# ESD Homework 2

# $March\ 7,\ 2022$

```
[1]: import sympy as sp
from msu_esd import parallel_single_pass, counter_single_pass,_

shell_and_tube_one_shell_pass
```

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# 1 Problem 1

# 1.1 Given

Water enters a counterflow, double-pipe heat exchanger at a rate of  $70 \frac{kg}{min}$  and is heated from  $15^{\circ}C$  to  $60^{\circ}C$  by an oil with a specific heat of  $1.9 \frac{kJ}{kg K}$ . The oil enters at  $116^{\circ}C$  and leaves at  $27^{\circ}C$ . The overall heat transfer coefficient is  $300 \frac{W}{m^2 K}$ 

#### 1.2 Find

- a. What heat transfer area is required?
- b. What area is required if all conditions remain the same except that a shell and tube heat exchanger is used, with the water making one shell pass and the oil making two tube passes?
- c. What exit water temperature would result if, for the exchanger of part (a), the water flow rate were decreased to  $50 \frac{kg}{min}$

#### 1.3 Solution

The specific heat of water will be taken at the average temperature of the water entrance and exit  $(C_p = 4.18 \frac{kJ}{kqK})$ 

# 1.3.1 Part A

The oil is the hot fluid and the water is the cold fluid. The condition is unmixed because the fluids never meet.

[2]: 
$$C_c (-T_{c,in} + T_{c,out}) = C_h (T_{h,in} - T_{h,out})$$

[3]: 
$$\frac{C_c \left(-T_{c,in} + T_{c,out}\right)}{T_{h,in} - T_{h,out}}$$

```
[4]: # Solving for Cc

Cc_ = mc_*Cp_c_

Cc_ # kJ per (min deg C)
```

[4]: 292.5999999999997

[5]: 147.94382022471908

[6]: 147.94382022471908

[7]: 13166.99999999998

[8]: 14942.325842696626

[9]: 0.881188118813

[10]: 0.5056179775280899

[11]: 3.11590019646128

The NTU relationship is,

$$NTU = \frac{UA}{C_{min}} \rightarrow A = NTU \frac{C_{min}}{U}$$

```
[12]:  # Finding the area (unit manipulation added)

A_ = ntu_*C_min_/U_*1000/60

A_ # m^2
```

[12]: 25.609898805746354

# 1.3.2 Part B

Everything is the same except a different correlation is used to determine the NTU value. The correct correlation is equation 2-30 in the book, which is a single shell pass and some multiple of 2 tube passes.

```
[13]: ntu_ = shell_and_tube_one_shell_pass(epsilon_, C_)
ntu_
```

C:\Users\gmbra\Downloads\Senior First Semester\ESD\Homework
2\msu\_esd\ntu\_effectiveness.py:61: RuntimeWarning: invalid value encountered in
log

```
ntu_func = lambda e: np.log((C*e - e*np.sqrt(C**2 + 1.0) + e - 2.0)/(C*e + e*(C**2 + 1.0)**0.5 + e - 2.0))/np.sqrt(
```

[13]: nan

There is no such value of NTU, indicating that this scenario is not possible.

# 1.3.3 Part C

The area is the same, but the heat transfer could be different. We can solve for NTU first, then get the effectiveness. It is also assumed that the inlet temperature of water and hot fluid temperatures (oil) are the same along with the  $C_h$  value for the oil.

```
[14]: # Get the new capacity for the water
Cc_ = Cp_c_*50
Cc_ # kJ per (min*deg C)
```

[14]: 209.0

Because the value of  $C_c$  is still greater than the value of  $C_h$ , the heat transfer is the same. The steps for finding the value of NTU and continuing will result in the same q.

```
q = C_c (T_{out} - T_{in})_c
```

```
[15]: # Solve for the water exit
Tc_out_ = q_act_/Cc_ + Tc_in_
Tc_out_ # deg F
```

[15]: 78.0

#### 1.4 Answer

a. 
$$A = 25.6m^2$$

- b. Not Possible c.  $T_{c,out} = 78^{\circ}C$

# 2 Problem 2

#### 2.1 Given

The attributes of the inlet streams to a heat exchanger are,

Stream	Inlet Temperature (° $F$ )	Capacity $(\frac{Btu}{hr \circ F})$
Hot	600	50,000
Cold	500	25,000

The UA product in  $\frac{Btu}{hr \circ F}$  for the heat exchanger is given by,

$$UA = \frac{1}{\frac{0.12}{C_b^{0.8}} + \frac{0.06}{C_c^{0.8}} + 2 \times 10^{-7}}$$

where  $C_h$  and  $C_c$  are the capacities in  $\frac{Btu}{hr \circ F}$ .

# 2.2 Find

Using only the NTU method,

- a. Find the outlet temperatures and rating for a parallel flow arrangement
- b. Find the outlet temperatures and rating for a counter flow arrangement
- c. Find the outlet temperatures and rating if two of these heat exchangers are placed in series and are operated in a parallel flow arrangement. What are the interface temperatures?
- d. Find the outlet temperatures and rating if two of these heat exchangers are placed in series and operated in a counterflow arrangement. What are the interface temperatures?
- e. Based ont he results of the above, discuss the utility of placing parallel and counterflow heat exchangers in series.

