

# Monetary Policy Spillovers

## Transmission Through Networks

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June 26, 2025

# Introduction

- Effects of US monetary policy shocks on stock returns using Input-Output networks (Ozdagli and Weber 2017; Di Giovanni and Hale 2022)

$$y_t = \alpha + \rho W y_t + X_t \beta + \varepsilon_t$$

## Does the choice of network matter?

- Pure trade weights for all variables outperformed in model fit or predictive accuracy by other linkages in GVAR setting (Eickmeier and Ng 2015; Feldkircher and Huber 2016; Martin and Crespo Cuaresma 2017)

# Network Visuals

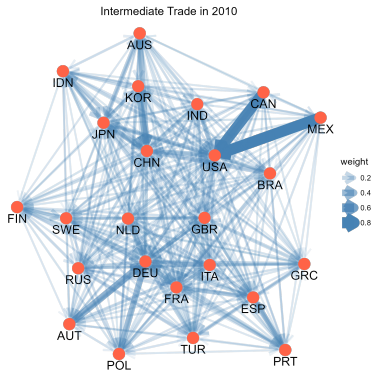


Figure 1: Intermediate Trade

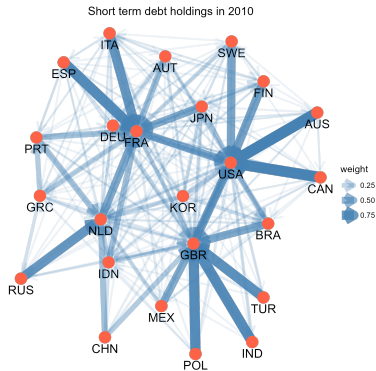


Figure 2: Short-term debt

## **Which networks are important for the transmission of US monetary policy shocks?**

- ▶ Evaluate spillovers of US monetary policy shocks to international stock returns using SAR model
- ▶ Estimate convex combinations of time-varying networks
- ▶ BMA for uncertainty wrt. number of networks

Dynamic setting with multiple variables

Deal with endogeneity of networks

# Introduction

Model uncertainty in linear regression model

(Fernández, Ley, and Steel 2001)



Model uncertainty wrt.  $X$  in SAR model

(LeSage and Parent 2007)



Uncertainty wrt.  $W$

(LeSage and Fischer 2008; Piribauer and Crespo Cuaresma 2016)



Estimate convex combination  $W_c = \sum_{\ell=1}^L \gamma_{\ell} W_{\ell}$

(Debarsy and LeSage 2018; Debarsy and LeSage 2022)

# Introduction

**Table 1:** Comparison of Di Giovanni and Hale (2022), Debarsy and LeSage (2022) and this project.

	DGH22	DL22	Here
HETSAR	✓		
Panel	✓		✓
Time-varying $W$			✓
Estimate $W_c(\Gamma)$		✓	✓
BMA		✓	✓

## Setup

$$y = \rho W_c(\Gamma)y + X\beta + \varepsilon, \quad \varepsilon \sim N(0, \sigma^2 I_{NT})$$

$$W_c(\Gamma) = \sum_{\ell=1}^L \gamma_{\ell} W_{\ell}, \quad 0 \leq \gamma_{\ell} \leq 1, \quad \sum_{\ell=1}^L \gamma_{\ell} = 1, \quad \Gamma = (\gamma_1, \dots, \gamma_L)'$$

$$W_{\ell} = \begin{pmatrix} W_{\ell,1} & 0 & \dots & 0 \\ 0 & W_{\ell,2} & \dots & 0 \\ \vdots & \ddots & \ddots & \vdots \\ 0 & \dots & \dots & W_{\ell,T} \end{pmatrix}$$

- ▶  $W_{\ell,t}$  connectivity matrix:
  - ▶ Main diagonal = 0
  - ▶ Row-sums = 1
  - ▶  $N \times N$  number of cross-sectional observations

Computationally efficient expression:

$$\tilde{y}\omega = X\beta + \varepsilon$$

$$\tilde{y} = (y, W_1y, W_2y, \dots, W_Ly)$$

$$\omega = (1, -\rho\Gamma')'$$

$$W_\ell y = \begin{bmatrix} W_{\ell,1} & 0 & \cdots & 0 \\ 0 & W_{\ell,2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & W_{\ell,T} \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_T \end{bmatrix} = \begin{bmatrix} W_{\ell,1}y_1 \\ W_{\ell,2}y_2 \\ \vdots \\ W_{\ell,T}y_T \end{bmatrix}$$



