

pyResToolbox MCP

Formula Reference Guide

Quick Reference for Reservoir Engineering Calculations

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November 20, 2025

Version 1.0

Abstract

This document provides a comprehensive reference guide for all calculation tools available in the pyResToolbox Model Context Protocol (MCP) server. It includes mathematical formulas, symbol definitions, unit systems, and correlation methods for 47 production-ready tools covering oil PVT, gas PVT, well performance, simulation support, brine properties, and reservoir heterogeneity analysis. All calculations use Field Units (US Oilfield standard).

Based on pyResToolbox: This MCP server is built upon the excellent *pyResToolbox* library by Mark W. Burgoyne (<https://github.com/mwburgoyne/pyResToolbox>), which provides the underlying reservoir engineering calculations.

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1 Introduction

1.1 About pyResToolbox MCP

pyResToolbox MCP is a Model Context Protocol server that provides AI agents like Claude with access to industry-standard petroleum engineering calculations. Built on the comprehensive pyResToolbox library by Mark Burgoyne, it offers 47 production-ready tools for reservoir engineering workflows.

1.2 Unit System

All calculations use **Field Units (US Oilfield standard)**:

Property	Unit	Example
Pressure	psia	3000 psia
Temperature	°F	180°F
Permeability	mD	100 mD
Pay Thickness	ft	50 ft
Viscosity	cP	0.85 cP
Oil Rate	STB/day	542 STB/day
Gas Rate	MSCF/day	1250 MSCF/day
Oil Gravity	API° or SG	35° API
Gas Gravity	SG (air=1)	0.75
Solution GOR	scf/stb	800 scf/stb
Oil FVF	rb/stb	1.25 rb/stb
Gas FVF	rcf/scf	0.0045 rcf/scf
Compressibility	1/psi	1.2×10^{-5} 1/psi
Density	lb/ft ³	42.5 lb/ft ³

Table 1: Field Units Used in All Calculations

2 Oil PVT Calculations

2.1 Bubble Point Pressure (P_b)

2.1.1 Description

The bubble point pressure is the pressure at which the first gas bubble evolves from solution oil. It is a critical PVT property that defines the boundary between undersaturated (single-phase) and saturated (two-phase) oil behavior.

2.1.2 Available Methods

1. Standing (1947) - STAN

$$P_b = 18.2 \left[\left(\frac{R_{sb}}{\gamma_g} \right)^{0.83} \times 10^a - 1.4 \right] \quad (1)$$

where:

$$a = 0.00091 \times T - 0.0125 \times \text{API} \quad (2)$$

Symbol Definitions:

- P_b : Bubble point pressure (psia)
- R_{sb} : Solution GOR at bubble point (scf/stb)
- γ_g : Gas specific gravity (air=1)
- T : Temperature (°F)
- **API**: Oil API gravity (degrees)

2. Valko-McCain (2003) - VALMC

$$P_b = -C_1 - C_2 \times A - C_3 \times A^2 \quad (3)$$

where:

$$A = \ln \left(\frac{R_{sb}}{\gamma_{sp}} \right) \quad (4)$$

$$C_1 = 7.916 \times 10^{-4} \times \text{API}^{1.541} - 4.561 \times 10^{-5} \times T^{1.3911} \quad (5)$$

$$C_2 = 4.51 \times 10^{-5} \times \text{API}^{1.3911} \times T^{0.7849} \quad (6)$$

$$C_3 = 1.046 \times 10^{-7} \times \text{API}^{1.3911} \times T^{1.007} \quad (7)$$

Additional Symbols:

- γ_{sp} : Separator gas specific gravity (air=1)
- C_1, C_2, C_3 : Correlation coefficients

3. Velarde-Blasingame-McCain (1997) - VELAR

$$\ln(P_b) = a_0 + a_1 \ln(R_{sb}) + a_2 [\ln(R_{sb})]^2 + a_3 \ln(\gamma_{sp}) + a_4 \ln(\text{API}) + a_5 \ln(T + 460) \quad (8)$$

Coefficients a_0 through a_5 are empirically determined from regression analysis.

2.2 Solution Gas-Oil Ratio (R_s)

2.2.1 Description

The solution gas-oil ratio represents the volume of gas dissolved in oil at a given pressure and temperature. It increases with pressure up to the bubble point, then remains constant (equal to R_{sb}) above the bubble point.

2.2.2 Standing (1947) Method

$$R_s = \gamma_g \left[\frac{P}{18.2} + 1.4 \right] \times 10^{-a} \quad (9)$$

where:

$$a = 0.0125 \times \text{API} - 0.00091 \times T \quad (10)$$

Symbol Definitions:

- R_s : Solution gas-oil ratio (scf/stb)
- P : Pressure (psia)
- γ_g : Gas specific gravity (air=1)
- API : Oil API gravity (degrees)
- T : Temperature (°F)

Behavior:

- $P < P_b$: R_s calculated from correlation
- $P \geq P_b$: $R_s = R_{sb}$ (constant)

2.3 Oil Formation Volume Factor (B_o)

2.3.1 Description

The formation volume factor relates the volume of oil at reservoir conditions to its volume at stock tank conditions. It accounts for thermal expansion and gas in solution.