# 2.3 Solution

[16]: 
$$\frac{1}{\frac{0.06}{C_c^{0.8}} + \frac{0.12}{C_b^{0.8}} + 2.0 \cdot 10^{-7}}$$

```
[17]: UA_ = float(UA.subs([(Cc, Cc_), (Ch, Ch_)]))
UA_ # In Btu per (hr*deg F)
```

[17]: 25457.073923275435

```
[18]:  # Find NTU

C_min_ = min([Cc_, Ch_])

NTU_ = UA_/C_min_

NTU_
```

[18]: 1.0182829569310174

```
[19]: # Get the C_value

C_ = C_min_/max([Cc_, Ch_])

C_
```

[19]: 0.5

#### 2.3.1 Part A

We know the NTU value and C, which is enough to solve for the effectiveness.

```
[20]: # Get the effectiveness/rating
# Assuming a one pass parallel
parallel_effectiveness = parallel_single_pass(NTU_, C_, find='e')
parallel_effectiveness
```

[20]: 0.5219372748457521

```
[21]:  # Find q max

q_max_ = C_min_*(Th_in_ - Tc_in_)

q_max_ # Btu per hr
```

[21]: 2500000

```
[22]: # Find the actual q
q_act_A = q_max_*parallel_effectiveness
q_act_A # In btu per hour
```

[22]: 1304843.1871143803

```
[23]: # Find cold outlet temperature
Tc_out_A = q_act_A/Cc_ + Tc_in_
Tc_out_A # deg F
```

[23]: 552.1937274845752

```
[24]: # Find the hot outlet temperature
Th_out_A = Th_in_ - q_act_A/Ch_
Th_out_A # deg F
```

[24]: 573.9031362577124

#### 2.3.2 Part B

Everything is the same except the effectiveness correlation is different.

```
[25]: # Solving for the effectiveness/rating
counter_effectiveness = counter_single_pass(NTU_, C_, find='e')
counter_effectiveness
```

[25]: 0.5703958472801851

```
[26]: q_act_B = q_max_*counter_effectiveness
q_act_B # Btu per hr
```

[26]: 1425989.6182004628

```
[27]: # Find cold outlet temperature
Tc_out_B = q_act_B/Cc_ + Tc_in_
Tc_out_B # deg F
```

[27]: 557.0395847280186

```
[28]: # Find the hot outlet temperature
Th_out_B = Th_in_ - q_act_B/Ch_
Th_out_B # deg F
```

[28]: 571.4802076359907

#### 2.3.3 Part C

In order to solve this, take the outlet temperatures solved in the previous problems and apply that to the next heat exchanger in the series. The values of NTU, C,  $\xi$ , and UA are all the same because the capacity and conductance does not change. The heat transfer is different across each unit.

```
[29]: # From the part A in deg F
Tc_in_ = Tc_out_A
Th_in_ = Th_out_A

q_max_ = C_min_*(Th_in_ - Tc_in_)
q_max_ # Btu per hr
```

[29]: 542735.2193284292

```
[30]: q_act_C = parallel_effectiveness*q_max_
q_act_C # Btu per hr
```

[30]: 283273.7413390919

```
[31]: Tc_out_ = q_act_C/Cc_ + Tc_in_
Tc_out_ # deg F
```

[31]: 563.5246771381389

```
[32]: Th_out_ = Th_in_ - q_act_C/Ch_
Th_out_ # deg F
```

[32]: 568.2376614309305

#### 2.3.4 Part D

The process is the same as Part C.

```
[33]: # From the part B in deg F
Tc_in_ = Tc_out_B
Th_in_ = Th_out_B

q_max_ = C_min_*(Th_in_ - Tc_in_)
q_max_ # Btu per hr
```

[33]: 361015.57269930426

```
[34]: # Get the actual heat across the second unit
q_act_D = q_max_*counter_effectiveness
q_act_D # Btu per hr
```

[34]: 205921.78347116092

```
[35]: Tc_out_ = q_act_D/Cc_ + Tc_in_
Tc_out_ # deg F
```

[35]: 565.276456066865

```
[36]: Th_out_ = Th_in_ - q_act_D/Ch_
Th_out_ # deg F
```

[36]: 567.3617719665675

#### 2.3.5 Part E

Based on the above results, two heat exchangers in series does bring the overall outlet temperatures closer together, but it does increase the power required to obtain this heat transfer. If the total power is the sum of the heat transfers across each unit,

```
[37]: # Power change from parallel arrangement
power_A = q_act_A
power_C = q_act_A + q_act_C
(power_C - power_A)/power_A*100 # %
```

[37]: 21.709408773137167

```
[38]: # Power change from counter flow arrangement
power_B = q_act_B
power_D = q_act_B + q_act_D
(power_D - power_B)/power_B*100 # %
```

#### [38]: 14.440622907972179

For the parallel flow arrangement, there is an additional 21.7% more power lost to heat when utilizing the two heat exchangers in series. For the counter flow arrangement, there is an additional 14.4% more power lost to heat when placing two heat exchangers in series. Therefore, the counter flow arrangement is better than the parallel arrangement because the counter flow requires less power and brings the two outlet temperatures closer together. This is due to the higher effectiveness value for the counter flow arrangement.

It may also be concluded from this analysis that the addition of another heat exchanger does not necessarily double the heat transfer, meaning that the additional heat exchanger does not provide a substantial impact compared to just the one. It may be more beneficial to increase the effectiveness of just one heat exchanger rather than implementing two heat exchangers.

#### 2.4 Answer

- a.  $\xi = 0.522, T_{c,out} = 552.19^{\circ}F, T_{h,out} = 573.90^{\circ}F$ b.  $\xi = 0.570, T_{c,out} = 557.04^{\circ}F, T_{h,out} = 571.48^{\circ}F$
- c. Effectiveness and temperatures at the interface is the same as Part A. Coming out of the second heat exchanger is:  $T_{c,out} = 563.52^{\circ}F$ ,  $T_{h,out} = 568.24^{\circ}F$
- d. The effectiveness and temperatures at the interface is the same as Part B. Coming out of the second heat exchanger is:  $T_{c.out} = 565.28^{\circ}F$ ,  $T_{h.out} = 567.36^{\circ}F$
- e. See above