# Likelihood

## Standard Notation

$$y = \rho W_c y + X\beta + \varepsilon$$

$$(I - \rho W_c)y = X\beta + \varepsilon$$

$$Ry = X\beta + \varepsilon$$

$$\varepsilon = Ry - X\beta$$

## Computationally Efficient

$$\tilde{y}\omega = X\beta + \varepsilon$$

$$\varepsilon = \tilde{y}\omega - X\beta$$

$$\begin{aligned} f_Y(y) &= \left| \frac{\partial \varepsilon}{\partial y} \right| f_\varepsilon(Ry - X\beta) \\ &= |R| \frac{1}{(2\pi\sigma^2)^{n/2}} \exp \left( -\frac{1}{2\sigma^2} (Ry - X\beta)^\top (Ry - X\beta) \right) \end{aligned}$$

$$f(y \mid X, \mathcal{W}; \rho, \Gamma, \sigma^2, \beta) = |R(\omega)| (2\pi\sigma^2)^{-n/2} \exp \left( -\frac{e'e}{2\sigma^2} \right)$$

# Priors and Joint Posterior

Size of parameter space:

$$\Omega := \Omega_{\rho} \times \Omega_{\Gamma} \times \Omega_{\beta} \times \Omega_{\sigma} = (-1, 1) \times [0, 1]^L \times \mathbb{R}^k \times (0, \infty)$$

Flat or uniform priors for  $\rho, \Gamma, \beta, \log(\sigma^2)$ :

$$p(\rho) \sim U(-1, 1), \quad p(\Gamma) \sim U(0, 1), \quad p(\beta) \propto 1, \quad p(\sigma^2) \propto \frac{1}{\sigma^2}$$

Joint Posterior

$$p(\rho, \Gamma, \sigma^2, \beta \mid y, X, \mathcal{W}) \propto |R(\omega)| (\sigma^2)^{-\frac{(n+2)}{2}} \exp\left(-\frac{1}{2\sigma^2} e' e\right)$$

# MCMC Summary

- ▶ Draw  $\beta$  conditional on  $\omega$  and  $\sigma^2$   
 $p(\beta \mid \sigma^2, \omega, \tilde{y}, X) \sim N$
- ▶ Draw  $\sigma^2$  conditional on  $\omega$  and  $\beta$   
 $p(\sigma^2 \mid \beta, \omega, \tilde{y}, X) \sim IG$

Metropolis–Hastings to sample  $\omega$  from  $p(\omega \mid \tilde{y}, X, \mathcal{W})$ :

- ▶ Sample  $\rho$  conditional on  $\Gamma$
- ▶ Block-sample  $\Gamma$  conditional on  $\rho$

## Joint Posterior for $\omega$

$\beta$  and  $\sigma^2$  can be integrated out analytically from the joint posterior:<sup>1</sup>

$$p(\omega \mid \tilde{y}, X, \mathcal{W}) \propto |R(\omega)| |X'X|^{-1/2} (\omega' F \omega)^{-(n-k)/2}$$
$$\ln p(\omega \mid \tilde{y}, X, \mathcal{W}) \propto \ln |R(\omega)| - \frac{n-k}{2} \ln (\omega' F \omega)$$

- ▶ Condition this expression on  $\Gamma$  to sample  $\rho$  and vice versa
- ▶ Numerically integrate this expression to arrive at the log marginal likelihood

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<sup>1</sup> $F = U'U, \quad U = M\tilde{y}, \quad M = I_n - X(X'X)^{-1}X'$

# Sampling $\rho$

Initial value:  $\rho = 0.7$

1. Draw  $\rho^p = \rho^c + cN(0, 1)$ 
  - ▶ If  $\rho^p \in (-1, 1)$ , continue
  - ▶ Else set  $\rho^c = \rho^p$  and repeat
2. Decide acceptance: If  $\alpha \geq U \sim U(0, 1)$  accept  $\rho^p$  and set  $\rho^c = \rho^p$ . Else stay at  $\rho^c$

$$\alpha(\rho^c, \rho^p) = \min(1, \exp[\ln p(\rho^p | \Gamma) - \ln p(\rho^c | \Gamma)])$$