2.3.2 McCain et al. (1988) Method - MCAIN

$$B_o = \frac{\rho_{ST}}{\rho_o} \quad (11)$$

where oil density ρ_o is calculated from:

$$\rho_o = \frac{\rho_{ST} + 0.01357 \times R_s \times \gamma_g}{0.972 + 0.000147 \times (T + 460)^{1.175}} \quad (12)$$

Symbol Definitions:

- B_o : Oil formation volume factor (rb/stb)
- ρ_o : Oil density at reservoir conditions (lb/ft³)
- ρ_{ST} : Oil density at stock tank conditions (lb/ft³)
- R_s : Solution gas-oil ratio (scf/stb)
- γ_g : Gas specific gravity (air=1)
- T : Temperature (°F)

2.3.3 Standing (1947) Method - STAN

$$B_o = 0.9759 + 0.00012 \left[R_s \sqrt{\frac{\gamma_g}{\gamma_o}} + 1.25T \right]^{1.2} \quad (13)$$

Additional Symbols:

- γ_o : Oil specific gravity (water=1)

2.4 Oil Viscosity (μ_o)**2.4.1 Description**

Oil viscosity is a measure of the oil's resistance to flow. It decreases with increasing temperature and decreasing pressure (above bubble point).

2.4.2 Beggs-Robinson (1975) Method - BR**Dead Oil Viscosity:**

$$\mu_{od} = 10^X - 1 \quad (14)$$

where:

$$X = T^{-1.163} \times \exp(6.9824 - 0.04658 \times \text{API}) \quad (15)$$

Live Oil Viscosity:

$$\mu_o = A \times \mu_{od}^B \quad (16)$$

where:

$$A = 10.715 \times (R_s + 100)^{-0.515} \quad (17)$$

$$B = 5.44 \times (R_s + 150)^{-0.338} \quad (18)$$

Symbol Definitions:

- μ_o : Oil viscosity (cP)
- μ_{od} : Dead oil viscosity (cP)

- R_s : Solution gas-oil ratio (scf/stb)
- T : Temperature (°F)
- **API**: Oil API gravity (degrees)

2.5 Oil Density (ρ_o)

2.5.1 Description

Oil density at reservoir conditions accounts for dissolved gas and thermal expansion effects.

2.5.2 Standing-White-McCain-Hill (1995) Method - SWMH

$$\rho_o = \frac{62.4 \times \gamma_o + 0.0136 \times R_s \times \gamma_g}{B_o} \quad (19)$$

Symbol Definitions:

- ρ_o : Oil density (lb/ft³)
- γ_o : Oil specific gravity (water=1)
- γ_g : Gas specific gravity (air=1)
- R_s : Solution gas-oil ratio (scf/stb)
- B_o : Oil formation volume factor (rb/stb)

2.6 Oil Compressibility (c_o)

2.6.1 Description

Oil compressibility describes the fractional change in oil volume with pressure. It is critical for material balance calculations and pressure transient analysis.

2.6.2 Explicit Method - EXPLT

$$c_o = -\frac{1}{B_o} \left[\frac{dB_o}{dP} - \frac{B_g}{5.61458} \frac{dR_s}{dP} \right] \quad (20)$$

Symbol Definitions:

- c_o : Oil compressibility (1/psi)
- B_o : Oil formation volume factor (rb/stb)
- B_g : Gas formation volume factor (rcf/scf)
- R_s : Solution gas-oil ratio (scf/stb)
- P : Pressure (psia)

Note: Derivatives are calculated numerically using finite differences.

2.7 API-Specific Gravity Conversions

2.7.1 API to Specific Gravity

$$\gamma_o = \frac{141.5}{\text{API} + 131.5} \quad (21)$$

2.7.2 Specific Gravity to API

$$\text{API} = \frac{141.5}{\gamma_o} - 131.5 \quad (22)$$

Symbol Definitions:

- **API:** Oil API gravity (degrees)
- γ_o : Oil specific gravity (water=1)

3 Gas PVT Calculations

3.1 Gas Z-Factor (Compressibility Factor)

3.1.1 Description

The Z-factor corrects the ideal gas law for real gas behavior. It is defined as:

$$PV = ZnRT \quad (23)$$

where $Z = 1$ for ideal gas, $Z < 1$ for most real gases at reservoir conditions.

