

03.01

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Integrazione per sostituzione: ex. 484/509 pag. 123

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[P. 112 ES. 312]

$$f(x) = x \quad g'(x) = e^{1-2x}$$

312 $\int x e^{1-2x} dx$

$$\left[-\frac{1}{4}(2x+1)e^{1-2x} + c \right]$$

INTEGRAZIONE
PER PARTI $\rightarrow \left[\int f(x)g'(x)dx = f(x)g(x) - \int f'(x)g(x)dx + c \right]$

$$= \int f(x) \cdot g'(x) = \int x \cdot e^{1-2x}$$

$$g(x) = \int e^{1-2x} dx \quad \begin{aligned} A &= 1-2x \rightarrow \frac{A-1}{2} = \frac{-2x}{2} \\ dA &= -2dx \end{aligned}$$

$$= 2 \cdot \frac{1}{2} \int e^A dA$$

$$= e^A + c = e^{1-2x} + c \rightarrow g$$

$$\left[dx = \frac{1}{2} \right]$$

312 $\int x e^{1-2x} dx$

$$\left[-\frac{1}{4}(2x+1)e^{1-2x} + c \right]$$

$\int \underbrace{f(x)}_x \underbrace{g'(x)}_{e^{1-2x}} dx = f(x)g(x) - \int \underbrace{f'(x)}_1 \underbrace{g(x)}_{e^{1-2x}} dx + c$

$$\begin{aligned} f(x) &= x \\ f'(x) &= 1 \end{aligned}$$

$$\int x e^{1-2x} dx = -\frac{x}{2} e^{1-2x} - \int \frac{1}{2} e^{1-2x}$$

P. 112 SS. 314

314

$$\int x e^{4x} dx$$

$$f = x \quad g' = e^{4x}$$

$$f' = 1$$

$$\left[e^{4x} \left(\frac{x}{4} - \frac{1}{16} \right) + c \right]$$

INTEGRATION BY PARTS $\rightarrow \left[\int f(x)g'(x)dx = f(x)g(x) - \int f'(x)g(x)dx + c \right]$

$$\int x e^{4x} dx = x \underbrace{\int e^{4x} dx}_{g(x)} \dots$$

$$g(x) = \int e^{4x} dx$$

$$\frac{dx}{4} = \frac{dt}{4}$$

$$dx = \frac{1}{4} dt$$

$$= \frac{1}{4} \int e^t dt = \frac{1}{4} e^{4x} + c$$

$$\left[\int f(x)g'(x)dx = f(x)g(x) - \int f'(x)g(x)dx + c \right]$$

$$= x \cdot \frac{1}{4} e^{4x} - \int \frac{1}{4} e^{4x} dx$$

$$= x \cdot \frac{1}{4} e^{4x} - \frac{1}{16} e^{4x} + c = \left(\frac{x}{4} - \frac{1}{16} \right) e^{4x} + c$$

P. 122 SS. 484

484

$$\int x \sqrt[3]{1+x} dx$$

$$\int (1+x)^{1/3} = \frac{4}{3} (1+x)^{4/3}$$

$$\left[\frac{3}{28} (4x-3) \sqrt[3]{(x+1)^4} + c \right]$$

$$1+x = t$$

$$x = t - 1$$

$$dx = 1$$

$$= \int (t-1) \sqrt[3]{t} dt$$

INTEGR.

BY PARTS ...

$$\frac{4}{3} \left(\frac{1}{2} \right)^2 \sqrt[3]{(1+x)^4}$$

$$\frac{2}{3} \sqrt[3]{(1+x)^4}$$

Q5/01

P. 122 57.
488

488 $\int \frac{x}{4x^2+1} dx$

$\left[\frac{1}{8} \ln(4x^2+1) + c \right]$

$A = 4x^2 + 1 \rightarrow A - 1 = 4x^2$

$dA = 4 \cdot 2x^{2-1} dx = 8x dx$

$dx = \frac{1}{8} \frac{dA}{x}$

~~$\frac{A-1}{4} = x$~~
 ~~$\frac{A-1}{4} - \frac{1}{4} = x$~~
 ~~$\frac{1}{4} = x$~~

$\int \frac{x}{4x^2+1} dx \rightarrow = \left(\frac{1}{8} \right) \int \frac{1}{A} dA = \frac{1}{8} \ln(A)$

$= \frac{1}{8} \ln(4x^2+1) + c$

55. 503 P. 123

505 $\int \frac{t}{\sqrt{t^2+4}} dt$

$\left[\sqrt{t^2+4} + c \right]$

$A^2 + 4 = S$

$A = \frac{1}{2} \quad \frac{2A dA}{2A} = \frac{dS}{2A}$


$\int \frac{A^{\frac{1}{2}} dA}{\sqrt{A^2+4}} = \frac{1}{2} \int \frac{1}{\sqrt{S}} dS$

$= \frac{1}{2} \int \frac{1}{\sqrt{S}} dS$

$= \frac{1}{2} \int S^{-1/2} dS = \frac{1}{2} \frac{S^{1/2}}{1/2} = \frac{1}{2} \cdot 2 S^{1/2}$


$= \left[\sqrt{A^2+4} + c \right]$

ES. 508 p. 123

 **509** $\int x(x+3)^{10} dx$


$$\left[\frac{1}{12}(x+3)^{12} - \frac{3}{11}(x+3)^{11} + c \right]$$

ES. 518 p. 123

 **518** $\int e^{\sin t} \cos t dt$

$$[e^{\sin t} + c]$$

ES. 526 p. 123

 **526** $\int x e^{3x} dx$

$$\left[\frac{1}{9}(3x-1)e^{3x} + c \right]$$