Exercise (Example 8.2 from textbook)

final state and occupt.

Construct a Turing Hachine accepting the language $\{O^m 1^m \mid n \geqslant 1\}$

Solution

the lefternost 0, turns it into X, and moves right until it reaches a 1, that is turned into Y. Then the head moves left again to the leftenost 0 (on the right to a X), and starts again until all 0's and 1's are turned into X's and Y's respectively.

If the imput is mot in 0*1*, M will fail to find a move and it won't eccept. If M changes the last 0 and the last 1 in the same round, it will go into the

$$Q = \{90, 91, 91, 93, 94\}$$

$$\Sigma = \{0, 1\}$$

$$\Gamma = \{0, 1, x, Y, t\}$$

$$\{0, 1, x, Y, t\}$$

$$\{0$$

In go is the state in which M is when the head preceds the left most 0. In state 91, M master right shipping 0's and 1's until it gets to a 1. In state 92, M moves left while skipping 1's and 0's again, until it gets to a X and goes again in 90.

(E 2.2

Starting from 90, if a Y is reed involend of a O, M poet in 93 and moves right: if a 1 is found, then there are more 1's then 9's; if a 5 is read, then the initial string is accepted (tremstion to 94).

	0	1	X	- Υ	t
90	(q_1, \times, R)		-Nilitanee	(9314, R)	
	(91,0,R)	(92, Y, L)		(91, Y, R)	
92	(92,0,L)		(q_o, x, R)	(92, Y, L)	
93			-	(93, r, R)	(94,5,R)
94					

Exercise Show the computation of the TM above when the imput string is:

- (a) 00
- (b) 000111

(b) $q_0 000111 \vdash xq_100111 \vdash x0q_10111 \vdash x00q_10111 \vdash x00q_1111 \vdash x00q_1111 \vdash x00q_1111 \vdash x00q_1111 \vdash xq_000Y11 \vdash xxq_10Y11 \vdash xx0q_1Y11 \vdash xx0Yq_111 \vdash xx0Yq_111 \vdash xx0q_1Y11 \vdash xxq_00YY1 \vdash xxq_00YY1 \vdash xxxq_1YY1 \vdash xxxYq_1Y1 \vdash xxxYq_1Y1 \vdash xxxYq_1Y1 \vdash xxxYq_1Y1 \vdash xxxYq_1YY \vdash xxxYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1Y \vdash xxxYYYq_1YY \vdash xxxYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1Y \vdash xxxYYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1YY \vdash xxxYYYq_1Y \vdash xxxYYq_1YY \vdash xxxYYq_1Y \vdash xxxYYq_1YY \vdash xxxYYq_1YY \vdash xxxYYq_1YY \vdash xxxYYq_1YY \vdash xxxYYq_1YY \vdash xxxYYq_1YY \vdash xxxYYq_1Y \vdash xxxYYq_1Y \vdash xxxYYq_1Y \vdash xxxYYq_1Y \vdash xxxYYq_1YY \vdash xxxYYq_1YY \vdash xxxY$

Exercise (8.2,3 from textbook);

Design a Turing Machine that takes as imput a number N in bianery and turns it into N+1 (in binary); the number N is preceded by the symbol \$, which may be destroyed during the computation. For exemple, \$111 is turned into \$1010.

solution

the idea is to topple the nightment digit, and, from right to left, all consecutive 1's until we get to the first o (which is also toppled). If there is no 0 to be toppled, a 1 is added on the left of the first digit (i.e., in place of the \$). We need three states, where only 92 is the final state; we briefly describe what the TM does in the different states.

90: the TM goes right until it reaches to, efter the highternoot digit. When to is reached, the TM goes into 92.

92: goes left togeting all 1's and the first 0 (from right); when 0 or \$ is reached, the symbol is turned into 1.

92: final state; the TM does nothing

Exercise (8,22 from textbook),

Design turing machiner accepting the following languages:

[W \in [0,1]* | w has an equal number of 0's and 1'2]

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The idea is that the head of our Th M moves back and forth on the tape, "deleting" one I for each 1; if there are no I's and 1's in the end, the string is accepted.

When in state 92, M her found a 1 and looks for a 0; in state 92 is the other way around.

Note than the head never moves left of any x, so that there are never numeticled 0's and 1's on the left of an x.

From initial state qo, M picks up a O or a 1 and turns it into X. The only final state is 94. In state 93 M moves head left looking for the nightancost X.

***************************************	+ 0	1	t	X	Y
90	(92, x, R)	(91,×,R)	$(9_{4}, 5, R)$		(90, Y, R)
91	(93, Y, L)	$(q_1, 1, R)$	_		(92, Y, R)
92	(92,0,R)	(93, Y, L)	_	-	(q_i, Y, R)
93	(93,0,L)	(93,1 L)	_	(9.,×, R)	(93, Y, L)
94	_	_	-		N