

ANGOLI ASSOCIATI

Angoli associati

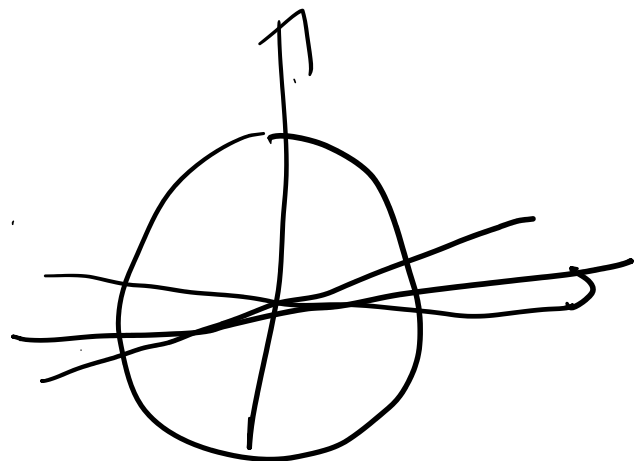
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angoli complementari (I quadrante)	angoli che differiscono di 90° (II quadrante)
$\sin\left(\frac{\pi}{2} - \alpha\right) = \cos \alpha$	$\sin\left(\frac{\pi}{2} + \alpha\right) = \cos \alpha$
$\cos\left(\frac{\pi}{2} - \alpha\right) = \sin \alpha$	$\cos\left(\frac{\pi}{2} + \alpha\right) = -\sin \alpha$
$\tan\left(\frac{\pi}{2} - \alpha\right) = \cotg \alpha$	$\tan\left(\frac{\pi}{2} + \alpha\right) = -\cotg \alpha$
$\cotg\left(\frac{\pi}{2} - \alpha\right) = \tan \alpha$	$\cotg\left(\frac{\pi}{2} + \alpha\right) = -\tan \alpha$
angoli supplementari (II quadrante)	angoli che differiscono di 180° (III quadrante)
$\sin(\pi - \alpha) = \sin \alpha$	$\sin(\pi + \alpha) = -\sin \alpha$
$\cos(\pi - \alpha) = -\cos \alpha$	$\cos(\pi + \alpha) = -\cos \alpha$
$\tan(\pi - \alpha) = -\tan \alpha$	$\tan(\pi + \alpha) = \tan \alpha$
$\cotg(\pi - \alpha) = -\cotg \alpha$	$\cotg(\pi + \alpha) = -\cotg \alpha$
angoli la cui somma è 270° (III quadrante)	angoli che differiscono di 270° (IV quadrante)
$\sin\left(\frac{3}{2}\pi - \alpha\right) = -\sin \alpha$	$\sin\left(\frac{3}{2}\pi + \alpha\right) = \sin \alpha$
$\cos\left(\frac{3}{2}\pi - \alpha\right) = \cos \alpha$	$\cos\left(\frac{3}{2}\pi + \alpha\right) = -\cos \alpha$
$\tan\left(\frac{3}{2}\pi - \alpha\right) = \tan \alpha$	$\tan\left(\frac{3}{2}\pi + \alpha\right) = -\tan \alpha$
$\cotg\left(\frac{3}{2}\pi - \alpha\right) = \cotg \alpha$	$\cotg\left(\frac{3}{2}\pi + \alpha\right) = -\cotg \alpha$
angoli esplementari (IV quadrante)	angoli opposti (IV quadrante)
$\sin(2\pi - \alpha) = -\sin \alpha$	$\sin(-\alpha) = -\sin \alpha$
$\cos(2\pi - \alpha) = \cos \alpha$	$\cos(-\alpha) = \cos \alpha$
$\tan(2\pi - \alpha) = -\tan \alpha$	$\tan(-\alpha) = -\tan \alpha$
$\cotg(2\pi - \alpha) = -\cotg \alpha$	$\cotg(-\alpha) = -\cotg \alpha$

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ANGOLI NOTABILI

Angolo		Seno	Coseno	Tangente	Cotangente
Radiani	Gradi				
0	0°	0	1	0	∞
$\frac{\pi}{6}$	30°	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{3}}{3}$	$\sqrt{3}$
$\frac{\pi}{4}$	45°	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	1	1
$\frac{\pi}{3}$	60°	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$	$\frac{\sqrt{3}}{3}$
$\frac{\pi}{2}$	90°	1	0	∞	0
π	180°	0	-1	0	∞
$\frac{3\pi}{2}$	270°	-1	0	∞	0
2π	360°	0	1	0	∞



FORMULA FONDAMENTALE

$$\rightarrow \sin^2(x) + \cos^2(x) = 1$$

SOMMA E DIFFER. DEL SENO (PROSTAFONESE)

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

FORMULE DI DUPLICAZIONE

FORMULE DI DUPLICATIONE

$$\sin(2\alpha) = 2 \sin \alpha \cos \alpha$$

$$\cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha$$

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

TANGENZE

$$\tan(\alpha + \beta) = \frac{\sin(\alpha + \beta)}{\cos(\alpha + \beta)} \rightarrow$$

$$\tan(\alpha + \beta) = \frac{\frac{\sin \alpha}{\cos \alpha} + \frac{\sin \beta}{\cos \beta}}{1 - \frac{\sin \alpha \sin \beta}{\cos \alpha \cos \beta}}$$

$$\tan(\alpha - \beta) = \frac{\tan \alpha - \tan \beta}{1 + \tan \alpha \tan \beta} \rightarrow$$

$$\tan(\alpha - \beta) = \frac{\tan \alpha + \tan(-\beta)}{1 - \tan \alpha \tan(-\beta)}$$

