## Machine Design Test 2

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```
[1]: # Notebook Preamble
import sympy as sp
import matplotlib.pyplot as plt
from IPython.display import display

plt.style.use('maroon_ipynb.mplstyle')
```

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## 1 Problem 6-4

## 1.1 Given

A steel rotating-beam test specimen has an ultimate strength of 1600 MPa.

#### 1.2 Find

Estimate the life of the specimen if it is tested at a completely reversed stress amplitude of 900 MPa.

## 1.3 Solution

The first step is to find  $S'_e$ .

```
[2]: sig_ar, S_ut = sp.S(900), sp.S(1600)

# Eq. 6-10

S_e_prime = sp.S(700)

S_e_prime # MPa
```

[2]: <sub>700</sub>

The  $S_e'$  value will be used in place of  $S_e$  from Figure 6-23 description. We can use the following relationships to determine N.

$$N = \left(\frac{\sigma_{ar}}{a}\right)^{1/b}$$

$$a = \frac{(fS_{ut})^2}{S_e}$$

$$b = -\frac{1}{3}\log\left(\frac{fS_{ut}}{Se}\right)$$

The value of f is 0.77 from Figure 6-23 (estimated even though it is off the graph).

```
[3]: def log10(x_):
    return sp.log(x_)/sp.log(10)

f = sp.S('0.77')
a = (f*S_ut)**2/S_e_prime
b = -sp.Rational(1, 3)*log10(f*S_ut/S_e_prime)

display(sp.Eq(sp.Symbol('a'), a.n()),
    sp.Eq(sp.Symbol('b'), b.n()))

N = ((sig_ar/a)**(1/b)).n()
N # cycles
```

a = 2168.32

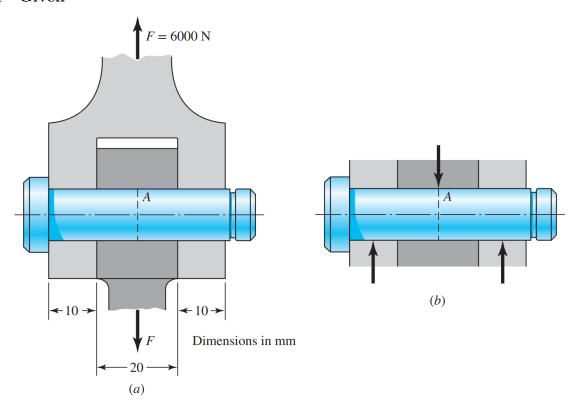
b = -0.0818375559380499

# [3]: 46379.6905856764

The life of the specimen is 46400 cycles.

## 2 Problem 6-11

## 2.1 Given



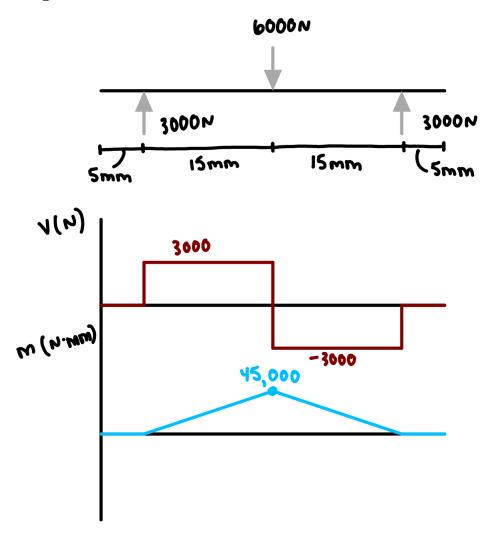
A pin in a knuckle joint is shown in part (a) of the figure above. The joint is subject to a repeatedly applied and released load of 6000 N in tension. Assume the loading on the pin is modeled as concentrated forces as shown in part (b) of the figure. The shaft is made from AISI 1018 hot-rolled steel that has been machined to its final diameter.

## 2.2 Find

Based on a stress element on the outer surface at the cross-section A, determine a suitable diameter of the pin, rounded up to the next mm increment, to provide at least a factor of safety of 1.5 for both infinite fatigue life and for yielding.

## 2.3 Solution

## 2.3.1 Yielding



The equation for the maximum stress may be found using the bending moment diagram above.

[5]:  $\frac{458366.236104659}{d^3}$ 

For yielding,

$$n = \frac{S_y}{\sigma_{max}}$$

```
[6]: eq1 = sp.Eq(sp.S('1.5'), Sy/sig_max)
    display(eq1)
    d_ = sp.solve(eq1)[0]
    display(sp.Eq(d, d_))
```

 $1.5 = 0.000479965544298441d^3$ 

d = 14.6204385310094

So for yielding, a suitable diameter would be  $d = 15 \, mm$ .

#### 2.3.2 Infinite Life

The Goodman method will be used to determine the diameter that results in an infinite life with a factor of safety of 1.5. The relationship for this is,

$$\frac{1}{n_f} = \frac{\sigma_a}{S_e} + \frac{\sigma_m}{S_{ut}}$$

The load is not reversible, but is fluctuating on and off, so the mean stress is positive.

