

# Green Algorithm Design

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ICT and Environment



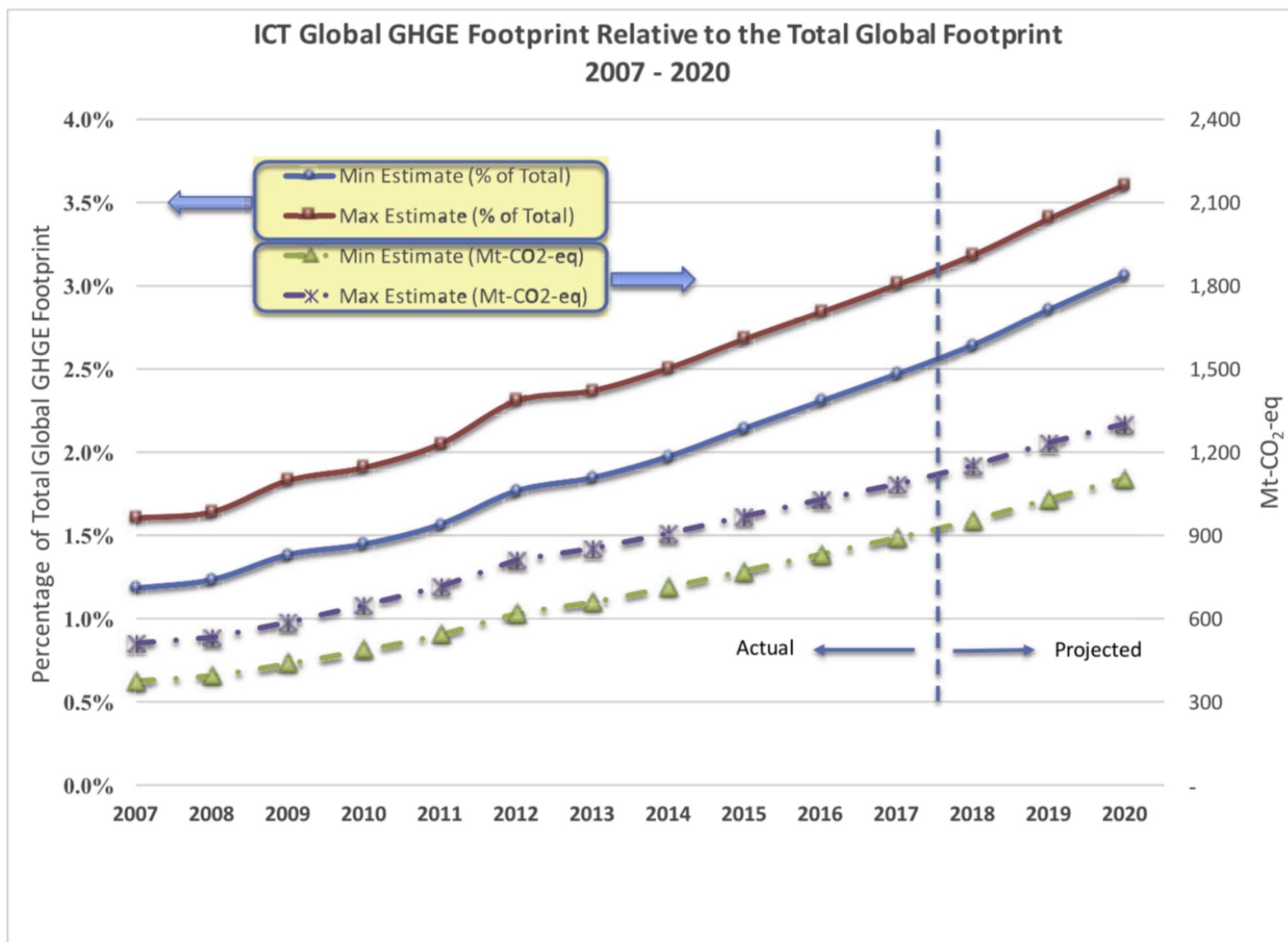
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2. In data centers: Virtual Machine Consolidation
3. Mobile networks: Putting Antennas to Sleep
4. In wired networks: Energy Aware Routing.

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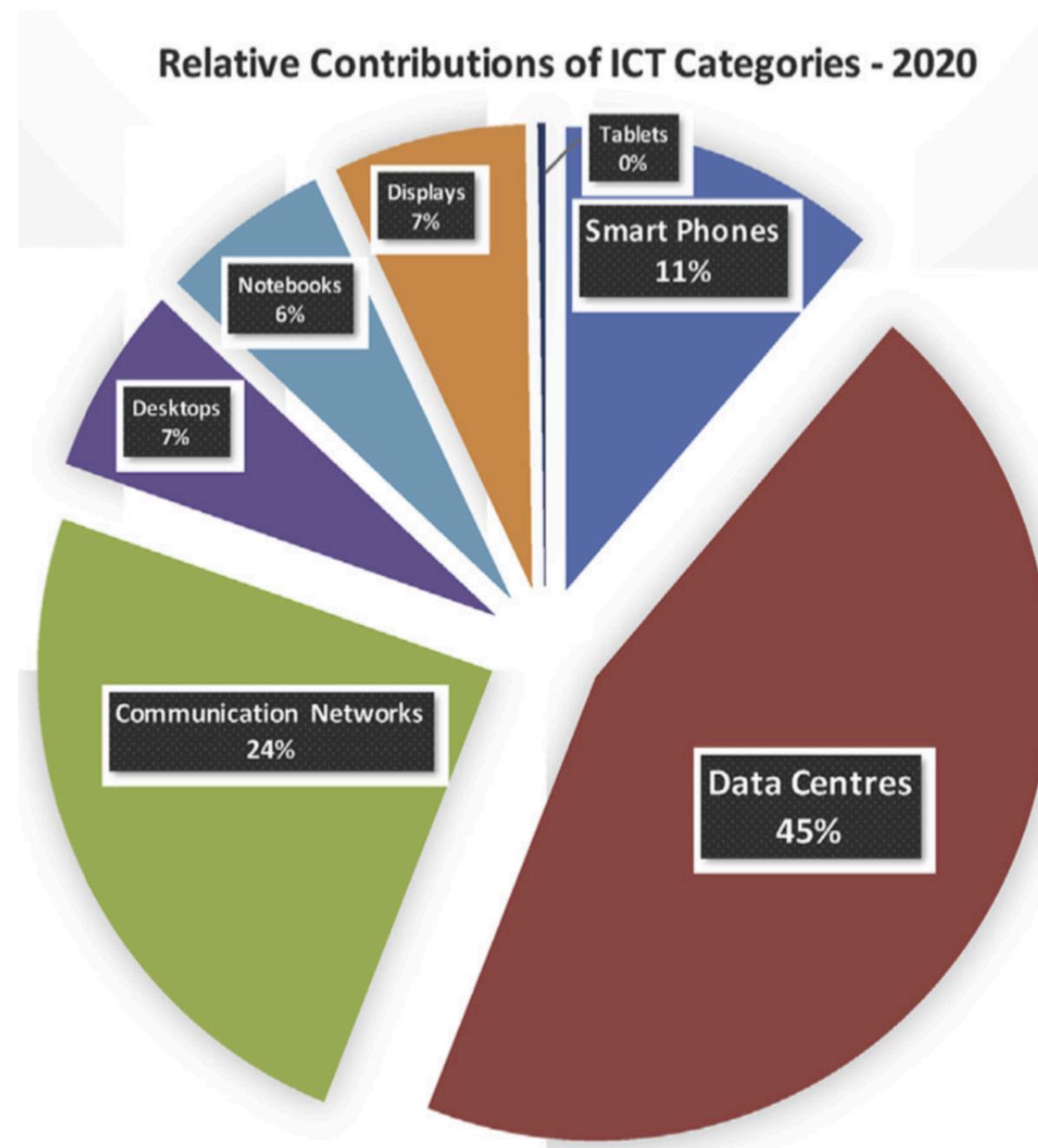
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# Internet Energy Consumption



3-4% and increasing

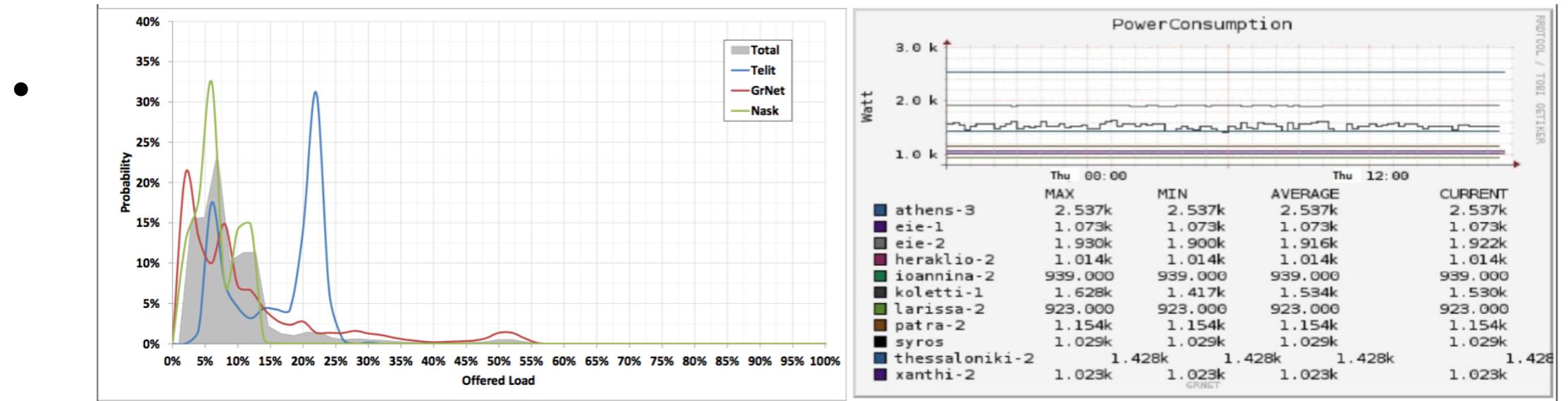
# Internet Energy Consumption



Data centers and Networks

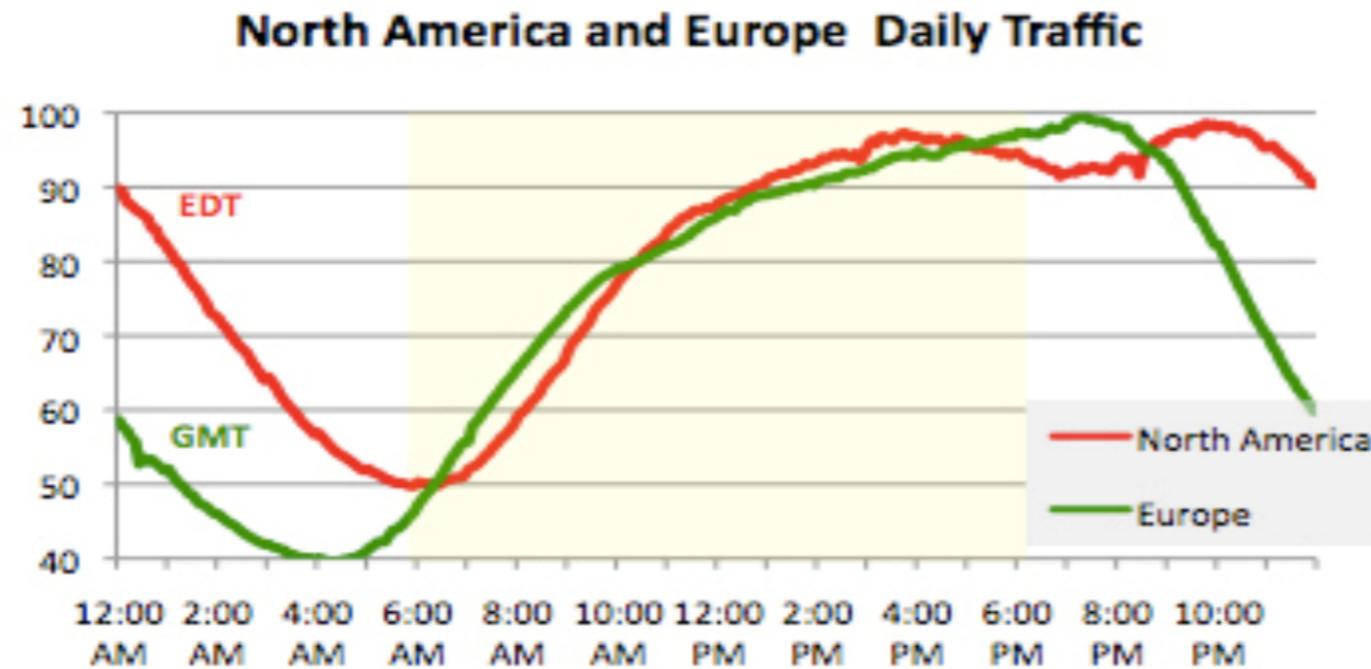
# Reasons for energy inefficiencies...

- The origin of these trends can be certainly found in current Internet infrastructures, technologies and protocols, which are designed to be extremely **over-dimensioned** and **available 24/7**.
- Links and devices are **provisioned for rush hour load**.
- The **overall power consumption** in today's networks **remains more or less constant** even in the presence of **fluctuating traffic loads**.



# ...despite wide traffic variations

- The profiles exhibit regular, daily cyclical traffic patterns with Internet traffic dropping at night and growing during the day.

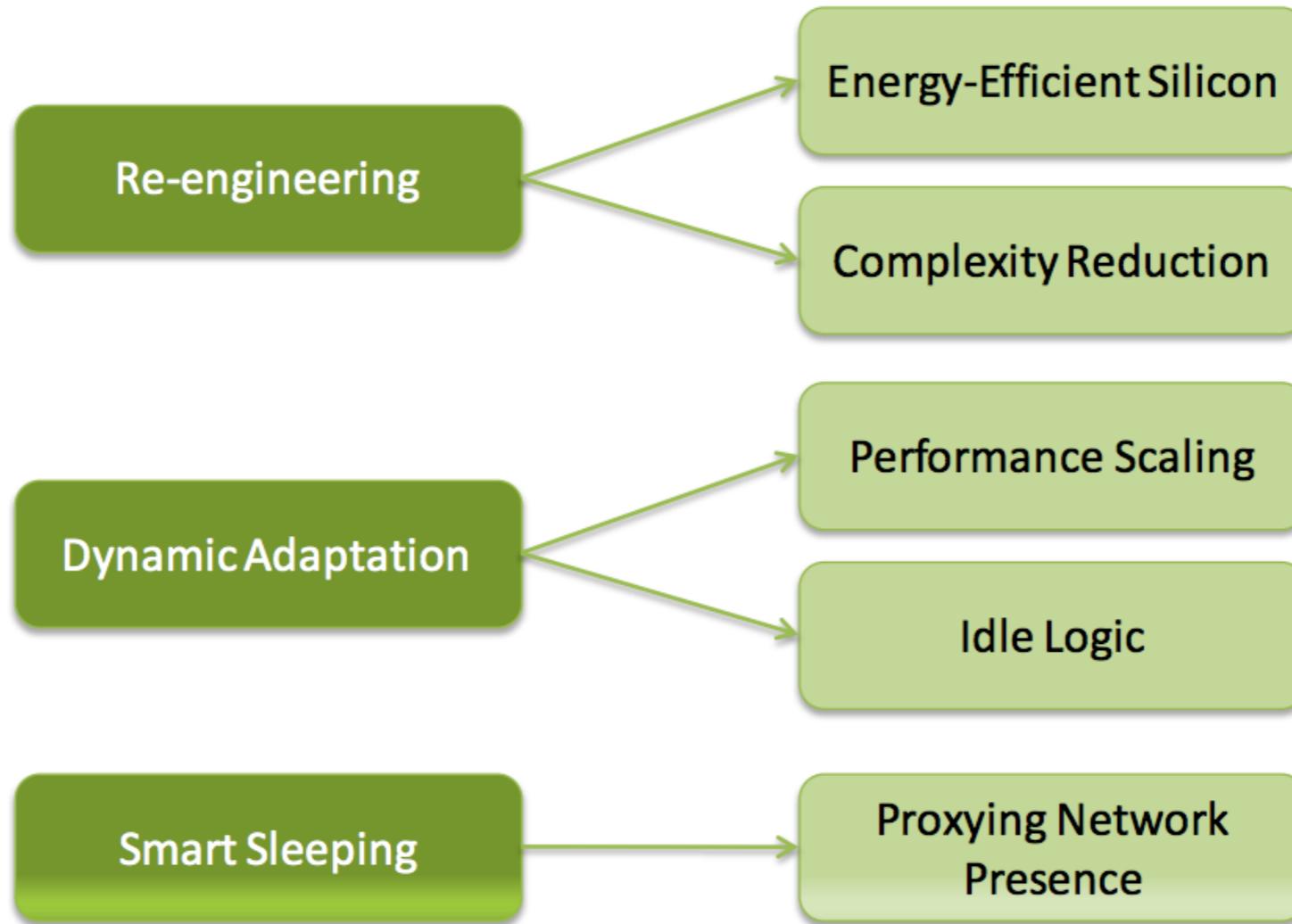


*Traffic load fluctuation at peering links for about 40 ISPs from USA and Europe (percentage / peak level)*

# History

- **Ground-breaking works on energy consumption in the Internet:** [Gupta et al. 2003 ], [Christensen et al. in 2004], showing that this is a mandatory issue to improve the energy efficiency of the whole Internet.
- However, **massive effort** in this direction by researchers, operators, and device manufacturers only **2008-2009**.

