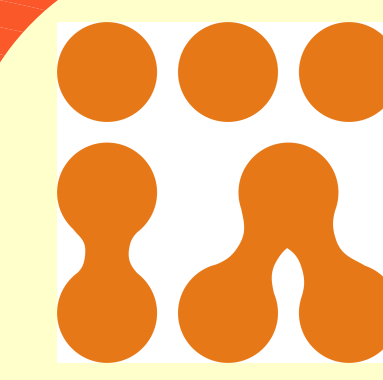


# Formal Model to Integrate Multi-Agent System and Interactive Graphic Systems

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## Abstract:

- A formal grammar-based model is presented to integrate the essential characteristics of a Multi-Agent System with the visualization given by an Interactive Graphic Systems.
- This model adds several advantages, such as the separation between the implementation of the system activity and the hardware devices, or the easy reusability of components.

## Grammar

Let  $M = \langle \Sigma, N, R, s \rangle$  a grammar where:

$$\Sigma = P \cup T \cup O \cup A_{ST}^D$$

$$N = \{ \text{WORLD, OBJECTS, OBJECT, AGENT, TRANSFOR, FIGURE} \}$$

$$s = \text{WORLD}$$

$R$  is the set of grammar rules defined as:

1. **WORLD**  $\rightarrow$  OBJECTS
2. **OBJECTS**  $\rightarrow$  OBJECT | OBJECTS · OBJECTS
3. **OBJECT**  $\rightarrow$  FIGURE | TRANSFOR | AGENT
4. **AGENT**  $\rightarrow a_{st}^d(\text{OBJECTS}), a_{st}^d \in A_{ST}^D, d \in D, st \in ST$
5. **TRANSFOR**  $\rightarrow t(\text{OBJECTS}), t \in T$
6. **FIGURE**  $\rightarrow p^+, p \in P$

## Evolution

Evolution function  $\lambda$ :

$$\lambda(a_{st}^d(v), e^f) = \begin{cases} u \in L(M) & \text{if } f = d \\ a_{st}^d(v) & \text{if } f \neq d \end{cases}$$

Visualization function  $\theta$ :

$$\theta(a_{st}^d(v), e^f) = \begin{cases} u \in L(E) & \text{if } f = d \\ \epsilon & \text{if } f \neq d \end{cases}$$

Function System Evolution  $\eta$ :

$$\eta(w, e^v) = \begin{cases} w & \text{if } w \in P \\ t(\eta(y, e^v)) & \text{if } w = t(y) \\ \prod_{f \in v} (\lambda(a_{st}^f(\eta(y, e^v)), e^f)) & \text{if } w = a_{st}^f(y) \\ \eta(s, e^v) \cdot \eta(t, e^v) & \text{if } w = s \cdot t \end{cases}$$

