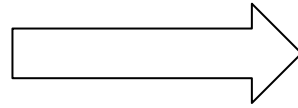


# county-aware redistricting

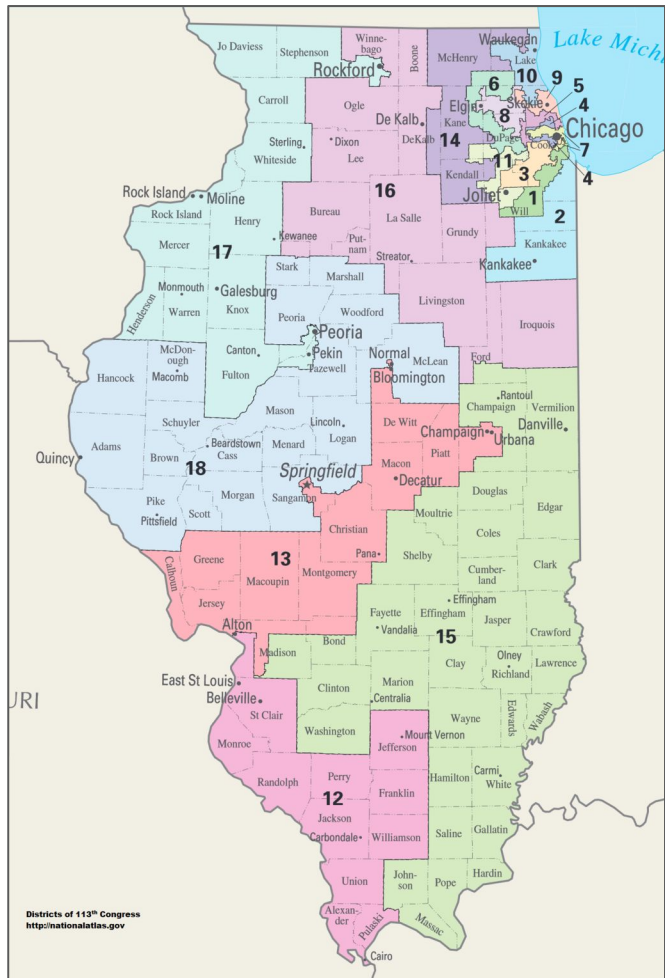
gabe schoenbach

mggg redistricting lab | tufts university | oct. 2021

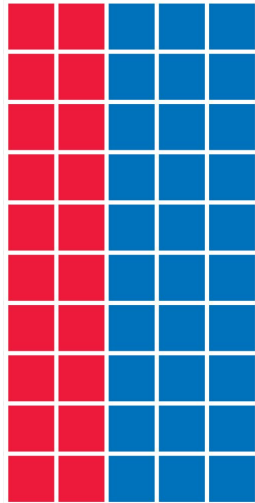
background



# what is redistricting?

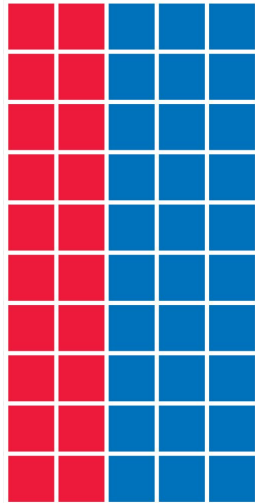


# what is redistricting?

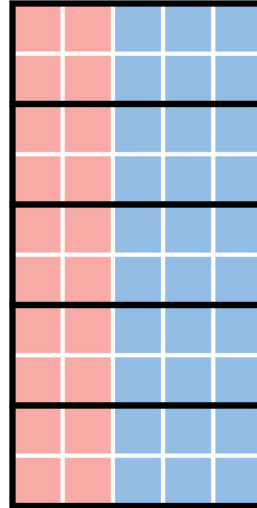


**50 PRECINCTS**  
**60% BLUE**  
**40% RED**

# what is redistricting?

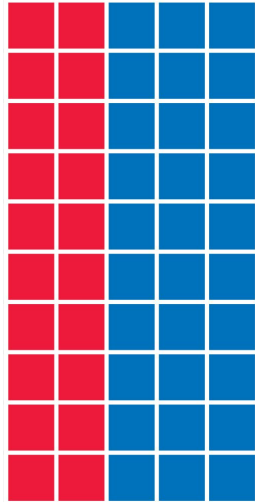


**50 PRECINCTS**  
**60% BLUE**  
**40% RED**

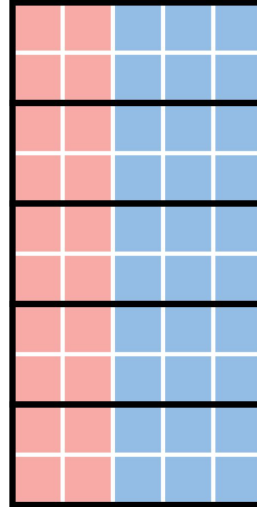


**5 DISTRICTS**  
**5 BLUE**  
**0 RED**  
**BLUE WINS**

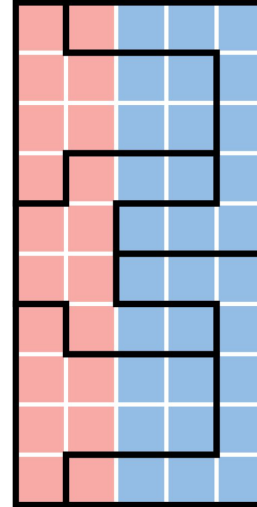
# what is redistricting?



**50 PRECINCTS**  
**60% BLUE**  
**40% RED**



**5 DISTRICTS**  
**5 BLUE**  
**0 RED**  
**BLUE WINS**

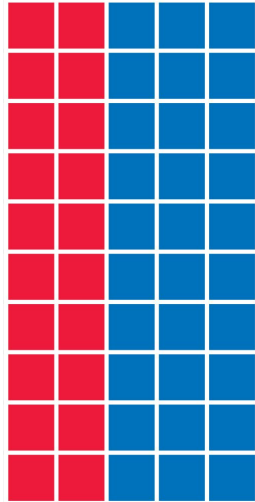


**5 DISTRICTS**  
**3 RED**  
**2 BLUE**  
**RED WINS**

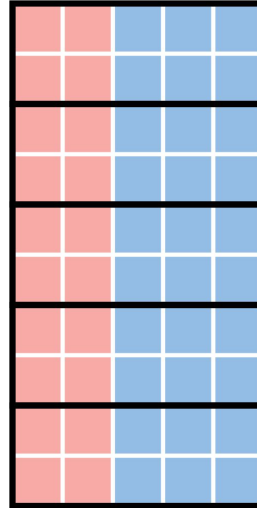
# what is redistricting?

gerrymandering?

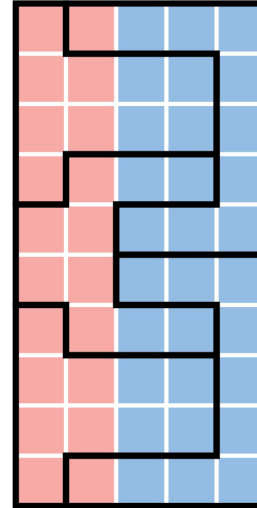
gerrymandering?