# Classifying Proposed Methods



Taxonomy of undertaken approaches for the energy efficiency of the Future Internet.

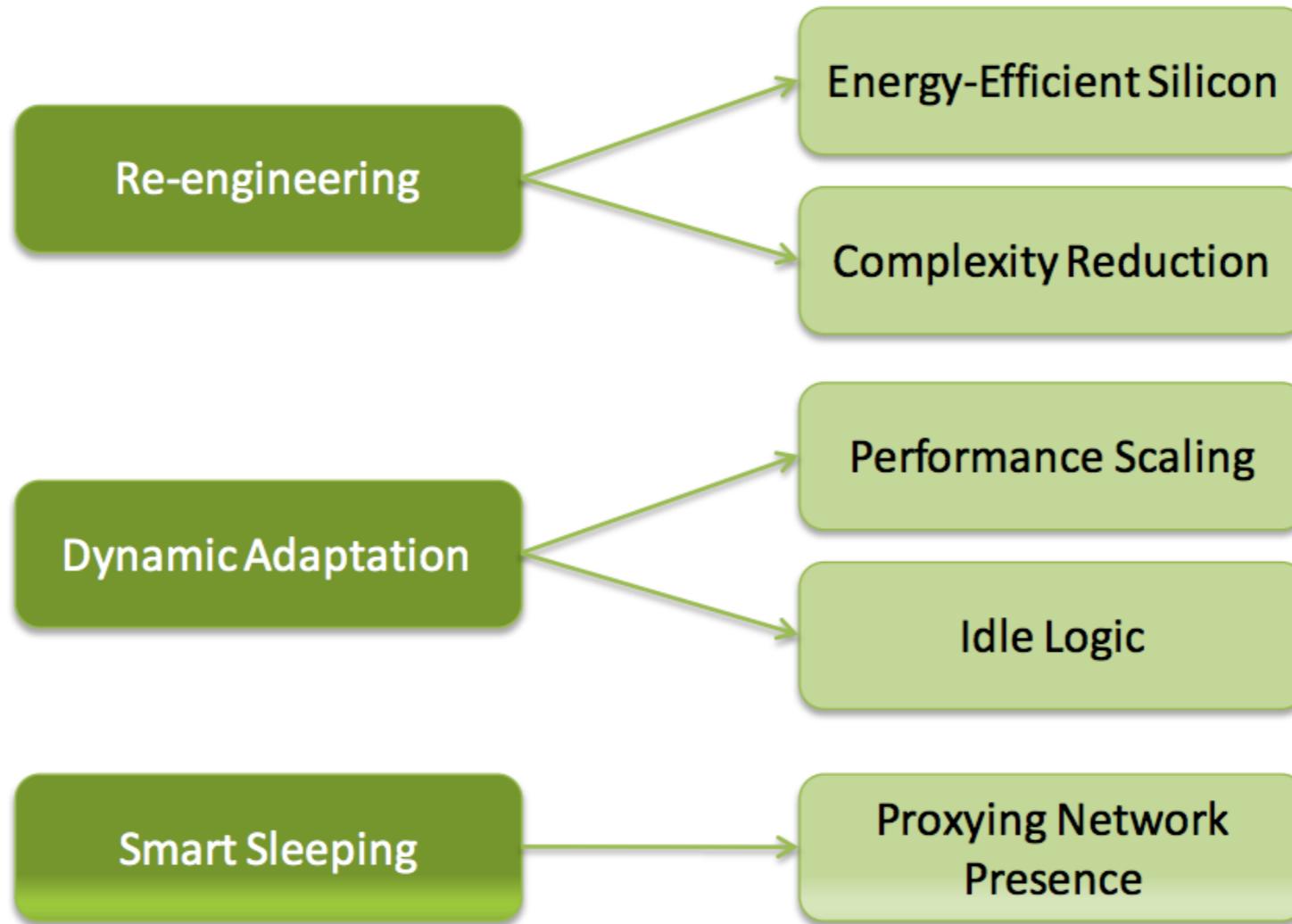
# Re-engineering approaches

- **Re-engineering approaches** aim
  - at **introducing and designing more energy-efficient elements** for network device architectures,
  - at suitably dimensioning and **optimizing internal organization devices**, as well as
  - at **reducing their intrinsic complexity levels**.

# Re-engineering approaches

- **Example:**
  - adoption of **pure optical switching architectures** for replacing the **current electronic based devices.**
  - They can potentially provide terabits of bandwidth at **much lower power dissipation than current network devices**
  - **Lots of work [Baliga 2007] but adoption still far from reality.** Current technological problems mainly regard the Control Plane.

# Classifying Proposed Methods



Taxonomy of undertaken approaches for the energy efficiency of the Future Internet.

# Dynamic Adaptation

- **Dynamic adaptation of network/device resources:** modulate capacities of packet processing engines and of network interfaces, to meet actual traffic loads and requirements.
- This can be performed by using two main power aware capabilities, namely,
  - **dynamic voltage scaling** and
  - **idle logic,**

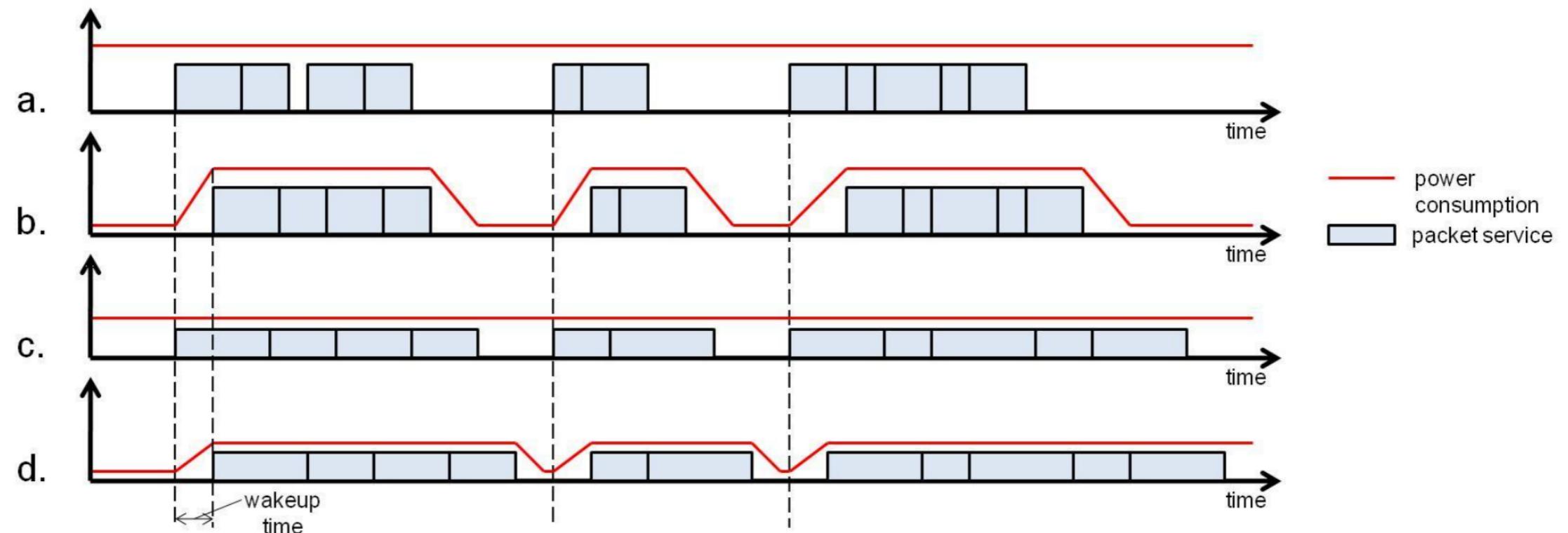
# Dynamic Adaptation: Power scaling

- Key feature in today's processors
- But, nowadays, **not included in the largest part of current network equipment.**
- Power scaling capabilities allow **dynamically reducing the working rate** of processing engines or of link interfaces. This is usually accomplished by tuning the **clock frequency** and/or the **voltage of processors**

# Dynamic Adaptation: Idle logic

- Idle logic allows reducing power consumption by **rapidly turning off sub-components** when no activities are performed, and by **re-waking them up** when the system receives new activities.
- In detail, wake-up instants are triggered by a **system internal scheduling process** (e.g., the system wakes itself up every certain time periods, and controls if there are new activities to process).

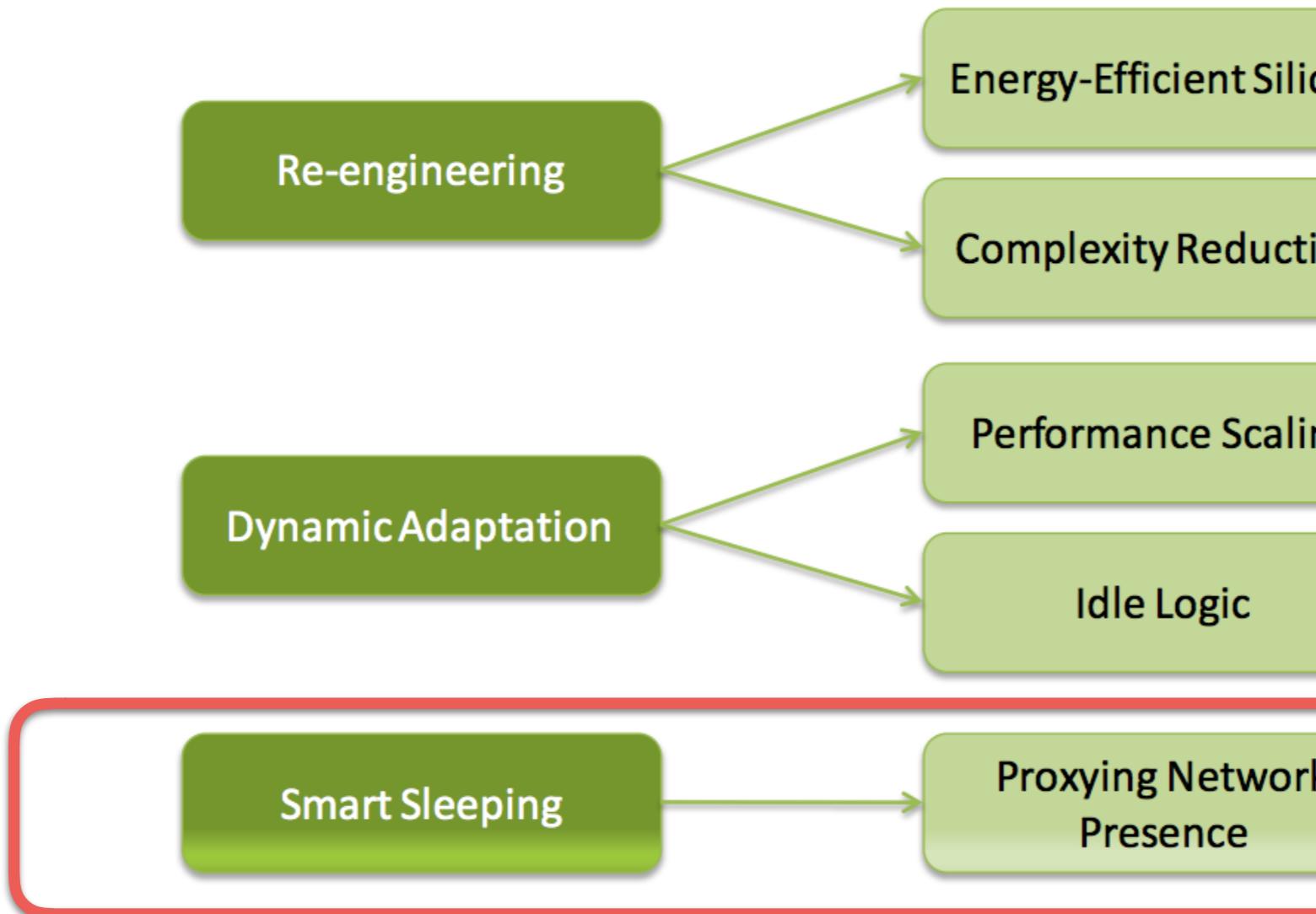
# Dynamic Adaptation



Packet service times and power consumptions in the following cases [Nevedschi et al. 2008]:

- (a) no power-aware optimizations,
- (b) only idle logic,
- (c) only performance scaling,
- (d) performance scaling and idle logic.

# Classifying Proposed Methods



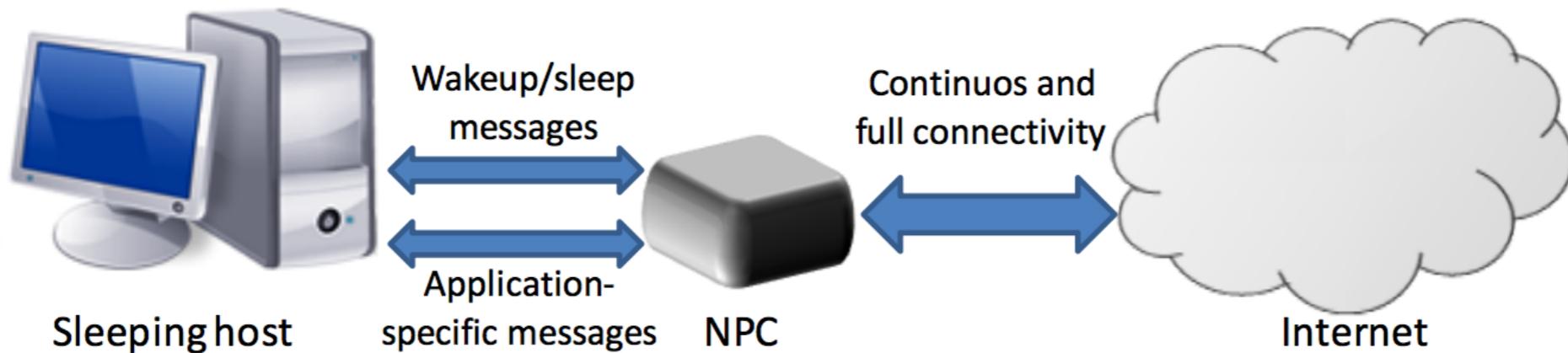
Taxonomy of undertaken approaches for the energy efficiency of the Future Internet.

