

### **Title**

rdrbounds — Rosenbaum bounds for inference in RD designs under local
randomization.

### Syntax

```
rdrbounds outvar runvar [if] [in] [, cutoff(#) ulist(numlist) wlist(numlist)
    gammalist(numlist) expgamma(numlist) bound(string) statistic(stat_name) p(#)
    evalat(point) kernel(kerneltype) nulltau(#) fuzzy(fuzzy_var [fuzzy_stat])
    prob(varname) fmpval reps(#) seed(#) ]
```

### Description

- rdrbounds computes Rosenbaum bounds for p-values in regression discontinuity (RD) designs under local randomization. See <u>Cattaneo</u>, <u>Frandsen and Titiunik</u> (2015) and <u>Cattaneo</u>, <u>Titiunik and Vazquez-Bare</u> (2017) for an introduction to this methodology. See also Rosenbaum (2002) for a background review.
- A detailed introduction to this command is given in <u>Cattaneo, Titiunik and Vazquez-Bare (2016)</u>.

  Companion <u>R</u> functions are also available <u>here</u>.
- Companion functions are <u>rdrandinf</u>, <u>rdwinselect</u> and <u>rdsensitivity</u>.
- Related Stata and R packages useful for inference in RD designs are described in the following website:
  - https://sites.google.com/site/rdpackages/

### Options

cutoff(#) specifies the RD cutoff for the running variable runvar. Default is cutoff(0).

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Bounds
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- ulist(#) specifies the list of vectors of the unobserved confounder to be
   evaluated. Default is all vectors with ones in the first k positions and
   zeros in the remaining positions.
- wlist(#) specifies the list of window lengths to be evaluated. By default the
   program constructs 10 windows around the cutoff, the first one including 10
   treated and control observations and then adding 5 observations to each group
   in subsequent windows.
- gammalist (numlist) specifies the list of values of gamma to be evaluated.
- expgamma(numlist) specifies the list of values of exp(gamma) to be evaluated. Default is  $expgamma(1.5 \ 2 \ 2.5 \ 3)$ .
- bound(string) specifies which bounds the command calculates. Options are upper for upper bound, lower for lower bound and both for both upper and lower bounds. Default is bound(both).

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Statistic
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statistic(stat\_name) specifies the statistic to be used. Options are:
 diffmeans for difference in means statistic.

ksmirnov for Kolmogorov-Smirnov statistic.

ranksum for Wilcoxon-Mann-Whitney studentized statistic. This is the default option.

The option **ttest** is equivalent to **diffmeans** and included for backward compatibility.

- p(#) specifies the order of the polynomial for outcome adjustment model. Default is p(0).
- evalat(point) specifies the point at which the adjusted variable is evaluated.
   Allowed options are cutoff and means. Default is evalat(cutoff).
- kernel(kerneltype) specifies the type of kernel to use as weighting scheme.
  Allowed kernel types are uniform (uniform kernel), triangular (triangular kernel) and epan (Epanechnikov kernel). Default is kernel(uniform).
- fuzzy(fuzzy\_var [fuzzy\_stat]) name of the endogenous treatment variable in fuzzy
  design. This option employs an Anderson-Rubin-type statistic.

Inference

- $\underline{\text{null}} au$  (#) sets the value of the treatment effect under the null hypothesis. Default is  $\underline{\text{null}} au$  (0).
- prob(varname) specifies the name of the variable containing individual
   probabilities of treatment in a Bernoulli trial when the selection factor
   gamma is zero. Default is the porportion of treated units in each window
   (assumed equal for all units).
- fmpval calculates the p-value under fixed margins randomization, in addition to the p-value under Bernoulli trials.
- reps(#) specifies the number of replications. Default is reps(500).
- seed(#) sets the seed for the randomization test. With this option, the user can
  manually set the desired seed, or can enter the value -1 to use the system
  seed. Default is seed(666).

# Example: Cattaneo, Frandsen and Titiunik (2015) Incumbency Data

Setup

. use rdlocrand\_senate.dta, clear

Bounds using 1000 replications specifying exp(gamma)

. rdrbounds demvoteshfor2 demmv, expgamma(1.2 1.5 2) wlist(.75 1) reps(1000)

Bounds specifying gamma

. rdrbounds demvoteshfor2 demmv, gamma(0.2 0.5 1) wlist(.75 1) reps(1000)

Including fixed margins p-value

. rdrbounds demvoteshfor2 demmv, expgamma(1.2 1.5 2) wlist(.75 1) reps(1000) fmpval

Calculate upper bound only

. rdrbounds demvoteshfor2 demmv, expgamma(1.2 1.5 2) wlist(.75 1) reps(1000) bound(upper)

# Saved results

rdrbounds saves the following in r():

Matrices

r(lbounds)matrix of lower boundsr(ubounds)matrix of upper boundsr(pvals)matrix of p-values

### References

- Cattaneo, M. D., Frandsen, B., and R. Titiunik. 2015. Randomization Inference in the Regression Discontinuity Design: An Application to Party Advantages in the U.S. Senate.

  Journal of Causal Inference 3(1): 1-24.
- Cattaneo, M.D., Titiunik, R. and G. Vazquez-Bare. 2016. <u>Inference in Regression Discontinuity Designs under Local Randomization</u>.

  Stata Journal 16(2): 331-367.
- Cattaneo, M. D., Titiunik, R. and G. Vazquez-Bare. 2017. <u>Comparing Inference Approaches for RD Designs: A Reexamination of the Effect of Head Start on Child Mortality</u>.

  Journal of Policy Analysis and Management 36(3): 643-681.
- Rosenbaum, P.R. 2002. Observational Studies. New York: Springer.

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