**50 PRECINCTS**  
**60% BLUE**  
**40% RED**

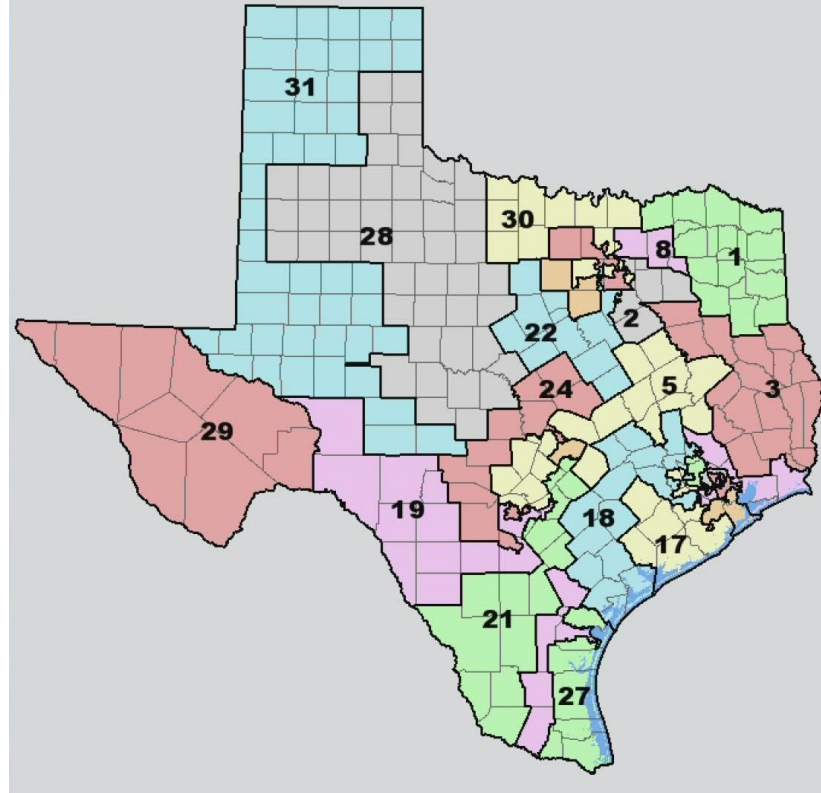


**5 DISTRICTS**  
**5 BLUE**  
**0 RED**  
**BLUE WINS**



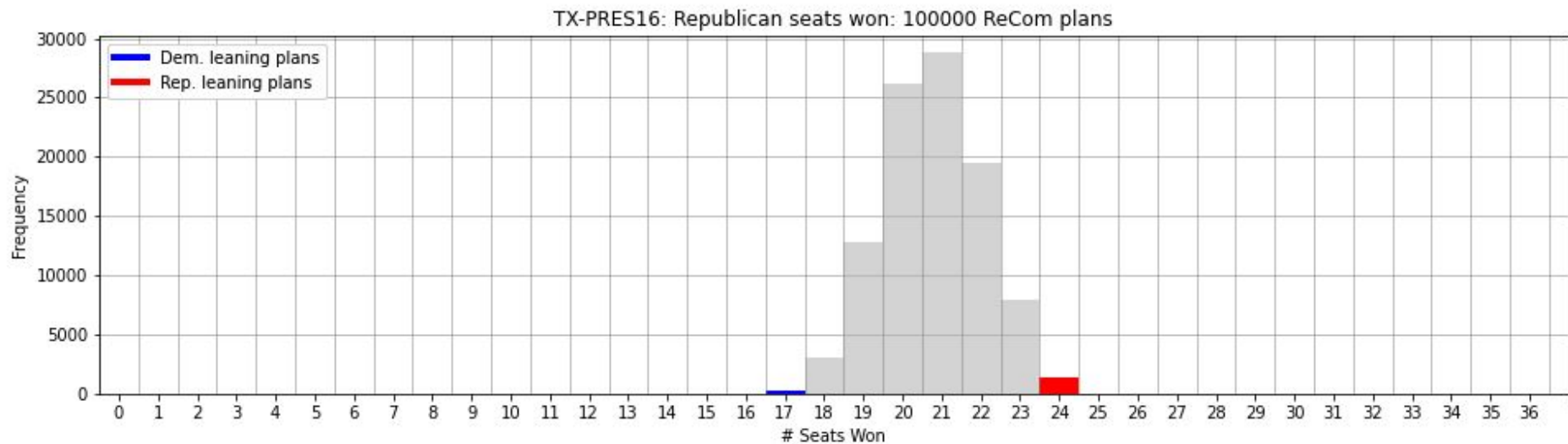
**5 DISTRICTS**  
**3 RED**  
**2 BLUE**  
**RED WINS**

ensemble analysis — putting plans in context

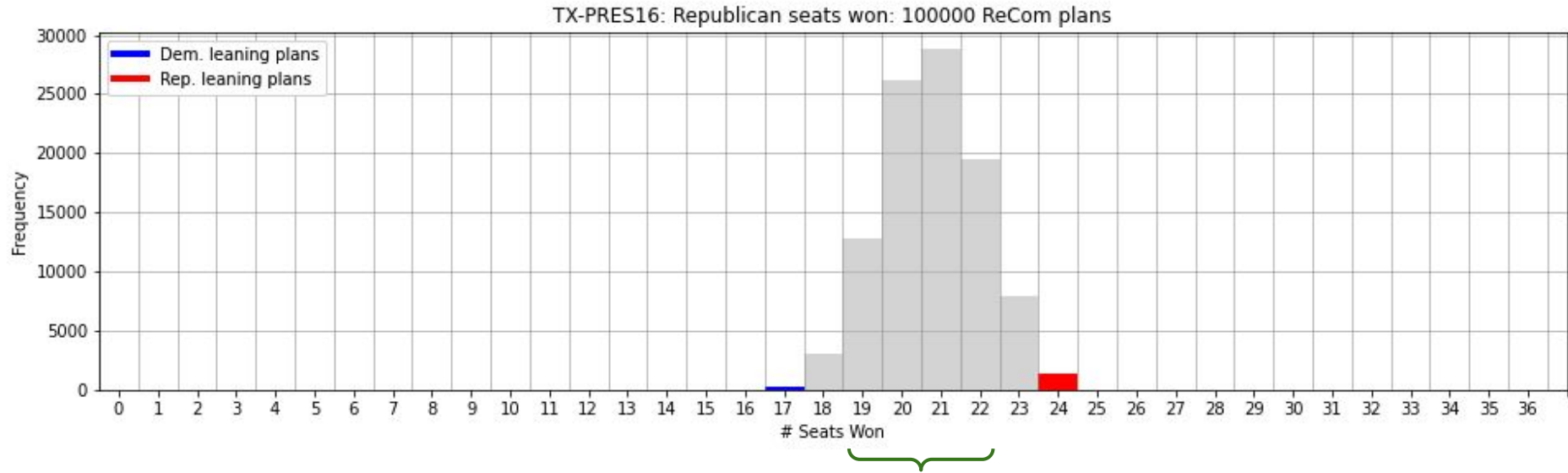




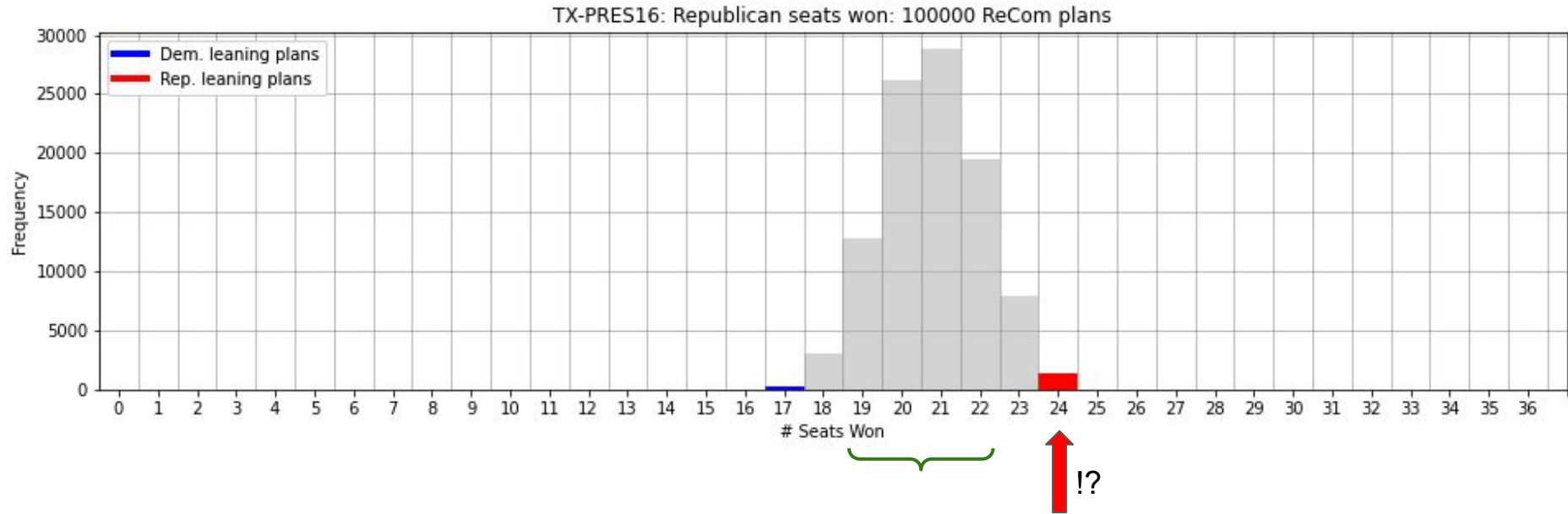
# ensemble analysis — putting plans in context



# ensemble analysis — putting plans in context



# ensemble analysis — putting plans in context



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans
- 6 x 6 grid: 451,206 plans



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans
- 6 x 6 grid: 451,206 plans
- 7 x 7 grid: 158,753,814 plans



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans
- 6 x 6 grid: 451,206 plans
- 7 x 7 grid: 158,753,814 plans
- 8 x 8 grid: 189,497,290,034 plans

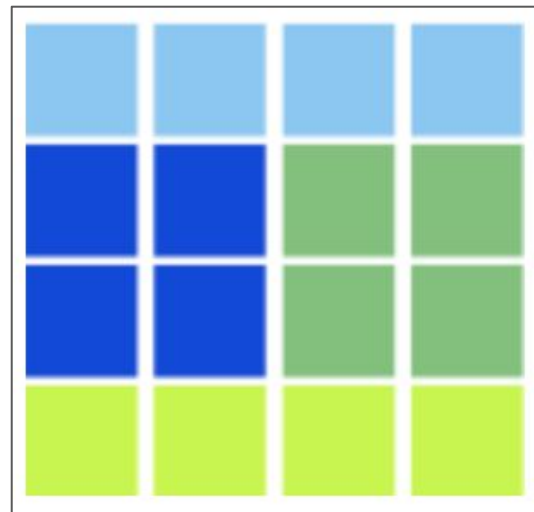




# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans
- 6 x 6 grid: 451,206 plans
- 7 x 7 grid: 158,753,814 plans
- 8 x 8 grid: 189,497,290,034 plans
- 9 x 9 grid: 706,152,947,468,301 plans



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

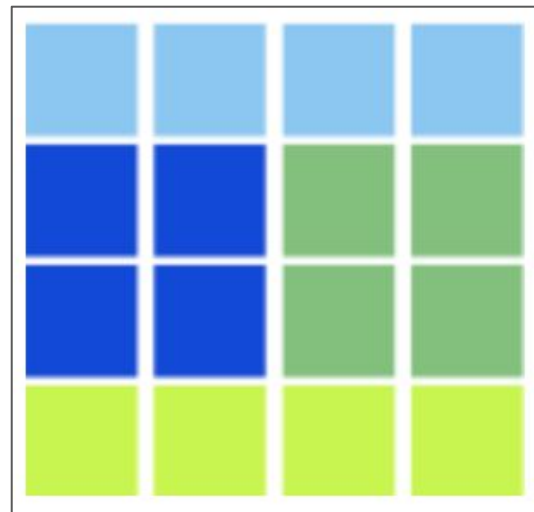
- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans
- 6 x 6 grid: 451,206 plans
- 7 x 7 grid: 158,753,814 plans
- 8 x 8 grid: 189,497,290,034 plans
- 9 x 9 grid: 706,152,947,468,301 plans
- 10 x 10 grid: ???