# Sleeping/standby Approaches

- **Sleeping/standby approaches** are used to **smartly and selectively drive unused network/device** portions to low standby modes, and to **wake them up** only if necessary.
- However, today's networks and related services and applications designed to be **continuously and always available**.
- Standby modes have to be explicitly supported with **special proxying techniques** able to maintain the —network presence of sleeping nodes/components

# Sleeping/standby Approaches

- [Christensen and Nordman 2004] directly faced energy efficient enhancements in such kind of scenario.



*Example of Network Connection Proxy.*

- **Solution:** maintain continuous network presence by having ***a network host transfer network presence to a proxy***, namely Network Connectivity Proxy (NCP), when entering sleep mode.

# Classifying Proposed Methods

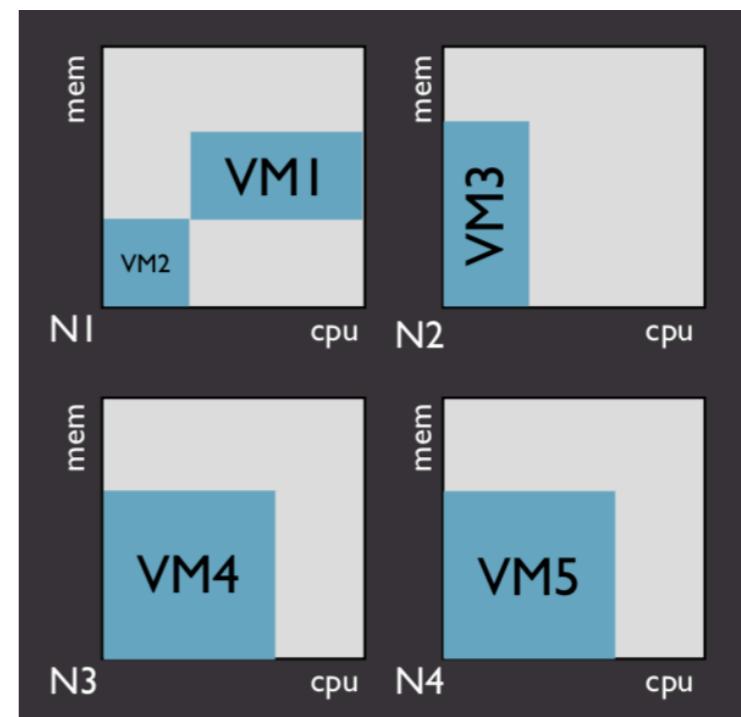
- All these approaches are not exclusive among themselves,
- All such directions in order to effectively develop new-generation green networks.

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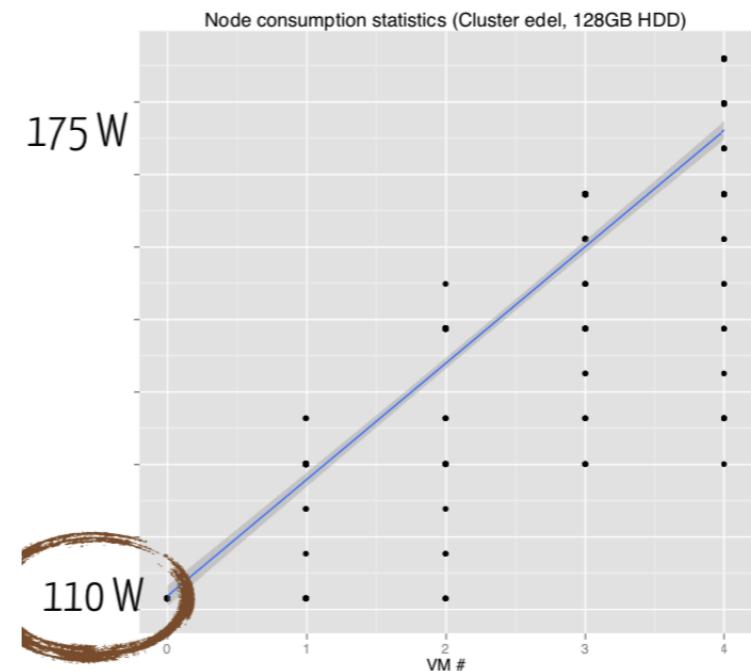
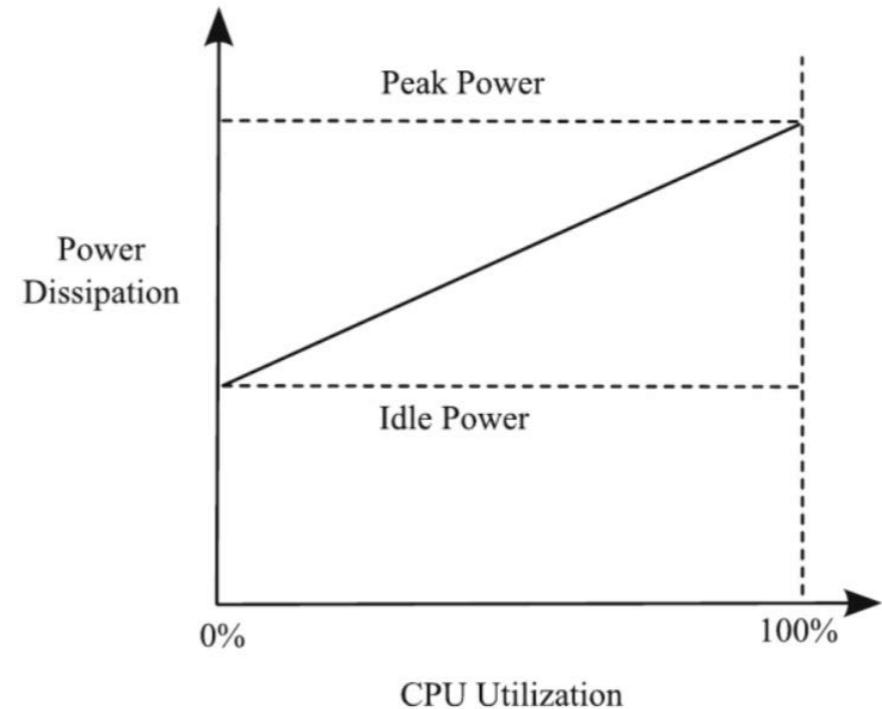
# Inside a data center

- Racks of **servers** to compute/store/run applications
- Applications launched in isolated environment: **Virtual Machines (VMs)**
- **Scheduler** places VMs on servers
  - with sufficient resources
  - to have an “efficient” data center



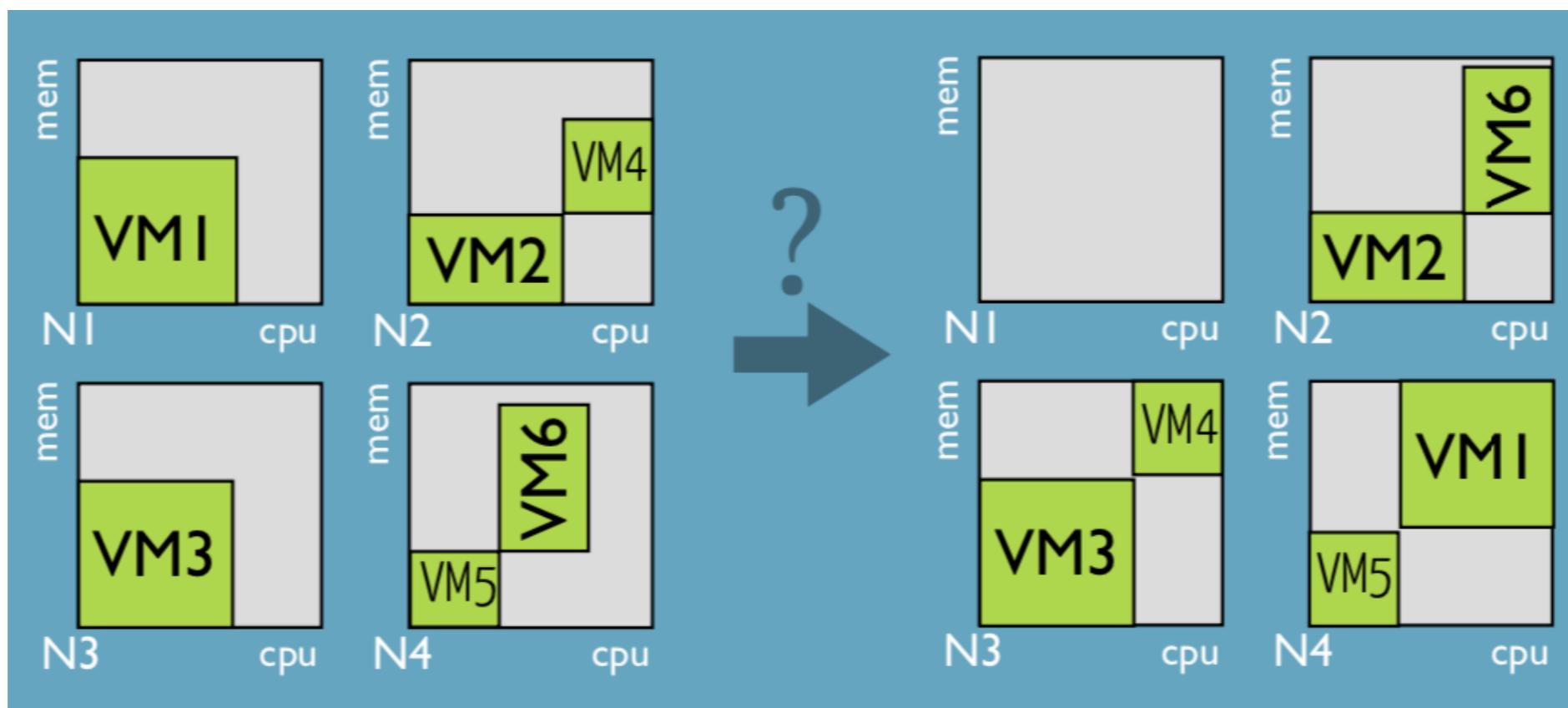
# Power Model

- Servers are **not energy efficient**  
= not energy proportional to usage
- Close to an ON/OFF Model.

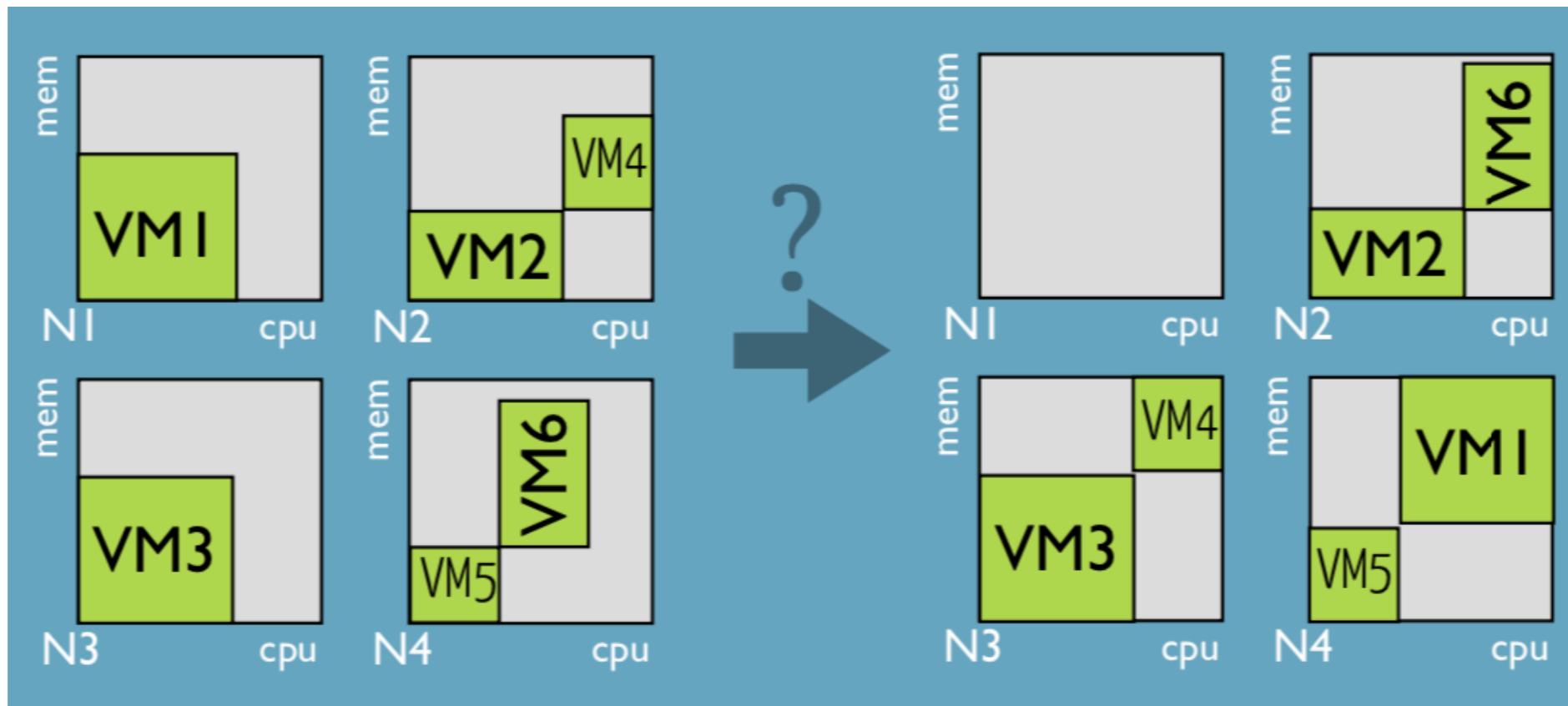


# Saving Energy

- Solution to save energy:
  - Consolidation of VMs on a **minimum** number of servers
  - Putting to sleep unused servers



# Challenge



How to find the placement using the minimum number of servers?

# Combinatorial Problem

## Classic Problem: Bin Packing

**Instance:** Finite set  $I$  of items. A size  $s(i) \in N$  for each  $i \in I$ , a positive bin capacity  $B$  and a positive integer  $K$ .

**Question:** Is there a partition of  $I$  into disjoint sets  $I_1, \dots, I_K$ , such that the sum of the sizes of the items in each  $I_j$  is  $B$  or less?

## Optimization variant.

What is the **minimum value** of  $K$ ?

A solution is optimal if it has minimal  $K$ . The  $K$ -value for an optimal solution for a set of items  $I$  is denoted by  $\text{OPT}(I)$  or just  $\text{OPT}$  if the set of items is clear from the context.

# Bin Packing - An Example

- Input:  $I = \{4, 8, 1, 4, 2, 1\}$ . Bin Capacity  $B = 10$ .
- Question: How many bins are necessary?

