*sig - (sig_x*sig_y*sig_z +
                           →2*tau_xy*tau_yz*tau_zx - sig_x*tau_yz**2 - sig_y*tau_zx**2 - sig_z*tau_xy**2)
                       display(sp.Eq(poly.simplify(), 0))
                       def get_principal(sx, sy, sz, txy, tyz, tzx):
                                       poly_= poly_subs([(sig_x, sx), (sig_y, sy), (sig_z, sz), (tau_xy, txy),_u
                            →(tau_yz, tyz), (tau_zx, tzx)])
                                       roots = [sp.re(root.n()) for root in sp.roots(poly_, sig)]
                                       roots_ = sorted(list(roots), reverse=True)
                                       for i, j in zip((sig1, sig2, sig3), roots_):
                                                      display(sp Eq(i, j))
                                       return roots_
                       def von_mises(s1_, s2_, s3_):
                                       return (1/sp.sqrt(2)*sp.sqrt((s1 - s2)**2 + (s2 - s3)**2 + (s3 - ___
                            ⇒s1_)**2)).n()
                       s1, s2, s3 = get_principal(-50, -75, 0, -50, 0, 0)
                    \sigma^3 - \sigma^2 \left(\sigma_x + \sigma_y + \sigma_z\right) + \sigma \left(\sigma_x \sigma_y + \sigma_x \sigma_z + \sigma_y \sigma_z - \tau_{xy}^2 - \tau_{yz}^2 - \tau_{zx}^2\right) - \sigma_x \sigma_y \sigma_z + \sigma_x \tau_{yz}^2 + \sigma_y \tau_{zx}^2 + \sigma_z \tau_{xy}^2 - \tau_{xy}^2 + \sigma_z \tau_{yz}^2 + \sigma_z \tau_{xy}^2 
                     2\tau_{xy}\tau_{yz}\tau_{zx} = 0
```

$$\begin{split} &\sigma^3 - \sigma^2 \left(\sigma_x + \sigma_y + \sigma_z\right) + \sigma \left(\sigma_x \sigma_y + \sigma_x \sigma_z + \sigma_y \sigma_z - \tau_{xy}^2 - \tau_{yz}^2 - \tau_{zx}^2\right) - \sigma_x \sigma_y \sigma_z + \sigma_x \tau_{yz}^2 + \sigma_z \tau_{xy}^2 - 2\tau_{xy}\tau_{yz}\tau_{zx} = 0 \\ &\sigma_1 = 0 \\ &\sigma_2 = -10.9611796797792 \end{split}$$

```
\sigma_3 = -114.038820320221
```

7.3.1 Maximum Shear Stress Method

```
[24]: Sy = 350
Sy/(s1 - s3)
```

[24]: 3.06913031033819

7.3.2 Distortion Energy Method

[25]: s_vm = von_mises(s1, s2, s3) Sy/s_vm

[25]: 3.21182027418786

8 Problem 5-12

8.1 Given

A ductile material has the properties $S_{yt}=60\ ksi$ and $S_{yc}=75\ ksi.$

8.2 Find

Using the ductile Coulomb-Mohr theory, determine the factor of safety for the states of plane stresses,

```
\begin{array}{l} \text{a. } \sigma_x = 25 \ ksi, \, \sigma_y = 15 \ ksi \\ \text{b. } \sigma_x = 15 \ ksi, \, \sigma_y = -15 \ ksi \\ \text{c. } \sigma_x = 20 \ ksi, \, \tau_{xy} = -10 \ ksi \\ \text{d. } \sigma_x = -12 \ ksi, \, \sigma_y = 15 \ ksi, \, \tau_{xy} = -9 \ ksi \\ \text{e. } \sigma_x = -24 \ ksi, \, \sigma_y = -24 \ ksi, \, \tau_{xy} = -15 \ ksi \end{array}
```

8.3 Solution

Using Eq. 5-26, the block below will execute all parameters in a for loop.

8.3.1 Part A

