Module Interface Specification for EOMEE

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1 Revision History

Date	Version	Notes
20-11-2020	1.0	MIS first draft

2 Symbols, Abbreviations and Acronyms

See SRS Documentation at SRS.
Additionaly, the following abbreaviations were used:

abbreviation	**description**
N	Number of electrons
orthog	Matrix orthogonalization method
tol	Tolerance
nspino	Number of spin orbital basis
lhs	Left-hand-side
rhs	Right-hand-side
neigs	Number of eigenvalues

Contents

3 Introduction

The following document details the Module Interface Specifications of EOMEE, a set of tools to implement and solve the Equation-of-Motion methods for excited states.

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at https://github.com/gabrielasd/eomee/tree/cas741.

4 Notation

The structure of the MIS for modules comes from Hoffman and Strooper (1995), with the addition that template modules have been adapted from Ghezzi et al. (2003). The mathematical notation comes from Chapter 3 of Hoffman and Strooper (1995). For instance, the symbol := is used for a multiple assignment statement and conditional rules follow the form $(c_1 \Rightarrow r_1|c_2 \Rightarrow r_2|...|c_n \Rightarrow r_n)$.

The following table summarizes the primitive data types used by EOMEE.

Data Type	Notation	Description
character	char	a single symbol or digit
integer	$\mathbb{Z}$	a number without a fractional component in (-∞, ∞)
natural number	$\mathbb{N}$	a number without a fractional component in [1, ∞)
real	$\mathbb{R}$	any number in (-∞, ∞)

The specification of EOMEE uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, EOMEE uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.
The following simplifications will be made in the mathematical notation for the sake of understandability:

- seq(l_1,l_2,...,l_n:T), will be used instead of sequence [l_1,l_2,...,l_n] of type T. For example seq($n, m : \mathbb{R}$), where $n, m > 0$, would map to sequence [n, m] of type $\mathbb{R}$. This type will generally be used to indicate NumPy.ndarray data types.
- Variables that are of type sequence will be denoted in bold font, i.e, the parameter **R** denotes a sequence.
- Subscripts will be used for indexing sequences, for instance, x_i will represent the ith element of **x**, the same as $x[i]$ from Hoffman and Strooper (1995).

- str will be used instead of string.
- bool will be used instead of boolean.
- EOMT will be used to define an element belonging to the EOM methods set {EOMIP, EOMEA, EOMExc, EOMDIP, EOMDEA},

Also, the absence of value will be defined by Python's data type NoneType, denoted as None.

5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	**Level 2**	**Level 3**
Hardware-Hiding Module		
Behaviour-Hiding Module	Control	
	Input	
	Integrals	
	RDMs	
	EOM Interface	IP EOM; EA EOM; DIP EOM; DEA EOM; Excitation EOM
	Output	
Software Decision Module	Solver	

Table 1: Module Hierarchy

6 MIS of Control Module

6.1 Module

main

6.2 Uses

input (7), Integrals (8), WfnRDMs (9), EOMIP (11), EOMEA (12), EOMExc (13), EOMDIP (14), EOMDEA (15), solver (17), output (16)

6.3 Syntax

6.3.1 Exported Constants

None

6.3.2 Exported Access Programs

Name	In	Out	Exceptions
main	str	-	-

6.4 Semantics

6.4.1 State Variables

None

6.4.2 Environment Variables

None

6.4.3 Assumptions

None

6.4.4 Access Routine Semantics

main():

- transition: The following steps are performed:
  - Get a file containing the input parameters from the user (inputFile).