# Bin Packing - Exercises

- Input:  $I = \{9, 8, 2, 2, 5, 4\}$ . Bin Capacity  $B = 10$ .
- Question: How many bins are necessary?

- Input:  $I = \{2, 5, 4, 7, 1, 3, 8\}$ . Bin Capacity  $B = 10$ .
- Question: How many bins are necessary?

- Question: Propose efficient algorithms to solve the pb

# Bin packing - Complexity

- The bin packing problem is **strongly NP-complete**.
- No approximation algorithm with absolute approximation ratio smaller than  $3/2$  unless  $P = NP$ .
- Bin packing is solvable in pseudo-polynomial time for any **fixed** number of bins  $K$ , and solvable in polynomial time for any **fixed** bin capacity  $B$ .

# Bin packing - Algorithms

- **First-Fit (FF)** keeps all bins open, in the order in which they were opened. It attempts to place each new item into the **first bin in which it fits**.  
Approximation ratio  $\text{FF}(L) \leq 1.7 \text{ OPT}$ .

# Aparté: Approximation algorithms

**Definition:** An **approximation algorithm** produces

- in **polynomial time**
- a **feasible solution**
- whose objective function value is close to the optimal OPT, by close we mean **within a guaranteed factor** of the optimal.

**Example:** A 2-approximation algorithm for Bin Packing partition the tasks into a number of bins  $\leq 2 \times \text{OPT}$  ( $\text{OPT} = \text{minimum number of bins}$ )

# Bin packing - Algorithms

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- Input:  $I = \{5, 7, 3, 4, 8\}$ . Bin Capacity  $B = 10$ .
  - Question: Apply FF algorithm.

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- **Best-Fit (BF)**, too, keeps all bins open, but attempts to place each new item into the **bin with the maximum load** in which it fits.  
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- Question: Apply BF algorithm.

# Bin packing - Algorithms

- Input:  $I = \{5, 7, 2, 4, 3, 8\}$ . Bin Capacity  $B = 10$ .
- Question: Apply FF and BF algorithms.

# Bin packing - Algorithms

- Input:  $I = \{5, 7, 2, 4, 3, 8\}$ . Bin Capacity  $B = 10$ .
- Question: Apply FF and BF algorithms.
- **First-fit-decreasing (FFD)** - **orders** the items by descending size, then calls First-Fit.  
Approximation ratio  $\text{FFD}(I) = \frac{11}{9} \text{OPT}(I) + \frac{6}{9}$ .

# Bin packing - Algorithms

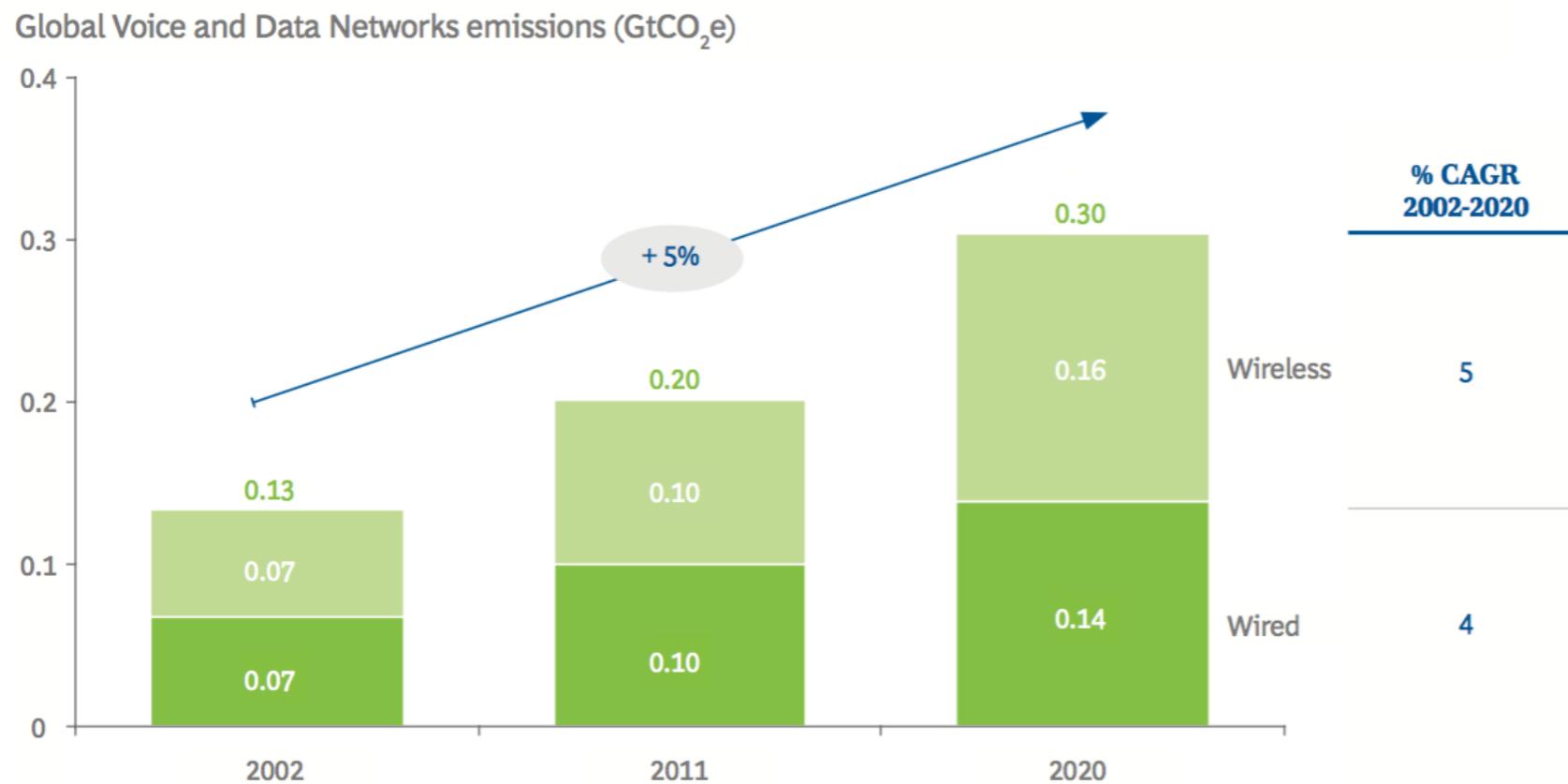
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- Question: Apply FFD algorithm.

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# Wired vs Wireless Networks



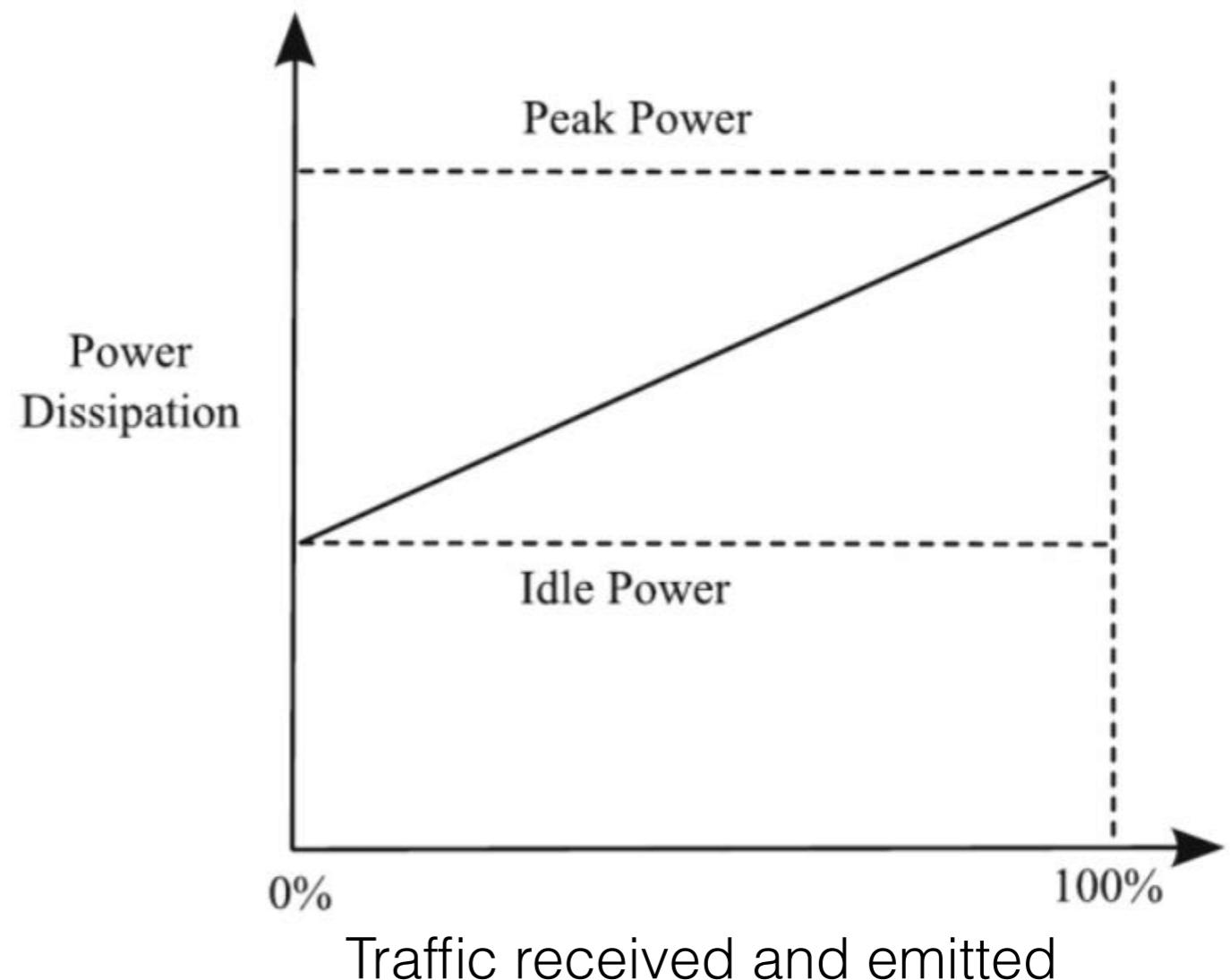
- **Wired network footprint = Wireless network footprint.**
- But **Mobile network emissions expected to grow faster** than wired networks emissions

# Mobile Networks

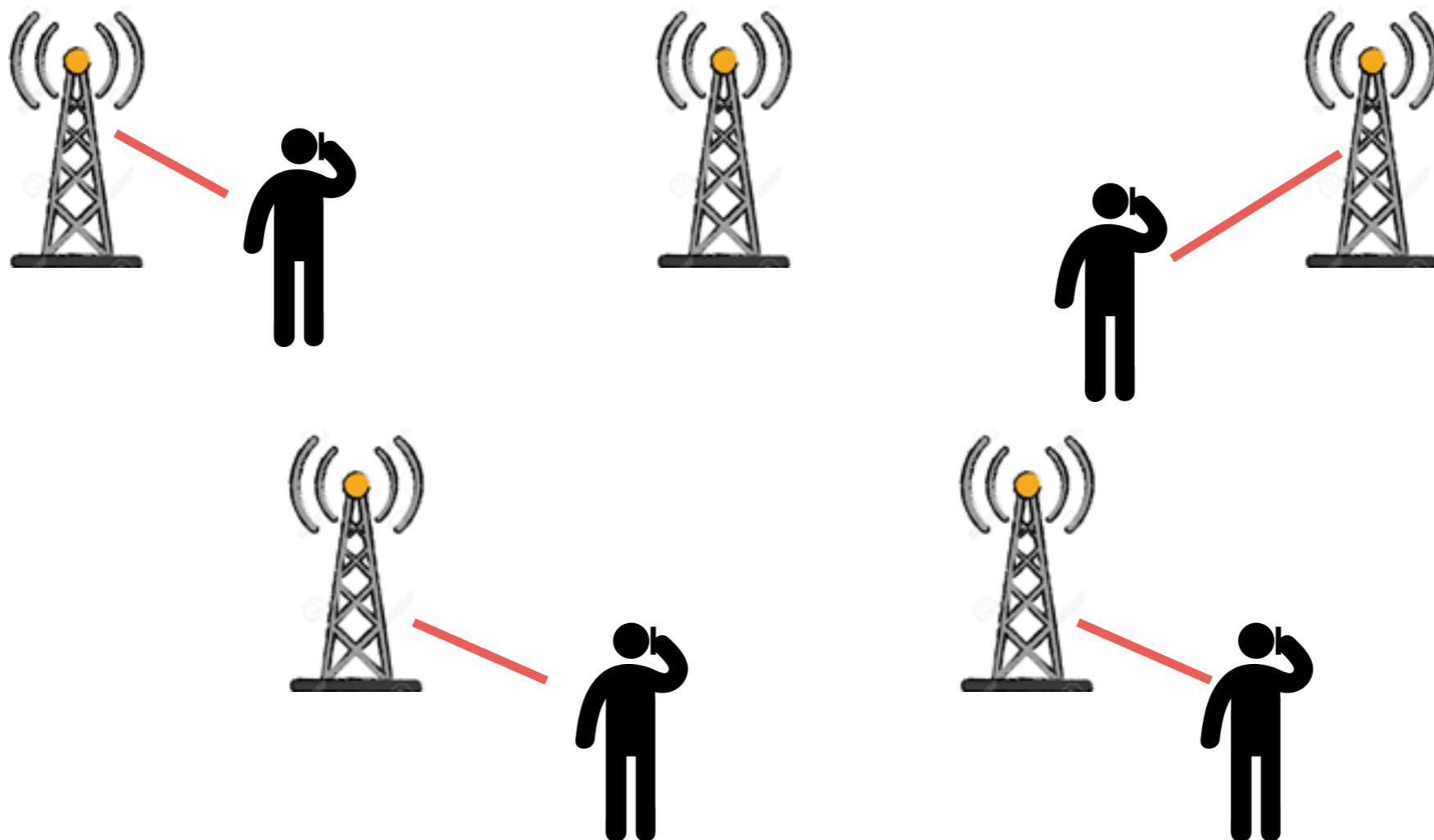


# Power models of Antennas

- Again: energy consumption **not** proportional to traffic
- A solution to save energy: **put antennas to sleep mode**

