

QUESTION 3

>  $\text{unfold } p \ f \ g \ x = \text{if } (p \ x) \text{ then } [] \text{ else } (f \ x) : \text{unfold } p \ f \ g \ (g \ x)$

(a) From the if-clause, we have

$x :: a$

$p :: a \rightarrow \text{Bool}$

and the result of  $\text{unfold}$  is  $[b]$

From the else-clause we get

$f :: a \rightarrow b$

$g :: a \rightarrow a$

Therefore, we have

$\text{unfold} :: (a \rightarrow \text{Bool}) \rightarrow (a \rightarrow b) \rightarrow (a \rightarrow a) \rightarrow a \rightarrow [b]$

(b)

>  $\text{iterate} :: (a \rightarrow a) \rightarrow a \rightarrow [a]$

>  $\text{iterate } f \ x = x : \text{iterate } f \ (f \ x)$

Using  $\text{takeWhile}$  and  $\text{iterate}$ , we have:

$\text{unfold } p \ f \ g = \text{map } f \cdot \text{takeWhile } (\backslash x \rightarrow p \ x == \text{False}) \cdot \text{iterate } g$

(c)

>  $\text{data } RTree \ a = \text{Node } a \ [RTree \ a]$

>  $\text{foldRTree} :: (a \rightarrow [b] \rightarrow b) \rightarrow RTree \ a \rightarrow b$

>  $\text{foldRTree } \text{mode } (\text{Node } a \ ms) = \text{mode } a \ (\text{map } (\text{foldRTree } \text{mode}) \ ms)$

(d)

(i)

>  $\text{dft} :: RTree \ a \rightarrow [a]$

>  $\text{dft } (\text{Node } a \ []) = [a]$

>  $\text{dft } (\text{Node } a \ ms) = a : \text{concat } (\text{map } \text{dft} \ ms)$

(ii)

>  $\text{dft}' :: RTree \ a \rightarrow [a]$

>  $\text{dft}' = \text{foldRTree } (\backslash x \ xss \rightarrow x : \text{concat } xss)$

(iii)

>  $\text{unfoldRTree} :: ([RTree\ a] \rightarrow \text{Bool}) \rightarrow (a \rightarrow b) \rightarrow ([RTree\ a] \rightarrow [RTree\ a]) \rightarrow RTree\ a \rightarrow [b]$

>  $\text{unfoldRTree}\ p\ f\ g\ (\text{Node}\ a\ nts) = \text{if}\ (p\ nts)\ \text{then}\ [f\ a]\ \text{else}\ [f\ a] : \text{concat}\ (\text{map}\ (\text{unfoldRTree}\ p\ f\ g)\ (g\ nts))$

>  $\text{dft}'' :: RTree\ a \rightarrow [a]$

>  $\text{dft}'' = \text{unfoldRTree}\ \text{null}\ \text{id}\ \text{id}$