3.1.2 Dranchuk-Abou-Kassem (1975) Method - DAK

$$Z = 1 + A_1\rho_r + A_2\rho_r^2 + A_3\rho_r^5 + A_4\rho_r^2(1 + A_5\rho_r^2)\exp(-A_5\rho_r^2) \quad (24)$$

$$+ \frac{A_6 + A_7\rho_r + A_8\rho_r^2}{T_{pr}^3}\rho_r^2 \quad (25)$$

where reduced density ρ_r is solved iteratively from:

$$\rho_r = \frac{0.27P_{pr}}{ZT_{pr}} \quad (26)$$

Symbol Definitions:

- Z : Gas compressibility factor (dimensionless)
- ρ_r : Reduced density (dimensionless)
- P_{pr} : Pseudo-reduced pressure = P/P_c
- T_{pr} : Pseudo-reduced temperature = $(T + 460)/T_c$
- P_c : Pseudo-critical pressure (psia)
- T_c : Pseudo-critical temperature ($^{\circ}\text{R}$)
- A_1, \dots, A_8 : Correlation constants

3.1.3 Hall-Yarborough (1973) Method - HY

Implicit equation for reduced density y :

$$\frac{0.06125P_{pr}t}{y}\exp[-1.2(1-t)^2] = F(y) \quad (27)$$

where:

$$F(y) = -A_1 + A_2/y + A_3/y^2 + A_4/y^3 + A_5/y^4 + y^2(A_6 + A_7/y + A_8/y^2)(1 + A_9y^2)\exp(-A_9y^2) \quad (28)$$

Then Z is calculated from:

$$Z = \frac{A_1P_{pr}}{y} \quad (29)$$

where $t = 1/T_{pr}$ and A_1, \dots, A_9 are correlation constants.

3.1.4 Burgoyne-Nielsen-Stanko (2025) Method - BUR

Universal EOS-based correlation for Z-factor, viscosity, and enthalpy. This is the most recent and comprehensive method, developed specifically to handle:

- High concentrations of non-hydrocarbons (CO₂, H₂S, N₂, H₂)
- Pure non-hydrocarbon streams (100% CO₂, 100% H₂)
- Hydrogen mixtures (only method supporting H₂)
- Full range of P-T conditions

Based on a tuned 5-component Peng-Robinson EOS model. Formulation details are proprietary, but the correlation is implemented in pyResToolbox for practical use.

Reference: SPE-229932-MS (ADIPEC 2025)

Method Comparison:

- **DAK:** Best for hydrocarbon gases with low non-HC content
- **HY:** Fast alternative for standard conditions
- **WYW:** Modern update to classical methods
- **BUR:** Universal method, required for H₂ or high non-HC content

3.2 Pseudo-Critical Properties

3.2.1 Description

Pseudo-critical properties (temperature and pressure) are used to calculate the reduced properties needed for Z-factor correlations.

3.2.2 Piper-McCain-Corredor (1993) Method - PMC

Without Non-Hydrocarbons:

$$T_c = 169.2 + 349.5\gamma_g - 74.0\gamma_g^2 \quad (^\circ\text{R}) \quad (30)$$

$$P_c = 756.8 - 131.07\gamma_g - 3.6\gamma_g^2 \quad (\text{psia}) \quad (31)$$

With CO₂ and H₂S Corrections:

$$T'_c = T_c - \epsilon_T \quad (32)$$

$$P'_c = \frac{P_c - \epsilon_P}{1 - y_{\text{CO}_2} - y_{\text{H}_2\text{S}}} \quad (33)$$

where:

$$\epsilon_T = 120(y_{\text{CO}_2}^{0.9} - y_{\text{CO}_2}^{1.6}) + 15(y_{\text{H}_2\text{S}}^{0.5} - y_{\text{H}_2\text{S}}^4) \quad (34)$$

$$\epsilon_P = 440y_{\text{CO}_2} + 600y_{\text{H}_2\text{S}} - 170y_{\text{CO}_2}y_{\text{H}_2\text{S}} \quad (35)$$

Symbol Definitions:

- T_c : Pseudo-critical temperature (°R)
- P_c : Pseudo-critical pressure (psia)
- γ_g : Gas specific gravity (air=1)
- y_{CO_2} : CO₂ mole fraction
- y_{H_2S} : H₂S mole fraction
- y_{N_2} : N₂ mole fraction
- ϵ_T : Temperature correction
- ϵ_P : Pressure correction

3.3 Gas Formation Volume Factor (B_g)

3.3.1 Description

The gas formation volume factor relates gas volume at reservoir conditions to its volume at standard conditions.

$$B_g = \frac{0.02827 \times Z \times (T + 460)}{P} \quad (\text{rcf/scf}) \quad (36)$$

Symbol Definitions:

- B_g : Gas formation volume factor (rcf/scf)
- Z : Gas compressibility factor (dimensionless)
- T : Temperature (°F)
- P : Pressure (psia)

3.4 Gas Viscosity (μ_g)

3.4.1 Description

Gas viscosity is required for flow calculations and increases with pressure and temperature.