  - Parse the file's content and verify all required input parameters are present:
  parse_inputfile(inputFile)
  check_inputs(ParsedParams)

- Load and verify the electron integrals ($\mathbf{h}$,$\mathbf{v}$) and RDMs ($\boldsymbol{\gamma}$, $\boldsymbol{\Gamma}$):
Integrals($\mathbf{h}$, $\mathbf{v}$)
WfnRDMs($\boldsymbol{\gamma}$, $\boldsymbol{\Gamma}$)

- Define an EOM type equation from the parameters $\mathbf{h}$,$\mathbf{v}$, $\boldsymbol{\gamma}$ and $\boldsymbol{\Gamma}$.
EOMT($\mathbf{h}$, $\mathbf{v}$, $\boldsymbol{\gamma}$, $\boldsymbol{\Gamma}$)

- Solve the EOM eigenvalue problem and evaluate the TDMs
ΔE, $\mathbf{C}$:= solve.dense(EOMT.lhs, EOMT.rhs, ortog, tol)

- Evaluate the TDMs:
$\mathbf{T}$:= EOMT.tdm($\mathbf{C}$)

- Output the results of the computations:
output(filename1, ΔE, $\mathbf{C}$, $\mathbf{T}$)

- exception: None

6.4.5 Local Functions

None

7 MIS of Input Module

7.1 Module

input

7.2 Uses

None

7.3 Syntax

7.3.1 Exported Constants

7.3.2 Exported Access Programs

Name	In	Out	Exceptions
parse_inputfile	str	ParsedParams	FileNotFoundError
check_inputs	ParsedParams	-	FileNotFoundError, ValueError
N		$(n1, n2 : \mathbb{N})$	
one_int_file		str	
two_int_file		str	
dm1_file		str	
dm2_file		str	
eom		str	
orthog		str	
tol		$\mathbb{R}$	

7.4 Semantics

7.4.1 State Variables

N: $\mathbb{N} \vee (n1, n2 : \mathbb{N})$
one_int_file: str
two_int_file: str
dm1_file: str
dm2_file: str
eom: str $\in \{$"*ip*", "*dip*", "*ea*", "*dea*", "*exc*"$\}$ which selects the EOMT
orthog: str $\in \{$"*symmetric*", "*asymmetric*"$\}$
tol: $\mathbb{R} > 0$

7.4.2 Environment Variables

inputFile: string representing a file or file path.

7.4.3 Assumptions

The first function called will be parse_infile, followed by check_inputs.

7.4.4 Access Routine Semantics

parse_infile(filename):

- transition: The input file *filename* is read sequentially and the state variables get assigned
- output: *out* := ParsedParams
- exception: FileNotFoundError

check_inputs(ParsedParams):

- output: None
- exception: *exc* :=

$\neg(\text{N} \in (n1, n2 : \mathbb{N}))$	$\Rightarrow$ TypeError |
"one_int_file" not in working directory	$\Rightarrow$ FileNotFoundError|
"two_int_file" not in working directory	$\Rightarrow$ FileNotFoundError|
"dm1_file" not in working directory	$\Rightarrow$ FileNotFoundError|
"dm2_file" not in working directory	$\Rightarrow$ FileNotFoundError|
$\neg(\text{eom} \in \{"ip", "dip", "ea", "dea", "exc"\})$	$\Rightarrow$ ValueError|
$\neg(\text{orthog} \in \{"symmetric", "asymmetric"\})$	$\Rightarrow$ ValueError|
$\neg(\text{tol} \in \mathbb{R})$	$\Rightarrow$ TypeError|
$\neg(\text{tol} > 0)$	$\Rightarrow$ ValueError|

ParsedParams.N:

- output: *out* := N
- exception: None

ParsedParams.tol:

- output: *out* := tol
- exception: None

ParsedParams.orthog:

- output: *out* := orthog
- exception: None

ParsedParams.eom:

- output: *out* := eom
- exception: None

ParsedParams.one_int_file:

- output: *out* := one_int_file
- exception: None

ParsedParams.two_int_file:

- output: *out* := two_int_file
- exception: None

ParsedParams.dm1_file:

- output: *out* := dm1_file
- exception: None

ParsedParams.dm2_file:

- output: *out* := dm2_file
- exception: None

7.4.5 Local Functions

None

8 MIS of Integrals Module

8.1 Template Module

Integrals

8.2 Uses

input (7)