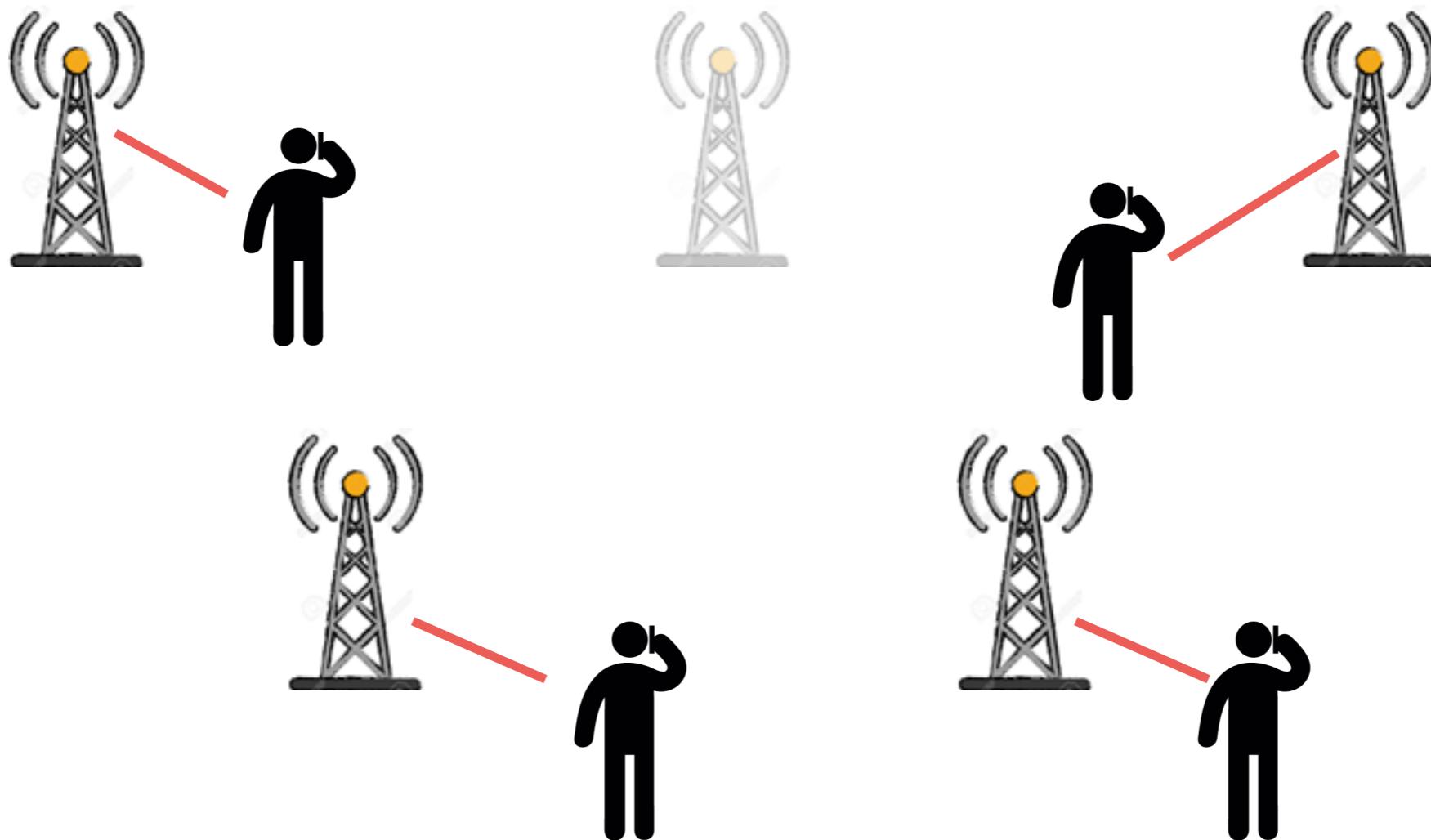


# Mobile Networks



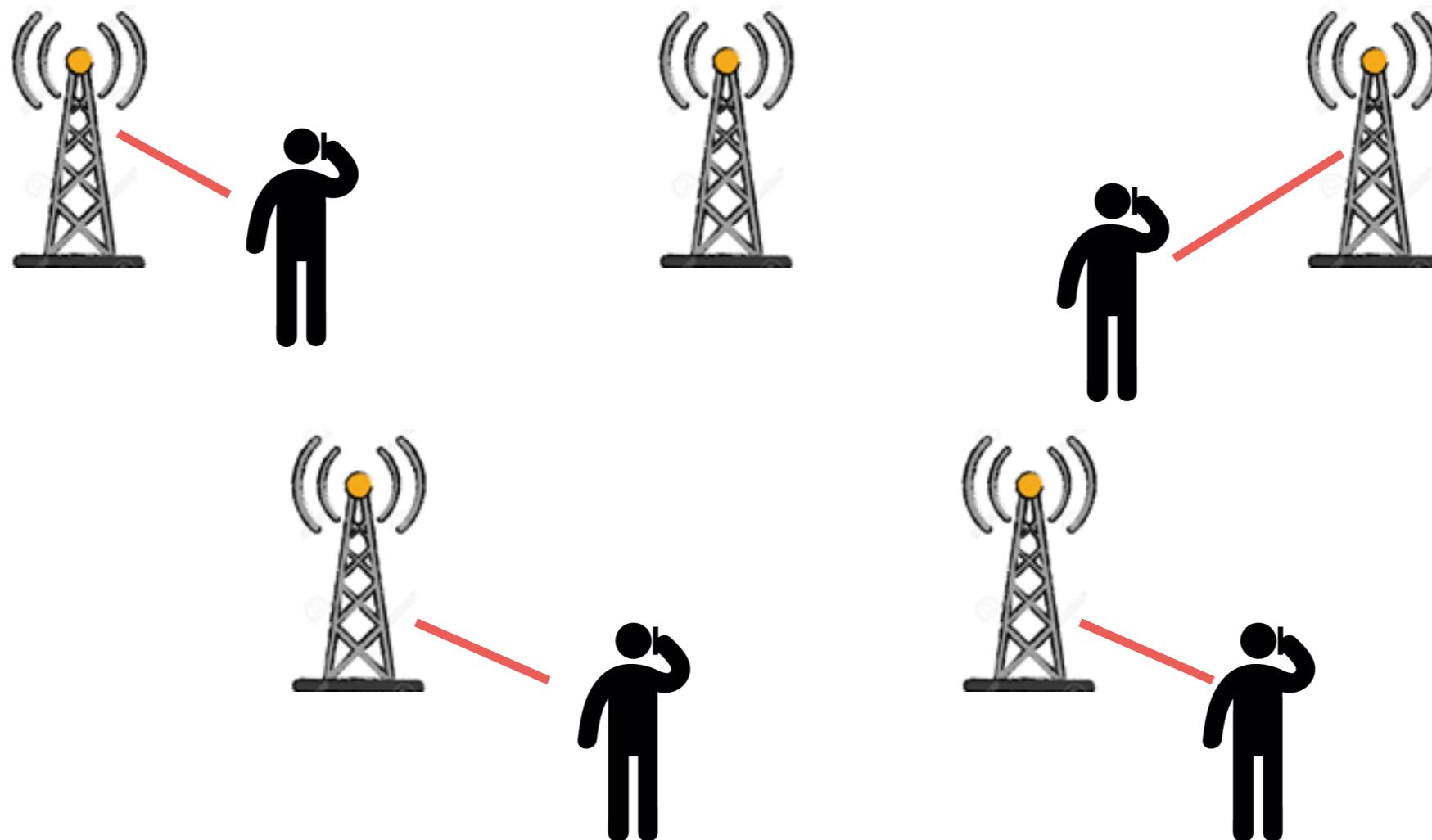
Association user phone - Antennas

# Mobile Networks



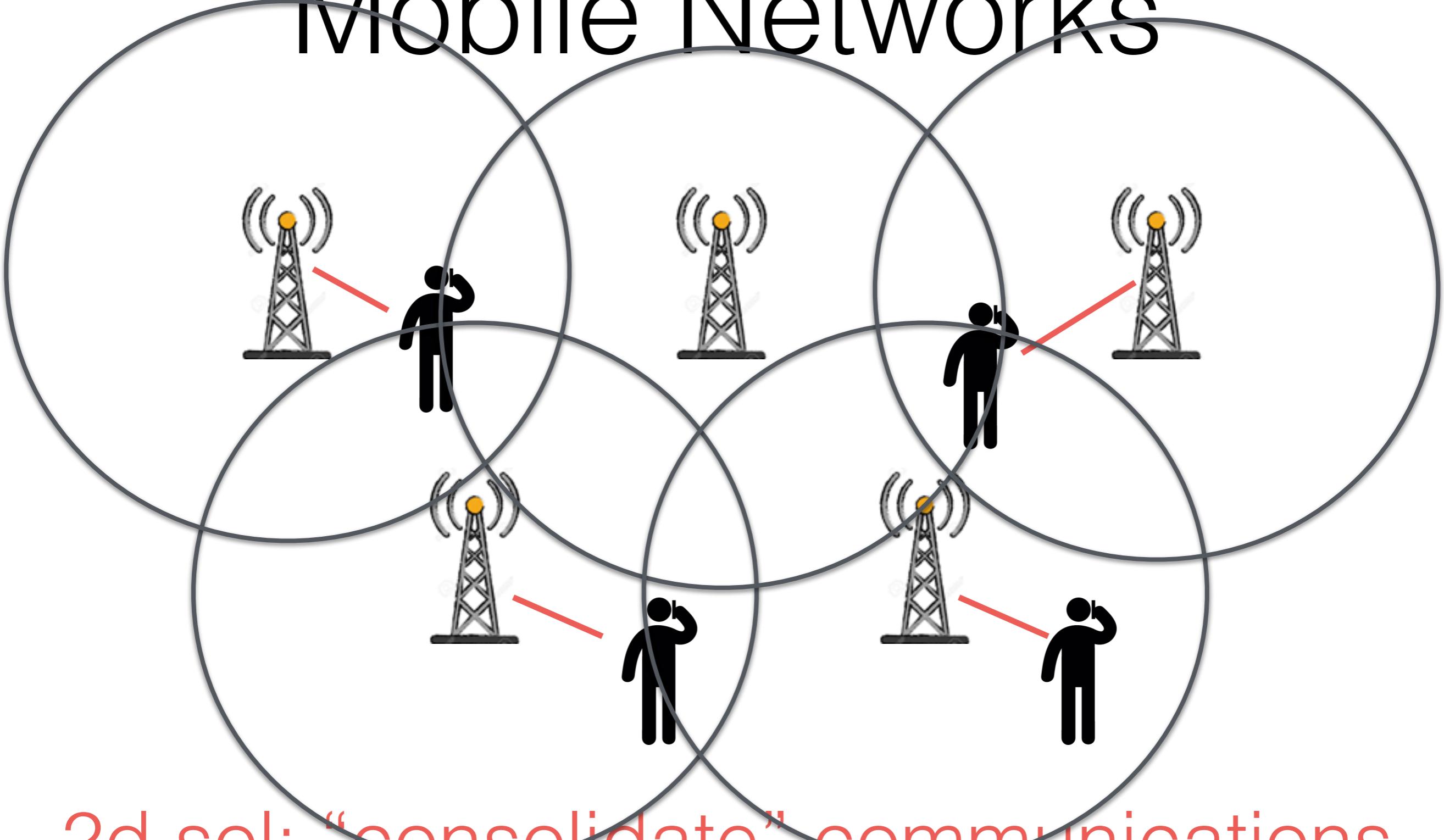
1st sol: Put to sleep unused antennas

# Mobile Networks



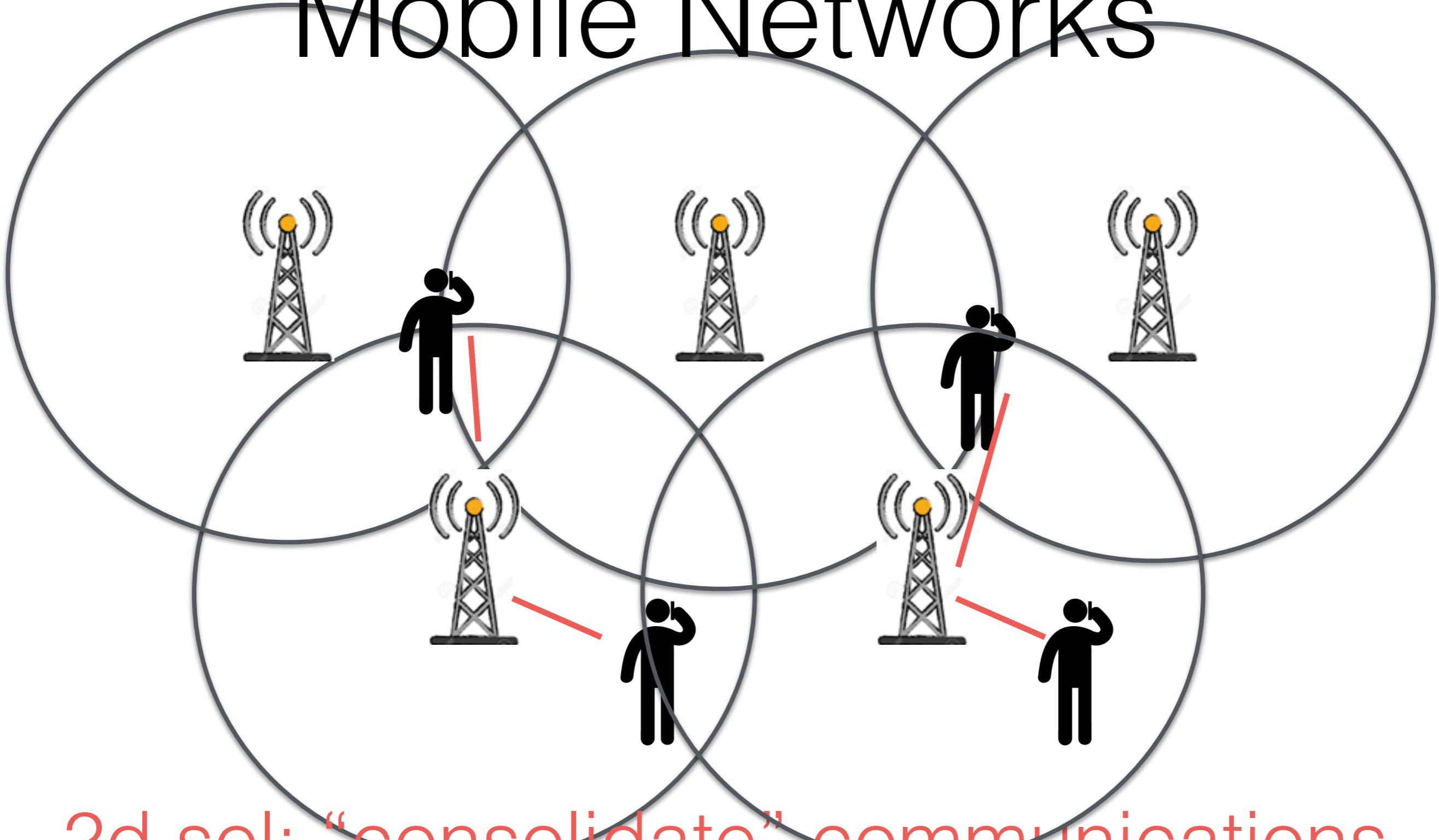
2d sol: “consolidate” communications

# Mobile Networks



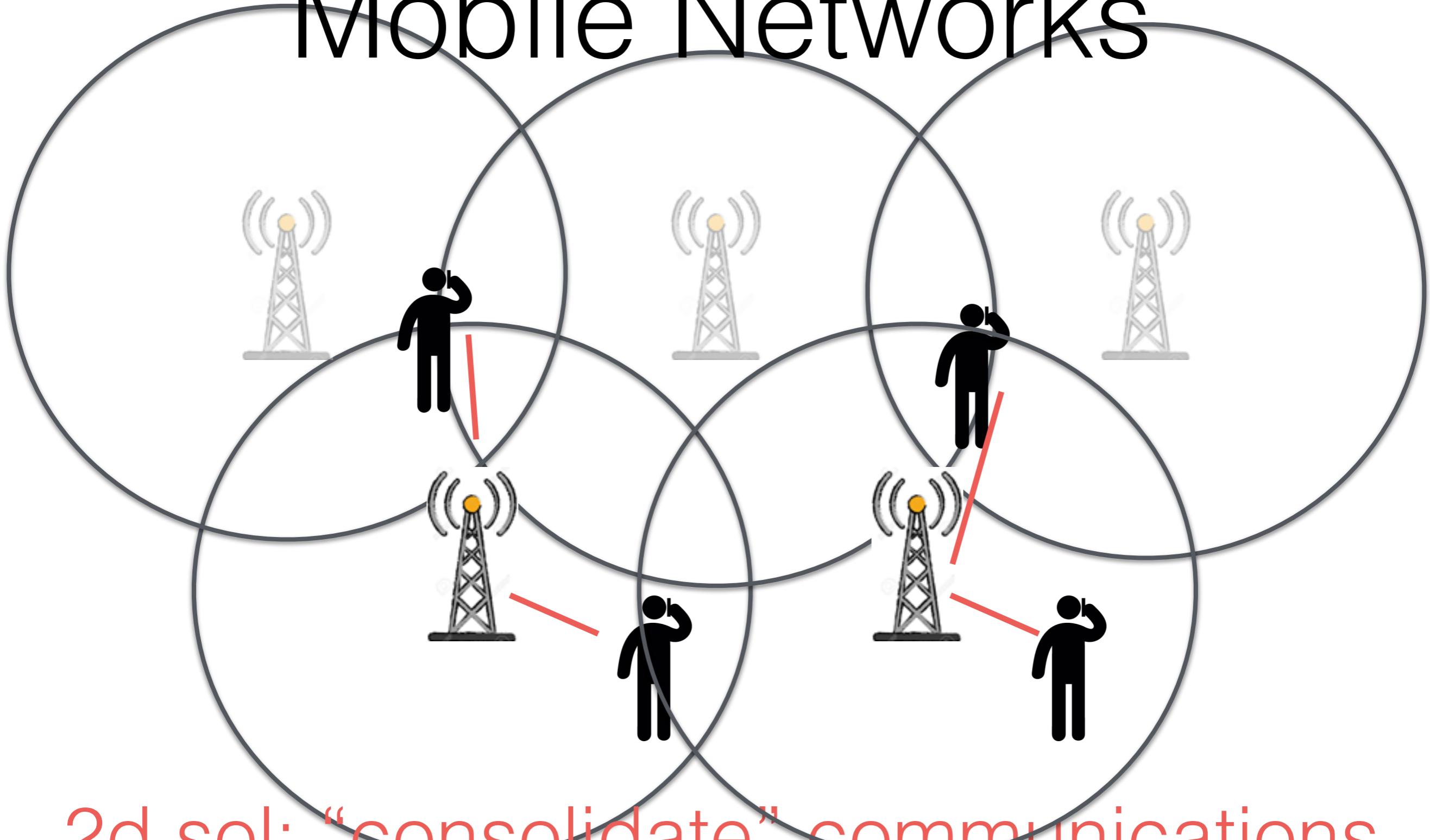
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# Mobile Networks



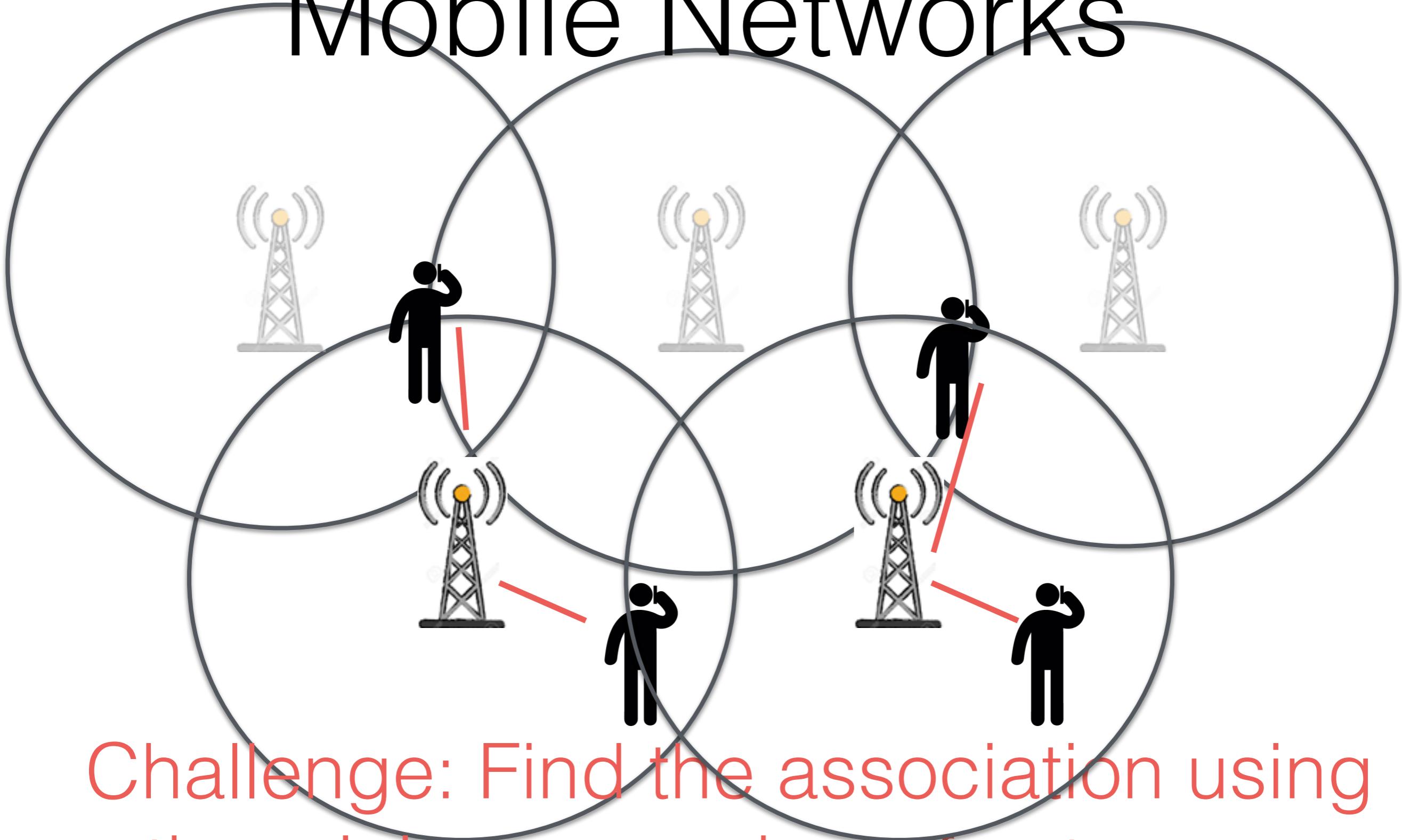
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# Mobile Networks



2d sol: “consolidate” communications

# Mobile Networks



Challenge: Find the association using the minimum number of antennas.

# Combinatorial Optimization Problem

- Minimum Set Cover Problem

**Problem:** Given a universe  $U$  of  $n$  elements, a collection of subsets of  $U$ ,  $\mathcal{S} = S_1, \dots, S_k$ , and a cost function  $c : S \rightarrow Q^+$ , find a minimum cost subcollection of  $S$  that covers all elements of  $U$ .

- Here, we consider that the cost of all  $S_i$  is uniform  $c=1$ .