3.4.2 Lee-Gonzalez-Eakin (1966) Method - LGE

$$\mu_g = K \times 10^{-4} \times \exp [X \times \rho_g^Y] \quad (37)$$

where:

$$K = \frac{(9.4 + 0.02M)(T + 460)^{1.5}}{209 + 19M + (T + 460)} \quad (38)$$

$$X = 3.5 + \frac{986}{T + 460} + 0.01M \quad (39)$$

$$Y = 2.4 - 0.2X \quad (40)$$

$$M = 28.97\gamma_g \quad (41)$$

Symbol Definitions:

- μ_g : Gas viscosity (cP)
- ρ_g : Gas density (lb/ft³)
- M : Gas molecular weight (lb/lbmol)
- γ_g : Gas specific gravity (air=1)
- T : Temperature (°F)

3.5 Gas Density (ρ_g)

$$\rho_g = \frac{P \times 28.97 \times \gamma_g}{Z \times 10.73 \times (T + 460)} \quad (\text{lb/ft}^3) \quad (42)$$

Symbol Definitions:

- ρ_g : Gas density (lb/ft³)
- P : Pressure (psia)
- γ_g : Gas specific gravity (air=1)
- Z : Gas compressibility factor (dimensionless)
- T : Temperature (°F)

3.6 Gas Compressibility (c_g)

3.6.1 Description

Gas compressibility describes the fractional change in gas volume with pressure.

$$c_g = \frac{1}{P} - \frac{1}{Z} \frac{dZ}{dP} \quad (43)$$

Symbol Definitions:

- c_g : Gas compressibility (1/psi)
- P : Pressure (psia)
- Z : Gas compressibility factor (dimensionless)

3.7 Gas Pseudopressure (ψ)

3.7.1 Description

Gas pseudopressure (or real gas potential) linearizes the gas diffusivity equation and is used in well test analysis.

$$\psi(P) = 2 \int_{P_0}^P \frac{P'}{\mu_g Z} dP' \quad (\text{psia}^2/\text{cP}) \quad (44)$$

Symbol Definitions:

- ψ : Gas pseudopressure (psia^2/cP)
- P : Pressure (psia)
- P_0 : Reference pressure (usually 0 psia)
- μ_g : Gas viscosity (cP)
- Z : Gas compressibility factor (dimensionless)

Note: Integral is evaluated numerically using trapezoidal rule or Simpson's rule.

4 Inflow Performance (Well Productivity)

4.1 Oil Rate - Radial Flow (Vertical Wells)

4.1.1 Description

Calculates oil production rate for vertical wells with radial flow geometry using Darcy's law for steady-state or pseudo-steady-state flow.

4.1.2 Darcy's Law - Undersaturated Reservoir

$$q_o = \frac{0.00708 \times k \times h \times (P_i - P_{wf})}{\mu_o \times B_o \times \left[\ln \left(\frac{r_e}{r_w} \right) - 0.75 + S \right]} \quad (\text{STB/day}) \quad (45)$$

Symbol Definitions:

- q_o : Oil production rate (STB/day)
- k : Permeability (mD)
- h : Net pay thickness (ft)
- P_i : Initial/reservoir pressure (psia)
- P_{wf} : Wellbore flowing pressure (psia)
- μ_o : Oil viscosity (cP)
- B_o : Oil formation volume factor (rb/stb)
- r_e : Drainage radius (ft)
- r_w : Wellbore radius (ft)
- S : Skin factor (dimensionless)

4.1.3 Vogel IPR - Saturated Reservoir

For saturated reservoirs ($P_i < P_b$), use Vogel's correlation:

$$\frac{q_o}{q_{o,max}} = 1 - 0.2 \left(\frac{P_{wf}}{P_i} \right) - 0.8 \left(\frac{P_{wf}}{P_i} \right)^2 \quad (46)$$

where maximum rate is:

$$q_{o,max} = q_o(P_{wf} = 0) \quad (47)$$

Additional Symbols:

- $q_{o,max}$: Maximum oil rate at zero bottomhole pressure (STB/day)
- P_b : Bubble point pressure (psia)

4.2 Oil Rate - Linear Flow (Horizontal Wells)

4.2.1 Description

Calculates oil production rate for horizontal wells or linear flow geometry.

$$q_o = \frac{0.00708 \times k \times h \times L \times (P_i - P_{wf})}{\mu_o \times B_o \times \left[\frac{r_e}{2} + S\right]} \quad (\text{STB/day}) \quad (48)$$

Additional Symbols:

- L : Horizontal well length (ft)

4.3 Gas Rate - Radial Flow (Vertical Wells)

4.3.1 Description

Calculates gas production rate for vertical wells using pseudopressure formulation.

$$q_g = \frac{0.00708 \times k \times h \times [\psi(P_i) - \psi(P_{wf})]}{\left[\ln\left(\frac{r_e}{r_w}\right) - 0.75 + S\right]} \quad (\text{MSCF/day}) \quad (49)$$

Symbol Definitions:

- q_g : Gas production rate (MSCF/day)
- $\psi(P)$: Gas pseudopressure (psia²/cP)
- k : Permeability (mD)
- h : Net pay thickness (ft)
- P_i : Reservoir pressure (psia)
- P_{wf} : Wellbore flowing pressure (psia)
- r_e : Drainage radius (ft)
- r_w : Wellbore radius (ft)
- S : Skin factor (dimensionless)

4.4 Gas Rate - Linear Flow (Horizontal Wells)

$$q_g = \frac{0.00708 \times k \times h \times L \times [\psi(P_i) - \psi(P_{wf})]}{\left[\frac{r_e}{2} + S\right]} \quad (\text{MSCF/day}) \quad (50)$$

Additional Symbols:

- L : Horizontal well length (ft)

5 Relative Permeability Correlations

5.1 Corey (1954) Correlation

5.1.1 Description

Simple power-law model for relative permeability as a function of normalized saturation.

