

# pyResToolbox MCP

## Formula Reference Guide

Quick Reference for Reservoir Engineering Calculations

Gabriel Serrão Seabra

November 21, 2025

Version 1.0

### Abstract

This document provides a comprehensive reference guide for calculation tools available in the pyResToolbox Model Context Protocol (MCP) server. It includes mathematical formulas, symbol definitions, unit systems, and correlation methods covering oil PVT, gas PVT, well performance, simulation support, brine properties, and reservoir heterogeneity analysis. All calculations use Field Units (US Oilfield standard).

**Note:** This guide covers the core petroleum engineering calculations. The MCP server also includes geomechanics and wellbore stability tools which are documented separately.

**Based on pyResToolbox:** This MCP server is built upon the excellent *pyResToolbox* library by Mark W. Burgoyne (<https://github.com/mwburgoyne/pyResToolbox>), which provides the underlying reservoir engineering calculations.

### DISCLAIMER

**No Warranty:** This document and the formulas contained herein are provided "AS IS" without warranty of any kind, either expressed or implied. While every effort has been made to ensure accuracy, all formulas, correlations, and calculations **MUST be independently verified** before use in any engineering or commercial application.

**Professional Responsibility:** Users are solely responsible for verifying the correctness and applicability of any formula, correlation, or calculation method presented in this document. The author and contributors assume no liability for errors, omissions, or consequences arising from the use of this information.

**Verification Required:** Always cross-reference formulas with original published sources and validate results against known benchmarks before applying to real reservoir engineering problems.

## Contents

<b>1</b>	<b>Introduction</b>	<b>5</b>
1.1	About pyResToolbox MCP	5
1.2	Unit System	5
<b>2</b>	<b>Oil PVT Calculations</b>	<b>6</b>
2.1	Bubble Point Pressure ( $P_b$ )	6
2.1.1	Description	6
2.1.2	Available Methods	6
2.2	Solution Gas-Oil Ratio ( $R_s$ )	7
2.2.1	Description	7
2.2.2	Standing (1947) Method	7
2.3	Oil Formation Volume Factor ( $B_o$ )	7
2.3.1	Description	7
2.3.2	McCain et al. (1988) Method - MCAIN	7
2.3.3	Standing (1947) Method - STAN	8
2.4	Oil Viscosity ( $\mu_o$ )	8
2.4.1	Description	8
2.4.2	Beggs-Robinson (1975) Method - BR	8
2.5	Oil Density ( $\rho_o$ )	9
2.5.1	Description	9
2.5.2	Standing-White-McCain-Hill (1995) Method - SWMH	9
2.6	Oil Compressibility ( $c_o$ )	9
2.6.1	Description	9
2.6.2	Explicit Method - EXPLT	9
2.7	API-Specific Gravity Conversions	10
2.7.1	API to Specific Gravity	10
2.7.2	Specific Gravity to API	10
<b>3</b>	<b>Gas PVT Calculations</b>	<b>11</b>
3.1	Gas Z-Factor (Compressibility Factor)	11
3.1.1	Description	11
3.1.2	Dranchuk-Abou-Kassem (1975) Method - DAK	11
3.1.3	Hall-Yarborough (1973) Method - HY	11
3.1.4	Burgoyne-Nielsen-Stanko (2025) Method - BUR	12
3.2	Pseudo-Critical Properties	12
3.2.1	Description	12
3.2.2	Piper-McCain-Corredor (1993) Method - PMC	12
3.3	Gas Formation Volume Factor ( $B_g$ )	13
3.3.1	Description	13
3.4	Gas Viscosity ( $\mu_g$ )	13
3.4.1	Description	13
3.4.2	Lee-Gonzalez-Eakin (1966) Method - LGE	13
3.5	Gas Density ( $\rho_g$ )	14
3.6	Gas Compressibility ( $c_g$ )	14
3.6.1	Description	14
3.7	Gas Pseudopressure ( $\psi$ )	14
3.7.1	Description	14

<b>4</b>	<b>Inflow Performance (Well Productivity)</b>	<b>16</b>
4.1	Oil Rate - Radial Flow (Vertical Wells)	16
4.1.1	Description	16
4.1.2	Darcy's Law - Undersaturated Reservoir	16
4.1.3	Vogel IPR - Saturated Reservoir	16
4.2	Oil Rate - Linear Flow (Horizontal Wells)	17
4.2.1	Description	17
4.3	Gas Rate - Radial Flow (Vertical Wells)	17
4.3.1	Description	17
4.4	Gas Rate - Linear Flow (Horizontal Wells)	17
<b>5</b>	<b>Relative Permeability Correlations</b>	<b>18</b>
5.1	Corey (1954) Correlation	18
5.1.1	Description	18
5.1.2	Normalized Saturation	18
5.1.3	Relative Permeability Functions	19
5.2	LET Correlation (Lomeland-Ebeltoft-Thomas 2005)	19
5.2.1	Description	19
<b>6</b>	<b>Brine Properties</b>	<b>21</b>
6.1	CH <sub>4</sub> -Saturated Brine Properties	21
6.1.1	Description	21
6.1.2	Calculation Method	21
6.2	CO <sub>2</sub> -Saturated Brine Properties	22
6.2.1	Description	22
6.2.2	Calculation Methods	22
6.3	Key Differences Between CH <sub>4</sub> and CO <sub>2</sub> Methods	23
<b>7</b>	<b>Reservoir Heterogeneity</b>	<b>24</b>
7.1	Lorenz Coefficient	24
7.1.1	Description	24
7.2	Dykstra-Parsons Coefficient ( $\beta$ )	24
7.2.1	Description	24
7.3	Lorenz-Beta Conversion	25
7.3.1	Description	25
7.4	Layer Permeability Distribution	25
7.4.1	Description	25
<b>8</b>	<b>Aquifer Models</b>	<b>27</b>
8.1	Van Everdingen-Hurst Model	27
8.1.1	Description	27
8.2	Influence Functions	27
<b>9</b>	<b>Phase Behavior</b>	<b>28</b>
9.1	Rachford-Rice Flash Calculation	28
9.1.1	Description	28

<b>10 Quick Reference Tables</b>	<b>29</b>
10.1 Physical Constants . . . . .	29
10.2 Conversion Factors . . . . .	29
10.3 Typical Property Ranges . . . . .	29
<b>11 Correlation Method Recommendations</b>	<b>30</b>
11.1 Oil PVT Methods . . . . .	30
11.2 Gas PVT Methods . . . . .	30
11.3 Relative Permeability Methods . . . . .	30
<b>12 Tool Categories and Count</b>	<b>31</b>
12.1 Available Tools by Category . . . . .	31
12.2 Key Features . . . . .	31
<b>13 Usage Notes and Best Practices</b>	<b>32</b>
13.1 General Guidelines . . . . .	32
13.1.1 Input Validation . . . . .	32
13.1.2 Method Selection . . . . .	32
13.1.3 Common Mistakes to Avoid . . . . .	33
13.2 PVT Calculation Workflow . . . . .	33
13.2.1 Typical Oil PVT Workflow . . . . .	33
13.2.2 Typical Gas PVT Workflow . . . . .	33
13.3 Well Performance Analysis . . . . .	34
13.3.1 IPR Generation Steps . . . . .	34
13.4 Simulation Preparation . . . . .	34
13.4.1 Relative Permeability Table Generation . . . . .	34
<b>14 References</b>	<b>35</b>
14.1 Key Publications . . . . .	35
14.1.1 Oil PVT Correlations . . . . .	35
14.1.2 Gas PVT Correlations . . . . .	35
14.1.3 Well Performance . . . . .	35
14.1.4 Relative Permeability . . . . .	36
14.1.5 Brine Properties . . . . .	36
14.1.6 Reservoir Heterogeneity . . . . .	36
14.2 Software and Tools . . . . .	36
<b>15 Appendix: Nomenclature</b>	<b>37</b>
15.1 Primary Symbols . . . . .	37
15.2 Subscripts . . . . .	38
<b>16 Index of Formulas</b>	<b>39</b>
16.1 By Property . . . . .	39

# 1 Introduction

## 1.1 About pyResToolbox MCP

pyResToolbox MCP is a Model Context Protocol server that provides AI agents like Claude with access to industry-standard petroleum engineering calculations. Built on the comprehensive pyResToolbox library by Mark Burgoyne, it offers 47 production-ready tools for reservoir engineering workflows.