3. Tuned random walk:
  - ▶ If acceptance ratio  $< 0.4 \implies c = c/1.1$
  - ▶ If acceptance ratio  $> 0.6 \implies c = c * 1.1$

# Block Sampling for $\Gamma$

Initial values:  $\gamma_\ell = 1/L, \quad \forall \ell$

1. Draw  $\Gamma^P = (\gamma_1^P, \dots, \gamma_L^P)$

► For  $\ell \in \{1, \dots, L-1\}$  draw  $V \sim U(0, 1)$ .<sup>2</sup>

Condition, Propose		$N \leq 1000$	$N > 1000$
$V \leq 1/3$	$\gamma_\ell^P \in$	$[0, \gamma_\ell^c]$	$[\gamma_\ell^c - d\sigma_{\gamma_\ell}, \gamma_\ell^c]$
$V > 2/3$	$\gamma_\ell^P \in$	$(\gamma_\ell^c, 1]$	$(\gamma_\ell^c, \gamma_\ell^c + d\sigma_{\gamma_\ell}]$
else	$\gamma_\ell^P =$	$\gamma_\ell^c$	$\gamma_\ell^c$

► Set  $\gamma_L = 1 - \sum_{\ell=1}^{L-1} \gamma_\ell$ , if  $\gamma_L < 0$  repeat.

2. Decide acceptance: If  $\alpha \geq U \sim U(0, 1)$  accept  $\Gamma^P$  and set  $\Gamma^c = \Gamma^P$ , else stay at  $\Gamma^c$

$$\alpha(\Gamma^c, \Gamma^P) = \min(1, \exp[\ln p(\Gamma^P | \rho) - \ln p(\Gamma^c | \rho)])$$

3. Tuned random walk ( $N > 1000$ ):

► If acceptance ratio  $< 0.1 \implies d = d/1.1$

► If acceptance ratio  $> 0.4 \implies d = d * 1.1$

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<sup>2</sup> $\sigma_{\gamma_\ell}$  is computed using rolling window interval of 1000 draws of  $\gamma_\ell$

## Calculating Average Effects ► Model

Effects decomposition akin to LeSage and Pace (2009)

$$\frac{\partial y}{\partial X^r} = S_r = (I_n - \rho W_c(\Gamma))^{-1} \beta_r$$

$$\bar{M}(r)_{\text{direct}} = \frac{1}{NT} \text{tr}(S_r)$$

$$\bar{M}(r)_{\text{total}} = \frac{\beta_r}{1 - \rho}$$

$$\bar{M}(r)_{\text{indirect}} = \bar{M}(r)_{\text{total}} - \bar{M}(r)_{\text{direct}}$$

These capture how changes in a covariate affect outcomes locally and across the spatial network.

# Marginal Likelihood and Model Averaging

- ▶ MH-MC integration of  $p(\omega \mid \tilde{y}, X, \mathcal{W})$  to arrive at the marginal likelihood
- ▶ Uniform prior over the model space
  - ▶ Posterior model probability boils down to marginal likelihood
- ▶ Debarsy and LeSage (2022) write their BMA estimation for combinations of 2 or more networks
  - ▶ We additionally estimate single network models in Appendix
  - ▶ Low marginal likelihood  $\implies$  posterior probability  $\approx 0$
- ▶ With 5 candidates for connectivity matrices, there are 26 potential combinations of 2 or more matrices



# Data: Stock Returns and Monetary Policy Shocks

Stock returns based on monthly closing prices of national stock market indices:

- ▶ 24 countries from 2001-2014
- ▶ US: SP500, Germany: DAX, ...

Identification of monetary policy shocks following Jarociński and Karadi (2020):

- ▶ MP shock = interest rate surprise
- ▶ Change in the three-month Federal Funds futures rate
- ▶ 30-minute window around FOMC announcements

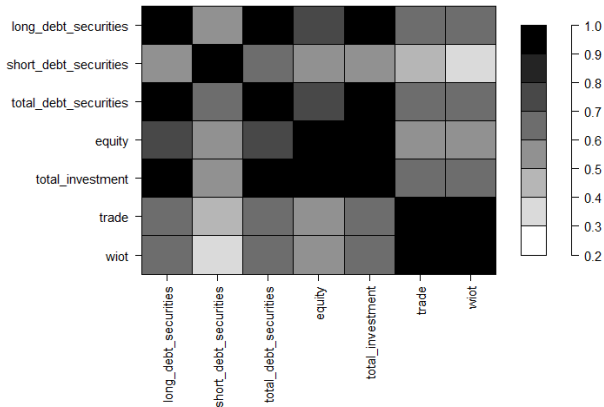
# Data: Transmission Networks

Quadratic network matrices of directed, bilateral links between countries.