5.1.2 Normalized Saturation

Water Phase:

$$S_w^* = \frac{S_w - S_{wc}}{1 - S_{wc} - S_{or}} \quad (51)$$

Oil Phase (Water-Oil):

$$S_o^* = \frac{S_o - S_{or}}{1 - S_{wc} - S_{or}} \quad (52)$$

Gas Phase:

$$S_g^* = \frac{S_g - S_{gc}}{1 - S_{wc} - S_{org}} \quad (53)$$

Symbol Definitions:

- S_w^* : Normalized water saturation
- S_o^* : Normalized oil saturation
- S_g^* : Normalized gas saturation
- S_w : Water saturation
- S_o : Oil saturation
- S_g : Gas saturation
- S_{wc} : Connate water saturation
- S_{or} : Residual oil saturation (to water)
- S_{org} : Residual oil saturation (to gas)
- S_{gc} : Critical gas saturation

5.1.3 Relative Permeability Functions

Water Relative Permeability:

$$k_{rw} = k_{rw}^{max} \times (S_w^*)^{n_w} \quad (54)$$

Oil Relative Permeability (to water):

$$k_{row} = k_{row}^{max} \times (1 - S_w^*)^{n_o} \quad (55)$$

Gas Relative Permeability:

$$k_{rg} = k_{rg}^{max} \times (S_g^*)^{n_g} \quad (56)$$

Oil Relative Permeability (to gas):

$$k_{rog} = k_{rog}^{max} \times (1 - S_g^*)^{n_o} \quad (57)$$

Additional Symbols:

- k_{rw} : Water relative permeability
- k_{row} : Oil relative permeability (to water)
- k_{rg} : Gas relative permeability
- k_{rog} : Oil relative permeability (to gas)
- k_{rw}^{max} : Maximum water relative permeability
- k_{row}^{max} : Maximum oil relative permeability
- k_{rg}^{max} : Maximum gas relative permeability
- n_w : Corey exponent for water
- n_o : Corey exponent for oil
- n_g : Corey exponent for gas

Typical Values:

- n_w : 1.5 - 3.0
- n_o : 2.0 - 4.0
- n_g : 2.0 - 3.5

5.2 LET Correlation (Lomeland-Ebeltoft-Thomas 2005)

5.2.1 Description

Flexible three-parameter model (L, E, T) that can fit complex relative permeability curves.

Water Relative Permeability:

$$k_{rw} = k_{rw}^{max} \times \frac{(S_w^*)^{L_w}}{(S_w^*)^{L_w} + E_w(1 - S_w^*)^{T_w}} \quad (58)$$

Oil Relative Permeability:

$$k_{ro} = k_{ro}^{max} \times \frac{(1 - S_w^*)^{L_o}}{(1 - S_w^*)^{L_o} + E_o(S_w^*)^{T_o}} \quad (59)$$

Gas Relative Permeability:

$$k_{rg} = k_{rg}^{max} \times \frac{(S_g^*)^{L_g}}{(S_g^*)^{L_g} + E_g(1 - S_g^*)^{T_g}} \quad (60)$$

Symbol Definitions:

- L_w, L_o, L_g : Low saturation parameters (controls curve near $S^* = 0$)
- E_w, E_o, E_g : Elevation parameters (controls height/position)
- T_w, T_o, T_g : Top saturation parameters (controls curve near $S^* = 1$)

Typical Ranges:

- L : 1.0 - 3.0
- E : 1.0 - 2.0
- T : 1.0 - 3.0

Advantages over Corey:

- More flexible curve shapes
- Better fitting to experimental data
- Independent control of endpoint behavior
- Smooth transitions

6 Brine Properties

6.1 Brine Density (ρ_w)

6.1.1 Description

Brine density depends on pressure, temperature, and salinity (NaCl concentration).

Pure Water Density:

$$\rho_{w,pure} = 62.368 + 0.438603 \times 10^{-3}P + f(T) \quad (61)$$

Brine Density with Salinity:

$$\rho_w = \rho_{w,pure} + \Delta\rho_{salt}(w_t) \quad (62)$$

where salinity correction is:

$$\Delta\rho_{salt} = w_t \times (a_0 + a_1T + a_2P) \quad (63)$$

Symbol Definitions:

- ρ_w : Brine density (lb/ft³)
- $\rho_{w,pure}$: Pure water density (lb/ft³)
- P : Pressure (psia)
- T : Temperature (°F)
- w_t : Salinity (wt% NaCl)
- a_0, a_1, a_2 : Correlation coefficients

6.2 Brine Viscosity (μ_w)

6.2.1 Description

Brine viscosity decreases with temperature and increases with pressure and salinity.