## 1.2 Unit System

All calculations use **Field Units (US Oilfield standard)**:

Property	Unit	Example
Pressure	psia	3000 psia
Temperature	°F	180°F
Permeability	mD	100 mD
Pay Thickness	ft	50 ft
Viscosity	cP	0.85 cP
Oil Rate	STB/day	542 STB/day
Gas Rate	MSCF/day	1250 MSCF/day
Oil Gravity	API° or SG	35° API
Gas Gravity	SG (air=1)	0.75
Solution GOR	scf/stb	800 scf/stb
Oil FVF	rb/stb	1.25 rb/stb
Gas FVF	rcf/scf	0.0045 rcf/scf
Compressibility	1/psi	$1.2 \times 10^{-5}$ 1/psi
Density	lb/ft <sup>3</sup>	42.5 lb/ft <sup>3</sup>

Table 1: Field Units Used in All Calculations

## 2 Oil PVT Calculations

### 2.1 Bubble Point Pressure ( $P_b$ )

#### 2.1.1 Description

The bubble point pressure is the pressure at which the first gas bubble evolves from solution oil. It is a critical PVT property that defines the boundary between undersaturated (single-phase) and saturated (two-phase) oil behavior.

#### 2.1.2 Available Methods

##### 1. Standing (1947) - STAN

$$P_b = 18.2 \left[ \left( \frac{R_{sb}}{\gamma_g} \right)^{0.83} \times 10^a - 1.4 \right] \quad (1)$$

where:

$$a = 0.00091 \times T - 0.0125 \times \text{API} \quad (2)$$

##### Symbol Definitions:

- $P_b$ : Bubble point pressure (psia)
- $R_{sb}$ : Solution GOR at bubble point (scf/stb)
- $\gamma_g$ : Gas specific gravity (air=1)
- $T$ : Temperature (°F)
- **API**: Oil API gravity (degrees)

##### 2. Valko-McCain (2003) - VALMC

$$P_b = -C_1 - C_2 \times A - C_3 \times A^2 \quad (3)$$

where:

$$A = \ln \left( \frac{R_{sb}}{\gamma_{sp}} \right) \quad (4)$$

$$C_1 = 7.916 \times 10^{-4} \times \text{API}^{1.541} - 4.561 \times 10^{-5} \times T^{1.3911} \quad (5)$$

$$C_2 = 4.51 \times 10^{-5} \times \text{API}^{1.3911} \times T^{0.7849} \quad (6)$$

$$C_3 = 1.046 \times 10^{-7} \times \text{API}^{1.3911} \times T^{1.007} \quad (7)$$

##### Additional Symbols:

- $\gamma_{sp}$ : Separator gas specific gravity (air=1)
- $C_1, C_2, C_3$ : Correlation coefficients

##### 3. Velarde-Blasingame-McCain (1997) - VELAR

$$\ln(P_b) = a_0 + a_1 \ln(R_{sb}) + a_2 [\ln(R_{sb})]^2 + a_3 \ln(\gamma_{sp}) + a_4 \ln(\text{API}) + a_5 \ln(T + 460) \quad (8)$$

Coefficients  $a_0$  through  $a_5$  are empirically determined from regression analysis.

## 2.2 Solution Gas-Oil Ratio ( $R_s$ )

### 2.2.1 Description

The solution gas-oil ratio represents the volume of gas dissolved in oil at a given pressure and temperature. It increases with pressure up to the bubble point, then remains constant (equal to  $R_{sb}$ ) above the bubble point.

### 2.2.2 Standing (1947) Method

$$R_s = \gamma_g \left[ \frac{P}{18.2} + 1.4 \right] \times 10^{-a} \quad (9)$$

where:

$$a = 0.0125 \times \text{API} - 0.00091 \times T \quad (10)$$

#### Symbol Definitions:

- $R_s$ : Solution gas-oil ratio (scf/stb)
- $P$ : Pressure (psia)
- $\gamma_g$ : Gas specific gravity (air=1)
- $\text{API}$ : Oil API gravity (degrees)
- $T$ : Temperature (°F)

#### Behavior:

- $P < P_b$ :  $R_s$  calculated from correlation
- $P \geq P_b$ :  $R_s = R_{sb}$  (constant)

## 2.3 Oil Formation Volume Factor ( $B_o$ )

### 2.3.1 Description

The formation volume factor relates the volume of oil at reservoir conditions to its volume at stock tank conditions. It accounts for thermal expansion and gas in solution.

### 2.3.2 McCain et al. (1988) Method - MCAIN

$$B_o = \frac{\rho_{ST}}{\rho_o} \quad (11)$$

where oil density  $\rho_o$  is calculated from:

$$\rho_o = \frac{\rho_{ST} + 0.01357 \times R_s \times \gamma_g}{0.972 + 0.000147 \times (T + 460)^{1.175}} \quad (12)$$

**Symbol Definitions:**

- $B_o$ : Oil formation volume factor (rb/stb)
- $\rho_o$ : Oil density at reservoir conditions (lb/ft<sup>3</sup>)
- $\rho_{ST}$ : Oil density at stock tank conditions (lb/ft<sup>3</sup>)
- $R_s$ : Solution gas-oil ratio (scf/stb)
- $\gamma_g$ : Gas specific gravity (air=1)
- $T$ : Temperature (°F)

**2.3.3 Standing (1947) Method - STAN**

$$B_o = 0.9759 + 0.00012 \left[ R_s \sqrt{\frac{\gamma_g}{\gamma_o}} + 1.25T \right]^{1.2} \quad (13)$$

**Additional Symbols:**

- $\gamma_o$ : Oil specific gravity (water=1)

**2.4 Oil Viscosity ( $\mu_o$ )****2.4.1 Description**

Oil viscosity is a measure of the oil's resistance to flow. It decreases with increasing temperature and decreasing pressure (above bubble point).

**2.4.2 Beggs-Robinson (1975) Method - BR****Dead Oil Viscosity:**

$$\mu_{od} = 10^X - 1 \quad (14)$$

where:

$$X = T^{-1.163} \times \exp(6.9824 - 0.04658 \times \text{API}) \quad (15)$$

**Live Oil Viscosity:**

$$\mu_o = A \times \mu_{od}^B \quad (16)$$

where:

$$A = 10.715 \times (R_s + 100)^{-0.515} \quad (17)$$

$$B = 5.44 \times (R_s + 150)^{-0.338} \quad (18)$$

**Symbol Definitions:**

- $\mu_o$ : Oil viscosity (cP)
- $\mu_{od}$ : Dead oil viscosity (cP)



- $R_s$ : Solution gas-oil ratio (scf/stb)
- $T$ : Temperature (°F)
- **API**: Oil API gravity (degrees)

## 2.5 Oil Density ( $\rho_o$ )

### 2.5.1 Description

Oil density at reservoir conditions accounts for dissolved gas and thermal expansion effects.

### 2.5.2 Standing-White-McCain-Hill (1995) Method - SWMH

$$\rho_o = \frac{62.4 \times \gamma_o + 0.0136 \times R_s \times \gamma_g}{B_o} \quad (19)$$

#### Symbol Definitions:

- $\rho_o$ : Oil density (lb/ft<sup>3</sup>)
- $\gamma_o$ : Oil specific gravity (water=1)
- $\gamma_g$ : Gas specific gravity (air=1)
- $R_s$ : Solution gas-oil ratio (scf/stb)
- $B_o$ : Oil formation volume factor (rb/stb)

## 2.6 Oil Compressibility ( $c_o$ )

### 2.6.1 Description

Oil compressibility describes the fractional change in oil volume with pressure. It is critical for material balance calculations and pressure transient analysis.

### 2.6.2 Explicit Method - EXPLT

$$c_o = -\frac{1}{B_o} \left[ \frac{dB_o}{dP} - \frac{B_g}{5.61458} \frac{dR_s}{dP} \right] \quad (20)$$

#### Symbol Definitions:

- $c_o$ : Oil compressibility (1/psi)
- $B_o$ : Oil formation volume factor (rb/stb)
- $B_g$ : Gas formation volume factor (rcf/scf)
- $R_s$ : Solution gas-oil ratio (scf/stb)
- $P$ : Pressure (psia)

**Note:** Derivatives are calculated numerically using finite differences.

## 2.7 API-Specific Gravity Conversions

### 2.7.1 API to Specific Gravity

$$\gamma_o = \frac{141.5}{\text{API} + 131.5} \quad (21)$$

### 2.7.2 Specific Gravity to API

$$\text{API} = \frac{141.5}{\gamma_o} - 131.5 \quad (22)$$

#### Symbol Definitions:

- **API:** Oil API gravity (degrees)
- $\gamma_o$ : Oil specific gravity (water=1)

### 3 Gas PVT Calculations

#### 3.1 Gas Z-Factor (Compressibility Factor)

##### 3.1.1 Description

The Z-factor corrects the ideal gas law for real gas behavior. It is defined as:

$$PV = ZnRT \quad (23)$$

where  $Z = 1$  for ideal gas,  $Z < 1$  for most real gases at reservoir conditions.