# Exercise

- Ex1. Solve the minimum set cover problem for the following instance:  $U=\{1,2,3,4,5,6\}$   $S1=\{1\}$   $S2=\{5,6\}$   $S3=\{3,4,5\}$   $S4=\{2,6\}$   $S5=\{1,3\}$

# Algorithm

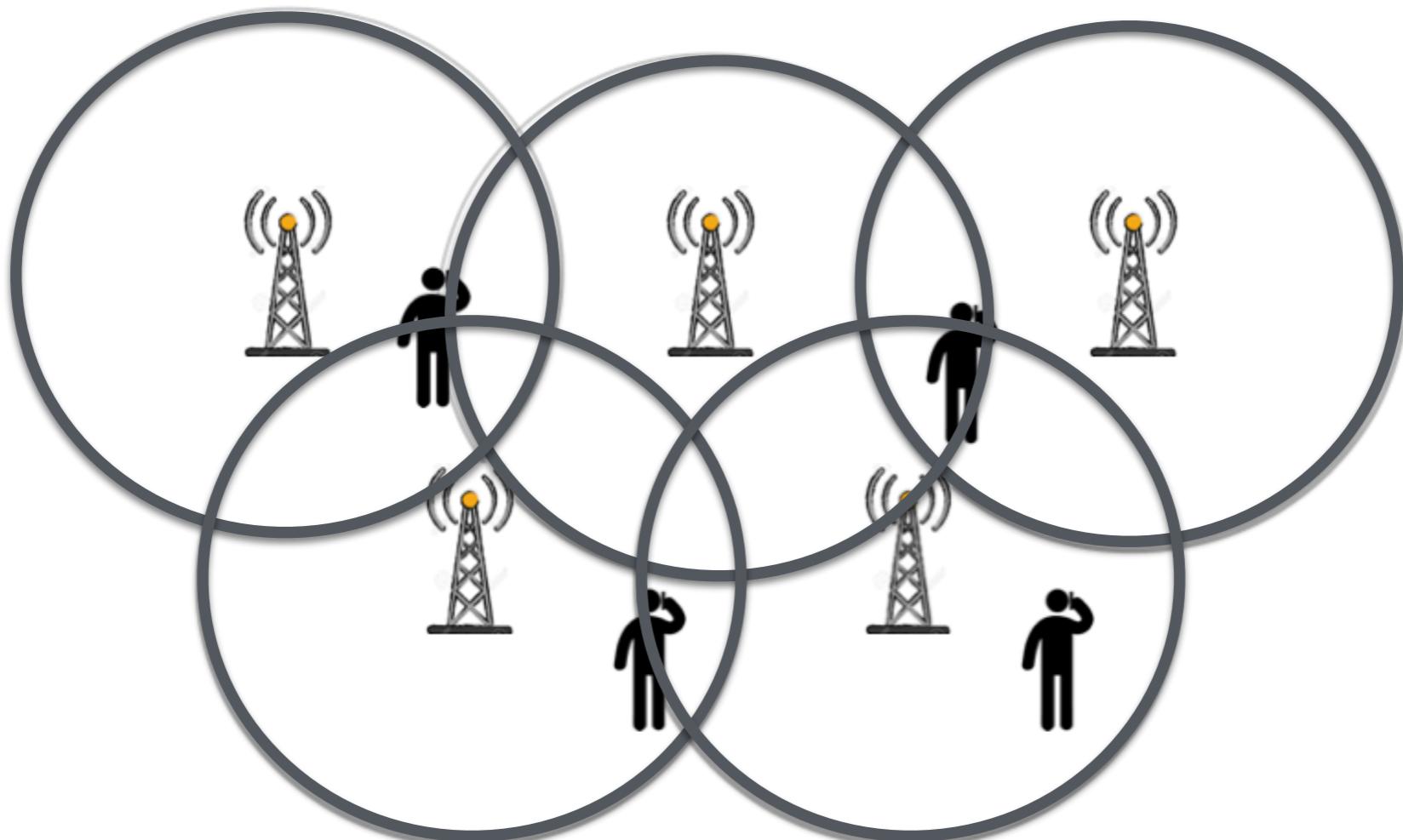
- Greedy approximation algorithm:
  - at each stage, choose the set that contains the largest number of uncovered elements.
- Algorithmic complexity: This method can be implemented in time linear in the sum of sizes of the input sets, using a bucket queue to prioritize the sets.
- Achieves an approximation ratio of  $H(s)$  ( $s$ -th harmonic number), where  $s$  is the size of the set to be covered.  
In other words, it finds a covering that may be  $H(s)$  times as large as the minimum one. 
$$H(n) = \sum_{k=1}^n \frac{1}{k} \leq \ln n + 1$$

# Exercises

- Ex2. Apply the greedy algorithm for the following instances:
  - $U=\{1,2,3,4,5,6\}$   $S_1=\{2,3,5\}$   $S_2=\{1,3\}$   $S_3=\{2,3,6\}$   
 $S_4=\{1,4\}$   $S_5=\{5,6\}$
  - $U = \{1,\dots,6\}$   $S_1=\{3,4\}$   $S_2=\{1,3,5\}$   $S_3=\{5,6\}$   
 $S_4=\{1,2\}$

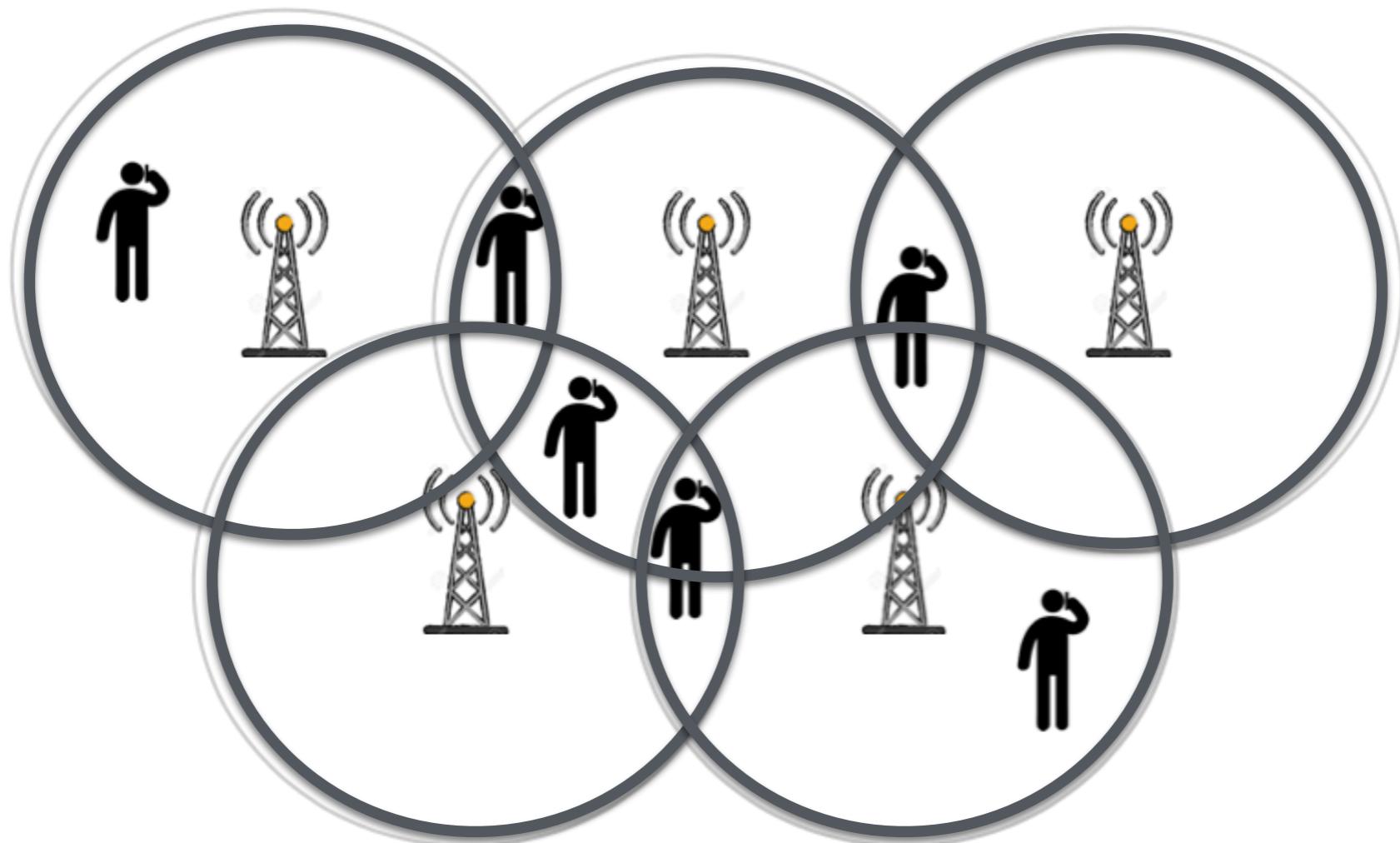
# Exercise

- Ex3. Apply the greedy algorithm for the following instance (if a person touches a disk or circle of an antenna, he can use it to communicate)