8.3 Syntax

8.3.1 Exported Constants

8.3.2 Exported Access Programs

Name	In	Out	Exceptions
new Integrlas	str, str	Integrlas	-
h	-	seq($m, m : \mathbb{R}$)	-
v	-	seq($m, m, m, m : \mathbb{R}$)	-
nspino	-	$\mathbb{N}$	-

8.4 Semantics

8.4.1 State Variables

h: seq($m, m : \mathbb{R}$)
v: seq($m, m, m, m : \mathbb{R}$)
nspino: $\mathbb{N}$

8.4.2 Environment Variables

intfile1: binary file in NumPy .npy format.
intfile2: binary file in NumPy .npy format.

8.4.3 Assumptions

The constructor of Integrals will be called before any state variable is invoked.

8.4.4 Access Routine Semantics

new Integrals(one_int_file, two_int_file):

- transition: Call load_integrals(one_int_file, two_int_file)
- output: *out* := self

- exception: None

Integrals.h:

- output: *out* := **h**
- exception: None

Integrals.v:

- output: *out* := **v**
- exception: None

Integrals.nspino:

- output: *out* := nspino
- exception: None

8.4.5 Local Functions

load_integrals(one_int_file, two_int_file):

- transition:
  Read the binary files one_int_file and two_int_file
  verify_integrals()
  If no exception is raised, assign the state variables **h** and **v**
- exception: exc := FileNotFoundError

verify_integrals():

- output: *out* := None
- exception: exc :=

$\neg$(**h**$\in$ sequence of $\mathbb{R}$)	$\Rightarrow$ TypeError |
$\neg$(**v**$\in$ sequence of $\mathbb{R}$)	$\Rightarrow$ TypeError |
h is not a bidimensional arrray	$\Rightarrow$ ValueError |
v is not a 4 dimensional array	$\Rightarrow$ ValueError|
$\neg(\|\mathbf{h}[0]\| = \|\mathbf{v}[0]\|)$	$\Rightarrow$ ValueError |
$\neg(h_{ij} = h_{ji})$	$\Rightarrow$ ValueError |
$\neg((v_{ijkl} = v_{jilk}) \wedge (v_{ijkl} = v_{klij}))$	$\Rightarrow$ ValueError |
$\neg((v_{ijkl} = -v_{jikl}) \wedge (v_{ijkl} = -v_{ijlk}))$	$\Rightarrow$ ValueError |

9 MIS of RDMs Module

9.1 Template Module

WfnRDMs

9.2 Uses

input (7)

9.3 Syntax

9.3.1 Exported Constants

9.3.2 Exported Access Programs

Name	In	Out	Exceptions
new WfnRDMs	$\mathbb{Z} \vee (n1, n2 : \mathbb{Z})$, str, str	WfnRDMs	-
$\boldsymbol{\gamma}$	-	seq$(m, m : \mathbb{R})$	-
$\boldsymbol{\Gamma}$	-	seq$(m, m, m, m : \mathbb{R})$	-
N	-	$(n1, n2 : \mathbb{N})$	-
nspino	-	$\mathbb{N}$	-

9.4 Semantics

9.4.1 State Variables

nspino: $(n1, n2 : \mathbb{N})$
nspino: $\mathbb{N}$
$\boldsymbol{\gamma}$: seq$(m, m : \mathbb{R})$, where $0 \leq \gamma_{ij} \leq 1$
$\boldsymbol{\Gamma}$: seq$(m, m, m, m : \mathbb{R})$, where $0 \leq \Gamma_{ijkl} \leq 1$

9.4.2 Environment Variables

file1: binary file in NumPy .npy format.
file2: binary file in NumPy .npy format.

9.4.3 Assumptions

The constructor of WfnRDMs will be called before invoking any state variable.