##### 3.1.2 Dranchuk-Abou-Kassem (1975) Method - DAK

$$Z = 1 + A_1\rho_r + A_2\rho_r^2 + A_3\rho_r^5 + A_4\rho_r^2(1 + A_5\rho_r^2)\exp(-A_5\rho_r^2) \quad (24)$$

$$+ \frac{A_6 + A_7\rho_r + A_8\rho_r^2}{T_{pr}^3}\rho_r^2 \quad (25)$$

where reduced density  $\rho_r$  is solved iteratively from:

$$\rho_r = \frac{0.27P_{pr}}{ZT_{pr}} \quad (26)$$

##### Symbol Definitions:

- $Z$ : Gas compressibility factor (dimensionless)
- $\rho_r$ : Reduced density (dimensionless)
- $P_{pr}$ : Pseudo-reduced pressure =  $P/P_c$
- $T_{pr}$ : Pseudo-reduced temperature =  $(T + 460)/T_c$
- $P_c$ : Pseudo-critical pressure (psia)
- $T_c$ : Pseudo-critical temperature ( $^{\circ}\text{R}$ )
- $A_1, \dots, A_8$ : Correlation constants

##### 3.1.3 Hall-Yarborough (1973) Method - HY

Implicit equation for reduced density  $y$ :

$$\frac{0.06125P_{pr}t}{y}\exp[-1.2(1-t)^2] = F(y) \quad (27)$$

where:

$$F(y) = -A_1 + A_2/y + A_3/y^2 + A_4/y^3 + A_5/y^4 + y^2(A_6 + A_7/y + A_8/y^2)(1 + A_9y^2)\exp(-A_9y^2) \quad (28)$$

Then  $Z$  is calculated from:

$$Z = \frac{A_1P_{pr}}{y} \quad (29)$$

where  $t = 1/T_{pr}$  and  $A_1, \dots, A_9$  are correlation constants.

### 3.1.4 Burgoyne-Nielsen-Stanko (2025) Method - BUR

**Universal EOS-based correlation** for Z-factor, viscosity, and enthalpy. This is the most recent and comprehensive method, developed specifically to handle:

- High concentrations of non-hydrocarbons (CO<sub>2</sub>, H<sub>2</sub>S, N<sub>2</sub>, H<sub>2</sub>)
- Pure non-hydrocarbon streams (100% CO<sub>2</sub>, 100% H<sub>2</sub>)
- Hydrogen mixtures (only method supporting H<sub>2</sub>)
- Full range of P-T conditions

Based on a tuned 5-component Peng-Robinson EOS model. The formulation methods are fully described in SPE-229932-MS, and the tuning datasets are available on GitHub. The correlation is implemented in pyResToolbox and provides open access to these calculations.

**Reference:** SPE-229932-MS (ADIPEC 2025) - Burgoyne, M.W. (Santos Ltd), Nielsen, M.H., and Stanko, M. (Whitson AS)

#### Method Comparison:

- **DAK:** Best for hydrocarbon gases with low non-HC content
- **HY:** Fast alternative for standard conditions
- **WYW:** Modern update to classical methods
- **BUR:** Universal method, required for H<sub>2</sub> or high non-HC content

## 3.2 Pseudo-Critical Properties

### 3.2.1 Description

Pseudo-critical properties (temperature and pressure) are used to calculate the reduced properties needed for Z-factor correlations.

### 3.2.2 Piper-McCain-Corredor (1993) Method - PMC

#### Without Non-Hydrocarbons:

$$T_c = 169.2 + 349.5\gamma_g - 74.0\gamma_g^2 \quad (^\circ\text{R}) \quad (30)$$

$$P_c = 756.8 - 131.07\gamma_g - 3.6\gamma_g^2 \quad (\text{psia}) \quad (31)$$

#### With CO<sub>2</sub> and H<sub>2</sub>S Corrections:

$$T'_c = T_c - \epsilon_T \quad (32)$$

$$P'_c = \frac{P_c - \epsilon_P}{1 - y_{\text{CO}_2} - y_{\text{H}_2\text{S}}} \quad (33)$$

where:

$$\epsilon_T = 120(y_{\text{CO}_2}^{0.9} - y_{\text{CO}_2}^{1.6}) + 15(y_{\text{H}_2\text{S}}^{0.5} - y_{\text{H}_2\text{S}}^4) \quad (34)$$

$$\epsilon_P = 440y_{\text{CO}_2} + 600y_{\text{H}_2\text{S}} - 170y_{\text{CO}_2}y_{\text{H}_2\text{S}} \quad (35)$$

**Symbol Definitions:**

- $T_c$ : Pseudo-critical temperature (°R)
- $P_c$ : Pseudo-critical pressure (psia)
- $\gamma_g$ : Gas specific gravity (air=1)
- $y_{CO_2}$ : CO<sub>2</sub> mole fraction
- $y_{H_2S}$ : H<sub>2</sub>S mole fraction
- $y_{N_2}$ : N<sub>2</sub> mole fraction
- $\epsilon_T$ : Temperature correction
- $\epsilon_P$ : Pressure correction

**3.3 Gas Formation Volume Factor ( $B_g$ )****3.3.1 Description**

The gas formation volume factor relates gas volume at reservoir conditions to its volume at standard conditions.

$$B_g = \frac{0.02827 \times Z \times (T + 460)}{P} \quad (\text{rcf/scf}) \quad (36)$$

**Symbol Definitions:**

- $B_g$ : Gas formation volume factor (rcf/scf)
- $Z$ : Gas compressibility factor (dimensionless)
- $T$ : Temperature (°F)
- $P$ : Pressure (psia)

**3.4 Gas Viscosity ( $\mu_g$ )****3.4.1 Description**

Gas viscosity is required for flow calculations and increases with pressure and temperature.

**3.4.2 Lee-Gonzalez-Eakin (1966) Method - LGE**

$$\mu_g = K \times 10^{-4} \times \exp [X \times \rho_g^Y] \quad (37)$$

where:

$$K = \frac{(9.4 + 0.02M)(T + 460)^{1.5}}{209 + 19M + (T + 460)} \quad (38)$$

$$X = 3.5 + \frac{986}{T + 460} + 0.01M \quad (39)$$

$$Y = 2.4 - 0.2X \quad (40)$$

$$M = 28.97\gamma_g \quad (41)$$

**Symbol Definitions:**

- $\mu_g$ : Gas viscosity (cP)
- $\rho_g$ : Gas density (lb/ft<sup>3</sup>)
- $M$ : Gas molecular weight (lb/lbmol)
- $\gamma_g$ : Gas specific gravity (air=1)
- $T$ : Temperature (°F)

**3.5 Gas Density ( $\rho_g$ )**

$$\rho_g = \frac{P \times 28.97 \times \gamma_g}{Z \times 10.73 \times (T + 460)} \quad (\text{lb/ft}^3) \quad (42)$$

**Symbol Definitions:**

- $\rho_g$ : Gas density (lb/ft<sup>3</sup>)
- $P$ : Pressure (psia)
- $\gamma_g$ : Gas specific gravity (air=1)
- $Z$ : Gas compressibility factor (dimensionless)
- $T$ : Temperature (°F)

**3.6 Gas Compressibility ( $c_g$ )****3.6.1 Description**

Gas compressibility describes the fractional change in gas volume with pressure.

$$c_g = \frac{1}{P} - \frac{1}{Z} \frac{dZ}{dP} \quad (43)$$

**Symbol Definitions:**

- $c_g$ : Gas compressibility (1/psi)
- $P$ : Pressure (psia)
- $Z$ : Gas compressibility factor (dimensionless)

**3.7 Gas Pseudopressure ( $\psi$ )****3.7.1 Description**

Gas pseudopressure (or real gas potential) linearizes the gas diffusivity equation and is used in well test analysis.

$$\psi(P) = 2 \int_{P_0}^P \frac{P'}{\mu_g Z} dP' \quad (\text{psia}^2/\text{cP}) \quad (44)$$

**Symbol Definitions:**

- $\psi$ : Gas pseudopressure (psia<sup>2</sup>/cP)
- $P$ : Pressure (psia)
- $P_0$ : Reference pressure (usually 0 psia)
- $\mu_g$ : Gas viscosity (cP)
- $Z$ : Gas compressibility factor (dimensionless)

**Note:** Integral is evaluated numerically using trapezoidal rule or Simpson's rule.

## 4 Inflow Performance (Well Productivity)

### 4.1 Oil Rate - Radial Flow (Vertical Wells)

#### 4.1.1 Description

Calculates oil production rate for vertical wells with radial flow geometry using Darcy's law for steady-state or pseudo-steady-state flow.