$$\mu_w = \mu_{w,pure} \times [1 + A \times w_t + B \times w_t^2] \quad (64)$$

where pure water viscosity is:

$$\mu_{w,pure} = a \times 10^{b/(T+c)} \quad (65)$$

Symbol Definitions:

- μ_w : Brine viscosity (cP)
- $\mu_{w,pure}$: Pure water viscosity (cP)
- w_t : Salinity (wt% NaCl)
- T : Temperature (°F)
- A, B, a, b, c : Correlation coefficients

6.3 Brine Compressibility (c_w)

6.3.1 Description

Brine compressibility is the fractional change in volume with pressure.

$$c_w = \frac{1}{B_w} \frac{dB_w}{dP} \quad (1/\text{psi}) \quad (66)$$

Empirical Correlation:

$$c_w = (c_1 + c_2T + c_3T^2)(1 + c_4w_t) \quad (67)$$

Symbol Definitions:

- c_w : Brine compressibility (1/psi)
- B_w : Water formation volume factor (rb/stb)
- T : Temperature (°F)
- w_t : Salinity (wt% NaCl)
- c_1, c_2, c_3, c_4 : Correlation coefficients

6.4 Brine Formation Volume Factor (B_w)

$$B_w = (1 + \Delta V_T)(1 + \Delta V_P)(1 + \Delta V_s) \quad (68)$$

where:

$$\Delta V_T = -1.0001 \times 10^{-2} + 1.33391 \times 10^{-4}T + 5.50654 \times 10^{-7}T^2 \quad (69)$$

$$\Delta V_P = -1.95301 \times 10^{-9}PT - 1.72834 \times 10^{-13}P^2T - 3.58922 \times 10^{-7}P \quad (70)$$

$$\Delta V_s = -w_t(2.65 \times 10^{-4} - 1.878 \times 10^{-6}w_t) \quad (71)$$

Symbol Definitions:

- B_w : Water formation volume factor (rb/stb)
- ΔV_T : Thermal expansion effect
- ΔV_P : Pressure effect
- ΔV_s : Salinity effect
- P : Pressure (psia)
- T : Temperature (°F)
- w_t : Salinity (wt% NaCl)

6.5 Gas Solubility in Brine (R_w)

6.5.1 Description

Volume of gas (CH_4 or CO_2) dissolved in brine at reservoir conditions.

Methane Solubility:

$$R_w = A(T, P) \times (1 - \alpha \times w_t) \quad (\text{scf/stb}) \quad (72)$$

where $A(T, P)$ is calculated from Henry's Law with temperature and pressure dependence.

Symbol Definitions:

- R_w : Gas solubility in brine (scf/stb)
- $A(T, P)$: Solubility function of temperature and pressure
- α : Salinity correction factor
- w_t : Salinity (wt% NaCl)

7 Reservoir Heterogeneity

7.1 Lorenz Coefficient

7.1.1 Description

The Lorenz coefficient quantifies reservoir heterogeneity based on the cumulative flow capacity vs cumulative storage capacity curve. It ranges from 0 (homogeneous) to 1 (completely heterogeneous).

$$L = 2 \times \int_0^1 [F(\phi) - \phi] d\phi \quad (73)$$

where $F(\phi)$ is the Lorenz curve:

$$F(\phi) = \frac{\text{Cumulative Flow Capacity}}{\text{Total Flow Capacity}} \quad (74)$$

Symbol Definitions:

- L : Lorenz coefficient (0-1)
- $F(\phi)$: Lorenz curve function
- ϕ : Cumulative storage fraction

Interpretation:

- $L = 0$: Perfectly homogeneous (all layers have same kh)
- $L = 0.3$: Low heterogeneity
- $L = 0.5$: Moderate heterogeneity
- $L = 0.7$: High heterogeneity
- $L \rightarrow 1$: Extreme heterogeneity

7.2 Dykstra-Parsons Coefficient (β)

7.2.1 Description

The Dykstra-Parsons coefficient measures permeability variation assuming a log-normal distribution.

$$\beta = \frac{k_{50} - k_{84.1}}{k_{50}} \quad (75)$$

where:

- k_{50} is the median permeability (50th percentile)
- $k_{84.1}$ is the 84.1th percentile permeability (1 standard deviation below mean in log space)

Symbol Definitions:

- β : Dykstra-Parsons coefficient (0-1)
- k_{50} : Median permeability (mD)
- $k_{84.1}$: 84.1th percentile permeability (mD)

Interpretation:

- $\beta < 0.5$: Low variation (homogeneous)
- $\beta = 0.5 - 0.7$: Moderate variation
- $\beta > 0.7$: High variation (heterogeneous)

7.3 Lorenz-Beta Conversion**7.3.1 Description**

Conversion between Lorenz coefficient and Dykstra-Parsons beta parameter, assuming log-normal permeability distribution.

