# Unlinkable Zero-Leakage Biometric Cryptosystem Theoretical Evaluation and Experimental Validation

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#### I. BACKGROUND [2]

Enrolled

template

Enrollment

Verification

template

Secret key

Turbo

encoder

 $QIM^{-1}$ 

Turbo

decoder

Hash

- Biometric Cryptosystems (BC) aim at binding the biometric template to a Pseudonymous Identifier (PI). [1]
- PI: renewable reference that represents an individual.
  - It should not contain any information that allows retrieval of the original biometric sample.
- Here, we focus on *Fuzzy Embedders*:
  - *PI*: hash of an independent key
  - **Auxiliary Data** (*AD*): information that assists the reconstruct the *PI* given a verification biometric sample.
- AD is a (irreversible) function of the enrolled template and the secret key linked to the PI.
- In [2] we proposed the following *Zero-Leakage BC*:

$$x = \Phi(w) = CDF_X^{-1} [CDF_W(w)]$$
$$AD := z \leftarrow [x + s]_{2\pi}$$

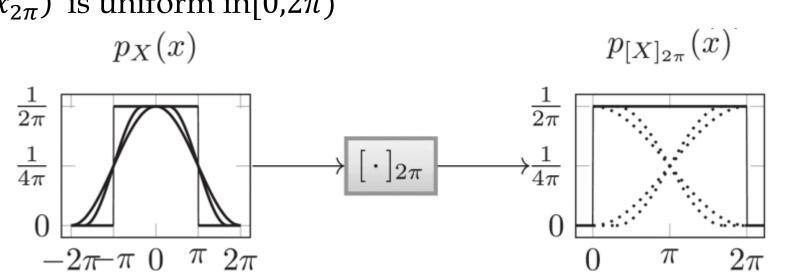
where  $[\cdot]_{2\pi}$  is the modulo- $2\pi$  operator, s is the set of symbols to be embedded encoding the PI, and w is the biometric template (continuous values).

- The pointwise mapping function  $\Phi(w)$  maps the original (population) distribution W to a target X
- The target distribution X is chosen, and so  $\Phi(\cdot)$ , so that:

1. I(S,Z) = 0 i.e., there is no *mutual information* between the *AD* and the *PI*;

2.  $P := \frac{E_{X,Z}\{[x-\hat{x}(z)]^2\}}{E_X\{x^2\}} \to 1$  i.e., the best estimate of x given z is no different from the best estimate we can have a-priori. That is z(x,s) is *irreversible*.

- Condition 1. is satisfied if and only if  $p_X(x_{2\pi})$  is uniform in  $[0,2\pi)$
- Condition 2. is fulfilled by carefully by designing  $\Phi(\cdot)$ :
  - Raised Cosine distribution family.



## II. THE LINKABILITY THREAT

- *Unlinkability:* Two or more biometric references should not be linked to each other or to the subject from whom they were derived <sup>[1]</sup>.
- The described Cryptosystem [2] is vulnerable to a Linkability attack.
- In fact, given a pair of instances of AD  $\{z_i = [x_i + s_i]_{2\pi} \mid i \in (1,2)\},$ 
  - $\Delta z = [z_1 z_2]_{2\pi} = [(x_1 x_2) + (s_1 s_2)]_{2\pi};$
  - If  $x_1$  and  $x_2$  are independent,

 $p_{\Delta Z}(\Delta z)$  is uniform in  $[0,2\pi)$ ;

• If  $x_1$  and  $x_2$  stand from the same subject,

$$|x_1 - x_2| \to 0$$

$$p_{\Delta Z}(\Delta z) \rightarrow p_S(s) = \sum_k P(k) \delta(s - s_k)$$

i.e. it tends to a discrete distribution around the symbols dictionary.

• An attacker may run a simple statistical analysis of the L  $z_1 - z_2$  coefficients to decide if the two AD stem from the same subjects.

### III. THE SOLUTION

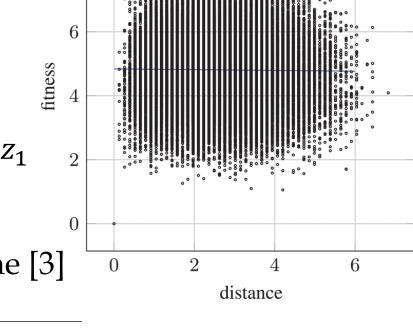
- Add to the chain a unitary matrix  $A \mid A^T A = I$
- $f(\cdot)$  maps W to  $U \sim \mathcal{N}(0, I)$
- Thanks to the rotational symmetry, also  $V \sim \mathcal{N}(0, I)$
- $g(\cdot)$  maps V to the target distribution X
- See sec. I for the rest, except that now  $AD := \{z, A\}$
- Given a properly designed A matrix, it is not possible to distinguish two independent realizations  $(u, u^*) \sim N(0, I) \times N(0, I)$  from the couple (u, Au)
- $(u,u^*)\sim N(0,I)\times N(0,I)$  from the couple (u,Au)• Any randomly rotated instance is undistinguishable from an independently sampled instance.