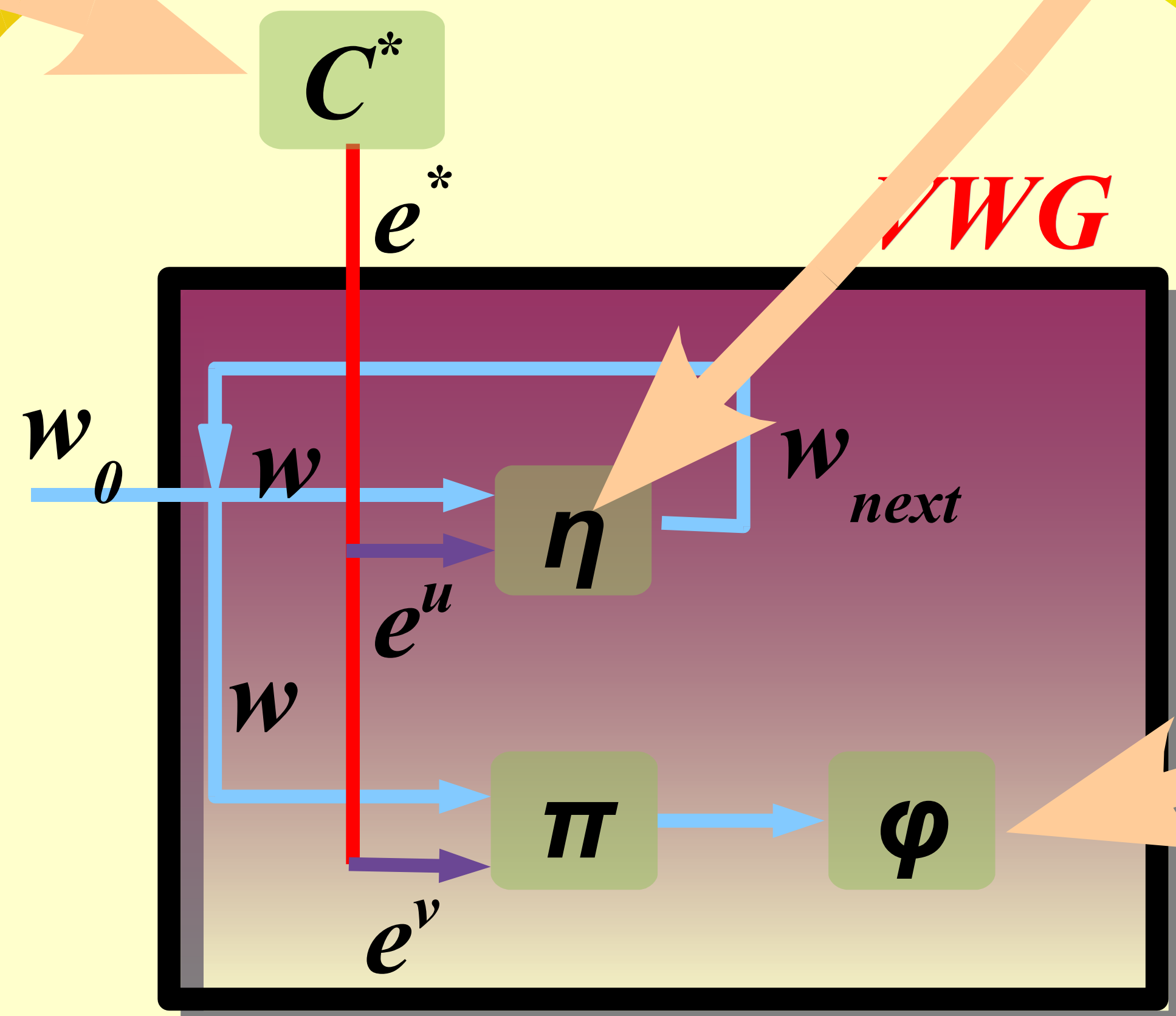
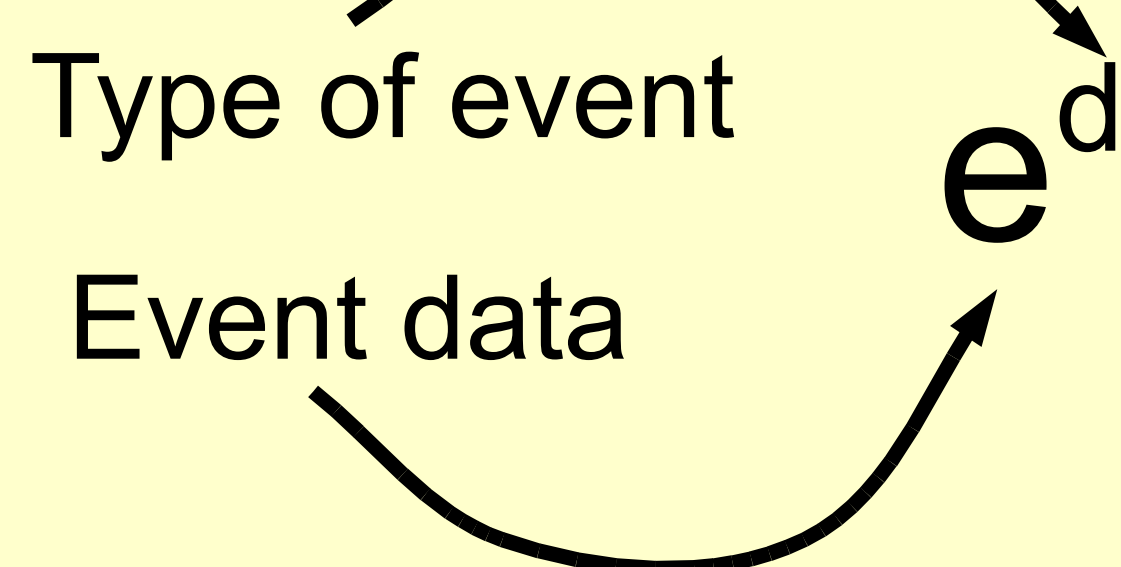
Function System Visualization  $\pi$ :

$$\pi(w, e^v) = \begin{cases} w & \text{if } w \in P \\ t(\pi(y, e^v)) & \text{if } w = t(y) \\ \prod_{f \in v} (\theta(a_{st}^f(\pi(y, e^v)), e^f)) & \text{if } w = a_{st}^f(y) \\ \pi(x, e^v) \cdot \pi(y, e^v) & \text{if } w = x \cdot y \end{cases}$$

## Events

$D$  is the set of all type events  
 $C^d(t)$  generator which create events type of  $d \in D$