# ...but how do you make an ensemble?

maybe, use every possible plan that the legislators could have picked, but how many are there?

- 4 x 4 grid: 117 plans (here is one → )
- 5 x 5 grid: 4,006 plans
- 6 x 6 grid: 451,206 plans
- 7 x 7 grid: 158,753,814 plans
- 8 x 8 grid: 189,497,290,034 plans
- 9 x 9 grid: 706,152,947,468,301 plans
- 10 x 10 grid: ???
- **Iowa** (building blocks: counties)



- **Everywhere else** (building blocks: Census blocks)

...but how do you make an ensemble?

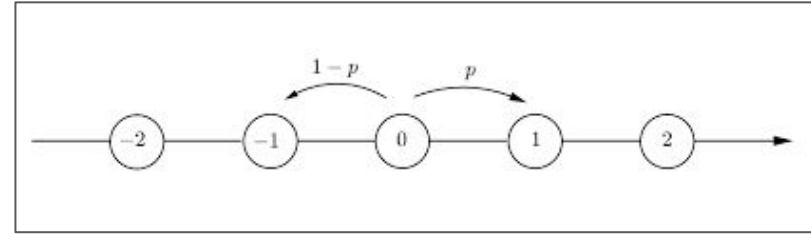
instead, use a **Markov chain** to take a **random walk** on the space of plans

# ...but how do you make an ensemble?

instead, use a **Markov chain** to take a **random walk** on the space of plans

definitions:

- **random walk**: a succession of random steps on some state space
- **Markov chain**: a random walk with no memory

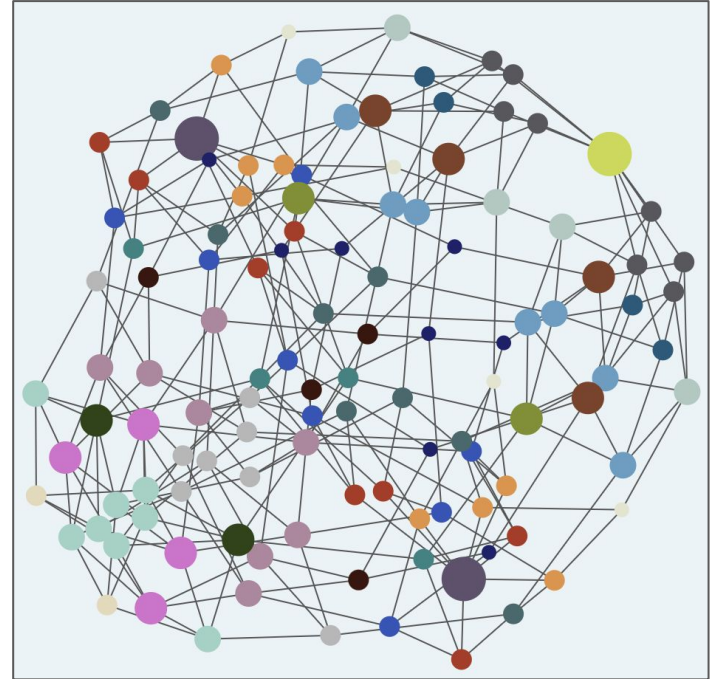


# ...but how do you make an ensemble?

instead, use a **Markov chain** to take a **random walk** on the space of plans

definitions:

- **random walk**: a succession of random steps on some state space
- **Markov chain**: a random walk with no memory
- **graph**: a collection of nodes and edges

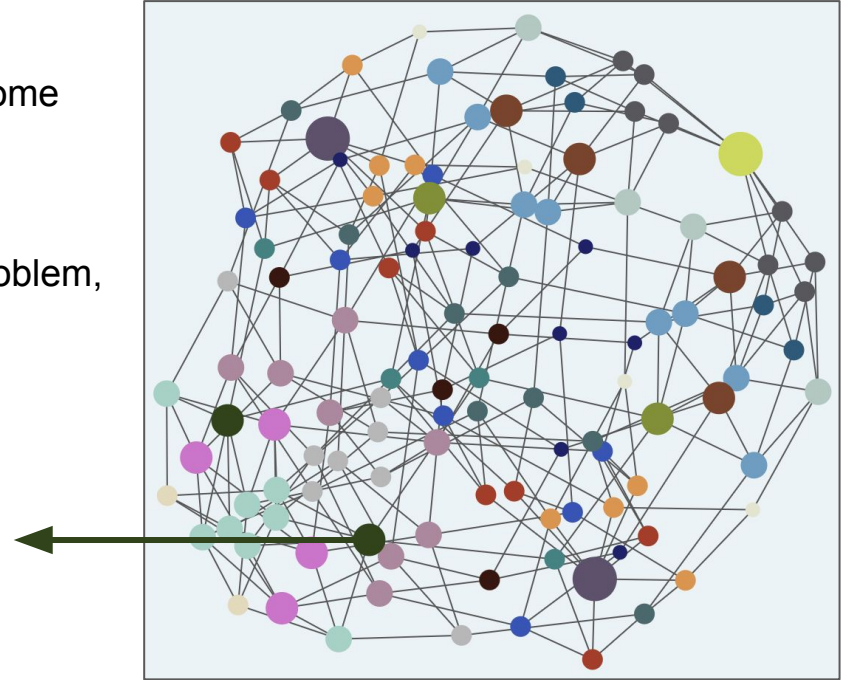


# ...but how do you make an ensemble?

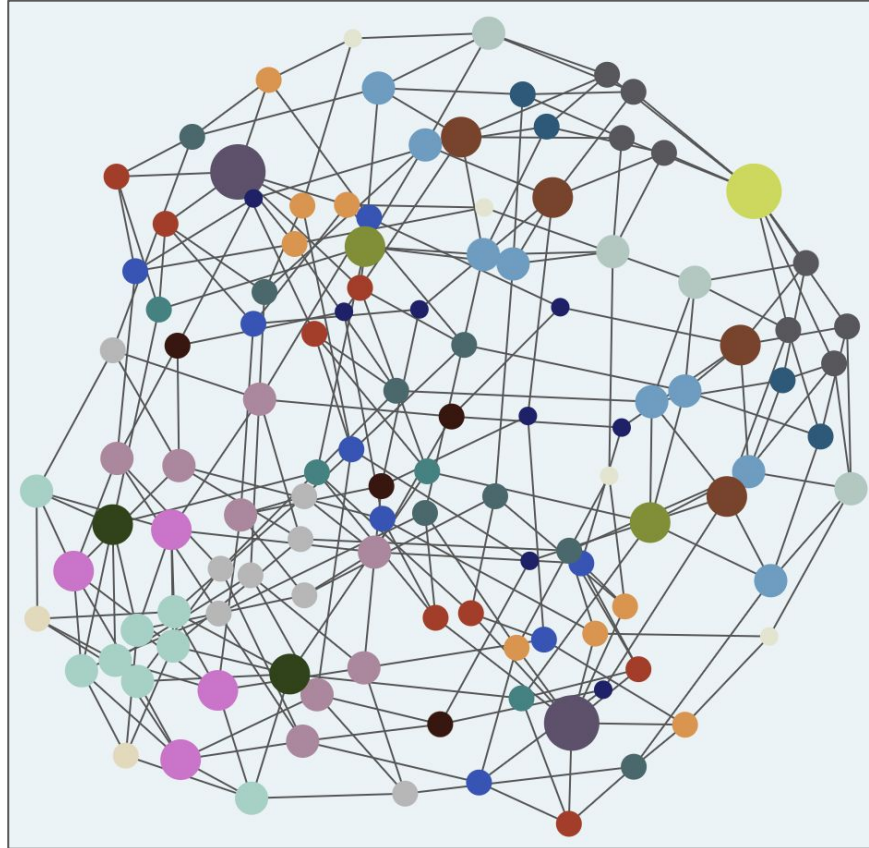
instead, use a **Markov chain** to take a **random walk** on the space of plans

definitions:

- **random walk**: a succession of random steps on some state space
- **Markov chain**: a random walk with no memory
- **graph**: a collection of nodes and edges
- **metagraph**: the state space for our redistricting problem, where each node is a plan

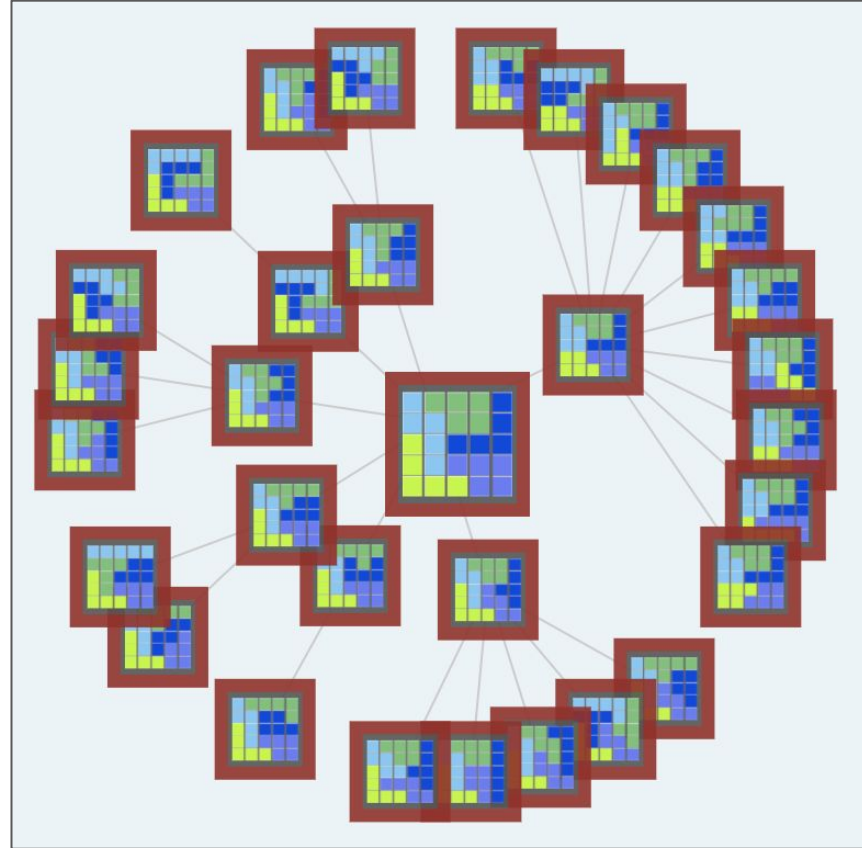


...but how do you make an ensemble?

