## Esercizi 4

## Primi esercizi sui limiti

1. 
$$\lim_{x \to +\infty} \frac{5x^4 + x^3 + 1}{3^{2x} + 5^x}$$

2. 
$$\lim_{x \to -\infty} \frac{5x^4 + x^3 + 1}{3^{2x} + 5^x}$$

3. 
$$\lim_{x\to 0^+} 4x^4 \log(x^5 + x^2)$$

4. 
$$\lim_{x\to 0^+} x^{x\log x}$$

5. 
$$\lim_{x\to 0^+} |\log x|^{1/x}$$

6. 
$$\lim_{x\to+\infty} \frac{\log x^5 + \sqrt{x} + 2x}{x + \arctan x + \sin x}$$

7. 
$$\lim_{x\to+\infty} (x+\sqrt{x})\sin\frac{5}{x}$$

8. 
$$\lim_{x \to \pi^{-}} \frac{\sqrt{1 + \sin x} - \sqrt{1 - \sin x}}{1 - \cos^{2} x}.$$

9. 
$$\lim_{x \to -\infty} \left( \sqrt{3x^2 - x} - \sqrt{3x^2 + x + 1} \right)$$
.

10. 
$$\lim_{x \to +\infty} \frac{1+3\sin x - x\sin(2x)}{x^2 - 1}$$
.

11. 
$$\lim_{x \to +\infty} \frac{\log(\log x)}{1 + \log x}.$$

12. 
$$\lim_{x \to 0} \frac{\sqrt{1+x} - \sqrt{1-x}}{x}$$
.

13. 
$$\lim_{x \to 0} \frac{\sin(\tan x)}{\sin x}.$$

14. 
$$\lim_{x \to \sqrt{2}} \frac{x - \sqrt{2}}{\sin(x^2 - 2)}$$
.

15. 
$$\lim_{x \to -\infty} \sqrt{x^2 + 3x + 2} + x$$

16. 
$$\lim_{x \to +\infty} 3^{x+1} - 3^{\sqrt{x^2+1}}$$

17. 
$$\lim_{x \to +\infty} \frac{a^x + 4^x + \sinh x}{7^x + 2^x \sin(e^x)}$$
, al variare del parametro reale a > 0.