```
[7]: # Getting Se
# Equations come from the road map starting on page 359

S_e_prime = Sut/2

a, b = sp.S('3.04'), sp.S('-0.217') # Table 6-2 (Machined)
k_a = (a*Sut**b).n()
k_b = sp.S('1.24')*d**sp.S('-0.107')

Se = k_a*k_b*S_e_prime
Se
```

[7]:  $\frac{205.436802219618}{d^{0.107}}$ 

```
[8]: # Applying the Goodman relationship
sig_a = sig_m = sig_max/2  # minimum stress is 0
eq1 = sp.Eq(sig_a/Se + sig_m/Sut, 1/sp.S('1.5'))
display(eq1)
d_inf = sp.nsolve(eq1, d, 10)  # Numerical solver
display(sp.Eq(d, d_inf))
```

d = 14.5624553895619

The above equation is complex and the diameter can only be solved using the numerical solver in sympy. The results show that the  $15 \, mm$  diameter should be used for both yielding and infinite life.

## 3 Problem 3-61

#### 3.1 Given

A machine part will be cycled at  $\pm 350\,MPa$  for  $5\cdot 10^3$  cycles. Then loading will be changed to  $\pm 260\,MPa$  for  $5\cdot 10^4$  cycles. Finally, the load will be changed to  $\pm 225\,MPa$ .

$$S_{ut} = 350\,MPA$$
 
$$f = 0.9$$
 
$$S_e = 210\,MPa$$

[9]: Sut, f, Se = 
$$sp.S(530)$$
,  $sp.S('0.9')$ ,  $sp.S(210)$ 

#### 3.2 Find

How many cycles of operation can be expected at this stress level using Miner's method?

#### 3.3 Solution

Minor's method is,

$$\frac{n_1}{N_1} + \frac{n_2}{N_2} + \frac{n_3}{N_3} = 1$$

```
[10]: def get_N(s_max, s_min, f_value, Sut_value, Se_value):
          s_m = (s_max + s_min)/2
          s_a = (s_max - s_min)/2
          s_ar = s_a/(1 - s_m/Sut_value)
          a_ = (f_value*Sut_value)**2/Se_value
          b_ = -sp.Rational(1, 3)*log10(f_value*Sut_value/Se_value)
          N_{-} = (s_{ar}/a_{-})**(1/b_{-})
          return N_.n()
      n1, n2 = sp.S(5e3), sp.S(5e4)
      N1 = get_N(sp.S(350), -sp.S(350), f, Sut, Se)
      N2 = get_N(sp.S(260), -sp.S(260), f, Sut, Se)
      N3 = get_N(sp.S(225), -sp.S(225), f, Sut, Se)
      n3 = sp.Symbol('n_3')
      eq1 = sp.Eq(n1/N1 + n2/N2 + n3/N3, 1)
      display(eq1)
      n3_ = sp.solve(eq1)[0]
      display(sp.Eq(n3, n3_))
```

 $\begin{aligned} &1.78766904825898 \cdot 10^{-6} n_3 + 0.670863205354351 = 1 \\ &n_3 = 184115.060316224 \end{aligned}$ 

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## 4 Problem 8-12

#### 4.1 Given

An  $M14 \times 2$  hex head bolt with a nut is used to clamp together two 15 mm steel plates. There is a 14R metric plain washer under the nut.

### 4.2 Find

- a. Determine a suitable length for the bolt, rounded up to the nearest 5 mm.
- b. Determine the bolt stiffness.
- c. Determine the stiffness of the members.

### 4.3 Solution

## 4.3.1 Part A

The bolt dimensions are found in Table A-31.

```
[11]: 1, H, t = sp.S(30), sp.S('12.8'), sp.S('3.5')
L = 1 + H + t
L # mm
```

[11]: <sub>46.3</sub>

The bolt length is  $50 \, mm$ .

#### 4.3.2 Part B

The fastener stiffness along with more relationships come from Table 8-7.

$$k_b = \frac{A_d A_t E}{A_d l_t + A_t l_d}$$

[12]: 808.240665447356

## 4.3.3 Part C

```
[13]: # Eq. 8-22

x = sp.S('0.5774')

km = (x*sp.pi*E*d)/(2*sp.log(5*(x*(1 + t) + sp.S('0.5')*d)/(x*(1 + t) + sp.S('2. 45')*d)))

km.n() # MN/m
```

[13]: <sub>2968.8853220629</sub>