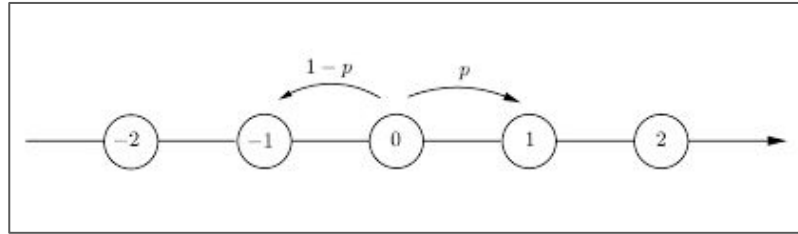




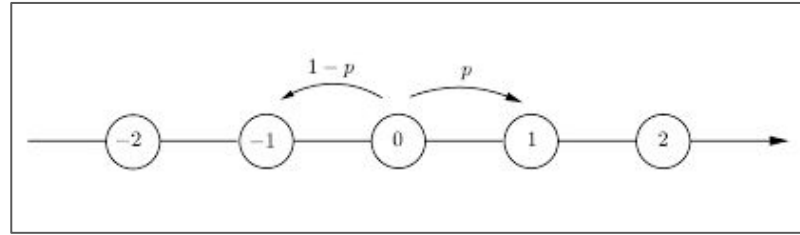
...but how do you make an ensemble?



how do we transition from one plan to another?

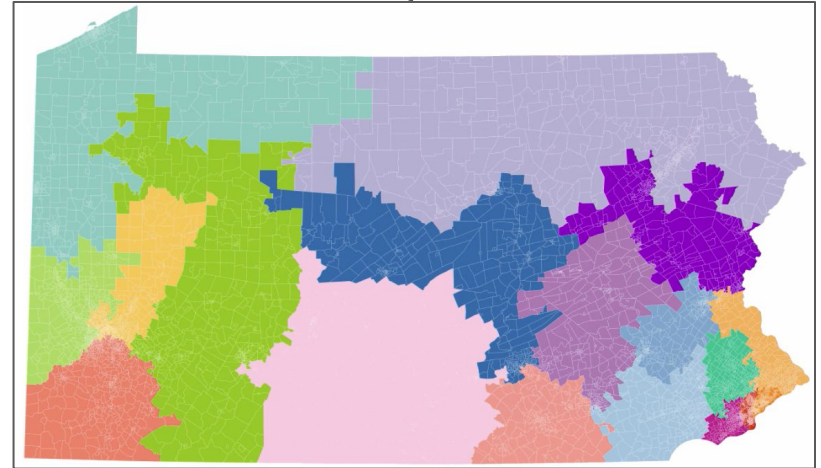
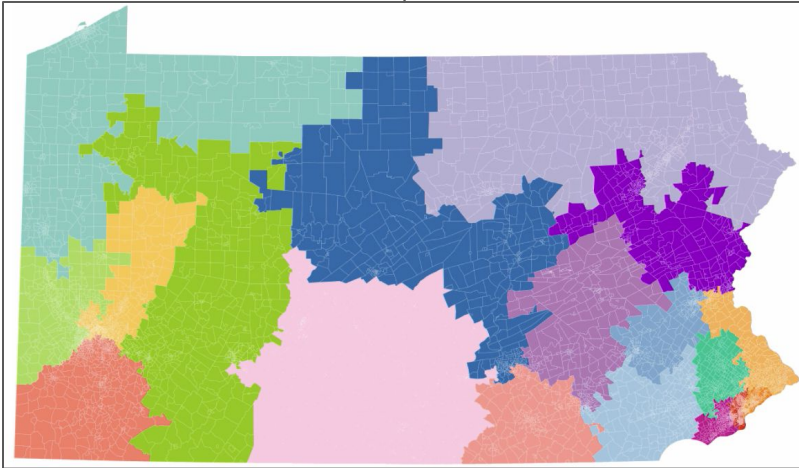


how do we transition from one plan to another?

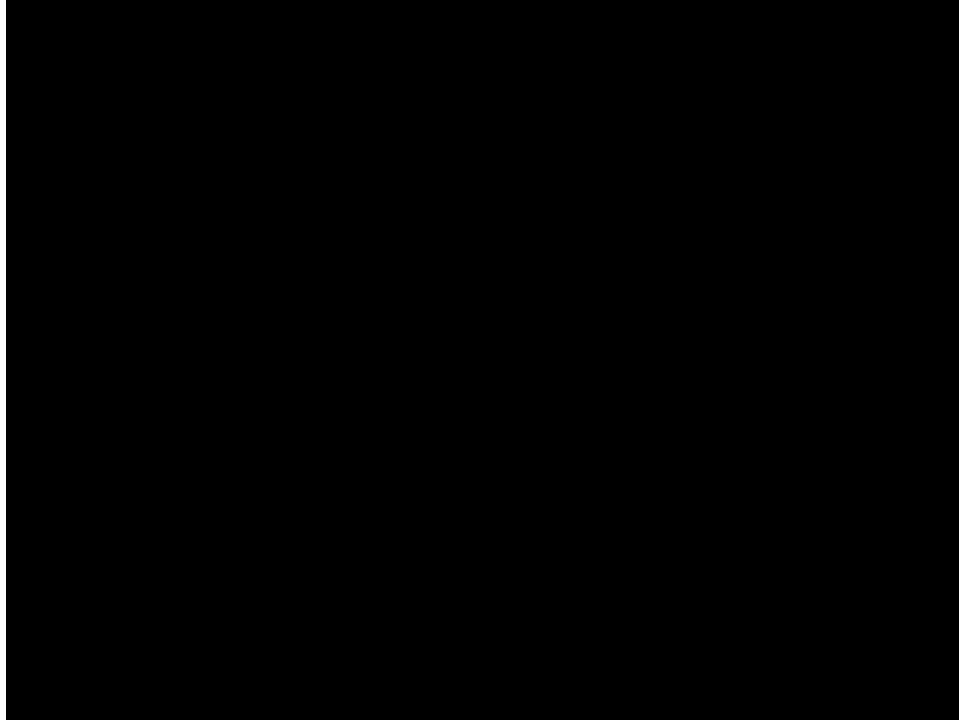


**ReCom**

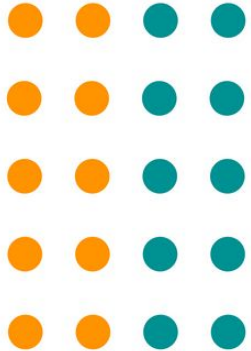
$p$



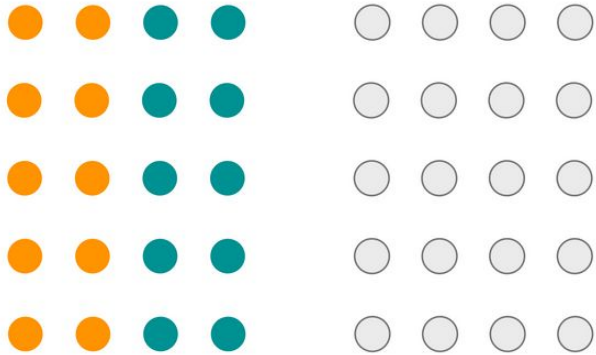
how do we transition from one plan to another?



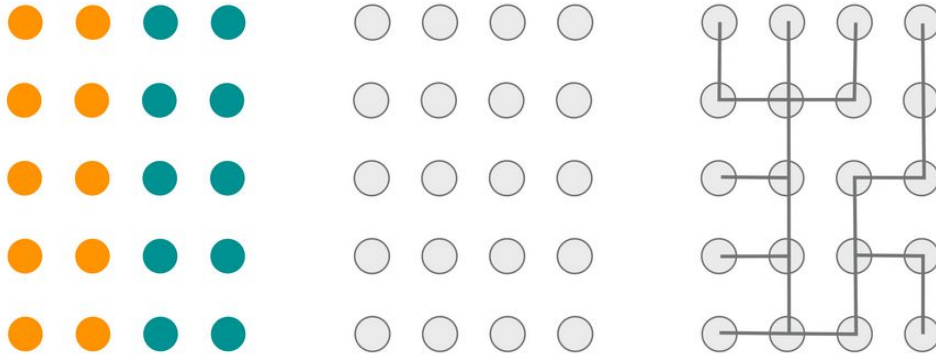
how do we transition from one plan to another?



how do we transition from one plan to another?