Beta to Lorenz:

$$L \approx 1 - \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \exp\left(-\frac{x^2}{2}\right) \times \exp(x\sigma) dx \quad (76)$$

where σ is related to β through:

$$\beta = 1 - \exp(-\sigma) \quad (77)$$

Approximate Conversion:

$$L \approx 0.632 \times \beta^{0.9} \quad (78)$$

Symbol Definitions:

- L : Lorenz coefficient
- β : Dykstra-Parsons coefficient
- σ : Standard deviation of $\ln(k)$

7.4 Layer Permeability Distribution**7.4.1 Description**

Generates permeability distribution for layered reservoirs based on Lorenz coefficient.

Log-Normal Distribution:

$$k_i = k_{avg} \times \exp \left[\sigma \times \Phi^{-1}(p_i) - \frac{\sigma^2}{2} \right] \quad (79)$$

where:

- k_i is permeability of layer i
- k_{avg} is average permeability
- Φ^{-1} is inverse standard normal CDF
- $p_i = (i - 0.5)/N$ is cumulative probability
- N is number of layers

Symbol Definitions:

- k_i : Layer permeability (mD)
- k_{avg} : Average permeability (mD)
- σ : Standard deviation of $\ln(k)$
- Φ^{-1} : Inverse cumulative normal distribution
- N : Number of layers

8 Aquifer Models

8.1 Van Everdingen-Hurst Model

8.1.1 Description

The Van Everdingen-Hurst model calculates water influx from an aquifer into a reservoir. It uses dimensionless influence functions based on the radial diffusivity equation.

Water Influx:

$$W_e(t) = B \times \sum_{j=1}^n \Delta P_j \times W_D(t_D - t_{D,j}) \quad (80)$$

where:

$$B = 1.119 \times \phi \times c_t \times h \times r_e^2 \quad (\text{rb/psi}) \quad (81)$$

Dimensionless Time:

$$t_D = \frac{0.000264 \times k \times t}{\phi \times \mu \times c_t \times r_e^2} \quad (82)$$

Dimensionless Radius:

$$r_D = \frac{r_{aq}}{r_e} \quad (83)$$

Symbol Definitions:

- W_e : Cumulative water influx (rb)
- B : Aquifer constant (rb/psi)
- ΔP_j : Pressure drop at time step j (psia)
- W_D : Dimensionless water influx function
- t_D : Dimensionless time
- ϕ : Aquifer porosity (fraction)
- c_t : Total compressibility (1/psi)
- h : Aquifer thickness (ft)
- r_e : Reservoir radius (ft)
- r_{aq} : Aquifer outer radius (ft)
- k : Aquifer permeability (mD)
- μ : Water viscosity (cP)
- t : Time (days)

8.2 Influence Functions

The dimensionless water influx $W_D(t_D)$ is tabulated for various dimensionless radius ratios r_D . For:

- Infinite aquifer: $r_D = \infty$
- Finite aquifer: $r_D = 2, 3, 5, 10, \text{etc.}$

9 Phase Behavior

9.1 Rachford-Rice Flash Calculation

9.1.1 Description

The Rachford-Rice equation is used to calculate vapor and liquid phase compositions and amounts for a multi-component mixture at specified temperature and pressure.

Rachford-Rice Equation:

$$\sum_{i=1}^n \frac{z_i(K_i - 1)}{1 + V(K_i - 1)} = 0 \quad (84)$$

where:

- V is vapor mole fraction (solve iteratively)
- $L = 1 - V$ is liquid mole fraction

Component Mole Fractions:

$$x_i = \frac{z_i}{1 + V(K_i - 1)} \quad (\text{liquid}) \quad (85)$$

$$y_i = \frac{K_i \times z_i}{1 + V(K_i - 1)} \quad (\text{vapor}) \quad (86)$$

Symbol Definitions:

- z_i : Overall mole fraction of component i
- x_i : Liquid phase mole fraction of component i
- y_i : Vapor phase mole fraction of component i
- K_i : Equilibrium K-value for component i ($K_i = y_i/x_i$)
- V : Vapor phase mole fraction
- L : Liquid phase mole fraction
- n : Number of components

Solution Method: Newton-Raphson iteration:

$$V^{n+1} = V^n - \frac{f(V^n)}{f'(V^n)} \quad (87)$$

where:

$$f(V) = \sum_{i=1}^n \frac{z_i(K_i - 1)}{1 + V(K_i - 1)} \quad (88)$$

$$f'(V) = - \sum_{i=1}^n \frac{z_i(K_i - 1)^2}{[1 + V(K_i - 1)]^2} \quad (89)$$

10 Quick Reference Tables

10.1 Physical Constants

Constant	Symbol	Value
Universal gas constant	R	10.73 psia·ft ³ /(lbmol·°R)
Standard pressure	P_{sc}	14.7 psia
Standard temperature	T_{sc}	60°F (520°R)
Air molecular weight	M_{air}	28.97 lb/lbmol
Water density at SC	ρ_w^{SC}	62.4 lb/ft ³
Conversion °F to °R	T_R	$T_F + 459.67$