#### 4.1.2 Darcy's Law - Undersaturated Reservoir

$$q_o = \frac{0.00708 \times k \times h \times (P_i - P_{wf})}{\mu_o \times B_o \times \left[ \ln \left( \frac{r_e}{r_w} \right) - 0.75 + S \right]} \quad (\text{STB/day}) \quad (45)$$

#### Symbol Definitions:

- $q_o$ : Oil production rate (STB/day)
- $k$ : Permeability (mD)
- $h$ : Net pay thickness (ft)
- $P_i$ : Initial/reservoir pressure (psia)
- $P_{wf}$ : Wellbore flowing pressure (psia)
- $\mu_o$ : Oil viscosity (cP)
- $B_o$ : Oil formation volume factor (rb/stb)
- $r_e$ : Drainage radius (ft)
- $r_w$ : Wellbore radius (ft)
- $S$ : Skin factor (dimensionless)

#### 4.1.3 Vogel IPR - Saturated Reservoir

For saturated reservoirs ( $P_i < P_b$ ), use Vogel's correlation:

$$\frac{q_o}{q_{o,max}} = 1 - 0.2 \left( \frac{P_{wf}}{P_i} \right) - 0.8 \left( \frac{P_{wf}}{P_i} \right)^2 \quad (46)$$

where maximum rate is:

$$q_{o,max} = q_o(P_{wf} = 0) \quad (47)$$

#### Additional Symbols:

- $q_{o,max}$ : Maximum oil rate at zero bottomhole pressure (STB/day)
- $P_b$ : Bubble point pressure (psia)



## 4.2 Oil Rate - Linear Flow (Horizontal Wells)

### 4.2.1 Description

Calculates oil production rate for horizontal wells or linear flow geometry.

$$q_o = \frac{0.00708 \times k \times h \times L \times (P_i - P_{wf})}{\mu_o \times B_o \times \left[\frac{r_e}{2} + S\right]} \quad (\text{STB/day}) \quad (48)$$

**Additional Symbols:**

- $L$ : Horizontal well length (ft)

## 4.3 Gas Rate - Radial Flow (Vertical Wells)

### 4.3.1 Description

Calculates gas production rate for vertical wells using pseudopressure formulation.

$$q_g = \frac{0.00708 \times k \times h \times [\psi(P_i) - \psi(P_{wf})]}{\left[\ln\left(\frac{r_e}{r_w}\right) - 0.75 + S\right]} \quad (\text{MSCF/day}) \quad (49)$$

**Symbol Definitions:**

- $q_g$ : Gas production rate (MSCF/day)
- $\psi(P)$ : Gas pseudopressure (psia<sup>2</sup>/cP)
- $k$ : Permeability (mD)
- $h$ : Net pay thickness (ft)
- $P_i$ : Reservoir pressure (psia)
- $P_{wf}$ : Wellbore flowing pressure (psia)
- $r_e$ : Drainage radius (ft)
- $r_w$ : Wellbore radius (ft)
- $S$ : Skin factor (dimensionless)

## 4.4 Gas Rate - Linear Flow (Horizontal Wells)

$$q_g = \frac{0.00708 \times k \times h \times L \times [\psi(P_i) - \psi(P_{wf})]}{\left[\frac{r_e}{2} + S\right]} \quad (\text{MSCF/day}) \quad (50)$$

**Additional Symbols:**

- $L$ : Horizontal well length (ft)

## 5 Relative Permeability Correlations

### 5.1 Corey (1954) Correlation

#### 5.1.1 Description

Simple power-law model for relative permeability as a function of normalized saturation.

#### 5.1.2 Normalized Saturation

**Water Phase:**

$$S_w^* = \frac{S_w - S_{wc}}{1 - S_{wc} - S_{or}} \quad (51)$$

**Oil Phase (Water-Oil):**

$$S_o^* = \frac{S_o - S_{or}}{1 - S_{wc} - S_{or}} \quad (52)$$

**Gas Phase:**

$$S_g^* = \frac{S_g - S_{gc}}{1 - S_{wc} - S_{org}} \quad (53)$$

**Symbol Definitions:**

- $S_w^*$ : Normalized water saturation
- $S_o^*$ : Normalized oil saturation
- $S_g^*$ : Normalized gas saturation
- $S_w$ : Water saturation
- $S_o$ : Oil saturation
- $S_g$ : Gas saturation
- $S_{wc}$ : Connate water saturation
- $S_{or}$ : Residual oil saturation (to water)
- $S_{org}$ : Residual oil saturation (to gas)
- $S_{gc}$ : Critical gas saturation

### 5.1.3 Relative Permeability Functions

**Water Relative Permeability:**

$$k_{rw} = k_{rw}^{max} \times (S_w^*)^{n_w} \quad (54)$$

**Oil Relative Permeability (to water):**

$$k_{row} = k_{row}^{max} \times (1 - S_w^*)^{n_o} \quad (55)$$

**Gas Relative Permeability:**

$$k_{rg} = k_{rg}^{max} \times (S_g^*)^{n_g} \quad (56)$$

**Oil Relative Permeability (to gas):**

$$k_{rog} = k_{rog}^{max} \times (1 - S_g^*)^{n_o} \quad (57)$$

**Additional Symbols:**

- $k_{rw}$ : Water relative permeability
- $k_{row}$ : Oil relative permeability (to water)
- $k_{rg}$ : Gas relative permeability
- $k_{rog}$ : Oil relative permeability (to gas)
- $k_{rw}^{max}$ : Maximum water relative permeability
- $k_{row}^{max}$ : Maximum oil relative permeability
- $k_{rg}^{max}$ : Maximum gas relative permeability
- $n_w$ : Corey exponent for water
- $n_o$ : Corey exponent for oil
- $n_g$ : Corey exponent for gas

**Typical Values:**

- $n_w$ : 1.5 - 3.0
- $n_o$ : 2.0 - 4.0
- $n_g$ : 2.0 - 3.5

## 5.2 LET Correlation (Lomeland-Ebeltoft-Thomas 2005)

### 5.2.1 Description

Flexible three-parameter model (L, E, T) that can fit complex relative permeability curves.

**Water Relative Permeability:**

$$k_{rw} = k_{rw}^{max} \times \frac{(S_w^*)^{L_w}}{(S_w^*)^{L_w} + E_w(1 - S_w^*)^{T_w}} \quad (58)$$

**Oil Relative Permeability:**

$$k_{ro} = k_{ro}^{max} \times \frac{(1 - S_w^*)^{L_o}}{(1 - S_w^*)^{L_o} + E_o(S_w^*)^{T_o}} \quad (59)$$

**Gas Relative Permeability:**

$$k_{rg} = k_{rg}^{max} \times \frac{(S_g^*)^{L_g}}{(S_g^*)^{L_g} + E_g(1 - S_g^*)^{T_g}} \quad (60)$$

**Symbol Definitions:**

- $L_w, L_o, L_g$ : Low saturation parameters (controls curve near  $S^* = 0$ )
- $E_w, E_o, E_g$ : Elevation parameters (controls height/position)
- $T_w, T_o, T_g$ : Top saturation parameters (controls curve near  $S^* = 1$ )

**Typical Ranges:**

- $L$ : 1.0 - 3.0
- $E$ : 1.0 - 2.0
- $T$ : 1.0 - 3.0

**Advantages over Corey:**

- More flexible curve shapes
- Better fitting to experimental data
- Independent control of endpoint behavior
- Smooth transitions

## 6 Brine Properties

**Important Note:** pyResToolbox uses **different calculation methods** for CH<sub>4</sub>-saturated versus CO<sub>2</sub>-saturated brines. The methods are described separately below.

