```
data_file = 'data_ex1_wt.csv' # absolute path respect to when the script is run
df = pd.read_csv(data_file, header=None, names=['time', 'metric'])
x = df['time'].values
y = df['metric'].values
p = np.polyfit(x, y, m)
yy = np.zeros(len(x))
for j in range(len(p)):
    k = len(p) - j - 1
    yy += p[j] * (x**k)
residuals = y - yy
y = residuals
       return (1/(sigma * np.sqrt(2 * np.pi))) * np.exp( - (x - mu)**2 / (2 * sigma**2))
 def em(data, gaussians, num epochs=90, print every=15):
       #random value in an internval [low, high] - we initialize in this way to speed up the convergence
def get_random(low=-np.std(data), high=np.std(data)):
    return np.random.rand() * (high-low) + low
              for k in range(gaussians):
    print("\tmu", k, "sigma", k, parameters[k][0], parameters[k][1])
print("\Priors: ", priors)
print("\n")
              numerator = f(datapoint, mu, sigma) * priors[i]
denominator = 0
              for k in range(gaussians):
    denominator += f(datapoint, parameters[k][0], parameters[k][1]) * priors[k]
return numerator / denominator
       #Parameters initialization
start1 = np.mean(data)
start2 = np.std(data)
       N = len(data)
               if print_every != 0 and epoch % print_every == 0:
    print("Epoch: ", epoch)
    print_parameters()
```

```
for k in range(gaussians):
                          for i in range(N):
    for k in range(gaussians):
                                                 counts(k) += assignments[i][k]
parameters(k)[0] += assignments[i][k] * data[i]
                          #std dev computation
for i in range(N):
                                     parameters[k][1] /= counts[k]
parameters[k][1] = np.sqrt(parameters[k][1])
                          #update the priors of the gaus
for k in range(gaussians):
    priors[k] = counts[k] / N
  parameters, assignments, priors = em(y, 3, num epochs=150, print every=30)
real_mu1, real_sigma1 = -5, np.sqrt(3)
real_mu2, real_sigma2 = 0, np.sqrt(6)
real_mu3, real_sigma3 = 4, np.sqrt(1)
print("Final mu1, sigma1", parameters[0][0], parameters[0][1])
print("Final mu2, sigma2", parameters[1][0], parameters[1][1])
print("Final mu3, sigma3", parameters[2][0], parameters[2][1])
print("Actual mu1, sigma1", real_mu1, real_sigma1)
print("Actual mu2, sigma2", real_mu2, real_sigma2)
print("Actual mu3, sigma3", real_mu3, real_sigma3)
###PLOTTING THE RESULTS
fig = plt.figure()
 plt.xlabel('Metric values')
plt.ylabel('Density')
points = np.linspace(-11, 11, 1000)
plt.plot(points, list(map(lambda x: f(x, parameters[0][0], parameters[0][1]), points)), color='green', linestyle='dashed')
plt.plot(points, list(map(lambda x: f(x, parameters[1][0], parameters[1][1]), points)), color='orange', linestyle='dashed')
plt.plot(points, list(map(lambda x: f(x, parameters[2][0], parameters[2][1]), points)), color='purple', linestyle='dashed')
plt.plot(points, list(map(lambda x: f(x, real_mul, real_sigma1), points)), color='black')
plt.plot(points, list(map(lambda x: f(x, real_mu2, real_sigma2), points)), color='brown')
plt.plot(points, list(map(lambda x: f(x, real_mu3, real_sigma3), points)), color='gray')
plt.tight_layout()
```