9.4.4 Access Routine Semantics

new WfnRDMs(n1, dm1_file, dm2_file):

- transition:
  N:= n1
  Call assign_rdms(dm2_file, dm2_file)
- output: *out* := self
- exception: None

WfnRDMs.dm1:

- output: *out* := $\boldsymbol{\gamma}$
- exception: None

WfnRDMs.dm2:

- output: *out* := $\boldsymbol{\Gamma}$
- exception: None

WfnRDMs.N:

- output: *out* := N
- exception: None

WfnRDMs.nspino:

- output: *out* := nspino
- exception: None

9.4.5 Local Functions

assign_rdms(dm1_file,dm2_file):

- transition: Read the binary files dm1_file and dm2_file.
  verify_rdms()
  If no exception is raised, assign the state variables $\boldsymbol{\gamma}$ and $\boldsymbol{\Gamma}$
- exception: exc := FileNotFoundError

verify_rdms():

- output: *out* := None
- exception: exc :=

$\neg(\boldsymbol{\gamma} \in \text{sequence of } \mathbb{R})$	$\Rightarrow$ TypeError |
$\neg(\boldsymbol{\Gamma} \in \text{sequence of } \mathbb{R})$	$\Rightarrow$ TypeError|
$\boldsymbol{\gamma}$ is not a bidimensional arrray	$\Rightarrow$ ValueError |
$\boldsymbol{\Gamma}$ is not a 4 dimensional array	$\Rightarrow$ ValueError |
$\neg(\gamma_{ij} = \gamma_{ji})$	$\Rightarrow$ ValueError |
$\neg(\Gamma_{ijkl} = \Gamma_{jilk}) \vee \neg(\Gamma_{ijkl} = \Gamma_{klij})$	$\Rightarrow$ ValueError |
$\neg(\Gamma_{ijkl} = -\Gamma_{jikl}) \vee \neg(\Gamma_{ijkl} = -\Gamma_{ijlk})$	$\Rightarrow$ ValueError |
$\text{Tr}(\boldsymbol{\gamma}) \neq N$	$\Rightarrow$ ValueError |
$\text{Tr}(\boldsymbol{\Gamma}) \neq N(N-1)$	$\Rightarrow$ ValueError |

10 MIS of EOM Base Module

10.1 Interface Module

EOMBase

10.2 Uses

None

10.3 Syntax

10.3.1 Exported Constants

None

10.3.2 Exported Access Programs

Name	In	Out	Exceptions
neigs	-	$\mathbb{N}$	NotImplementedError
compute_tdm	seq(k,k:$\mathbb{R}$)	seq(k,m,m:$\mathbb{R}$)	NotImplementedError
lhs	-	seq($k, k : \mathbb{R}$)	-
rhs	-	seq($k, k : \mathbb{R}$)	-
nspino	-	$\mathbb{N}$	-
h	-	seq($m, m : \mathbb{R}$)	-
v	-	seq($m, m, m, m : \mathbb{R}$)	-
$\boldsymbol{\gamma}$	-	seq($m, m : \mathbb{R}$)	-
$\boldsymbol{\Gamma}$	-	seq($m, m, m, m : \mathbb{R}$)	-

10.4 Semantics

10.4.1 State Variables

nspino: $\mathbb{N}$
h: seq($m, m : \mathbb{R}$)
v: seq($m, m, m, m : \mathbb{R}$)
$\boldsymbol{\gamma}$: seq($m, m : \mathbb{R}$)
$\boldsymbol{\Gamma}$: seq($m, m, m, m : \mathbb{R}$)
lhs: _compute_lhs()
rhs: _compute_rhs()

10.4.2 Assumptions

The EOMBase module can't be instantiated, it is inherited by EOMIP, EOMEA, EOMExc, EOMDIP and EOMDEA.