# Exercise

- Ex4. Apply the greedy algorithm for the following instance (if a person touches a disk or circle of an antenna, he can use it to communicate)

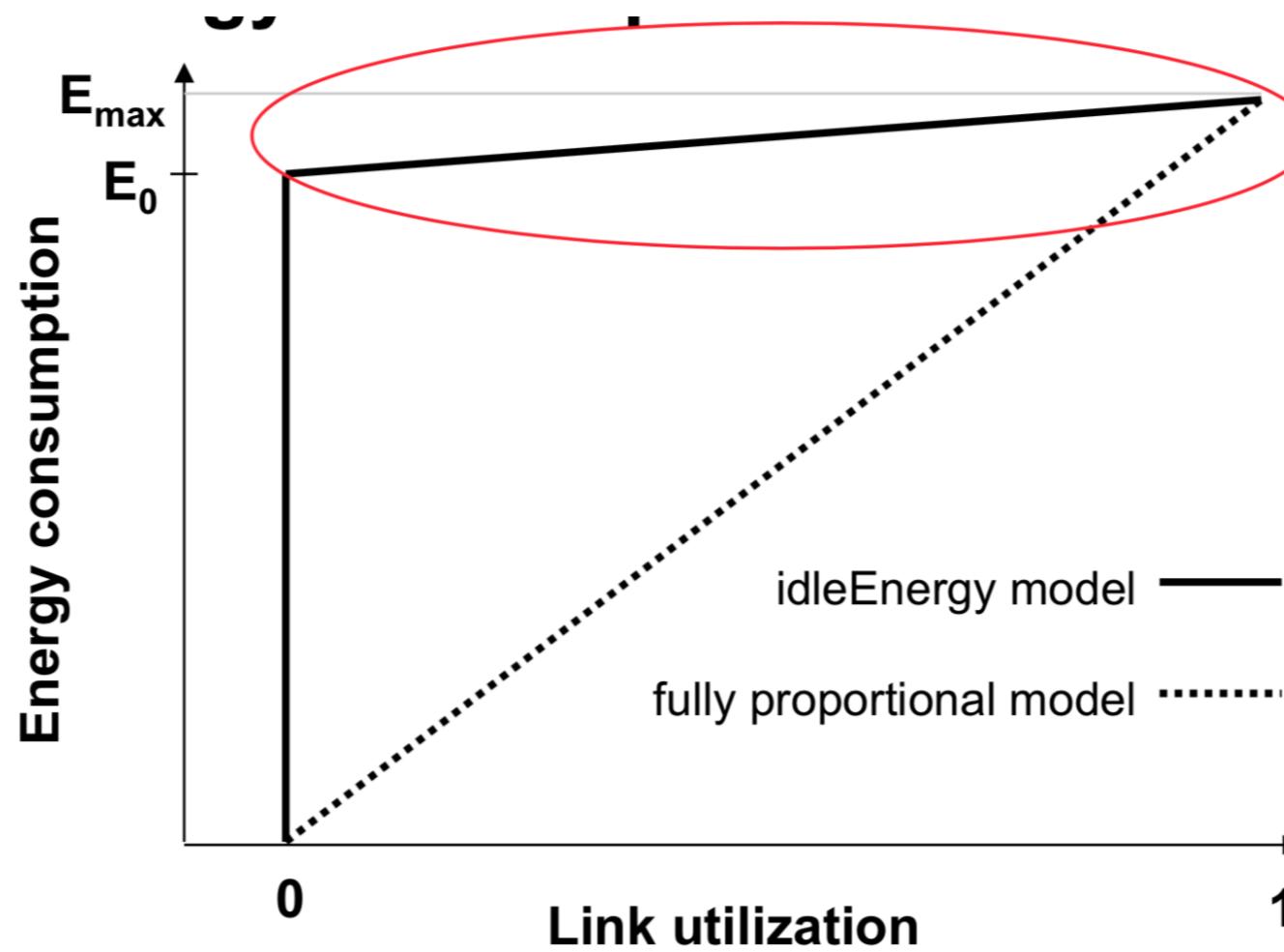


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# Energy Efficiency of Wired Networks

- Measurement on energy consumption on routers:

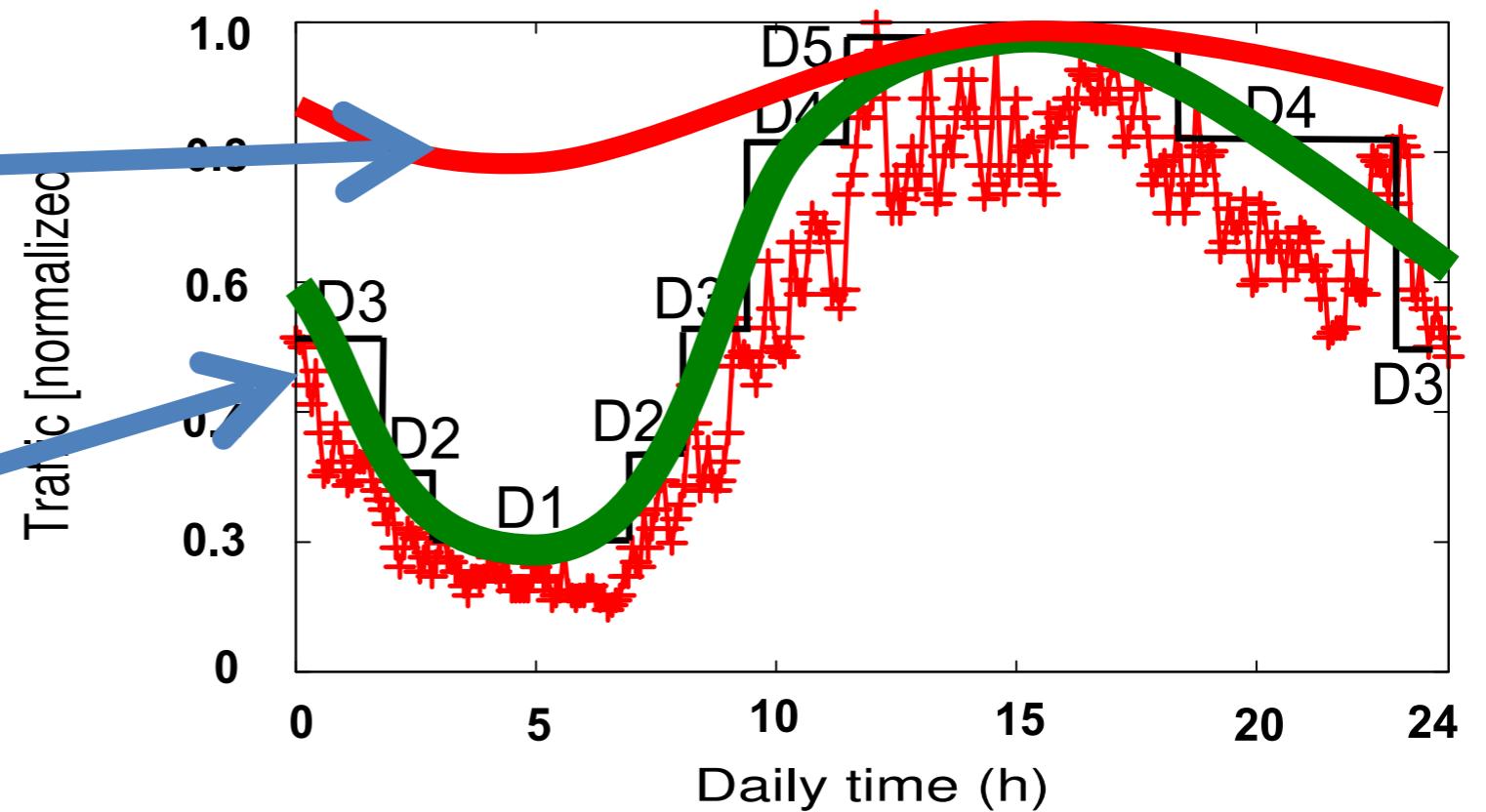


Small influence of traffic load  
To save energy switch off interfaces and chassis

# Energy Efficiency of Wired Networks

Current power consumption

Ideal power consumption



# Energy Aware Routing (EAR)

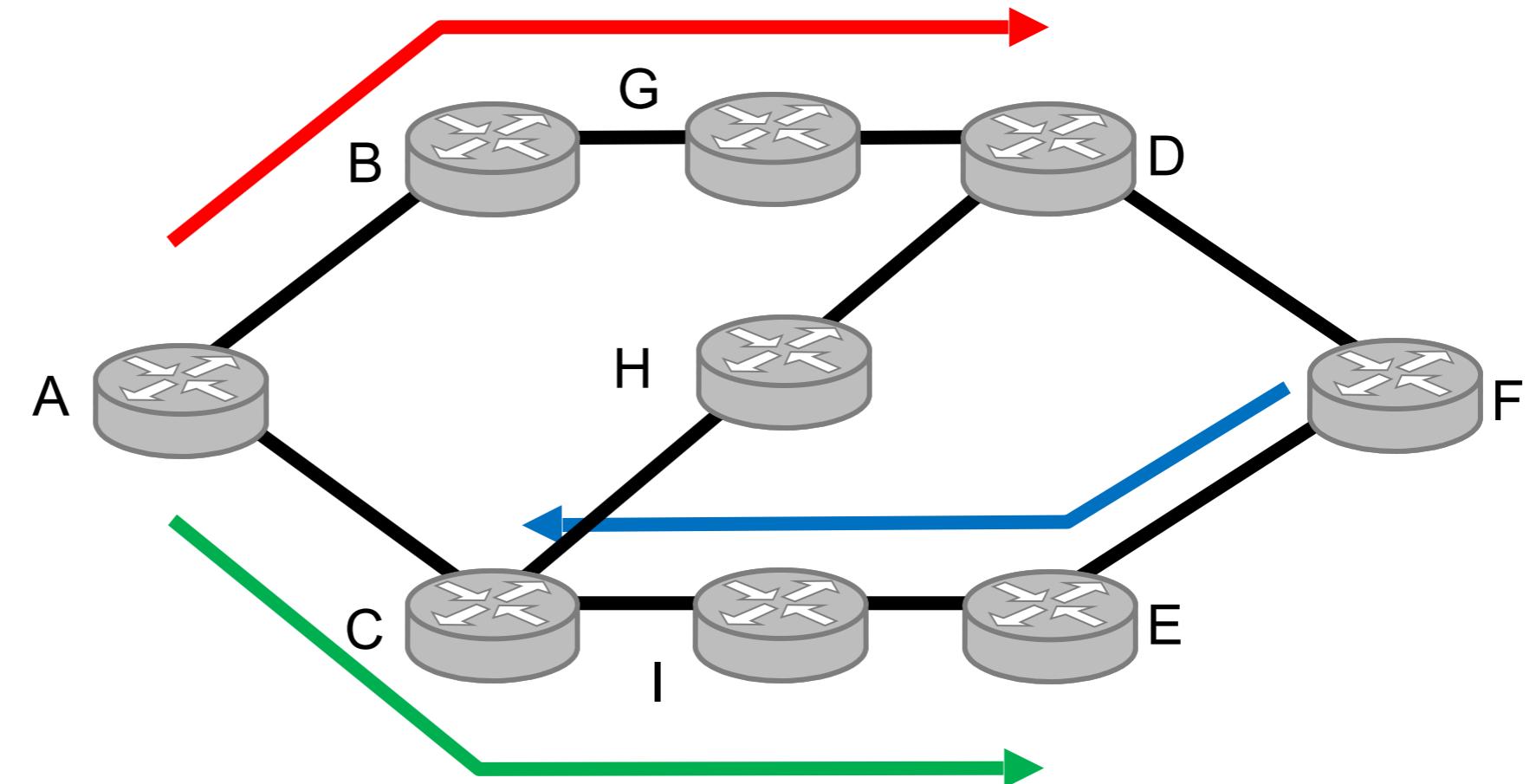
Link Capacity = 2

Path between:

**A et D**

**F et C**

**A et E**



Routing request while minimizing the number of active devices  
(routers and/or links)