```
\begin{split} \sigma_1 &= 25.0 \\ \sigma_2 &= 15.0 \\ \sigma_3 &= 0 \end{split}
```

n = 2.4

8.3.2 Part B

$$\sigma_1 = 15.0$$

$$\sigma_2 = 0$$

$$\sigma_3 = -15.0$$

n = 2.2222222222222

8.3.3 Part C

 $\sigma_1=24.142135623731$

$$\sigma_2 = 0$$

$$\sigma_3 = -4.14213562373095$$

n = 2.18532709217848

8.3.4 Part D

 $\sigma_1=17.724980739588$

$$\sigma_2 = 0$$

$$\sigma_3 = -14.724980739588$$

n = 2.03355602443072

8.3.5 Part E

$$\sigma_1 = 0$$

$$\sigma_2 = -9.0$$

$$\sigma_3 = -39.0$$

n = 1.92307692307692

Problem 5-19

9.1 Given

A brittle material has properties $S_{ut}=30\ ksi$ and $S_{uc}=90\ ksi.$

$$\sigma_x = 25~ksi,~\tau_{xy} = 15~ksi$$

9.2 Find

Using the Coulomb-Mohr and modified-Mohr methods, determine the factor of safety.

9.3 Solution

The principal stresses are,

$$\sigma_1 = 25.0$$

$$\sigma_2 = 15.0$$

$$\sigma_3 = 0$$

9.3.1 Brittle Coulomb-Mohr

Using Eq. 5-31,

[28]:
$$St = 30$$

 $St/s1$

[28]:

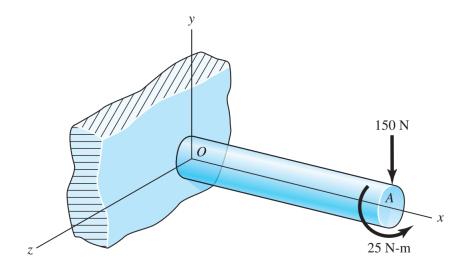
9.3.2 Modified-Mohr

Using Eq. 5-32,

[29]:

10 Problem 5-49

10.1 Given



Cantilevered rod OA is 0.5 meters long and made from AISI 1010 hot-rolled steel. A constant force and torque are applied as shown.

10.2 Find

Determine the minimum diameter for the rod that will achieve a minimum static factor of safety of 2 using,

- a. the maximum shear stress method
- b. the distortion energy method

10.3 Solution

There are three unknowns and adding and two equations for the principal stress as well as an extra equation for the factor of safety. The two principal stress equations with the substitutions for τ_{xy} and σ_x are,

```
eq2 = sp.Eq(sig3, (s_x_/2 - sp.sqrt((s_x_/2)**2 + t_xy_**2)).n())
       display(eq1, eq2)
      \sigma_1 = \frac{784.605560256445}{5}
      \sigma_3 = -\frac{20.6618334153475}{d^3}
      10.3.1 Maximum Shear Stress Method
[31]: Sy = sp.S('180e6') # Table A-20
       eq_mss = sp.Eq(sig1 - sig3, Sy/2)
       eq_mss
[31]: \sigma_1 - \sigma_3 = 90000000.0
[32]: # Solving
       sol = sp.solve([eq1, eq2, eq_mss], dict=True)[0]
       for key, value in sol.items():
            display(sp.Eq(key, value))
      \sigma_1 = 87690748.4122731
      \sigma_3 = -2309251.58772688
      d = 0.0207602478902345
      10.3.2 Distortion Energy Method
[33]: eq_de = sp.Eq(von_mises(sig1, 0, sig3), Sy/2)
       eq de
      0.707106781186548 \left(\sigma_1^2 + \sigma_3^2 + \left(-\sigma_1 + \sigma_3\right)^2\right)^{0.5} = 900000000.0
[33]:
[34]: sol2 = sp.solve([eq1, eq2, eq_de], dict=True)[0]
       for key, value in sol2.items():
            display(sp.Eq(key, value))
```

 $\sigma_1 = 88807873.0461385$

 $\sigma_3 = -2338669.99139147$ d = 0.0206728317903113