

QUESTION 3

```
class Bag {
```

```
  private var list = new Bag.Node(0, null) // dummy header
```

```
  private var end = list
```

```
  def add (n1: Bag.Node): Unit = {
```

```
    n1.next = null
```

```
    end.next = n1
```

```
  } end = n1
```

```
// (a)
```

```
def findMin: Bag.Node = {
```

```
  var current = list.next
```

```
  var minNode = current
```

```
  var min = current.datum
```

```
  if (current.next == null) return current // just one node in the list
```

```
  else current = current.next
```

```
  // invariant i: minNode.datum = min(L(list.next, current))
```

```
  while (current != null)
```

```
  { if (min > current.datum) { min = current.datum; minNode = current } }
```

```
    current = current.next
```

```
  // current = null => minNode.datum = min(L(list.next, null)), so we return minNode
```

```
}
```

```
// (b)
```

```
def remove (n: Bag.Node): Unit = {
```

```
  var current = list.next
```

```
  var prev = list
```

```
  // invariant i: n.datum is not in L(list.next, prev) & prev.next = current
```

```
  while (n != current) { prev = prev.next; current = current.next }
```

```
  // n == current, so now we want to delete current from the list
```

```
  prev.next = prev.next.next
```

```
}
```

// (c) The dummy header helps us get rid of the special case when we need to delete the first node of the list

```
def delMin : Bag.Node = {  
  var minNode = this.findMin  
  remove(minNode)  
  minNode  
}
```

// (d)

```
def sort : Bag = {  
  var sortedList = new Bag  
  var k = 0 // used for the invariant and to keep track of how many elements there  
  are in the list  
  // invariant i: sortedList contains the first k elements of the list, sorted increasingly  
  while (list.next != null) // as long as the list is non-empty  
  {  
    var minNode = this.delMin  
    sortedList.add(minNode)  
    k += 1  
  }  
  sortedList  
}
```

// Companion object

```
object Bag {  
  class Node (var datum : Int, var next : Node)  
}
```