10.4.3 Access Routine Semantics

EOMBase.nspino:

- output: *out* := nspino
- exception: None

EOMBase.h:

- output: *out* := $\mathbf{h}$
- exception: None

EOMBase.v:

- output: *out* := $\mathbf{v}$
- exception: None

EOMBase.dm1:

- output: *out* := $\boldsymbol{\gamma}$
- exception: None

EOMBase.dm2:

- output: *out* := $\boldsymbol{\Gamma}$
- exception: None

EOMBase.lhs:

- output: *out* := lhs $\in$ seq$(m, m : \mathbb{R})$
- exception: ValueError

EOMBase.rhs:

- output: *out* := rhs $\in$ seq$(m, m : \mathbb{R})$
- exception: ValueError

10.4.4 Local Functions

_compute_lhs():

- exception: NotImplementedError

_compute_rhs():

- exception: NotImplementedError

10.4.5 Considerations

EOMBase is an abstract class (ABC) defining an interface for the different EOM methods (Subsections (11), (12), (13), (14) and (15)). Each state variable has a corresponding access program. Only the methods *neigs*, compute_tdm, _compute_lhs and _compute_rhs are abstract.

11 MIS of EOM IP Module

11.1 Template Module

EOMIP inherits EOMBase

11.2 Uses

EOMBase (10), Integrals (8), WfnRDMs (9)

11.3 Syntax

11.3.1 Exported Constants

None

11.3.2 Exported Access Programs

Name	In	Out	Exceptions
new EOMIP	seq$(m, m : \mathbb{R})$, seq$(m, m, m, m : \mathbb{R})$, seq$(m, m : \mathbb{R})$, seq$(m, m, m, m : \mathbb{R})$	EOMIP	-

11.4 Semantics

11.4.1 State Variables

nspino: $\mathbb{N}$
h: seq$(m, m : \mathbb{R})$
v: seq$(m, m, m, m : \mathbb{R})$
$\boldsymbol{\gamma}$: seq$(m, m : \mathbb{R})$
$\boldsymbol{\Gamma}$: seq$(m, m, m, m : \mathbb{R})$
lhs: _compute_lhs()
rhs: _compute_rhs()

11.4.2 Environment Variables

None

11.4.3 Assumptions

The EOMIP constructor is called before any other access program in the class.

11.4.4 Access Routine Semantics

new EOMIP(h,v,dm1,dm2):

- transition: $\mathbf{h}$, $\mathbf{v}$, $\boldsymbol{\gamma}$, $\boldsymbol{\Gamma}$:= h,v,dm1,dm2,
  lhs:= _compute_lhs()
  rhs:= _compute_rhs()
  nspino := $|\boldsymbol{h}[0]|$

- output: *out* := self
- exception: None

neigs():

- output: *out* := $|\boldsymbol{h}[0]|$
- exception: None

compute_tdm($\mathbf{C}$):

- output: *out* := $\sum_n \gamma_{mn} c_n, \{n : \mathbb{Z} | 0 \leq n < nspino\}$
- exception: None

11.4.5 Local Functions

_compute_lhs():

- output: *out* :=
  $-\boldsymbol{h}\boldsymbol{\gamma} + 0.5 \sum_{qrs} \mathrm{v}_{qnrs} \Gamma_{mqrs}$
- exception: None

_compute_rhs():

- output: *out* := $\boldsymbol{\gamma}$
- exception: None

12 MIS of EOM EA Module

12.1 Template Module

EOMEA inherits EOMBase

12.2 Uses

EOMBase (10), Integrals (8), WfnRDMs (9)

12.3 Syntax

12.3.1 Exported Constants

None

12.3.2 Exported Access Programs

Name	In	Out	Exceptions
new EOMEA	seq$(m, m : \mathbb{R})$, seq$(m, m, m, m : \mathbb{R})$, seq$(m, m : \mathbb{R})$, seq$(m, m, m, m : \mathbb{R})$	EOMEA	-

12.4 Semantics

12.4.1 State Variables

nspino: $\mathbb{N}$
h: seq$(m, m : \mathbb{R})$
v: seq$(m, m, m, m : \mathbb{R})$
$\boldsymbol{\gamma}$: seq$(m, m : \mathbb{R})$
$\boldsymbol{\Gamma}$: seq$(m, m, m, m : \mathbb{R})$
lhs: _compute_lhs()
rhs: _compute_rhs()

12.4.2 Environment Variables

None

12.4.3 Assumptions

The EOMEA constructor is called before any other access program in that class.