### 6.1 CH<sub>4</sub>-Saturated Brine Properties

#### 6.1.1 Description

For methane-saturated brines, pyResToolbox uses the Modified Spivey Correlation per McCain *Petroleum Reservoir Fluid Properties*, Chapter 4, page 160.

#### 6.1.2 Calculation Method

##### General Approach:

Properties are calculated using empirical correlations that account for:

- Temperature and pressure effects
- Salinity (weight% NaCl, range 0-100%)
- Methane saturation fraction (0 = no methane, 1 = fully saturated)

##### Key Features:

- Density calculated from pure water density with salt and methane corrections
- Viscosity uses temperature-dependent base correlation with salinity adjustments
- Compressibility derived from density derivatives with respect to pressure
- Methane solubility from modified Henry's Law with salt correction (lambda and eta coefficients)
- Gas molar volume calculated using Z-factor correlation for methane
- Formation volume factor (B<sub>w</sub>) accounts for molar volume changes due to dissolved methane

##### Properties Calculated:

- $B_w$ : Water formation volume factor (rb/stb)
- $\rho_w$ : Brine density (specific gravity, dimensionless)
- $\mu_w$ : Brine viscosity (cP)
- $c_w$ : Brine compressibility (1/psi)
- $R_w$ : Methane solubility (scf/stb)

**Reference:** McCain, W.D. (2011). *Petroleum Reservoir Fluid Property Correlations*, Chapter 4.

## 6.2 CO<sub>2</sub>-Saturated Brine Properties

### 6.2.1 Description

For CO<sub>2</sub>-saturated brines, pyResToolbox uses a thermodynamic approach with multiple specialized correlations that differ significantly from the methane case.

### 6.2.2 Calculation Methods

#### Phase Equilibrium:

- **Spycher & Pruess (2010)**: Modified Redlich-Kwong (SRK) Cubic Equation of State
- Provides CO<sub>2</sub>-H<sub>2</sub>O mutual solubility via activity coefficients
- Temperature-dependent EOS coefficients (different for  $T < 99^\circ\text{C}$  vs  $T > 109^\circ\text{C}$ )
- Blended calculations for 99-109°C transition range

#### Pure Brine Density:

- **Spivey et al.** correlation (modified)
- Reference: McCain *Petroleum Reservoir Fluid Property Correlations*, Chapter 4

#### CO<sub>2</sub>-Corrected Brine Density:

- **Garcia (2001)** equation for CO<sub>2</sub> molar volume
- Combined with Spycher & Pruess  $x_{\text{CO}_2}$  and Spivey base density

#### Pure Brine Viscosity:

- **Mao-Duan (2009)** correlation

#### CO<sub>2</sub>-Corrected Brine Viscosity:

- **Islam-Carlson (2012)** model
- Adjusts base viscosity for dissolved CO<sub>2</sub> mole fraction

#### Properties Calculated:

- $x_{\text{CO}_2}$ : CO<sub>2</sub> mole fraction in brine
- $y_{\text{H}_2\text{O}}$ : H<sub>2</sub>O mole fraction in CO<sub>2</sub>-rich phase
- $\rho_{\text{CO}_2\text{-gas}}$ : CO<sub>2</sub>-rich gas density (lb/ft<sup>3</sup>)
- $\rho_{\text{brine-sat}}$ : CO<sub>2</sub>-saturated brine density (lb/ft<sup>3</sup>)
- $\rho_{\text{brine-pure}}$ : Pure brine density (lb/ft<sup>3</sup>)
- $\mu_{\text{brine-sat}}$ : CO<sub>2</sub>-saturated brine viscosity (cP)
- $\mu_{\text{brine-pure}}$ : Pure brine viscosity (cP)

- $B_{w-sat}$ : CO<sub>2</sub>-saturated brine FVF (rb/stb)
- $R_w$ : CO<sub>2</sub> solubility (scf/stb)
- $c_{w-unsat}$ : Undersaturated brine compressibility (1/psi)
- $c_{w-sat}$ : Saturated brine compressibility (1/psi)

**Salinity Input:** Parts per million (ppm) NaCl

**Key References:**

- Spycher, N. and Pruess, K. (2010). *Geochimica et Cosmochimica Acta*
- Garcia, J.E. (2001). *Fluid Phase Equilibria*
- Mao, S. and Duan, Z. (2009). *Chemical Geology*
- Islam, A.W. and Carlson, E.S. (2012). *Geothermics*

### 6.3 Key Differences Between CH<sub>4</sub> and CO<sub>2</sub> Methods

Aspect		CH <sub>4</sub> -Saturated	CO <sub>2</sub> -Saturated
Phase Equilibrium		Henry's Law-based empirical	Cubic EOS (Spycher & Pruess)
Density Correction		Dissolved CH <sub>4</sub> molar volume	Garcia (2001) CO <sub>2</sub> molar volume
Viscosity Adjustment		Salinity effect factors	Islam-Carlson (2012) model
Salinity Units		Weight% NaCl (0-100)	ppm NaCl
Compressibility		From density derivatives	Numerical differentiation (sat/unsat)

Table 2: Comparison of CH<sub>4</sub> vs CO<sub>2</sub> Brine Calculation Methods

## 7 Reservoir Heterogeneity

### 7.1 Lorenz Coefficient

#### 7.1.1 Description

The Lorenz coefficient quantifies reservoir heterogeneity based on the cumulative flow capacity vs cumulative storage capacity curve. It ranges from 0 (homogeneous) to 1 (completely heterogeneous).

$$L = 2 \times \int_0^1 [F(\phi) - \phi] d\phi \quad (61)$$

where  $F(\phi)$  is the Lorenz curve:

$$F(\phi) = \frac{\text{Cumulative Flow Capacity}}{\text{Total Flow Capacity}} \quad (62)$$

#### Symbol Definitions:

- $L$ : Lorenz coefficient (0-1)
- $F(\phi)$ : Lorenz curve function
- $\phi$ : Cumulative storage fraction

#### Interpretation:

- $L = 0$ : Perfectly homogeneous (all layers have same  $kh$ )
- $L = 0.3$ : Low heterogeneity
- $L = 0.5$ : Moderate heterogeneity
- $L = 0.7$ : High heterogeneity
- $L \rightarrow 1$ : Extreme heterogeneity

### 7.2 Dykstra-Parsons Coefficient ( $\beta$ )

#### 7.2.1 Description

The Dykstra-Parsons coefficient measures permeability variation assuming a log-normal distribution.

$$\beta = \frac{k_{50} - k_{84.1}}{k_{50}} \quad (63)$$

where:

- $k_{50}$  is the median permeability (50th percentile)
- $k_{84.1}$  is the 84.1th percentile permeability (1 standard deviation below mean in log space)

#### Symbol Definitions:



- $\beta$ : Dykstra-Parsons coefficient (0-1)
- $k_{50}$ : Median permeability (mD)
- $k_{84.1}$ : 84.1th percentile permeability (mD)

**Interpretation:**

- $\beta < 0.5$ : Low variation (homogeneous)
- $\beta = 0.5 - 0.7$ : Moderate variation
- $\beta > 0.7$ : High variation (heterogeneous)

**7.3 Lorenz-Beta Conversion****7.3.1 Description**

Conversion between Lorenz coefficient and Dykstra-Parsons beta parameter, assuming log-normal permeability distribution.

**Beta to Lorenz:**

$$L \approx 1 - \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \exp\left(-\frac{x^2}{2}\right) \times \exp(x\sigma) dx \quad (64)$$

where  $\sigma$  is related to  $\beta$  through:

$$\beta = 1 - \exp(-\sigma) \quad (65)$$

**Approximate Conversion:**

$$L \approx 0.632 \times \beta^{0.9} \quad (66)$$

**Symbol Definitions:**

- $L$ : Lorenz coefficient
- $\beta$ : Dykstra-Parsons coefficient
- $\sigma$ : Standard deviation of  $\ln(k)$

**7.4 Layer Permeability Distribution****7.4.1 Description**

Generates permeability distribution for layered reservoirs based on Lorenz coefficient.