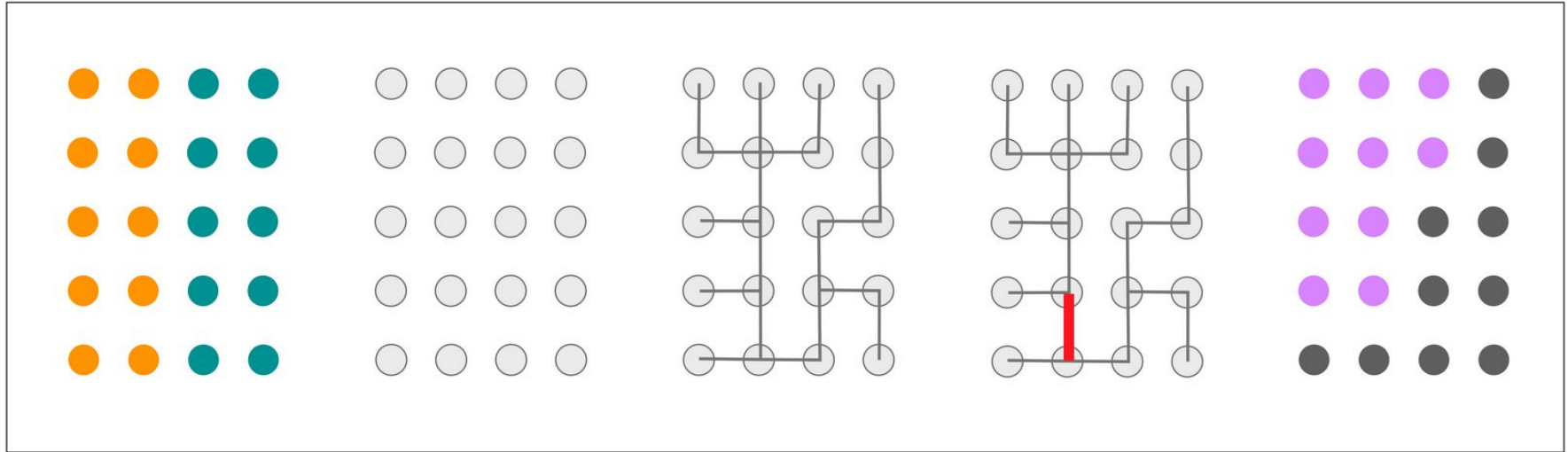
how do we transition from one plan to another?







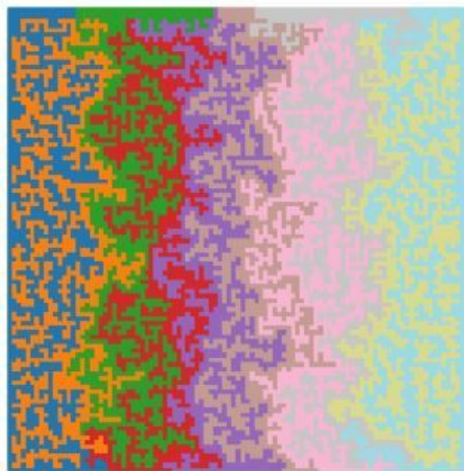
how do we transition from one plan to another?



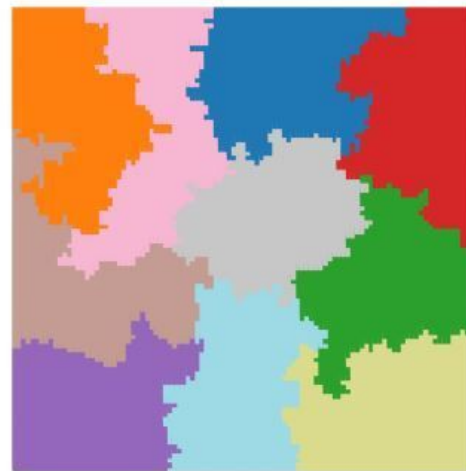
what is our “target” distribution? Not uniform sampling!



Initial Partition

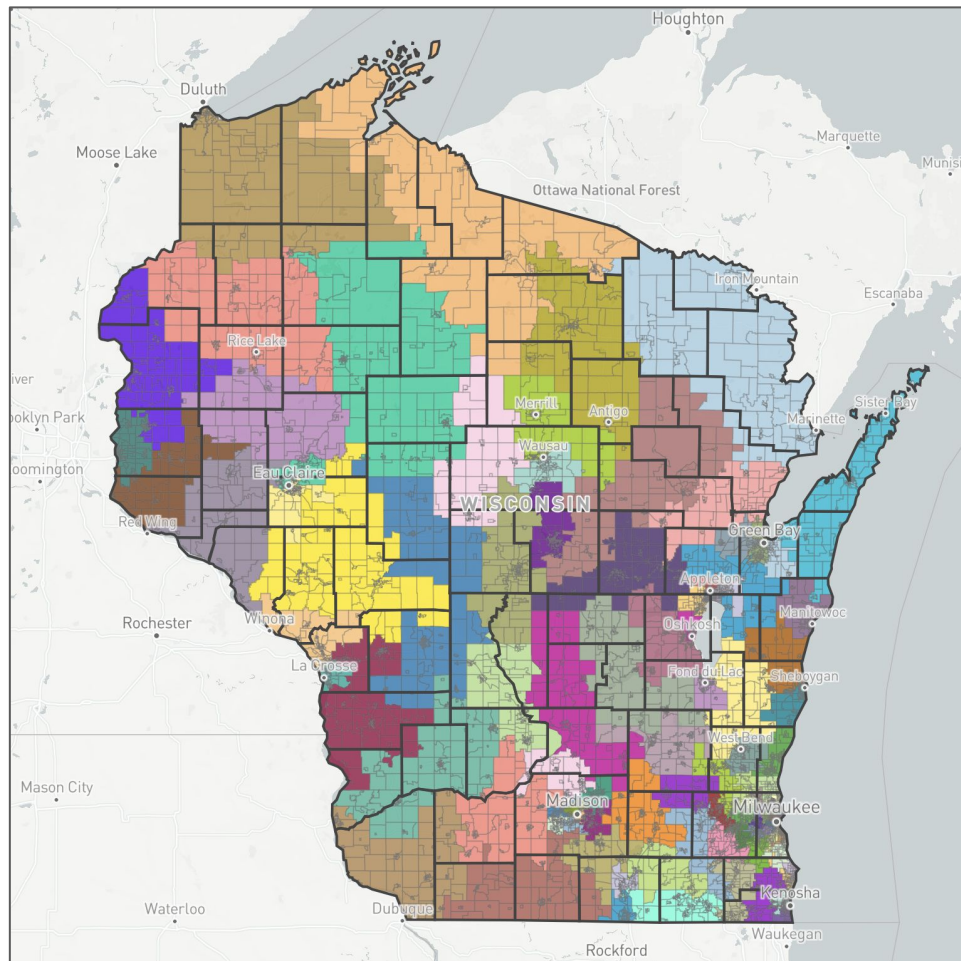


1,000,000 Flip steps



100 ReCom steps

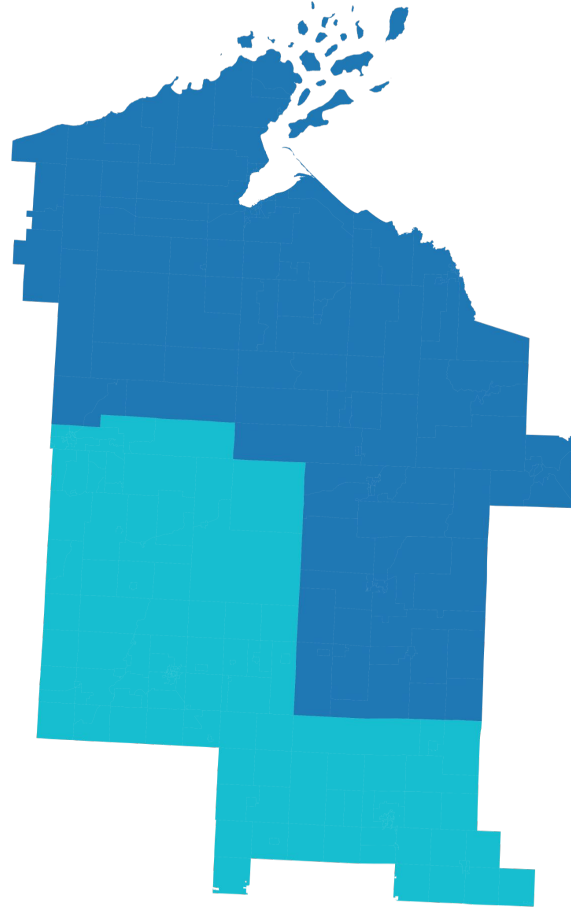
## adding county awareness



# adding county awareness

normal ReCom:

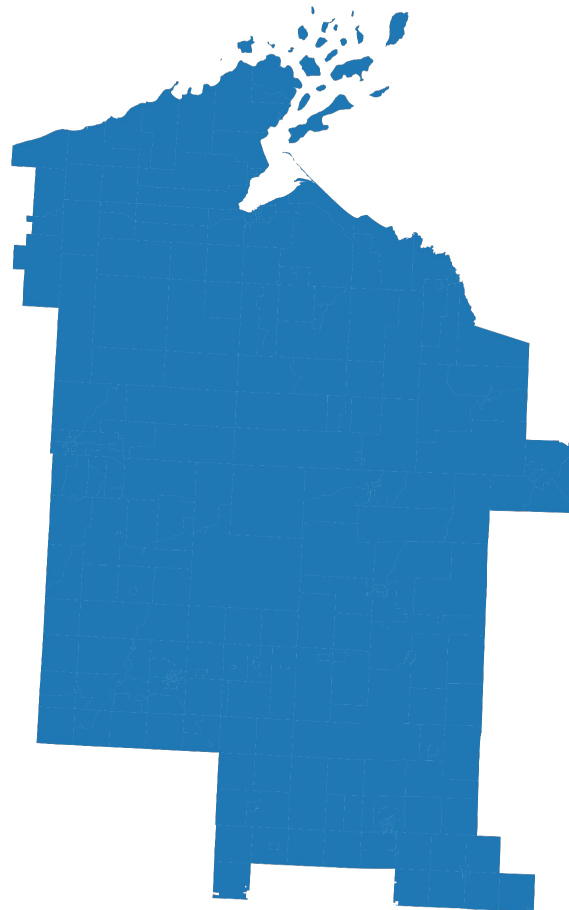
- two original districts



# adding county awareness

normal ReCom:

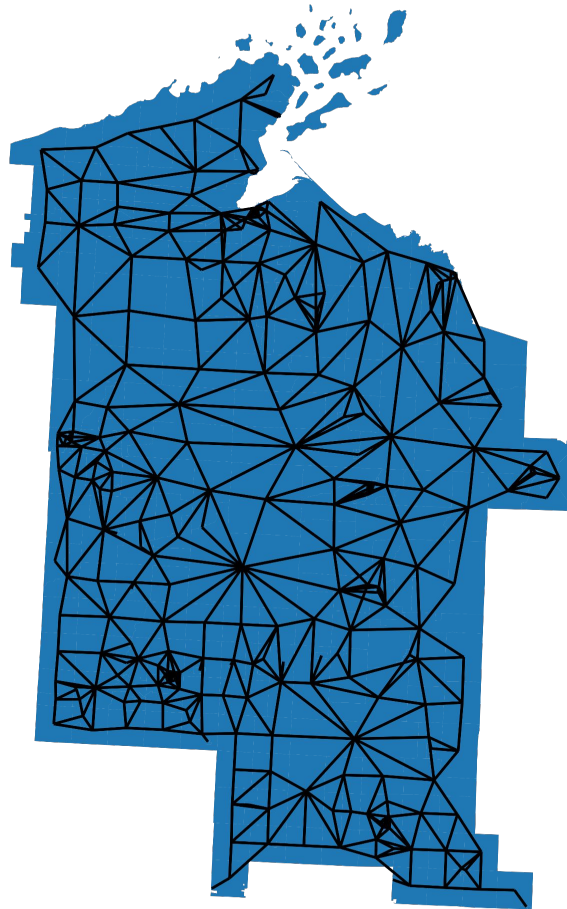
- two original districts
- combine into mega-district



# adding county awareness

normal ReCom:

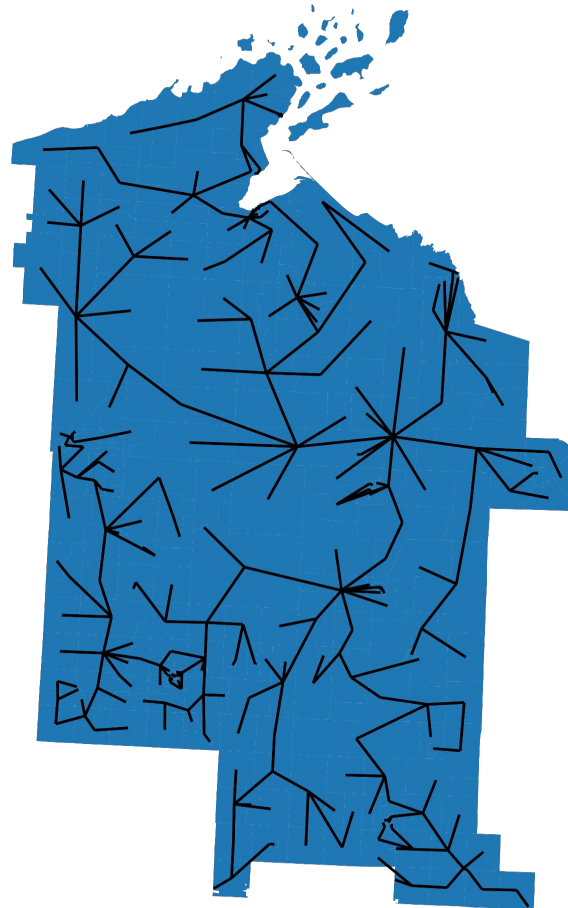
- two original districts
- combine into mega-district
- geographic adjacency graph



# adding county awareness

normal ReCom:

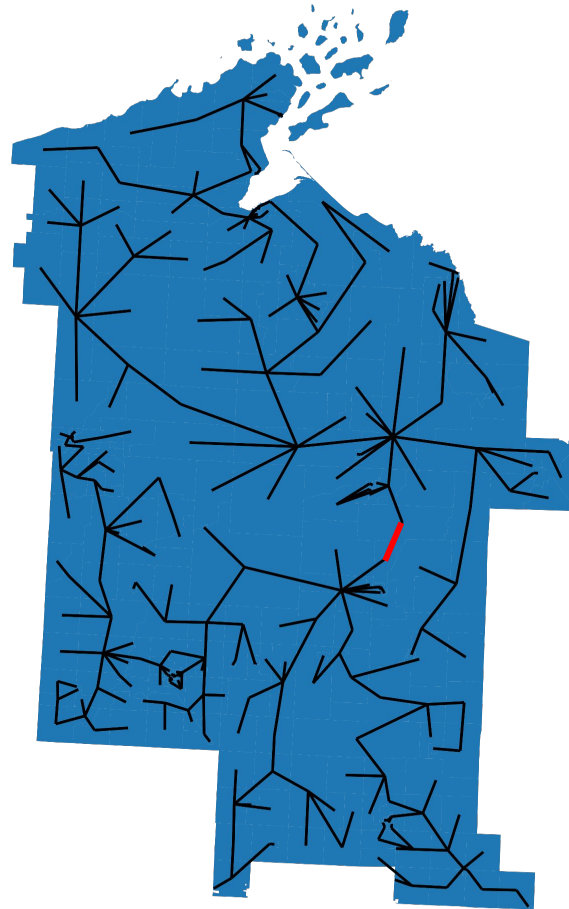
- two original districts
- combine into mega-district
- geographic adjacency graph
- spanning tree



# adding county awareness

normal ReCom:

- two original districts
- combine into mega-district
- geographic adjacency graph
- spanning tree
- cut edge into equal-sized pieces

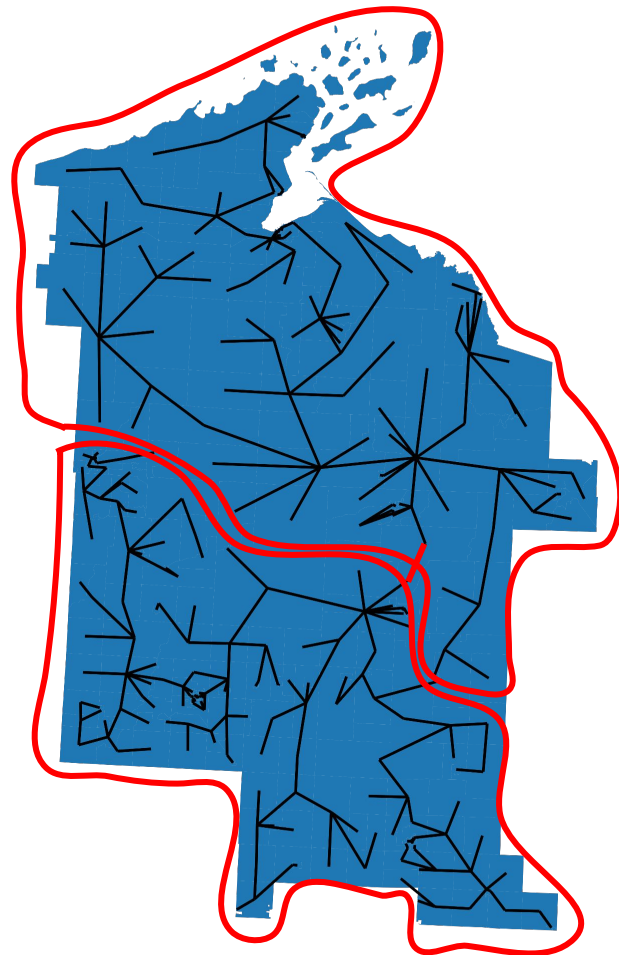




# adding county awareness

normal ReCom:

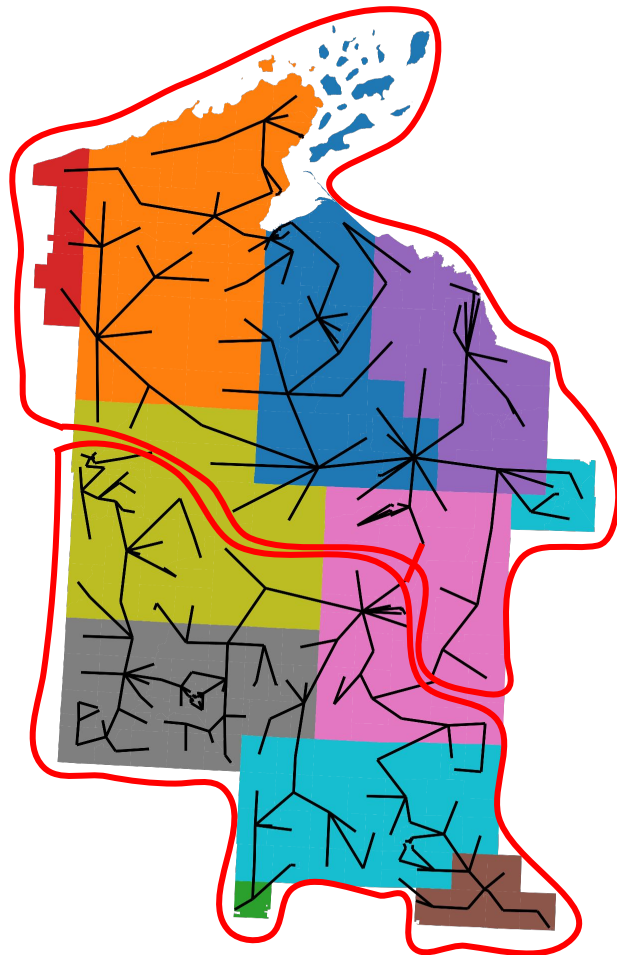
- two original districts
- combine into mega-district
- geographic adjacency graph
- spanning tree
- cut edge into equal-sized pieces