# Energy Aware Routing (EAR)

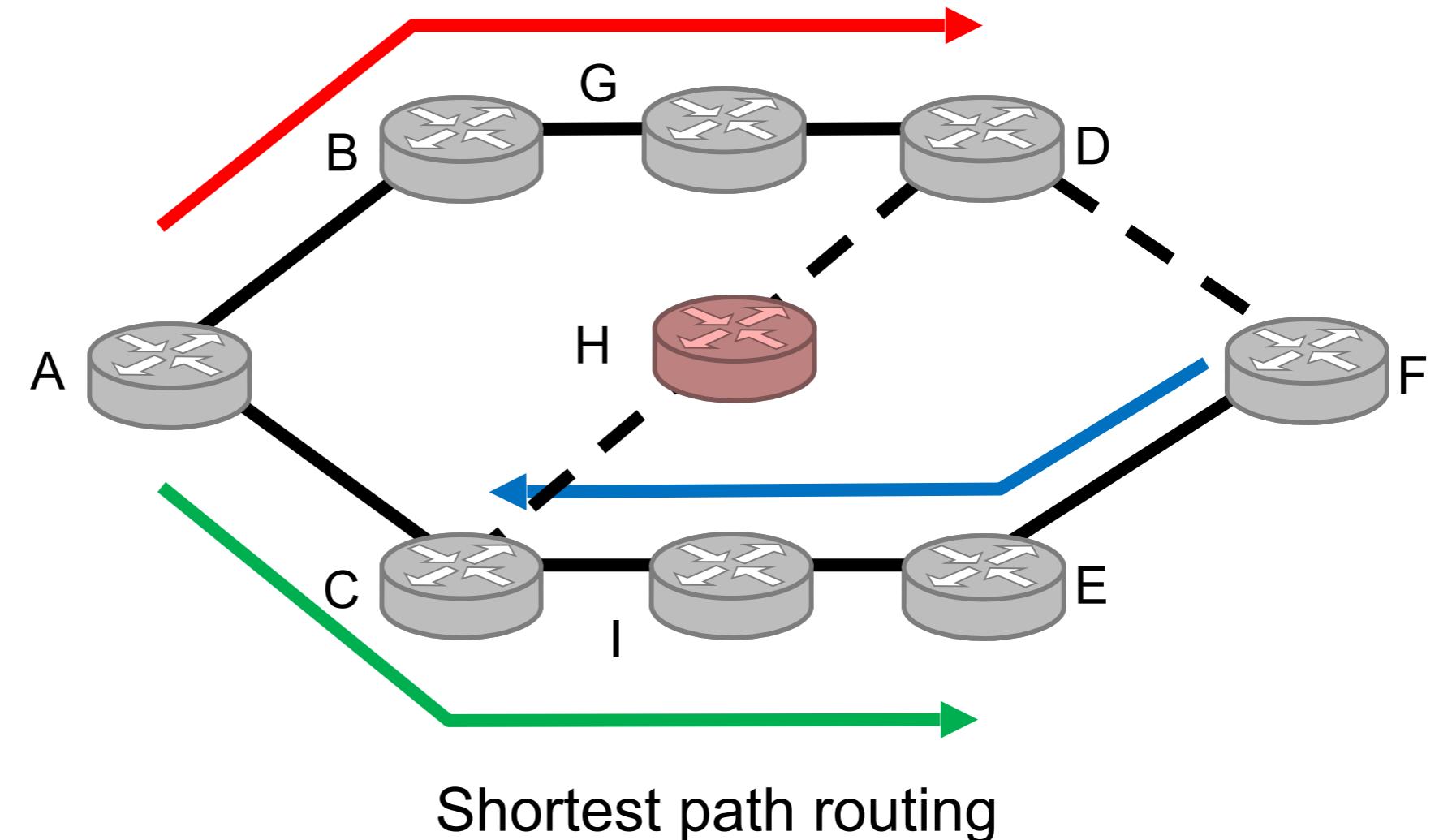
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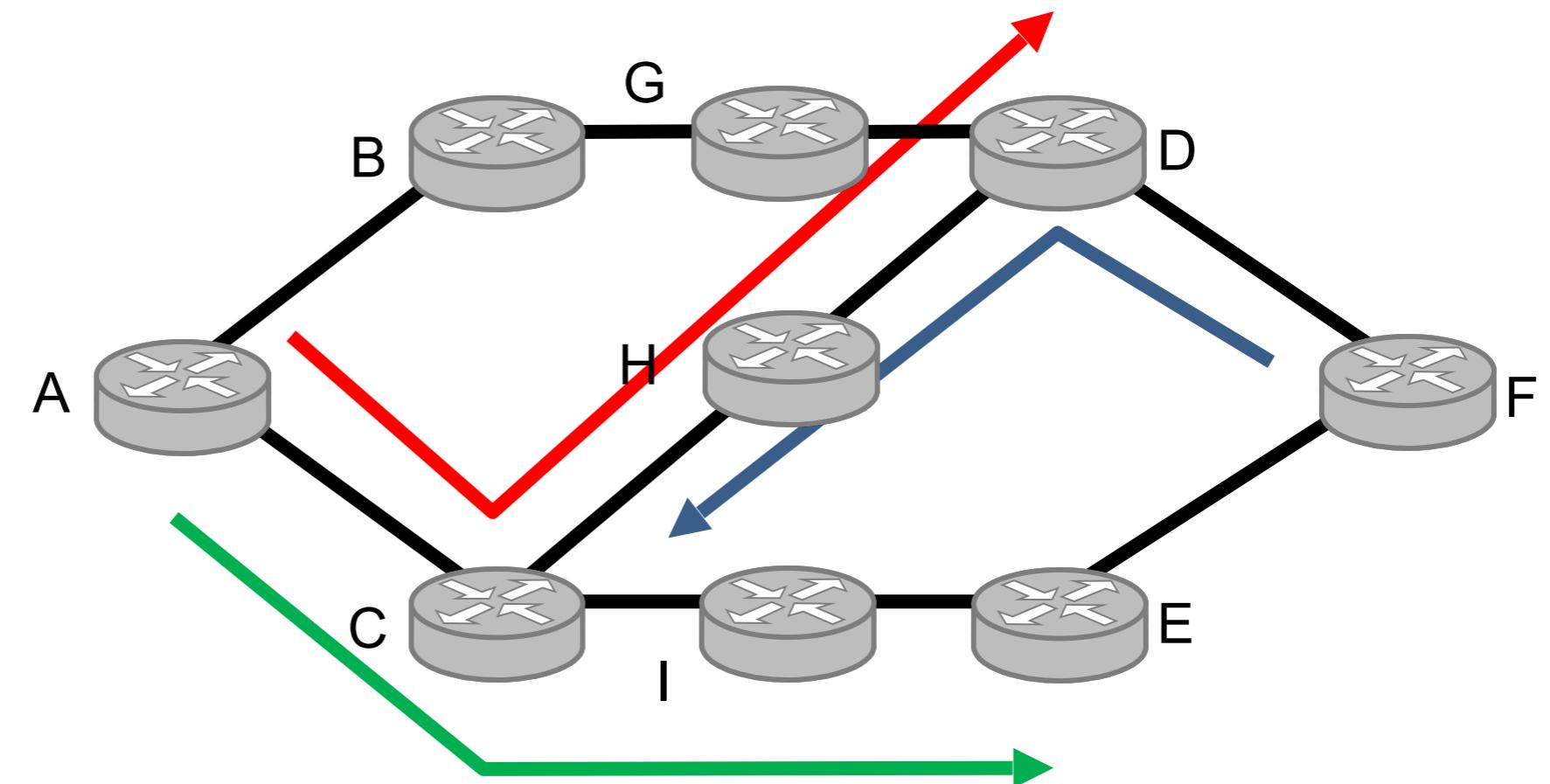
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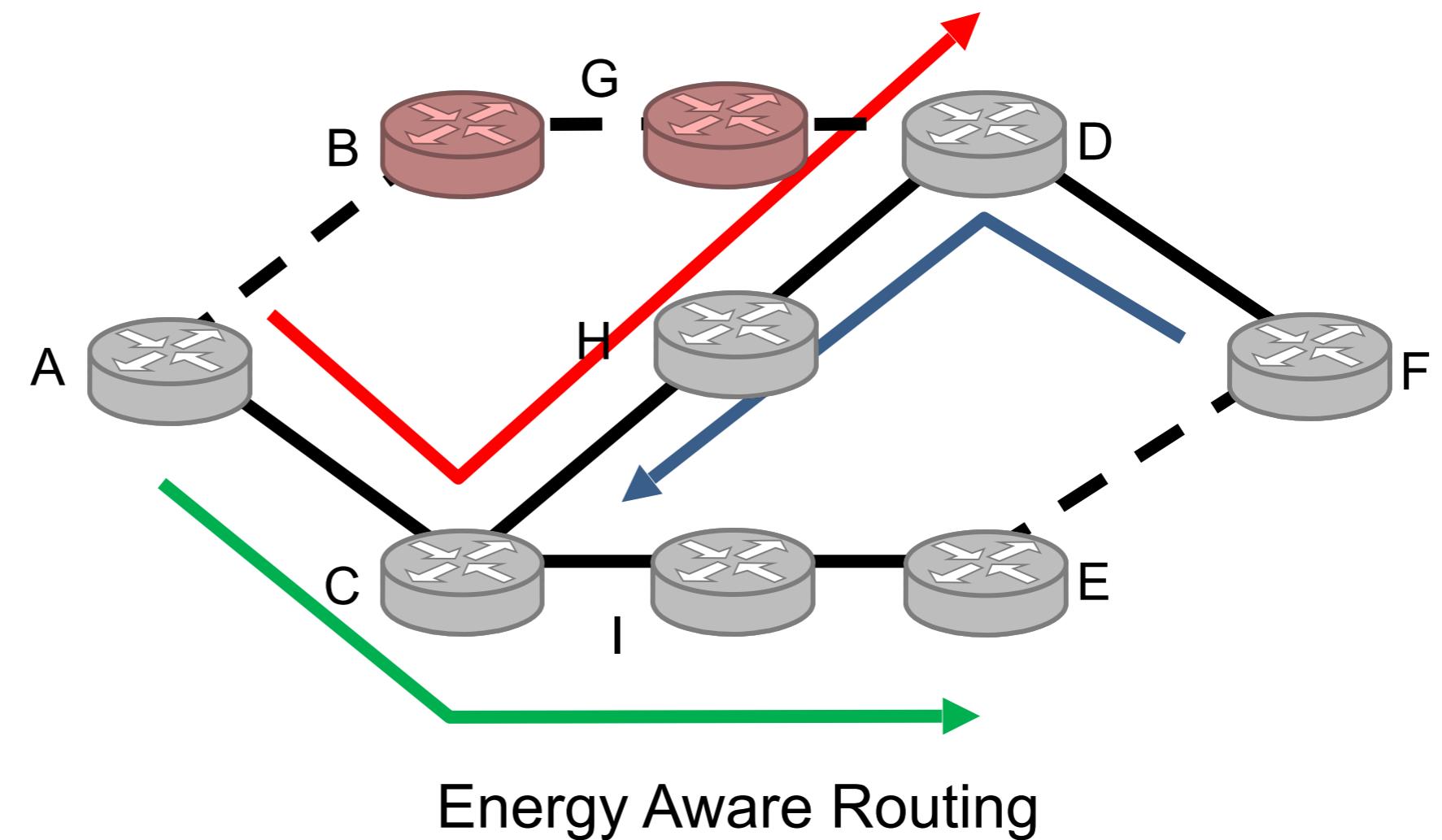
Link Capacity = 2

Path between:

**A et D**

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**A et E**



Routing request while minimizing the number of active devices  
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# Solving the Problem

- **Complexity:** NP-complete, Not-approximable.
- Modeling the problem as Mixed Integer Linear Program (MILP) and use solvers.
- **Heuristic algorithms.**
  - Least loaded + shortest path (LL-SP): try to put into sleep the least loaded ressource.

# Algorithms

## **Algorithm: Least loaded + shortest path (LL-SP)**

$L = V$

While ( $L$  not empty):

    Select the least loaded node  $/l_n$  in  $L$

    Try to put  $/l_n$  to sleep.

    Route all demands using SPs

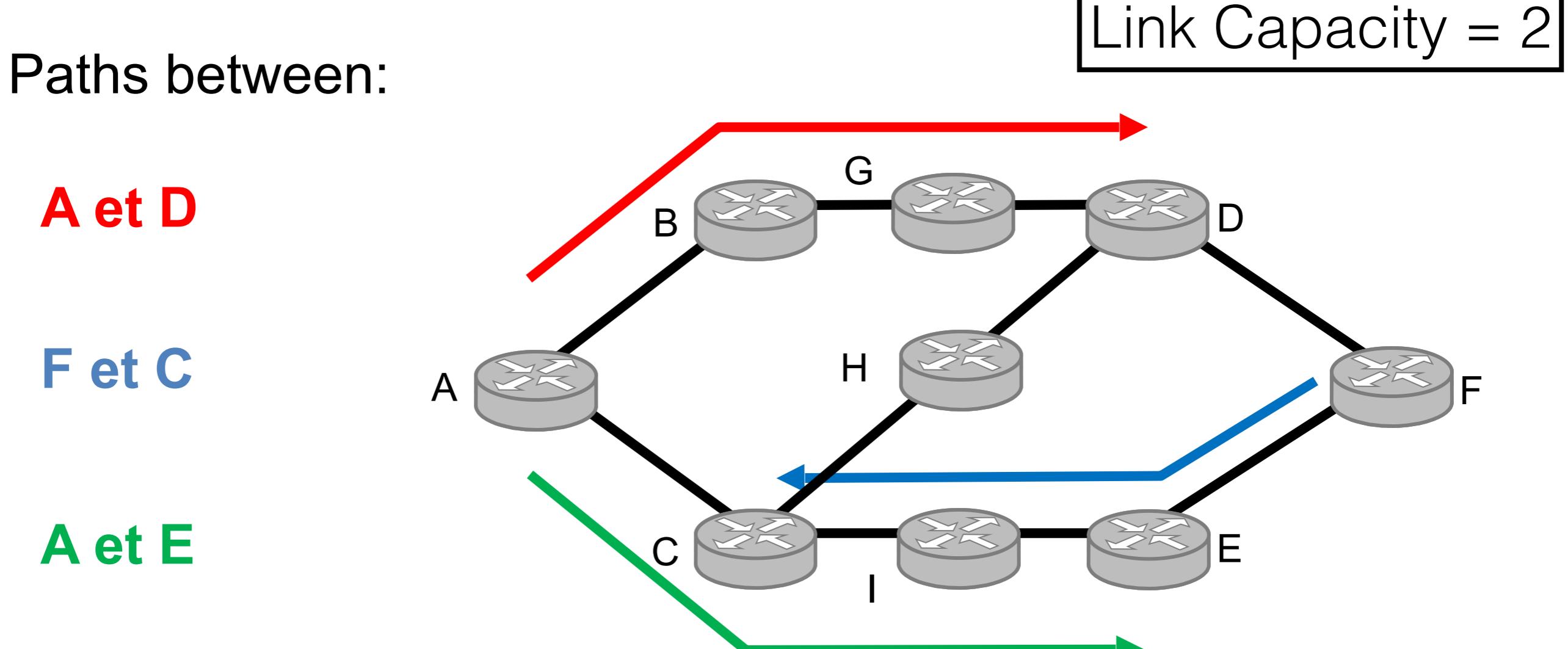
    If routing NOT feasible

        Put  $/l_n$  back ON

        Go back to previous routing  
        remove  $/l_n$  from  $L$ .

# Exercise

- Apply LL-SP to the following instance:



# Take-aways

- In data centers.
  - VM consolidation
  - Bin packing problem
  - Classic algorithms



\*

# Take-aways

- In mobile networks
  - Putting to sleep antennas
  - Set cover problem
  - Greedy approximation algorithm



\*

# Take-aways

- In core networks
  - Energy aware routing
  - LL-SP heuristic



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# Take-aways

- A lot proposed since 2008.
- A lot remains to be put into reality  
(good for us :-)



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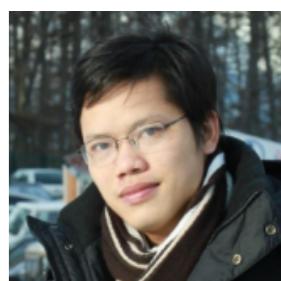
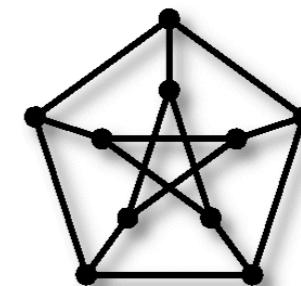
# Who we are?



- Working in the **team COATI** at Sophia Antipolis (Inria and I3S/CNRS/University of Nice Sophia Antipolis)



- **Expertise:**



- **In General:** Algorithmics, combinatorics and optimization for telecommunication networks.



- **On Energy Efficiency:** mostly **networks and data centers.**



# Conclusions

- Encouraging technology advances and challenges:
  - More energy efficient hardwares
  - SDN revolution and virtualisation
  - Ubiquitous networking and multiple joint optimization



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# Conclusions

- Encouraging technology advances and challenges:
  - More energy efficient hardwares
  - SDN revolution and virtualisation
  - Ubiquitous networking and multiple joint optimization



**Thanks for your attention!!!**

## Credits due to:

- **Surveys:**

- Bolla, R., Bruschi, R., Davoli, F., & Cucchietti, F. (2011). Energy efficiency in the future internet: a survey of existing approaches and trends in energy-aware fixed network infrastructures. *Communications Surveys & Tutorials*, IEEE, 13(2), 223-244.

- **Slides:**

- F. Davoli. Green Networking and Network Programmability: A Paradigm for the Future Internet? 22d ITC Specialist Seminar. 2013
- Christensen, K., & Nordman, B. Reducing the energy consumption of networked devices. IEEE 802.3 tutorial.
- D. Kilper, Tutorial: Energy Efficient Networks.
- D. Lopez & F. Giroire, Green Networks, Master Course, University Nice-Sophia Antipolis, 2016.
- Design and Management of Networks with Low Power Consumption, Truong Khoa Phan, *PhD Defense*, Sophia Antipolis, 2014
- Slides from presentations from J. Moulierac, N. Huin and M. Rifai.
- F. Hermenier, Resource management in IaaS cloud

- **Reports:**

- Global e-Sustainability Initiative. (2012). GeSI SMARTer 2020: the role of ICT in driving a sustainable future. *Global e-Sustainability Initiative*, Brussels, Belgium.