**Log-Normal Distribution:**

$$k_i = k_{avg} \times \exp \left[ \sigma \times \Phi^{-1}(p_i) - \frac{\sigma^2}{2} \right] \quad (67)$$

where:

- $k_i$  is permeability of layer  $i$
- $k_{avg}$  is average permeability
- $\Phi^{-1}$  is inverse standard normal CDF
- $p_i = (i - 0.5)/N$  is cumulative probability
- $N$  is number of layers

**Symbol Definitions:**

- $k_i$ : Layer permeability (mD)
- $k_{avg}$ : Average permeability (mD)
- $\sigma$ : Standard deviation of  $\ln(k)$
- $\Phi^{-1}$ : Inverse cumulative normal distribution
- $N$ : Number of layers

## 8 Aquifer Models

### 8.1 Van Everdingen-Hurst Model

#### 8.1.1 Description

The Van Everdingen-Hurst model calculates water influx from an aquifer into a reservoir. It uses dimensionless influence functions based on the radial diffusivity equation.

**Water Influx:**

$$W_e(t) = B \times \sum_{j=1}^n \Delta P_j \times W_D(t_D - t_{D,j}) \quad (68)$$

where:

$$B = 1.119 \times \phi \times c_t \times h \times r_e^2 \quad (\text{rb/psi}) \quad (69)$$

**Dimensionless Time:**

$$t_D = \frac{0.000264 \times k \times t}{\phi \times \mu \times c_t \times r_e^2} \quad (70)$$

**Dimensionless Radius:**

$$r_D = \frac{r_{aq}}{r_e} \quad (71)$$

**Symbol Definitions:**

- $W_e$ : Cumulative water influx (rb)
- $B$ : Aquifer constant (rb/psi)
- $\Delta P_j$ : Pressure drop at time step  $j$  (psia)
- $W_D$ : Dimensionless water influx function
- $t_D$ : Dimensionless time
- $\phi$ : Aquifer porosity (fraction)
- $c_t$ : Total compressibility (1/psi)
- $h$ : Aquifer thickness (ft)
- $r_e$ : Reservoir radius (ft)
- $r_{aq}$ : Aquifer outer radius (ft)
- $k$ : Aquifer permeability (mD)
- $\mu$ : Water viscosity (cP)
- $t$ : Time (days)

### 8.2 Influence Functions

The dimensionless water influx  $W_D(t_D)$  is tabulated for various dimensionless radius ratios  $r_D$ . For:

- Infinite aquifer:  $r_D = \infty$
- Finite aquifer:  $r_D = 2, 3, 5, 10, \text{etc.}$

## 9 Phase Behavior

### 9.1 Rachford-Rice Flash Calculation

#### 9.1.1 Description

The Rachford-Rice equation is used to calculate vapor and liquid phase compositions and amounts for a multi-component mixture at specified temperature and pressure.

**Rachford-Rice Equation:**

$$\sum_{i=1}^n \frac{z_i(K_i - 1)}{1 + V(K_i - 1)} = 0 \quad (72)$$

where:

- $V$  is vapor mole fraction (solve iteratively)
- $L = 1 - V$  is liquid mole fraction

**Component Mole Fractions:**

$$x_i = \frac{z_i}{1 + V(K_i - 1)} \quad (\text{liquid}) \quad (73)$$

$$y_i = \frac{K_i \times z_i}{1 + V(K_i - 1)} \quad (\text{vapor}) \quad (74)$$

**Symbol Definitions:**

- $z_i$ : Overall mole fraction of component  $i$
- $x_i$ : Liquid phase mole fraction of component  $i$
- $y_i$ : Vapor phase mole fraction of component  $i$
- $K_i$ : Equilibrium K-value for component  $i$  ( $K_i = y_i/x_i$ )
- $V$ : Vapor phase mole fraction
- $L$ : Liquid phase mole fraction
- $n$ : Number of components

**Solution Method:** Newton-Raphson iteration:

$$V^{n+1} = V^n - \frac{f(V^n)}{f'(V^n)} \quad (75)$$

where:

$$f(V) = \sum_{i=1}^n \frac{z_i(K_i - 1)}{1 + V(K_i - 1)} \quad (76)$$

$$f'(V) = - \sum_{i=1}^n \frac{z_i(K_i - 1)^2}{[1 + V(K_i - 1)]^2} \quad (77)$$

## 10 Quick Reference Tables

### 10.1 Physical Constants

Constant	Symbol	Value
Universal gas constant	$R$	10.73 psia·ft <sup>3</sup> /(lbmol·°R)
Standard pressure	$P_{sc}$	14.7 psia
Standard temperature	$T_{sc}$	60°F (520°R)
Air molecular weight	$M_{air}$	28.97 lb/lbmol
Water density at SC	$\rho_w^{SC}$	62.4 lb/ft <sup>3</sup>
Conversion °F to °R	$T_R$	$T_F + 459.67$

Table 3: Physical Constants Used in Calculations

### 10.2 Conversion Factors

From	To	Multiply By
psia	bara	0.06895
°F	°C	$(T_F - 32) \times 5/9$
ft	m	0.3048
mD	m <sup>2</sup>	$9.869 \times 10^{-16}$
cP	Pa·s	0.001
STB	m <sup>3</sup>	0.1590
MSCF	m <sup>3</sup>	28.32
lb/ft <sup>3</sup>	kg/m <sup>3</sup>	16.02

Table 4: Common Unit Conversions

### 10.3 Typical Property Ranges

Property	Typical Range	Comments
API gravity	10 - 50°	Light crude: 30-50°, Heavy: 10-25°
Gas gravity	0.6 - 1.2	Dry gas: 0.6-0.7, Wet gas: 0.7-0.9
$R_s$ at $P_b$	100 - 3000 scf/stb	Depends on oil type and pressure
$B_o$	1.01 - 2.0 rb/stb	Increases with $R_s$
$\mu_o$	0.5 - 100 cP	Light oil: 0.5-5, Heavy: 10-100+
Z-factor	0.7 - 1.2	Lower at medium pressures
$B_g$	0.003 - 0.010 rcf/scf	Increases with T, decreases with P
$\mu_g$	0.01 - 0.03 cP	Increases with P and T
Permeability	0.1 - 1000 mD	Tight: <1, Good: 100-1000
Porosity	0.05 - 0.35	Low: 0.05-0.15, Good: 0.20-0.30

Table 5: Typical Property Ranges for Petroleum Reservoirs

## 11 Correlation Method Recommendations

### 11.1 Oil PVT Methods

Property	Recommended	When to Use
Bubble Point	VALMC	Wide range of conditions, most accurate
	STAN	Classic correlation, quick estimates
	VELAR	Regional correlations, comparison
Solution GOR	VELAR	Default choice, good accuracy
	STAN	Compatibility with older studies
	VALMC	Alternative method
FVF	MCAIN	Most accurate, density-based
	STAN	Simple correlation, fast
Viscosity	BR	Industry standard, widely validated

Table 6: Recommended Correlations for Oil PVT

### 11.2 Gas PVT Methods

Property	Recommended	When to Use
Z-Factor	DAK	Most accurate, industry standard
	HY	Fast, good for most conditions
	WYW	Newer correlation, comparison
	BUR	High non-hydrocarbons, 100% CO <sub>2</sub> , H <sub>2</sub>
Critical Props	PMC	Best accuracy, accounts for non-HCs
	SUT	Classic method, compatibility
	BUR	High non-hydrocarbon content
Viscosity	LGE	Industry standard

Table 7: Recommended Correlations for Gas PVT

### 11.3 Relative Permeability Methods

Method	Use For	Advantages
Corey	Quick estimates	Simple, fast, widely used
	Standard cases	Few parameters, easy to understand
	Initial models	Good starting point
LET	History matching	Flexible curve shapes
	Complex systems	Better fit to lab data
	Final models	Independent endpoint control

Table 8: Relative Permeability Method Selection

## 12 Tool Categories and Count

### 12.1 Available Tools by Category

### 12.2 Key Features

- **Production Ready:** All tools tested and validated
- **Field Units:** Consistent use of US oilfield units
- **Array Support:** Calculate properties at multiple pressures simultaneously
- **Multiple Methods:** Choose from various industry-standard correlations
- **Type Safety:** Pydantic models ensure input validation
- **Zero Configuration:** Works out of the box with Claude Desktop
- **GPL-3.0 Licensed:** Free and open source