# adding county awareness

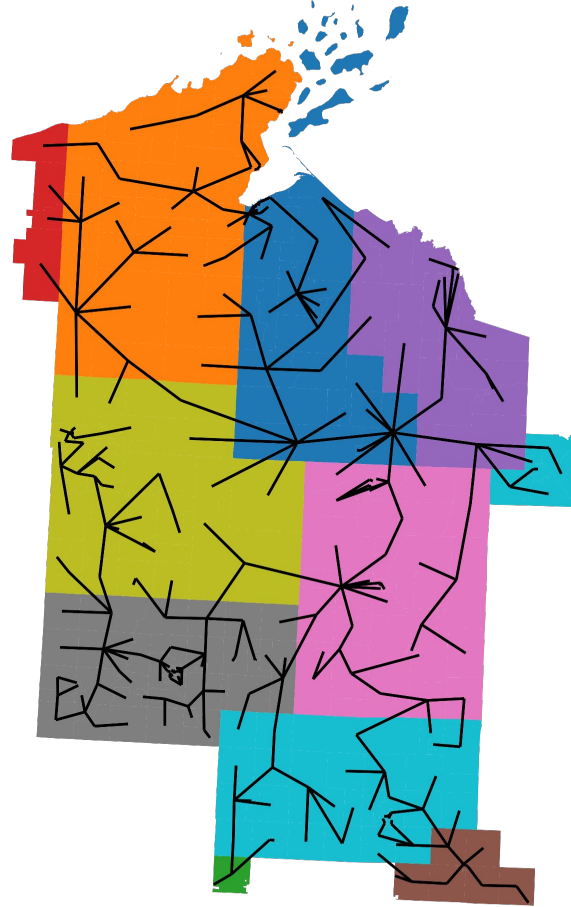
normal ReCom:

- two original districts
- combine into mega-district
- geographic adjacency graph
- spanning tree
- cut edge into equal-sized pieces
- ...but we split counties!



adding county awareness

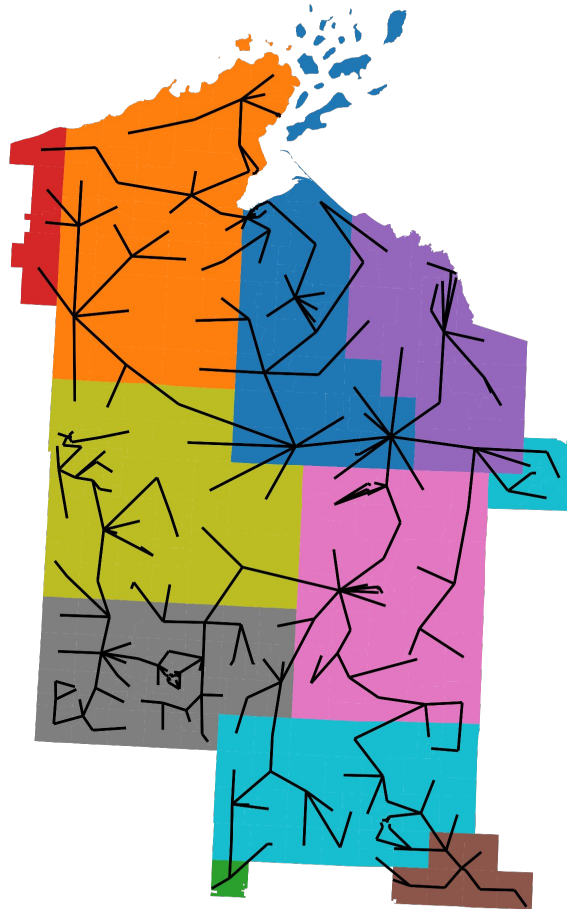
instead...



# adding county awareness

instead...

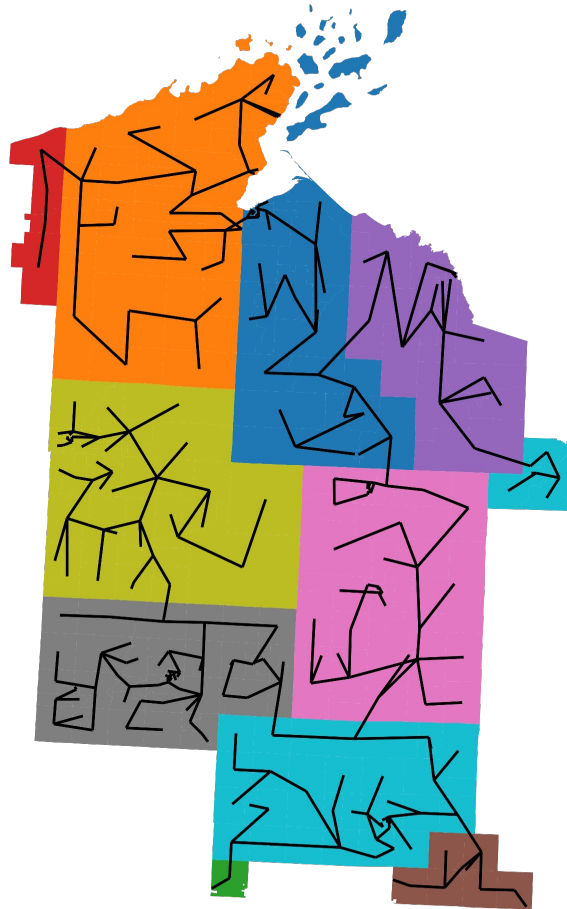
- draw little trees in each county



# adding county awareness

instead...

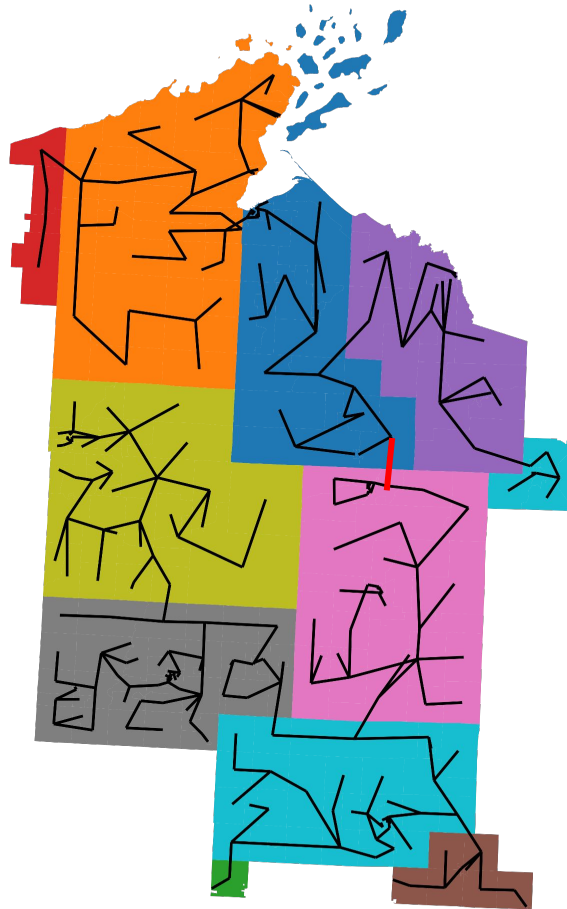
- draw little trees in each county
- connect them up



# adding county awareness

instead...

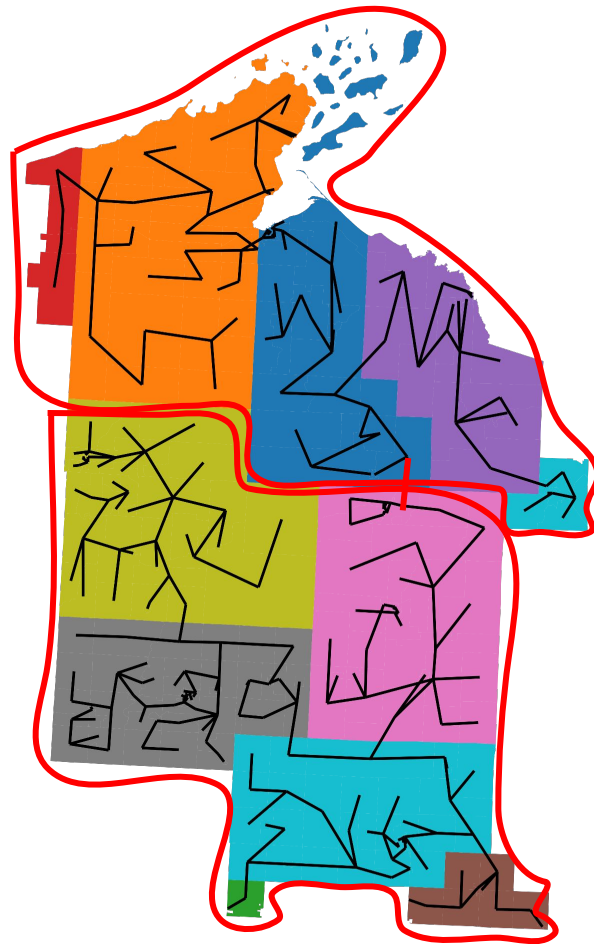
- draw little trees in each county
- connect them up
- try to cut an edge across counties...



