

a)  $n \log(n) < n \log(n) \log(\log(n)) < n (\log(n))^{\frac{3}{2}} < n^{\frac{4}{3}} (\log(n))^2 < n^{\frac{3}{2}} < 2^{100n} < n^n < 2^{n^2}$

b) True. There exists two constants  $c_1, c_2 > 0$  and  $n_0$  such that  $c_1 \cdot g(n) \leq f(n) \leq c_2 g(n)$  for all  $n \geq n_0$ , which is  $f(n) = \theta(g(n))$