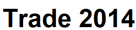
- ▶ Short-term debt securities: with original maturity  $< 1$  year
- ▶ Long-term debt securities: with original maturity  $> 1$  year
- ▶ Equity holdings: Equity titles
- ▶ Trade in intermediates: input-output matrix at country-level
- ▶ Total trade: import and export flows

# Network Similarity 2001-2014 (Link)

**Network Similarity - Correlation 2014**



Network Evolution 2001-2014 (Link)



# Results BMA 2001-2014

Table 2: Top 5 Models by Posterior Probability

Rank	LogLik	PostProb	$\rho$	W1	W2	W3	W4	W5
1	-5330.3	0.91	0.87	0.29	-	-	-	0.71
2	-5333.7	0.03	0.87	0.24	0.05	-	-	0.71
3	-5333.9	0.02	0.86	0.28	-	-	0.13	0.59
4	-5334.1	0.02	0.87	0.26	-	0.03	-	0.71
5	-5334.6	0.01	0.85	-	0.14	-	-	0.86
BMA	-5330.7	0.99	0.87	0.28	0.00	0.00	0.01	0.71

W1 Long Debt Securities

W2 Short Debt Securities

W3 Equity

W4 Trade

W5 Wiot

## Chain Diagnostics Best Model ► Full model

Table 3: MCMC Diagnostics (ndraws = 20000)

	Mode	Mean	MC Error	IACT	ESS	Geweke
$\alpha$	0.2166	0.2173	0.0002	1.3722	14579	0.9995
$\beta$	-0.9534	-0.9595	0.0031	1.0179	19648	0.9863
$\rho$	0.8665	0.8649	0.0005	5.7472	3481	0.9996
$\gamma_1$	0.2842	0.2860	0.0017	7.5656	2644	0.9952
$\gamma_2$	0.7158	0.7140	0.0017	7.5656	2644	0.9981

## Results BMA 2001-2014

Table 4: Averaged Posterior Estimates

Variable	0.01	Median	0.99
$\alpha$	0.16	0.22	0.27
$x$	-1.81	-0.96	-0.10
$\rho$	0.80	0.86	0.93
$\gamma_1$	0.11	0.28	0.45
$\gamma_2$	0.00	0.00	0.01
$\gamma_3$	0.00	0.00	0.00
$\gamma_4$	0.00	0.00	0.02
$\gamma_5$	0.54	0.71	0.88

Table 5: Posterior Estimates for Effect Decomposition

Effect	0.01	Median	0.99
Direct	-2.31	-1.21	-0.13
Indirect	-14.99	-5.89	-0.66
Total	-17.13	-7.13	-0.80

## Results Subsample 2001-2006

Table 6: Top 5 Models by Posterior Probability

Rank	LogLik	PostProb	$\rho$	W1	W2	W3	W4	W5
1	-2424.7	0.58	0.68	0.57	0.00	0.00	0.00	0.43
2	-2425.8	0.18	0.68	0.66	0.00	0.00	0.34	0.00
3	-2427.4	0.04	0.69	0.89	0.11	0.00	0.00	0.00
4	-2427.6	0.03	0.69	0.47	0.00	0.13	0.00	0.40
5	-2427.5	0.03	0.68	0.48	0.10	0.00	0.00	0.42
BMA	-2425.7	1.00	0.68	0.58	0.01	0.02	0.08	0.31

W1 Long Debt Securities

W2 Short Debt Securities

W3 Equity

W4 Trade

W5 Wiot



## Results Subsample 2001-2006

Table 7: Averaged Posterior Estimates

Variable	0.01	Median	0.99
$\alpha$	0.31	0.38	0.44
$x$	-2.45	-1.54	-0.66
$\rho$	0.60	0.68	0.76
$\gamma_1$	0.30	0.58	0.82
$\gamma_2$	0.00	0.01	0.03
$\gamma_3$	0.01	0.02	0.04
$\gamma_4$	0.02	0.08	0.16
$\gamma_5$	0.08	0.31	0.58