#### IV. UNLINKABILITY ANALISYS

• Given two sets of  $AD(z_1, A_1)$  and  $(z_2, A_2)$ , if  $w_1 = w_2$ , we can write:

$$[g\{A_2 A_1^T g^{-1}([z_1 + s_1]_{2\pi} - 2\pi \xi_1)\} - z_2]_{\frac{2\pi}{M}} = 0$$

- This is a system of non-linear equations whose unknowns are the coefficients of  $s_i$  and  $\xi_i$ , and whose solution would demonstrate that  $z_1$  and  $z_2$  are linked to the same identity.
- We claim that no algorithm can solve this problem in polynomial time [3]

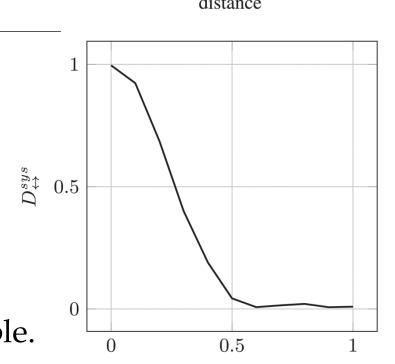


• Another linkability attack consists of estimating the templates from different ADs and trying to match them.

$$\hat{u} = E_{S,\Xi}[A^T g^{-1}([z+s]_{2\pi} - 2\pi\xi)]$$

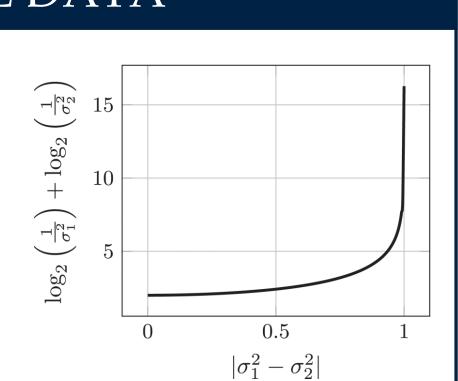
being  $E_{S,\Xi}[\cdot]$  the expected value over all  $(s,\xi)$  couples. $(e.g.\ Monte-Carlo)$ 

• We showed that we can design g so that the likability [4] of  $\hat{u}$  is negligible.