Category	Description	Tools
<b>Oil PVT</b>	Oil property calculations Bubble point, Rs, Bo, viscosity, density, etc.	17
<b>Gas PVT</b>	Gas property calculations Z-factor, critical props, Bg, viscosity, etc.	11
<b>Inflow</b>	Well performance Oil/gas rates for radial/linear flow	4
<b>Simulation</b>	Reservoir simulation support Rel perm tables, aquifer functions, flash	3
<b>Brine</b>	Brine properties CH <sub>4</sub> and CO <sub>2</sub> saturated brine	2
<b>Heterogeneity</b>	Layer analysis Lorenz, beta, layer distributions	5
<b>Library</b>	Component properties Critical properties for 100+ components	1
<b>Config</b>	Configuration resources Units, methods, constants, help	4
<b>Geomechanics</b>	Wellbore stability & stress ( <i>Documented separately</i> )	15
<b>Total (Covered)</b>		<b>47</b>
<b>Total (All Tools)</b>		<b>62</b>

Table 9: pyResToolbox MCP Tool Categories (This guide covers 47 core petroleum engineering tools)

## 13 Usage Notes and Best Practices

### 13.1 General Guidelines

#### 13.1.1 Input Validation

- Always use absolute pressures (psia, not psig or barg)
- Temperature must be in Fahrenheit, not Celsius
- Check that input ranges are physically realistic
- Verify that saturation endpoints sum correctly (e.g.,  $S_{wc} + S_{or} < 1.0$ )

#### 13.1.2 Method Selection

- Use recommended methods unless specific requirements exist
- For bubble point: VALMC is most accurate for wide ranges
- For Z-factor: DAK is industry standard, BUR for high non-HCs
- For relative permeability: Corey for quick estimates, LET for accuracy



### 13.1.3 Common Mistakes to Avoid

- Using separator temperature instead of reservoir temperature
- Confusing  $R_{sb}$  (solution GOR at bubble point) with separator GOR
- Not setting Vogel=True when  $P_i < P_b$  (saturated reservoir)
- Using wrong gas gravity (separator vs weighted average)
- Not accounting for non-hydrocarbon components ( $H_2S$ ,  $CO_2$ ,  $N_2$ )
- Forgetting to convert units from SI to Field Units

## 13.2 PVT Calculation Workflow

### 13.2.1 Typical Oil PVT Workflow

1. Calculate bubble point pressure ( $P_b$ ) from  $R_{sb}$ , API,  $T$ ,  $\gamma_g$
2. Check if reservoir is undersaturated ( $P_i > P_b$ ) or saturated ( $P_i < P_b$ )
3. Calculate  $R_s(P)$  at desired pressures
4. Calculate  $B_o(P, R_s)$  using McCain or Standing method
5. Calculate  $\mu_o(P, R_s)$  using Beggs-Robinson
6. Calculate  $\rho_o(B_o, R_s)$  using SWMH method
7. Calculate  $c_o$  from numerical derivatives of  $B_o$
8. Generate complete PVT table for simulation

### 13.2.2 Typical Gas PVT Workflow

1. Calculate pseudo-critical properties ( $T_c$ ,  $P_c$ ) from  $\gamma_g$  and impurities
2. Calculate Z-factor at desired pressures using DAK or BUR
3. Calculate  $B_g(P, T, Z)$  from real gas equation
4. Calculate gas density  $\rho_g(P, T, Z)$
5. Calculate gas viscosity  $\mu_g(\rho_g, T)$  using LGE method
6. Calculate gas compressibility  $c_g$  from Z-factor derivatives
7. Calculate pseudopressure  $\psi(P)$  by integrating  $P/(\mu_g Z)$

### 13.3 Well Performance Analysis

#### 13.3.1 IPR Generation Steps

1. Gather reservoir data:  $P_i$ ,  $P_b$ , API,  $T$ ,  $h$ ,  $k$ ,  $S$ ,  $r_e$ ,  $r_w$
2. Calculate PVT properties at average pressure
3. Choose flow geometry: radial (vertical well) or linear (horizontal well)
4. For saturated reservoir ( $P_i < P_b$ ), set Vogel=True
5. Calculate rates at multiple flowing pressures:  $P_{wf} = 0$  to  $P_i$
6. Plot  $q$  vs  $P_{wf}$  to generate IPR curve
7. Identify AOF (absolute open flow = rate at  $P_{wf} = 0$ )

### 13.4 Simulation Preparation

#### 13.4.1 Relative Permeability Table Generation

1. Choose table type: SWOF (water-oil), SGOF (gas-oil), or SGWFN (3-phase)
2. Choose correlation: Corey (simple) or LET (flexible)
3. Specify saturation endpoints:  $S_{wc}$ ,  $S_{or}$ ,  $S_{org}$ ,  $S_{gc}$
4. Set maximum relative permeabilities:  $k_{rw}^{max}$ ,  $k_{ro}^{max}$ ,  $k_{rg}^{max}$
5. Define correlation parameters (Corey exponents or LET parameters)
6. Generate table with 20-50 saturation points
7. Validate endpoints and curves against core data
8. Export to ECLIPSE/CMG format for simulation

## 14 References

### 14.1 Key Publications

#### 14.1.1 Oil PVT Correlations

- Standing, M.B. (1947). "A Pressure-Volume-Temperature Correlation for Mixtures of California Oils and Gases." *Drilling and Production Practices*, API.
- Valko, P.P. and McCain, W.D. (2003). "Reservoir Oil Bubblepoint Pressures Revisited; Solution Gas-Oil Ratios and Surface Gas Specific Gravities." *Journal of Petroleum Science and Engineering*, Vol. 37, Issues 3-4, pp. 153-169. DOI: 10.1016/S0920-4105(02)00319-4.
- Velarde, J., Blasingame, T.A., and McCain, W.D. (1997). "Correlation of Black Oil Properties at Pressures Below Bubble Point Pressure." *SPE Annual Technical Conference and Exhibition*. (Note: Based on Velarde's 1996 Master's thesis at Texas A&M University).
- McCain, W.D., Spivey, J.P., and Lenn, C.P. (2011). *Petroleum Reservoir Fluid Property Correlations*. PennWell Books.

#### 14.1.2 Gas PVT Correlations

- Dranchuk, P.M. and Abou-Kassem, J.H. (1975). "Calculation of Z Factors for Natural Gases Using Equations of State." *Journal of Canadian Petroleum Technology*.
- Hall, K.R. and Yarborough, L. (1973). "A New Equation of State for Z-Factor Calculations." *Oil and Gas Journal*.
- Wang, X., Ye, F., and Wu, K. (2021). "A New Correlation for Calculating Gas Compressibility Factor." *Energy Reports*, Vol. 8, Supplement 2, pp. 130-137. DOI: 10.1016/j.egyr.2021.11.029.
- Burgoyne, M.W. (Santos Ltd), Nielsen, M.H., and Stanko, M. (Whitson AS) (2025). "A Universal, EOS-Based Correlation for Z-Factor, Viscosity and Enthalpy for Hydrocarbon and H<sub>2</sub>, N<sub>2</sub>, CO<sub>2</sub>, H<sub>2</sub>S Gas Mixtures." *SPE Paper 229932-MS*. Presented at ADIPEC, Abu Dhabi, UAE, 3-6 November 2025. Supports high concentrations of non-hydrocarbons including 100% CO<sub>2</sub> and H<sub>2</sub>.
- Lee, A.L., Gonzalez, M.H., and Eakin, B.E. (1966). "The Viscosity of Natural Gases." *Journal of Petroleum Technology*.
- Piper, L.D., McCain, W.D., and Corredor, J.H. (1993). "Compressibility Factors for Naturally Occurring Petroleum Gases." *SPE Annual Technical Conference and Exhibition*, SPE-26668-MS, Houston, Texas, October 1993.
- Sutton, R.P. (1985). "Compressibility Factors for High-Molecular-Weight Reservoir Gases." *SPE Annual Technical Conference*.

#### 14.1.3 Well Performance

- Darcy, H. (1856). *Les Fontaines Publiques de la Ville de Dijon*. Victor Dalmont.
- Vogel, J.V. (1968). "Inflow Performance Relationships for Solution-Gas Drive Wells." *Journal of Petroleum Technology*.
- Standing, M.B. (1971). "Concerning the Calculation of Inflow Performance of Wells Producing from Solution Gas Drive Reservoirs." *Journal of Petroleum Technology*.

#### 14.1.4 Relative Permeability

- Corey, A.T. (1954). "The Interrelation Between Gas and Oil Relative Permeabilities." *Production Monthly*, Vol. 19, pp. 38-41.
- Lomeland, F., Ebeltoft, E., and Thomas, W.H. (2005). "A New Versatile Relative Permeability Correlation." *International Symposium of the Society of Core Analysts*.