Table 8: Posterior Estimates for Effect Decomposition

Effect	0.01	Median	0.99
Direct	-2.61	-1.66	-0.72
Indirect	-5.93	-3.24	-1.41
Total	-8.36	-4.91	-2.15

# Conclusion

- ▶ We analyze importance of individual networks for spillovers of US monetary policy to international stock returns
- ▶ We use panel SAR with convex combinations of time-varying networks
- ▶ Spillovers more pronounced through intermediate input trade and long-term debt linkages
- ▶ The effect sizes and the importance of individual networks change for a sub-sample before GFC

# Next Steps


## Issues:

- ▶ Include more variables
- ▶ Include lagged variables
- ▶ Endogeneity of networks

## Next steps:

- ▶ Reconcile results with absolute sizes of links
- ▶ Dynamic setting with multiple variables
- ▶ Data on banking claims?

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## Posteriors for $\beta$ and $\sigma^2$

$$p(\beta \mid \sigma^2, \omega, \tilde{y}, X) \sim N(\tilde{\beta}, \tilde{\Sigma}_\beta)$$

$$\tilde{\beta} = (X'X)^{-1} (X'\tilde{y}\omega)$$

$$\tilde{\Sigma}_\beta = \sigma^2 (X'X)^{-1}$$

$$p(\sigma^2 \mid \beta, \omega, \tilde{y}, X) \propto (\sigma^2)^{-\left(\frac{n}{2}\right)} \exp\left(-\frac{e'e}{2\sigma^2}\right)$$

$$\sim IG(\tilde{a}, \tilde{b})$$

$$\tilde{a} = n/2$$

$$\tilde{b} = (e'e)/2$$

$$e = \tilde{y}\omega - X\beta$$

## MH-MC Integration and Marginal Likelihood

Marginal likelihood by Metropolis-Hastings guided MC Integration:

$$\begin{aligned}\log p(\text{data}) &= \log \int p(\text{data} \mid \omega) p(\omega) d\omega \\ &\approx \log \left( \frac{1}{S} \sum_{s=1}^S p(\text{data} \mid \omega^{(s)}) p(\omega^{(s)}) \right)\end{aligned}$$

In the code:

$$\frac{1}{S} \sum_{s=1}^S \log p(\omega^{(s)} \mid \text{data}) + \log C$$



# MH-MC Integration and Marginal Likelihood

DL22: Monte Carlo integration estimate of  $p(\omega \mid \tilde{y}, X, \mathcal{W})$  is its mean. Add constants of integration to produce log marginal likelihood.

$$\frac{1}{S} \sum_{s=1}^S \log p(\omega^{(s)} \mid \text{data}) + \log C$$

```
results.logmarginal = mean(logp) + logC_sar;
```

Normalized nonlog joint posterior:

$$\exp[\log p(\omega) - \max(\log p(\omega))]$$

# MATLAB Code

In the code:

$$\frac{1}{S} \sum_{s=1}^S \log p(\omega^{(s)} \mid \text{data}) + \log C$$

```
% calculate log-marginal likelihood (using Mh-MC integration)
logp = results.drawpost;
rho_gamma = results.rho_gamma;
[adj,mind] = max(logp);
results.rho_mode = rho_gamma(mind,1);
results.beta_mode = betapost(mind,:);
results.sig_mode = sigpost(mind,1);
results.gamma_mode = rho_gamma(mind,2:end);
isum = exp(logp -adj);
lndetx_sar = log(det(xpx));

% constant terms
dof = (n - m)/2; % we must include the # of weight matrices
D = (1 - 1/rmin); % from uniform prior on rho
logC_sar = -log(D) + gammaln(dof)
           - dof*log(2*pi) - 0.5*lndetx_sar;

results.logmarginal = mean(logp) + logC_sar;
results.logC_sar = logC_sar; % return constants
results.logm_profile = [rho_gamma betapost sigpost isum];
```

# Log-Determinants Based on Trace Approximations

Approximation based on 4-th order Taylor series expansion:

$$\begin{aligned}\ln |I_n - \rho W_c(\Gamma)| &= - \sum_{i=1}^{\infty} \rho^i \operatorname{tr} (W_c^i(\Gamma)) / i \\ &\simeq - \sum_{j=2}^q \rho^j \operatorname{tr} (W_c^j(\Gamma)) / j\end{aligned}$$