# adding county awareness

instead...

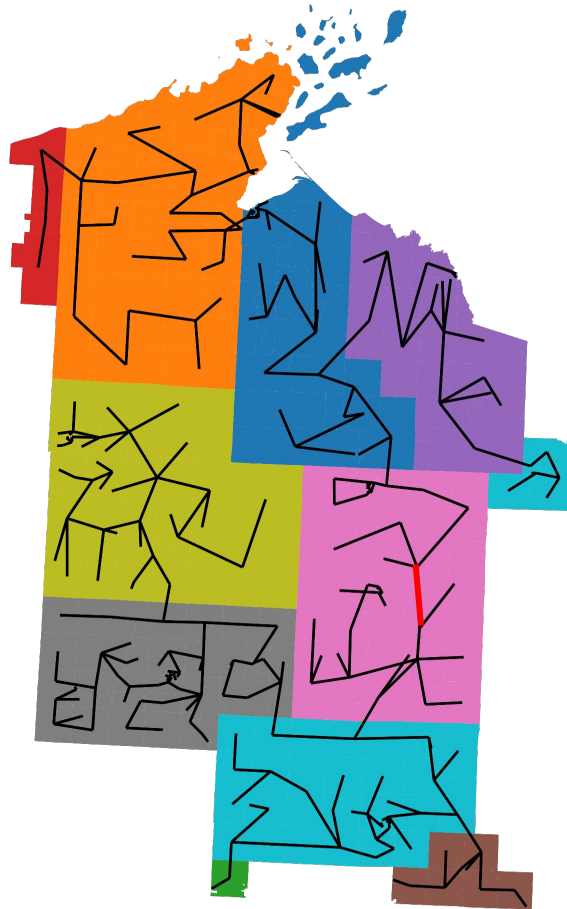
- draw little trees in each county
- connect them up
- try to cut an edge across counties...



# adding county awareness

instead...

- draw little trees in each county
- connect them up
- try to cut an edge across counties...
- but if not, that's okay

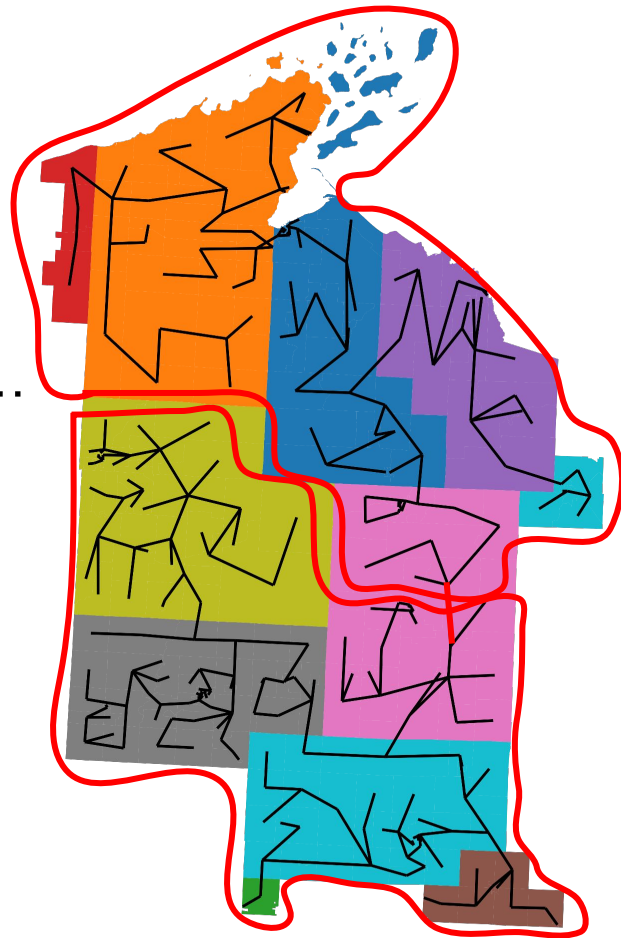




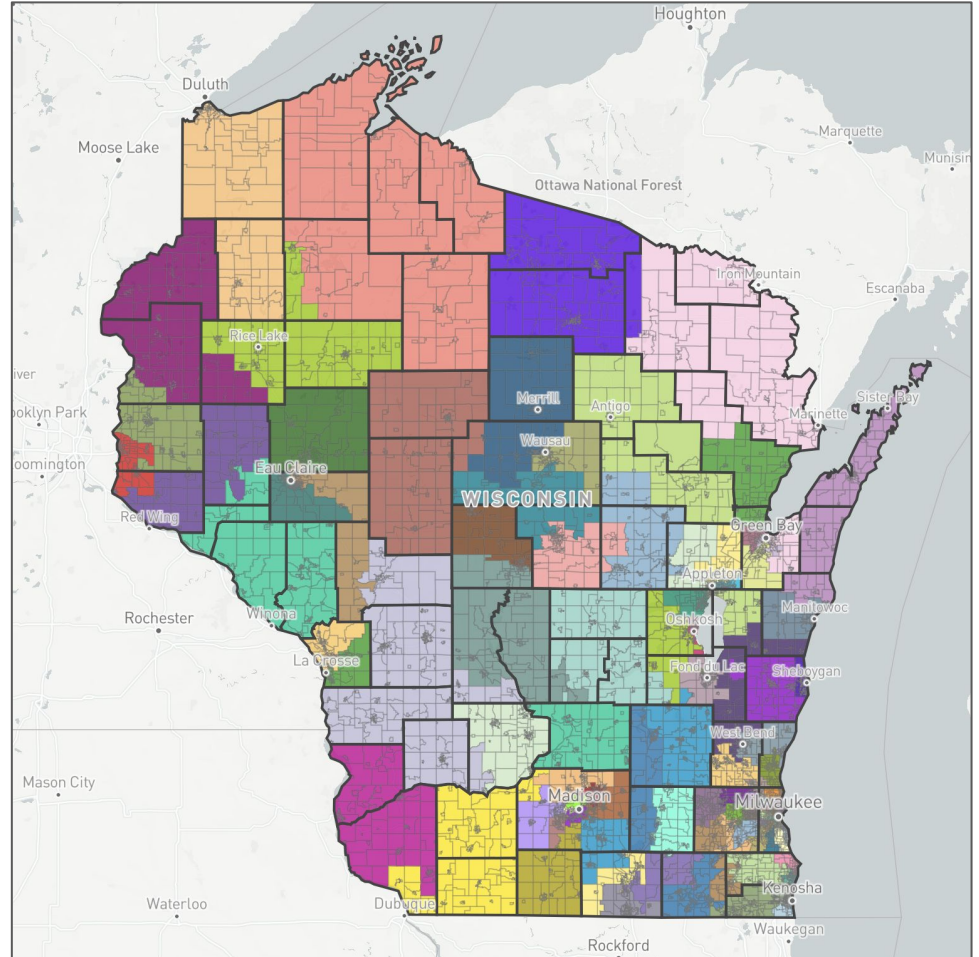
# adding county awareness

instead...

- draw little trees in each county
- connect them up
- try to cut an edge across counties...
- but if not, that's okay

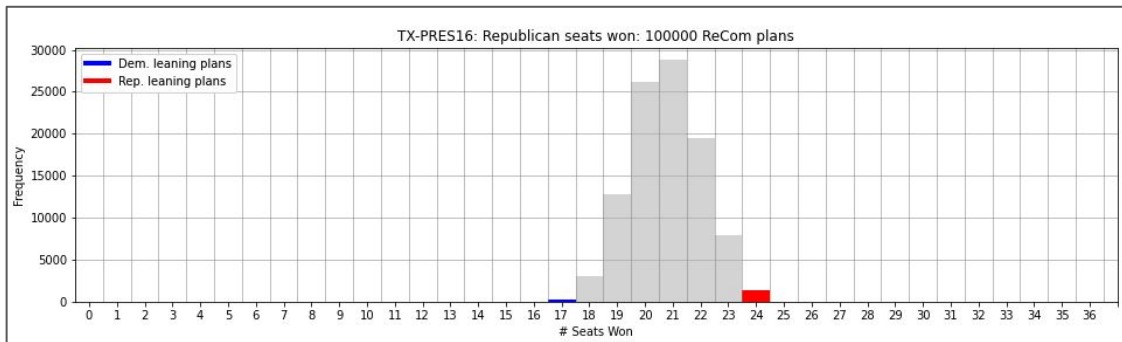
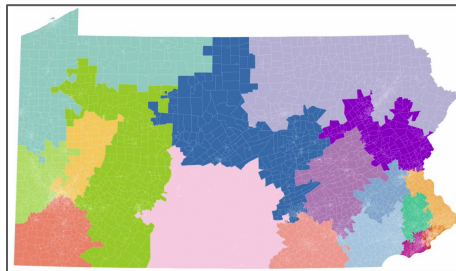
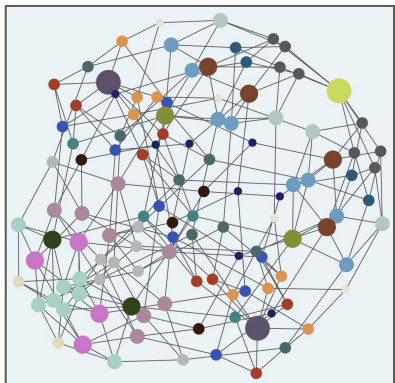


adding county awareness  
the result!



# conclusion

- we use Markov chains to create ensembles of plans
- these ensembles should align with how legislators draw plans
- we can then put proposed plans in context, and spot gerrymandering



# questions?

