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# Cryptographic Properties of XOR



## XOR

$$0\ 0 \rightarrow 0$$

$$0\ 1 \rightarrow 1$$

$$1\ 0 \rightarrow 1$$

$$1\ 1 \rightarrow 0$$



$$\text{enc\_message} = \text{clear\_message} \wedge \text{key}$$

# Repeating XOR cipher



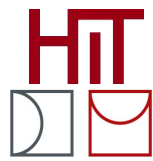
$\text{enc\_message} = \text{clear\_message} \wedge \text{key}$

$\text{clear\_message} = \text{"THIS IS A MESSAGE"}$

$\text{key} = \text{"YOU"}$

T	H	I	S		I	S		A		M	E	S	S	A	G	E
Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O

# Repeating XOR cipher



$$\text{enc\_message} = \text{clear\_message} \wedge \text{key}$$

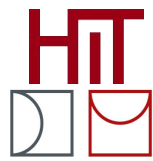
clear\_message = "THIS IS A MESSAGE"

key = "YOU"

T	H	I	S		I	S		A		M	E	S	S	A	G	E
84	72	73	83	32	73	83	32	65	32	77	69	83	83	65	71	69

Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O
89	79	85	89	79	85	89	79	85	89	79	85	89	79	85	89	79

# Repeating XOR cipher



$$\text{enc\_message} = \text{clear\_message} \wedge \text{key}$$

clear\_message = "THIS IS A MESSAGE"

key = "YOU"

clear\_message

84	72	73	83	32	73	83	32	65	32	77	69	83	83	65	71	69
89	79	85	89	79	85	89	79	85	89	79	85	89	79	85	89	79

key

enc\_message

13	7	28	10	111	28	10	111	20	121	2	16	10	28	20	30	10
----	---	----	----	-----	----	----	-----	----	-----	---	----	----	----	----	----	----

84 = 1010100

89 = 1011001

13 = 0001101

# Properties of the XOR cipher



- XOR is commutative  
 $a \wedge b = b \wedge a$
- XOR is associative  
 $a \wedge (b \wedge c) = (a \wedge b) \wedge c$
- Anything XORed with itself is zero  
 $a \wedge a = 0$
- Anything XORed with zero is anything  
 $a \wedge 0 = a$

# Properties of the XOR cipher



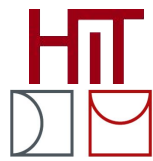
$\text{enc\_message} = \text{clear\_message} \wedge \text{key}$

$\text{clear\_message} = \text{enc\_message} \wedge \text{key}$

$\text{key} = \text{clear\_message} \wedge \text{enc\_message}$



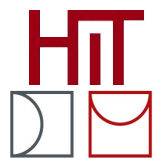
# Kasiski elimination



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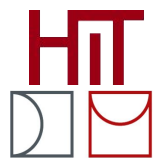
13	7	28	10	111	28	10	111	20	121	2	16	10	28	20	30	10
----	---	----	----	-----	----	----	-----	----	-----	---	----	----	----	----	----	----

# Kasiski elimination



13	7	28	10	111	28	10	111	20	121	2	16	10	28	20	30	10
----	---	----	----	-----	----	----	-----	----	-----	---	----	----	----	----	----	----

# Kasiski elimination



13	7	28	10	111	28	10	111	20	121	2	16	10	28	20	30	10

T	H	I	S		I	S		A		M	E	S	S	A	G	E
Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O

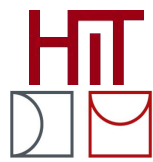
$$\text{ord}('I') \wedge \text{ord}('U') = 28$$

$$\text{ord}('S') \wedge \text{ord}('Y') = 10$$

$$\text{ord}(' ') \wedge \text{ord}('O') = 111$$



# Kasiski elimination



13	7	28	10	111	28	10	111	20	121	2	16	10	28	20	30	10

T	H	I	S		I	S		A		M	E	S	S	A	G	E
Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O	U	Y	O

$\text{clear\_message}(i) \wedge \text{key}(i) = 28$

$\text{clear\_message}(i + 1) \wedge \text{key}(i + 1) = 10$

$\text{clear\_message}(i + 2) \wedge \text{key}(i + 2) = 111$

Standard instruction to compute a XOR in Python. The result is a vector of numbers.

```
enc_message = [i ^ j for i, j in zip(clear_message, key)]
```

*i* and *j* should be integers

If you want the output as a string

```
enc_message = "".join([chr(i ^ j) for i, j in zip(clear_message, key)])
```