# Log-Determinants Based on Trace Approximations

Traces can be separated and precomputed. Example for  $j=2$

$$\text{tr}(W_c^2(\Gamma)) = \sum_{i=1}^L \sum_{j=1}^L \gamma_i \gamma_j \text{tr}(W_i W_j)$$

$$= \Gamma' Q \Gamma$$

$$= (\Gamma \otimes \Gamma)' \text{vec}(Q),$$

$$Q = \begin{pmatrix} \text{tr}(W_1^2) & \text{tr}(W_1 W_2) & \dots & \text{tr}(W_1 W_L) \\ \text{tr}(W_2 W_1) & \text{tr}(W_2^2) & \dots & \text{tr}(W_2 W_L) \\ \vdots & & \ddots & \\ \text{tr}(W_L W_1) & \text{tr}(W_L W_2) & \dots & \text{tr}(W_L^2) \end{pmatrix}$$

## Preliminary Analysis of Individual Networks

Table 9: Marginal log-likelihood and simplified effects of Individual Networks (2001–2014)

	LogLik	Total	Direct	Indirect (%)
W1 Long Debt Securities	-5382.0	-7.1	-1.4	80
W2 Short Debt Securities	-5454.4	-6.0	-1.6	73
W3 Equity	-5453.2	-6.5	-1.5	77
W4 Trade	-5365.5	-4.6	-1.3	72
W5 Wiot	-5358.1	-4.6	-1.2	73

# Preliminary Analysis of Individual Networks

Table 10: Marginal log-likelihood and effects of individual networks (2001–2006)

	LogLik	Total	Direct	Indirect (%)
W1 Long Debt Securities	-2430.8	-5.1	-1.8	65
W2 Short Debt Securities	-2451.5	-4.4	-1.9	57
W3 Equity	-2440.9	-4.4	-1.5	66
W4 Trade	-2435.8	-4.1	-1.7	59
W5 Wiot	-2432.9	-4.2	-1.7	59

# Trace Plot Full Model [▶ Back](#)

Chain Diagnostics

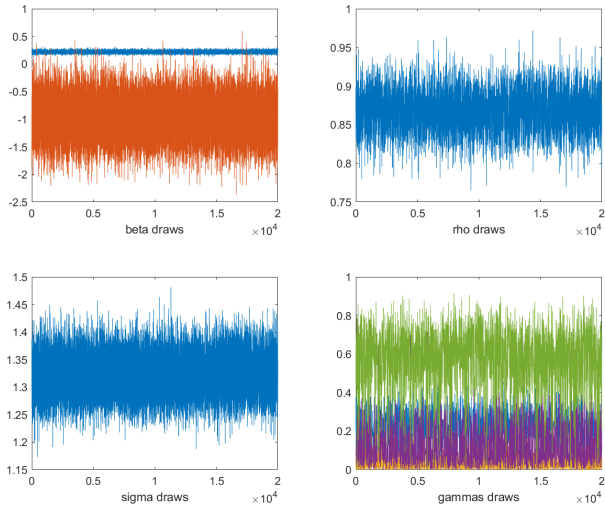


Table 11: MCMC Diagnostics (ndraws = 20000)

	Mode	Mean	MC error	Tau	ESS	Geweke
$\alpha$	0.2146	0.2194	0.0001	1.4656	13643	0.9962
$\beta$	-0.9505	-0.9568	0.0019	1.0327	19368	0.9828
$\rho$	0.8649	0.8684	0.0004	6.5876	3036	0.9986
$\gamma_1$	0.2476	0.2135	0.0025	14.5898	1371	0.9804
$\gamma_2$	0.0071	0.0495	0.0015	15.5361	1287	0.8318
$\gamma_3$	0.0024	0.0310	0.0006	18.3683	1089	0.9731
$\gamma_4$	0.0130	0.1268	0.0036	16.2311	1233	0.9108
$\gamma_5$	0.7299	0.5792	0.0038	14.4792	1381	0.9871



Table 12: Posterior Estimates

	0.01	0.05	Median	0.95	0.99
$\alpha$	0.1566	0.1718	0.2195	0.2677	0.2828
$\beta$	-1.9042	-1.6881	-0.9571	-0.2342	-0.0140
$\rho$	0.8013	0.8167	0.8686	0.9184	0.9365
$\gamma_1$	0.0138	0.0513	0.2165	0.3659	0.4111
$\gamma_2$	0.0006	0.0016	0.0413	0.1428	0.1815
$\gamma_3$	0.0002	0.0010	0.0222	0.1083	0.1437
$\gamma_4$	0.0011	0.0036	0.0946	0.4136	0.5609
$\gamma_5$	0.1608	0.2887	0.5942	0.7880	0.8388