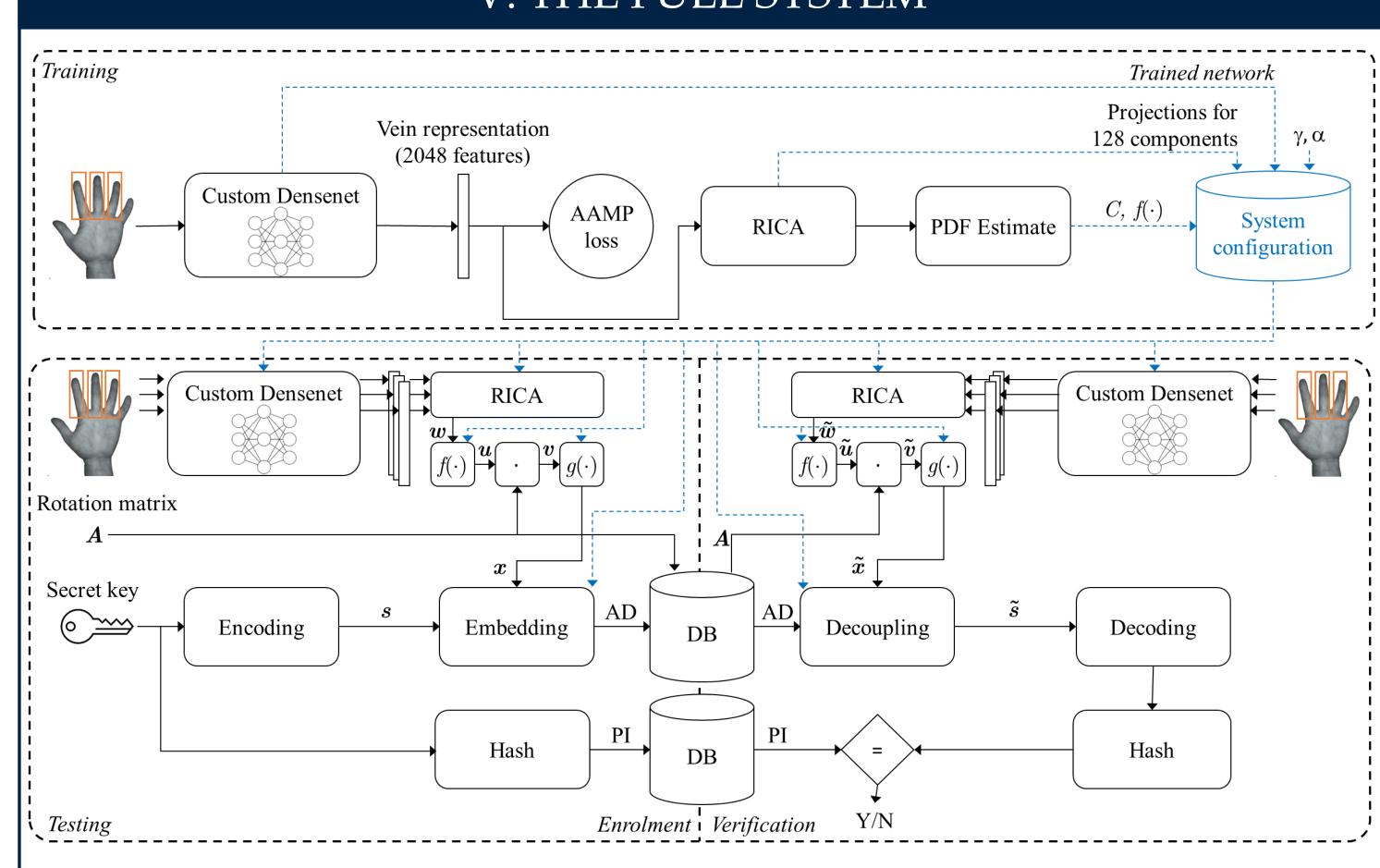


#### VI. DEALING WITH NON-IDEAL DATA

- The introduction of the rotation matrix degrades performance
- This is because the templates have an SNR that is unevenly distributed across features.
- Mixing good and bad features lowers the total *Channel capacity*.
- Solution: linearly combine together only features with similar SNR

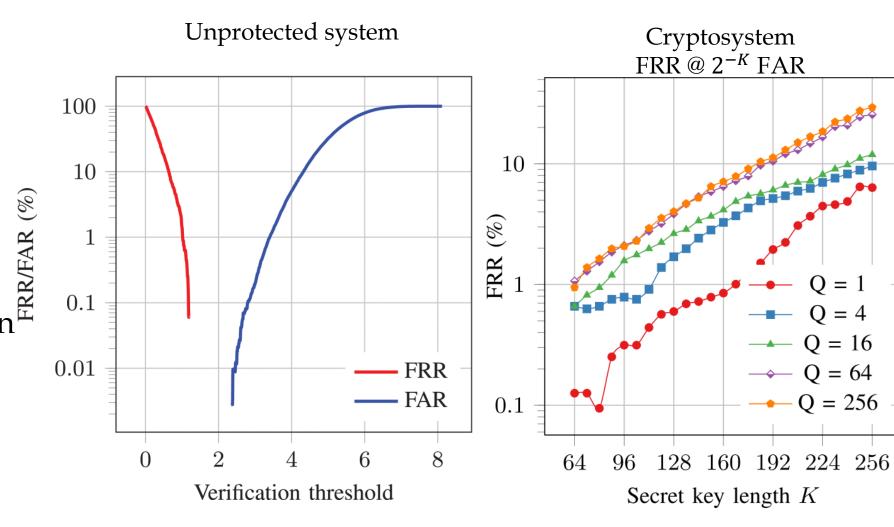


## V. THE FULL SYSTEM



#### VI. EXPERIMENTS ON REAL DATA

- Biometric trait: 3 fingers-veins.
- Dataset: SDUMLA: L/R index-, middle- and ring-fingers of 106 subjects.
- The bandwidth Q of the rotation matrix controls the tradeoff between features reliability and unlikability
- Reasonable long secret keys have been successfully tested



# REFERENCES

- 1. ISO/IEC 24745:2022 Information security, cybersecurity and privacy protection Biometric infomation protection
- 2. *G. E. Hine*, E. *Maiorana and P. Campisi* "A Zero-Leakage Fuzzy Embedder From the Theoretical Formulation to Real Data" in TIFS 2017
- 3. G. E. Hine, R. S. Kuzu, E. Maiorana and P. Campisi "Unlinkable Zero-Leakage Biometric Cryptosystem: Theoretical Evaluation and Experimental Validation" in TIFS 2023
- 4. *M. Gomez-Barrero, J. Galbally, C. Rathgeb and C. Busch* "General Framework to Evaluate Unlinkability in Biometric Template Protection Systems" in TIFS 2017







Secret key

Turbo

Encoder

Hash

template

matrix



