

**Instructions**

- This homework assignment is worth 64 points.
- Please submit either a **.ipynb** file or a **.R** file or a **word** document to Blackboard.
- Please strive for clarity and organization.
- Due Date: September 24, 2021 by 11:59 pm.

**Exercise 1**

Out of 300 students in an Iowa high-school, 95 play cricket only, 120 play football only, 80 play volleyball only and 5 play no games. If one student is chosen at random, find the probability that

- (4 points) the student plays volleyball
- (4 points) the student plays either cricket or volleyball
- (4 points) the student plays neither football nor volleyball.

**Exercise 2**

The seniors from an Ankeny high-school are required to participate in exactly one after-school sport. Data were gathered from a sample of 120 students regarding their choice of sport. The following data were recorded

Gender	Football	Tennis	Basketball	Total
Male	17	8	10	35
Female	31	17	37	85
Total	48	25	47	120

- (6 points) For this group of students, do the data suggest that gender and sports are independent of each other? Justify your answer.
- (6 points) Two students are chosen at random from 120 students. Find the probability that:
  - both play tennis
  - neither play football
- (6 points) One student is chosen at random. What is the probability that the student plays basketball given that the student is female?

**Exercise 3**

(5 points) Events  $A$  and  $B$  are independent. Suppose  $P(B) = 0.6$  and  $P(A \cap B) = 0.12$ . Find  $P(A)$ .

## Exercise 4

The table below shows the number of left and right handed tennis players in a sample of 50 males and females

.58

Gender	Left handed	Right handed	Total
Male	3	29	32
Female	2	16	18
Total	5	45	50

If a tennis player was selected at random from the group, find the probability that the player is

- (a) (4 points) female and right handed
- (b) (4 points) left handed
- (c) (4 points) right handed given that the player selected is male.

Conditional probability formula

## Exercise 5

(6 points) A soccer team wins 60% of its games when it scores the first goal, and 10% of its games when the opposing team scores first. If the team scores the first goal about 30% of the time, what is the probability of winning a game?

## Exercise 6

Cristiano Ronaldo is one of the most popular athletes in the worlds. From 2009 to 2018, he player for Real Madrid. Let  $X$  denote the number of goals that Cristiano scored per game in Real Madrid.

x	0	1	2	3	4	5
$p(X = x)$	0.20	0.45	0.20	0.11	0.03	0.01

- (a) (3 points) Find  $P(X \leq 2)$
- (b) (3 points) Find  $P(X > 1)$
- (c) (5 points) Find  $E(X)$