12.4.4 Access Routine Semantics

new EOMEA(h,v,dm1,dm2):

- transition: $\mathbf{h}$, $\mathbf{v}$, $\boldsymbol{\gamma}$, $\boldsymbol{\Gamma}$:= h,v,dm1,dm2,
  lhs:= _compute_lhs(),
  rhs:= _compute_rhs()
  nspino := $|\boldsymbol{h}[0]|$

- output: *out* := self
- exception: None

neigs():

- output: *out* := $|\boldsymbol{h}[0]|$
- exception: None

compute_tdm($\mathbf{C}$):

- output: *out* := $\sum_n(\delta_{mn} - \gamma_{mn})c_n, \{n : \mathbb{Z}|0 \leq n < nspino\}$
- exception: None

12.4.5 Local Functions

_compute_lhs():

- output: *out* :=
  $\mathbf{h}$ - $\mathbf{h}\boldsymbol{\gamma} + \sum_{ps} \mathrm{v}_{mpns}\gamma_{ps} + 0.5\sum_{pqs} \mathrm{v}_{pqns}\Gamma_{pqsm}$
- exception: None

_compute_rhs():

- output: *out* := $\boldsymbol{I} - \boldsymbol{\gamma}$, where $\mathbf{I}$ represents the identity matrix
- exception: None

13 MIS of EOM Excitation Module

13.1 Template Module

EOMExc inherits EOMBase

13.2 Uses

EOMBase (10), Integrals (8), WfnRDMs (9)

13.3 Syntax

13.3.1 Exported Constants

None

13.3.2 Exported Access Programs

Name	In	Out	Exceptions
new EOMExc	seq($m, m : \mathbb{R}$), seq($m, m, m, m : \mathbb{R}$), seq($m, m : \mathbb{R}$), seq($m, m, m, m : \mathbb{R}$)	EOMExc	-

13.4 Semantics

13.4.1 State Variables

nspino: $\mathbb{N}$
h: seq($m, m : \mathbb{R}$)
v: seq($m, m, m, m : \mathbb{R}$)
γ: seq($m, m : \mathbb{R}$)
Γ: seq($m, m, m, m : \mathbb{R}$)
lhs: _compute_lhs()
rhs: _compute_rhs()

13.4.2 Environment Variables

None

13.4.3 Assumptions

The EOMExc constructor is called before any other access program in that class.

13.4.4 Access Routine Semantics

new EOMExc(h,v,dm1,dm2):

- transition: $\mathbf{h}$, $\mathbf{v}$, $\boldsymbol{\gamma}$, $\boldsymbol{\Gamma}$:= h,v,dm1,dm2,
  lhs:= _compute_lhs(),
  rhs:= _compute_rhs()
  nspino := $|\boldsymbol{h}[0]|$
  neigs := $|\boldsymbol{h}[0]|$
- output: *out* := self
- exception: None

neigs():

- output: *out* := $|\boldsymbol{h}[0]|^2 \in \mathbb{Z}$
- exception: None

compute_tdm($\mathbf{C}$):

- output: *out* := $\sum_{ij}(\delta_{li}\gamma_{kj} - \Gamma_{kijl})c_{ij}, \{(i,j)|(i \in [0..\text{nspino}-1]) \wedge (j \in [0..\text{nspino}-1])\}$
- exception: None

13.4.5 Local Functions

_compute_lhs():

