

Calculo Lambda

Numerais de Charch

$1 \equiv \lambda s \lambda z. s(z)$
 $2 \equiv \lambda s \lambda z. s(s(z))$
 $3 \equiv \lambda s \lambda z. s(s(s(z)))$
...

SUC = $\lambda w \lambda y \lambda x. y(wyx)$

Por exemplo o sucessor de zero pode ser obtido aplicando a função SU C na representção de zero:

$(\lambda w \lambda y \lambda x. y(wyx))(\lambda s \lambda z. z)$
→ $\lambda y \lambda x. y((\lambda s \lambda z. z)yx)$
→ $\lambda y \lambda x. y((\lambda z. z)x)$
→ $\lambda y \lambda x. y(x)$

ADD = $\lambda x \lambda y \lambda w \lambda u. xw(ywu)$

Como exemplo podemos aplicar a função de adição para os números naturais 2 e 3:

$(\lambda x \lambda y \lambda w \lambda u. xw(ywu))(\lambda s \lambda z. s(s(z)))(\lambda s \lambda z. s(s(s(z))))$
→ $(\lambda y \lambda w \lambda u. (\lambda s \lambda z. s(s(z)))w(ywu))(\lambda s \lambda z. s(s(s(z))))$
→ $(\lambda y \lambda w \lambda u. (\lambda z. w(w(z)))(yw u))(\lambda s \lambda z. s(s(s(z))))$
→ $(\lambda y \lambda w \lambda u. w(w(ywu)))(\lambda s \lambda z. s(s(s(z))))$
→ $\lambda w \lambda u. w(w((\lambda s \lambda z. s(s(s(z))))wu))$
→ $\lambda w \lambda u. w(w((\lambda z. w(w(w(z))))u))$
→ $\lambda w \lambda u. w(w(w(w(u))))$

Booleanos

$V \equiv \lambda x \lambda y. x$
 $F \equiv \lambda x \lambda y. y$

Lógica

$E = \lambda x. \lambda y. xy(\lambda u \lambda v. v)$
 $OU = \lambda x \lambda y. (x(\lambda u \lambda v. u))y$
 $N AO = \lambda x. (x(\lambda u \lambda v. v))(\lambda a. \lambda b. a)$

Lambda em HASKELL

`zero::(a -> a) -> a -> a`
`zero = \s z -> z`
`um::(a -> a) -> a -> a`
`um = \s z -> s z`
`dois = \s z -> s (s z)`
`tres = \s z -> s (s (s z))`
`quatro = \s z -> s (s (s (s z)))`

`suc = \w y x -> y (w y x)`
`prede = \n f x -> n (\g h -> h (g f)) (\u -> x) (\u -> u)`
`add = \x y w u -> x w (y w u)`
`mul = \x y w u -> x (y w) u`

Arvore Binária

`data Arvore a = No a (Arvore a) (Arvore a) | Folha`
`deriving Show`

--Inserir elemento na Arvore

`ins a Folha = No a Folha Folha`
`ins a (No x esq dir) | a == x = (No x esq dir)`
`| a < x = (No x (ins a esq) dir)`
`| otherwise = (No x esq (ins a dir))`

--listToTree

`listToTree ls = listToTree' Folha ls`
`listToTree' arv [] = arv`
`listToTree' arv (x:xs) = listToTree' (ins x arv) xs`

--treeToList

`treeToList Folha = []`
`treeToList (No x esq dir) = (treeToList esq) ++ [x] ++`
`(treeToList dir)`