$C^*$  is the set of all event generators associated with input device



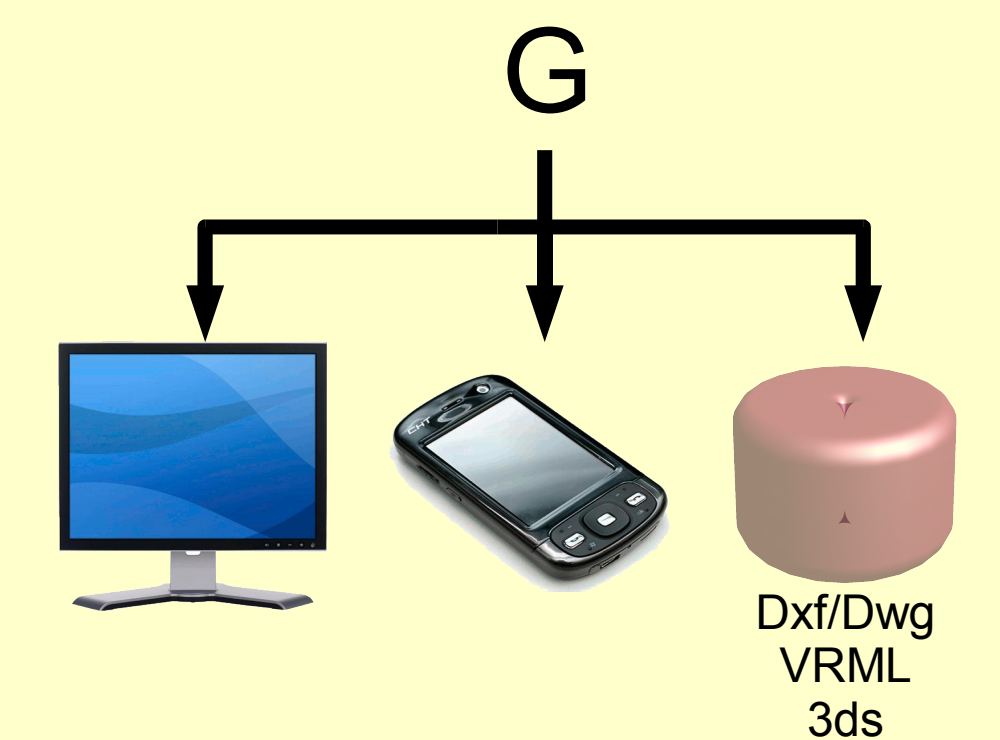
## Render

$\phi$  is render function defined as:

$$\phi(w) = \begin{cases} \alpha(w) & \text{if } w \in P \\ \beta(t); \phi(v); \delta(t) & \text{if } w = t(v) \\ & \wedge v \in L(M) \\ & \wedge t \in T \\ \phi(s); \phi(v) & \text{if } w = s \cdot v \\ & \wedge s, v \in L(M) \end{cases}$$

**P:** Primitives  
**T:** Transfor.

$$\left. \begin{aligned} \alpha: P &\rightarrow G \\ \beta: T &\rightarrow G \\ \delta: T &\rightarrow G \end{aligned} \right\}$$



## Case of Study

### Evolution Functions

$$\lambda(BO^{cfe}, e^i) = \begin{cases} TR_{s_1}^{t=1} \cdot BO^{cfe} & i = c \\ FA_{s_1}^{t=1} \cdot BO^{cfe} & i = f \\ BO^{cfe} & i = e \\ BO^{cfe} & i \neq cfe \end{cases}$$

$$\lambda(FA_{(f+1)}^t, e^i) = \begin{cases} FA_{(f+1)}^t & i = t \wedge f + 1 < N \\ \epsilon & i = t \wedge f + 1 \geq N \\ FA_{(f)}^t & i \neq t \end{cases}$$

$$\lambda(TR_{(s,f)}^{tb}, e^i) = \begin{cases} TR_{(s,f+1)}^{tb} & i = t \wedge f + 1 < N \wedge s = s_1 \\ TR_{(s2,N)}^{tb} & i = t \wedge f + 1 \geq N \wedge s = s_1 \\ TR_{(s3,N)}^{tb} & i = b \wedge s = s_2 \\ TR_{(s3,f-1)}^{tb} & i = t \wedge f \geq 0 \wedge s = s_3 \\ \epsilon & i = t \wedge f = 0 \wedge s = s_3 \\ TR_{(s,f)}^{tb} & i \neq b, t \end{cases}$$

### Visualization Functions

$$\pi(BO^v, e^i) = \begin{cases} BO & i = v \\ \epsilon & i \neq v \end{cases}$$

$$\pi(FA_{(f)}^v, e^i) = \begin{cases} D_{(i,j)}(FA) & i = v \\ \epsilon & i \neq v \end{cases}$$

$$\pi(TR_{(s,f)}^v, e^i) = \begin{cases} D_{(i,j)}(S_{(f)}(TR)) & i = v \wedge s = s_1 \\ D_{(i,j)}(TR) & i = v \wedge s = s_2 \\ D_{(i,j)}(S_{(-f)}(TR)) & i = v \wedge s = s_3 \\ \epsilon & i \neq v \end{cases}$$

This example is an application to simulate fires in forests caused by lightning

