

QUESTION 5

(a)

```
class CountTree{
```

```
    class Tree ( var word: String, var count: Int, var left: Tree, var right: Tree)
```

(b)

```
    private var root: Tree = null
```

```
    // ΔTi: Let  $B(t) = B(t.left) \# [(t.word, t.count)] \# B(t.right)$  &&  $B(null) = []$ 
```

```
    // Then, we have  $B(t)$  sorted increasingly (lexicographically) and finite after the first element of each  
    // pair, and all the first elements are distinct and all the second elements are positive integers.
```

(c)

```
def addToTree(word: String, t: Tree): Tree = {
```

```
    var current = t
```

```
    if (current == null) current = new Tree(word, 1, null, null)
```

```
    else if (current.word > word) current.left = addToTree(word, current.left)
```

```
    else if (current.word < word) current.right = addToTree(word, current.right)
```

```
    else current.count += 1
```

```
    current
```

```
}
```

(d)

```
(i) // ΔTi: Let  $L(a,b) = \text{if } (a \neq b) \text{ then } (a.word, a.count): L(a.right, b) \text{ else } [(b.word,$ 
```

```
    // b.count)]
```

```
    // Then, we have  $L(start, end)$  is lexicographically-increasingly sorted and finite
```

```
    // and  $a.left.right = a.right.left = a$  for all  $a$  except start and end &&  $start.right.left =$ 
```

```
    // start &&  $end.left.right = end$  and  $L(start, end)$  contains only pairs whose second elements
```

```
    // are positive integers
```

(ii)

```
def flatten(t: Tree): (Tree, Tree) = {
```

```
    if (t == null) return (null, null)
```

```
    else if ((t.left == null) && (t.right == null)) return (t, t)
```

```
    else if (t.left == null)
```

```
    { var (a,b) = flatten(t.right)
```

```
      a.left = t
```

```
      t.right = a
```

```
      return (t, b)
```

```

else if (t.right == null)
{
    var (a,b) = flatten(t.left)
    b.right = t
    t.left = b
    return (a,t)
}
else
{
    var (x,a) = flatten(t.left)
    var (b,y) = flatten(t.right)
    a.right = t ; b.left = t
    t.left = a ; t.right = b
    return (x,y)
}
}

```

}

(iii)

```

def flattenIter (t: Tree): (Tree, Tree) = {
    val stack = new scala.collection.mutable.Stack[Tree]
    var current = t
    var start: Tree = null
    var end: Tree = null
    while ((current != null) || (!stack.isEmpty))
    {
        if (current != null) { stack.push(current) ; current = current.left }
        else
        {
            current = stack.pop
            if (start == null)
            {
                start = current
                end = current
            }
            else
            {
                end.right = current
                current.left = end
                end = current
            }
            current = current.right
        }
    }
    (start, end)
}

```