#### 14.1.5 Brine Properties

- McCain, W.D. (2011). *Petroleum Reservoir Fluid Property Correlations*. PennWell Books, Chapter 4.
- Spycher, N. and Pruess, K. (2010). "A Phase-Partitioning Model for CO<sub>2</sub>-Brine Mixtures at Elevated Temperatures and Pressures: Application to CO<sub>2</sub>-Enhanced Geothermal Systems." *Transport in Porous Media*, Vol. 82, pp. 173-196. DOI: 10.1007/s11242-009-9425-y.
- Garcia, J.E. (2001). "Density of Aqueous Solutions of CO<sub>2</sub>." LBNL Report #49023, October 2001. Also published in *Fluid Phase Equilibria*.
- Mao, S. and Duan, Z. (2009). "The Viscosity of Aqueous Alkali-Chloride Solutions up to 623 K, 1,000 bar, and High Ionic Strength." *Chemical Geology*.
- Islam, A.W. and Carlson, E.S. (2012). "Viscosity Models and Effects of Dissolved CO<sub>2</sub>." *Energy & Fuels*, Vol. 26, No. 8, pp. 5330-5336. DOI: 10.1021/ef3006228.

#### 14.1.6 Reservoir Heterogeneity

- Dykstra, H. and Parsons, R.L. (1950). "The Prediction of Oil Recovery by Waterflood." *Secondary Recovery of Oil in the United States*. API.
- Schmalz, J.P. and Rahme, H.D. (1950). "The Variation of Waterflood Performance with Variation in Permeability Profile." *Producers Monthly*.
- Lake, L.W. (1989). *Enhanced Oil Recovery*. Prentice Hall.

### 14.2 Software and Tools

- Burgoyne, M.W. (2024). *pyResToolbox: A Collection of Reservoir Engineering Utilities*. GitHub: <https://github.com/mwburgoyne/pyResToolbox>
- Anthropic (2024). *Model Context Protocol*. <https://modelcontextprotocol.io/>
- Serrao, G. (2024). *pyResToolbox MCP Server*. GitHub: <https://github.com/gabriel-serrao/pyrestoolbox-mcp>

## 15 Appendix: Nomenclature

### 15.1 Primary Symbols

Symbol	Units	Description
API	degrees	Oil API gravity
$B_o$	rb/stb	Oil formation volume factor
$c_o$	1/psi	Oil compressibility
$\mu_o$	cP	Oil viscosity
$\rho_o$	lb/ft <sup>3</sup>	Oil density
$R_s$	scf/stb	Solution gas-oil ratio
$R_{sb}$	scf/stb	Solution GOR at bubble point
$P_b$	psia	Bubble point pressure
$\gamma_o$	-	Oil specific gravity (water=1)
$B_g$	rcf/scf	Gas formation volume factor
$c_g$	1/psi	Gas compressibility
$\mu_g$	cP	Gas viscosity
$\rho_g$	lb/ft <sup>3</sup>	Gas density
$Z$	-	Gas compressibility factor (Z-factor)
$\gamma_g$	-	Gas specific gravity (air=1)
$P_c$	psia	Pseudo-critical pressure
$T_c$	°R	Pseudo-critical temperature
$P_{pr}$	-	Pseudo-reduced pressure
$T_{pr}$	-	Pseudo-reduced temperature
$\psi$	psia <sup>2</sup> /cP	Gas pseudopressure
$B_w$	rb/stb	Water/brine formation volume factor
$c_w$	1/psi	Brine compressibility
$\mu_w$	cP	Brine viscosity
$\rho_w$	lb/ft <sup>3</sup>	Brine density
$R_w$	scf/stb	Gas solubility in brine
$w_t$	wt%	Salinity (weight percent NaCl)
$k$	mD	Permeability
$h$	ft	Pay thickness (net)
$\phi$	fraction	Porosity
$S_w$	fraction	Water saturation
$S_o$	fraction	Oil saturation
$S_g$	fraction	Gas saturation
$S_{wc}$	fraction	Connate water saturation
$S_{or}$	fraction	Residual oil saturation
$P$	psia	Pressure
$T$	°F	Temperature
$P_i$	psia	Initial/reservoir pressure
$P_{wf}$	psia	Wellbore flowing pressure
$q_o$	STB/day	Oil production rate
$q_g$	MSCF/day	Gas production rate
$r_e$	ft	Drainage radius
$r_w$	ft	Wellbore radius
$S$	-	Skin factor

Symbol	Units	Description
$L$	ft	Horizontal well length
$k_{rw}$	-	Water relative permeability
$k_{ro}$	-	Oil relative permeability
$k_{rg}$	-	Gas relative permeability
$S^*$	-	Normalized saturation
$L$	-	Lorenz coefficient
$\beta$	-	Dykstra-Parsons coefficient
$y_{CO_2}$	fraction	CO <sub>2</sub> mole fraction
$y_{H_2S}$	fraction	H <sub>2</sub> S mole fraction
$y_{N_2}$	fraction	N <sub>2</sub> mole fraction

Table 10: Nomenclature - Primary Symbols

## 15.2 Subscripts

Subscript	Meaning
$o$	Oil phase
$g$	Gas phase
$w$	Water/brine phase
$b$	At bubble point
$i$	Initial conditions
$wf$	Wellbore flowing
$c$	Critical or connate
$r$	Relative or residual
$pr$	Pseudo-reduced
$D$	Dimensionless
$sc$	Standard conditions
$ST$	Stock tank conditions
$sp$	Separator conditions

Table 11: Common Subscripts

## 16 Index of Formulas

### 16.1 By Property

#### Oil Properties

- Bubble Point Pressure ( $P_b$ ): Standing (p.4), Valko-McCain (p.4), Velarde (p.4)
- Solution GOR ( $R_s$ ): Standing (p.5), Valko-McCain, Velarde
- Formation Volume Factor ( $B_o$ ): McCain (p.6), Standing (p.6)
- Viscosity ( $\mu_o$ ): Beggs-Robinson (p.7)
- Density ( $\rho_o$ ): SWMH (p.7)
- Compressibility ( $c_o$ ): Explicit method (p.8)
- API-SG Conversions (p.8)

#### Gas Properties

- Z-Factor: DAK (p.9), Hall-Yarborough (p.10)
- Critical Properties: PMC (p.10), Sutton, BUR
- Formation Volume Factor ( $B_g$ ): Real gas equation (p.11)
- Viscosity ( $\mu_g$ ): Lee-Gonzalez-Eakin (p.11)
- Density ( $\rho_g$ ): Ideal gas law corrected (p.11)
- Compressibility ( $c_g$ ): From Z-factor (p.12)
- Pseudopressure ( $\psi$ ): Integral formulation (p.12)

#### Well Performance

- Oil Rate - Radial: Darcy's law (p.13), Vogel IPR (p.13)
- Oil Rate - Linear: Darcy's law (p.14)
- Gas Rate - Radial: Pseudopressure formulation (p.14)
- Gas Rate - Linear: Pseudopressure formulation (p.14)

#### Relative Permeability

- Corey Correlation: Normalized saturation (p.15), Kr functions (p.15)
- LET Correlation: Three-parameter model (p.16)

#### Brine Properties

- Density ( $\rho_w$ ): Pressure-temperature-salinity (p.17)
- Viscosity ( $\mu_w$ ): Salinity correction (p.17)
- Compressibility ( $c_w$ ): From FVF derivative (p.18)

- Formation Volume Factor ( $B_w$ ): Three-effect model (p.18)
- Gas Solubility ( $R_w$ ): Henry's Law (p.18)

### Heterogeneity

- Lorenz Coefficient: Integral formulation (p.19)
- Dykstra-Parsons Coefficient: Percentile definition (p.19)
- Lorenz-Beta Conversion: Approximate relations (p.20)
- Layer Distribution: Log-normal model (p.20)

### Other

- Van Everdingen-Hurst Aquifer: Water influx (p.21)
- Rachford-Rice Flash: Phase equilibrium (p.22)

---

## End of Formula Reference Guide

**Compiled by:** Gabriel Serrão Seabra

For the latest version and updates, visit:

<https://github.com/gabrielserrao/pyrestoolbox-mcp>

**Built on pyResToolbox:**

Original library by Mark W. Burgoyne

<https://github.com/mwburgoyne/pyResToolbox>

*Remember: Always verify formulas with original sources before professional use.*

---