- output: *out* :=
  $h_{li}\gamma_{kj} + h_{jk}\gamma_{il} - \sum_q(h_{jq}\delta_{li}\gamma_{kq} + h_{qi}\delta_{jk}\gamma_{ql})$
  $+ \sum_{qs}(\mathrm{v}_{lqis}\Gamma_{kqjs} + \mathrm{v}_{jqks}\Gamma_{iqls})$
  $+ 0.5\sum_{rs}(\mathrm{v}_{jlrs}\Gamma_{kirs} + \sum_q \mathrm{v}_{qjrs}\delta_{li}\Gamma_{kqrs})$
  $+ 0.5\sum_{pq}(\mathrm{v}_{pqik}\Gamma_{pqlj} + \sum_s \mathrm{v}_{pqsi}\delta_{jk}\Gamma_{pqls})$
- exception: None

_compute_rhs():

- output: *out* := $\delta_{li}\gamma_{kj} - \boldsymbol{\Gamma}$
- exception: None

14 MIS of EOM DIP Module

The MIS of EOM DIP is equivalent to the one for EOM Excitation (Section 13), therefore only the semantics of the methods that change will be declared.

14.1 Template Module

EOMDIP inherits EOMBase

14.2 Uses

EOMBase (10), Integrals (8), WfnRDMs (9)

14.3 Access Routine Semantics

compute_tdm(**C**):

- output: $out := \sum_{ij} \Gamma_{klji} c_{ij}, \{(i,j) | (i \in [0..\text{nspino}-1]) \wedge (j \in [0..\text{nspino}-1])\}$
- exception: None

14.3.1 Local Functions

_compute_lhs():

- output: $out :=$
  $2(h_{jk}\delta_{il} - h_{jl}\delta_{ik} + h_{ik}\gamma_{lj} - h_{il}\gamma_{kj})$
  $+ 2\sum_q h_{jq}(\delta_{ik}\gamma_{lq} - \delta_{il}\gamma_{kq}) + \mathbf{v}$
  $+ 2\sum_q \text{v}_{qjkl}\gamma_{qi} + \sum_r (\text{v}_{jilr}\gamma_{kr} - \text{v}_{jikr}\gamma_{lr})$
  $+ 2\sum_{qr} (\text{v}_{iqrk}\delta_{lj} + \text{v}_{iqlr}\delta_{kj})\gamma_{qr}$
  $+ 2\sum_{qr} (\text{v}_{jqrk}\Gamma_{qlri} + \text{v}_{jqlr}\Gamma_{qkri})$
  $+ \sum_{qrs} \text{v}_{qjrs}(\delta_{ki}\Gamma_{qlrs} - \delta_{li}\Gamma_{qkrs})$
- exception: None

_compute_rhs():

- output: $out := 2\delta_{jk}\gamma_{li} + 2\delta_{il}\gamma_{kj} - 2\delta_{jk}\delta_{il}$
- exception: None

15 MIS of EOM DEA Module

The MIS of EOM DEA is equivalent to the one for EOM Excitation (Section 13), therefore only the mothods that change are declared.

15.1 Template Module

EOMDEA inherits EOMBase

15.2 Uses

EOMBase (10), Integrals (8), WfnRDMs (9)

15.3 Access Routine Semantics

compute_tdm($\mathbf{C}$):

- output: $out :=$
  $\sum_{ij}(2\delta_{li}\delta_{kj}+2\delta_{lj}\gamma_{ik}+22\delta_{ki}\gamma_{jl}+\Gamma_{ijlk})c_{ij}, \{(i,j)|(i \in [0..\text{nspino}-1])\wedge(j \in [0..\text{nspino}-1])\}$
- exception: None

15.3.1 Local Functions

_compute_lhs():