Table 13: Posterior Estimates for Effect Decomposition

Effect	0.01	0.05	Median	0.95	0.99
Direct	-2.4862	-2.1555	-1.2152	-0.2994	-0.0178
Indirect	-16.5870	-12.8793	-6.0382	-1.5054	-0.0955
Total	-18.7172	-14.8541	-7.2596	-1.8194	-0.1133

Table 14: Posterior Estimates

	<b>0.01</b>	<b>0.05</b>	<b>Median</b>	<b>0.95</b>	<b>0.99</b>
$\alpha$	0.1553	0.1705	0.2172	0.2648	0.2790
$\beta$	-1.9155	-1.6953	-0.9572	-0.2307	-0.0100
$\rho$	0.7963	0.8144	0.8658	0.9127	0.9289
$\gamma_1$	0.0797	0.1343	0.2853	0.4385	0.4859
$\gamma_2$	0.5141	0.5615	0.7147	0.8657	0.9203

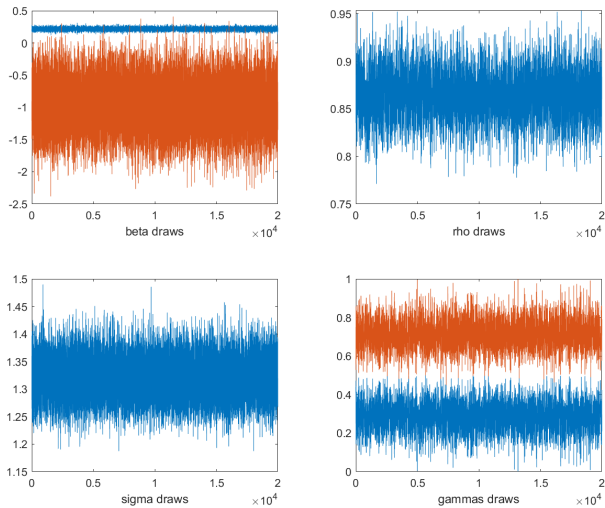
Table 15: Posterior Estimates for Effect Decomposition

<b>Effect</b>	<b>0.01</b>	<b>0.05</b>	<b>Median</b>	<b>0.95</b>	<b>0.99</b>
Direct	-2.4566	-2.1559	-1.2136	-0.2937	-0.0125
Indirect	-15.4240	-12.3373	-5.8572	-1.4261	-0.0583
Total	-17.6290	-14.3625	-7.0904	-1.7293	-0.0707

# Trace Plot Best Model

► Full model

Chain Diagnostics



# Theoretical Model of Di Giovanni and Hale 2022

Di Giovanni and Hale (2022) setup:  $N$  countries,  $J$  sectors

$$\underbrace{R_{mi}}_{\substack{\text{Sales of goods} \\ \text{produced by} \\ \text{country-sector} \\ mi}} = \underbrace{C_{mi}}_{\substack{\text{Final goods} \\ \text{expenditure on} \\ \text{good } mi \text{ across} \\ N \text{ countries}}} + \underbrace{\sum_{j=1}^J \sum_{n=1}^N \omega_{mi,nj} R_{nj}}_{\substack{\text{Intermediate} \\ \text{input} \\ \text{expenditure}}}$$

$\omega_{mi,nj}$  IO coefficient for country-sector  $nj$  purchases of the intermediate good from country-sector  $mi$  (as share of total purchases)

# Theoretical Model of Di Giovanni and Hale 2022

$R$  sales,  $C$  final goods expenditures,  $\Omega$  IO matrix

$$\begin{aligned} R_{NJ \times 1} &= C_{NJ \times 1} + \Omega_{NJ \times NJ} R, \\ R &= (I - \Omega)^{-1} C, \\ \hat{R} &= (I - \Omega)^{-1} \phi_R \circ \hat{C}, \\ \hat{q} &= (I - \Omega)^{-1} \beta \hat{M}, \end{aligned}$$

Assumptions:

$\hat{R} = \hat{\pi} = \hat{q}$ , Domestic firms owned by domestic HH.

Deviations in expenditures on final consumption  $\hat{C}$  are proportional to the monetary policy shocks  $\hat{M}$ .