- output: $out :=$
  $2(h_{li}\delta_{kj} - h_{ki}\delta_{lj} + h_{ki}\gamma_{jl} - h_{li}\gamma_{jk})$
  $+ 2\sum_p(h_{pi}\delta_{lj}\gamma_{pk} + h_{pj}\delta_{ki}\gamma_{pl})$
  $+\mathbf{v}+2\sum_r \mathrm{v}_{lkjr}\gamma_{ir}$
  $+ \sum_q(\mathrm{v}_{qlij}\gamma_{qk}-\mathrm{v}_{qkij}\gamma_{ql})$
  $+ 2\sum_{qr}(\mathrm{v}_{qljr}\delta_{ki}-\mathrm{v}_{qkjr}\delta_{li})\gamma_{qr}$
  $+ 2\sum_{qr}(\mathrm{v}_{qlir}\Gamma_{qjrk}-\mathrm{v}_{qkir}\Gamma_{qjrl})$
  $+ \sum_{pqr}\mathrm{v}_{pqjr}(\delta_{li}\Gamma_{pqrk} - \delta_{ki}\Gamma_{pqrl})$
- exception: None

_compute_rhs():

- output: $out := 2\delta_{li}\delta_{kj} - 2\delta_{li}\gamma_{jk} - 2\delta_{kj}\gamma_{il}$
- exception: None

16 MIS of Output module

16.1 Module

output

16.2 Uses

input (7)

16.3 Syntax

16.3.1 Exported Constants

16.3.2 Exported Access Programs

Name	In	Out	Exceptions
dump	fname: str, ParsedParams, $\boldsymbol{\Delta E}$:seq(k:$\mathbb{R}$), $\boldsymbol{C}$=seq(k,n:$\mathbb{R}$), $\boldsymbol{\gamma_{n;0k}}$=seq(k,n,n:$\mathbb{R}$)	-	-

16.4 Semantics

16.4.1 State Variables

None

16.4.2 Environment Variables

outputFile: A text file

16.4.3 Assumptions

16.4.4 Access Routine Semantics

dump(fname,ParsedParams,$\boldsymbol{\Delta E}$,$\boldsymbol{C}$,$\boldsymbol{\gamma_{n;0k}}$):

- transition: Write to fname the input parameters from ParsedParams and the results of the calculations: $\boldsymbol{\Delta E}$, $\boldsymbol{C}$ and $\boldsymbol{\gamma_{n;0k}}$
- exception: None

16.4.5 Local Functions

get_roots($\boldsymbol{\Delta E}$, ParsedParams.eom, roots):

- transition: Select from $\boldsymbol{\Delta E}$ the number of nonzero values indicated by roots and write them to fname.
- exception: $exc :=$

$\neg$(ParsedParams.eom $\in$ {"ip","dip","ea","dea","exc"}) $\Rightarrow$ ValueError

17 MIS of Solver Module

17.1 Module

solve

17.2 Uses

input (7)

17.3 Syntax

17.3.1 Exported Constants

17.3.2 Exported Access Programs

Name	In	Out	Exceptions
dense	**A**: seq(k,k:$\mathbb{R}$), **B**: seq(k,k:$\mathbb{R}$), tol: $\mathbb{R} > 0$, orthog: str $in\{$"$symm$", "$asymm$"$\}$	$\boldsymbol{\Delta E}$:seq(k:$\mathbb{R}$), $\boldsymbol{c}$=seq(k,k:$\mathbb{R}$)	DivideByZero

17.4 Semantics

17.4.1 State Variables

17.4.2 Environment Variables

17.4.3 Assumptions

17.4.4 Access Routine Semantics

dense(**A**,**B**,tol,orthog):

- output: $out := \boldsymbol{\Delta E}$, $\boldsymbol{c}$ that satifies $\boldsymbol{A}c_i = \Delta E_i \boldsymbol{B} c_i, \{i | 0 \leq i \leq k\}$
- exception: DivideByZero

17.4.5 Local Functions

None

References

Carlo Ghezzi, Mehdi Jazayeri, and Dino Mandrioli. *Fundamentals of Software Engineering*. Prentice Hall, Upper Saddle River, NJ, USA, 2nd edition, 2003.

Daniel M. Hoffman and Paul A. Strooper. *Software Design, Automated Testing, and Maintenance: A Practical Approach*. International Thomson Computer Press, New York, NY, USA, 1995. URL http://citeseer.ist.psu.edu/428727.html.

18 Appendix