Table 2: Physical Constants Used in Calculations

10.2 Conversion Factors

From	To	Multiply By
psia	bara	0.06895
°F	°C	$(T_F - 32) \times 5/9$
ft	m	0.3048
mD	m ²	9.869×10^{-16}
cP	Pa·s	0.001
STB	m ³	0.1590
MSCF	m ³	28.32
lb/ft ³	kg/m ³	16.02

Table 3: Common Unit Conversions

10.3 Typical Property Ranges

Property	Typical Range	Comments
API gravity	10 - 50°	Light crude: 30-50°, Heavy: 10-25°
Gas gravity	0.6 - 1.2	Dry gas: 0.6-0.7, Wet gas: 0.7-0.9
R_s at P_b	100 - 3000 scf/stb	Depends on oil type and pressure
B_o	1.01 - 2.0 rb/stb	Increases with R_s
μ_o	0.5 - 100 cP	Light oil: 0.5-5, Heavy: 10-100+
Z-factor	0.7 - 1.2	Lower at medium pressures
B_g	0.003 - 0.010 rcf/scf	Increases with T, decreases with P
μ_g	0.01 - 0.03 cP	Increases with P and T
Permeability	0.1 - 1000 mD	Tight: <1, Good: 100-1000
Porosity	0.05 - 0.35	Low: 0.05-0.15, Good: 0.20-0.30

Table 4: Typical Property Ranges for Petroleum Reservoirs

11 Correlation Method Recommendations

11.1 Oil PVT Methods

Property	Recommended	When to Use
Bubble Point	VALMC	Wide range of conditions, most accurate
	STAN	Classic correlation, quick estimates
	VELAR	Regional correlations, comparison
Solution GOR	VELAR	Default choice, good accuracy
	STAN	Compatibility with older studies
	VALMC	Alternative method
FVF	MCAIN	Most accurate, density-based
	STAN	Simple correlation, fast
Viscosity	BR	Industry standard, widely validated

Table 5: Recommended Correlations for Oil PVT

11.2 Gas PVT Methods

Property	Recommended	When to Use
Z-Factor	DAK	Most accurate, industry standard
	HY	Fast, good for most conditions
	WYW	Newer correlation, comparison
	BUR	High non-hydrocarbons, 100% CO ₂ , H ₂
Critical Props	PMC	Best accuracy, accounts for non-HCs
	SUT	Classic method, compatibility
	BUR	High non-hydrocarbon content
Viscosity	LGE	Industry standard

Table 6: Recommended Correlations for Gas PVT

11.3 Relative Permeability Methods

Method	Use For	Advantages
Corey	Quick estimates	Simple, fast, widely used
	Standard cases	Few parameters, easy to understand
	Initial models	Good starting point
LET	History matching	Flexible curve shapes
	Complex systems	Better fit to lab data
	Final models	Independent endpoint control

Table 7: Relative Permeability Method Selection

12 Tool Categories and Count

12.1 Available Tools by Category

Category	Description	Tools
Oil PVT	Oil property calculations Bubble point, Rs, Bo, viscosity, density, etc.	17
Gas PVT	Gas property calculations Z-factor, critical props, Bg, viscosity, etc.	11
Inflow	Well performance Oil/gas rates for radial/linear flow	4
Simulation	Reservoir simulation support Rel perm tables, aquifer functions, flash	3
Brine	Brine properties CH ₄ and CO ₂ saturated brine	2
Heterogeneity	Layer analysis Lorenz, beta, layer distributions	5
Library	Component properties Critical properties for 100+ components	1
Config	Configuration resources Units, methods, constants, help	4
Total		47

Table 8: pyResToolbox MCP Tool Categories

12.2 Key Features

- **Production Ready:** All 47 tools tested and validated
- **Field Units:** Consistent use of US oilfield units
- **Array Support:** Calculate properties at multiple pressures simultaneously
- **Multiple Methods:** Choose from various industry-standard correlations

- **Type Safety:** Pydantic models ensure input validation
- **Zero Configuration:** Works out of the box with Claude Desktop
- **GPL-3.0 Licensed:** Free and open source

13 Usage Notes and Best Practices

13.1 General Guidelines

13.1.1 Input Validation

- Always use absolute pressures (psia, not psig or barg)
- Temperature must be in Fahrenheit, not Celsius
- Check that input ranges are physically realistic
- Verify that saturation endpoints sum correctly (e.g., $S_{wc} + S_{or} < 1.0$)

13.1.2 Method Selection

- Use recommended methods unless specific requirements exist
- For bubble point: VALMC is most accurate for wide ranges
- For Z-factor: DAK is industry standard, BUR for high non-HCs
- For relative permeability: Corey for quick estimates, LET for accuracy

13.1.3 Common Mistakes to Avoid

- Using separator temperature instead of reservoir temperature
- Confusing R_{sb} (solution GOR at bubble point) with separator GOR
- Not setting Vogel=True when $P_i < P_b$ (saturated reservoir)
- Using wrong gas gravity (separator vs weighted average)
- Not accounting for non-hydrocarbon components (H_2S , CO_2 , N_2)
- Forgetting to convert units from SI to Field Units

13.2 PVT Calculation Workflow

13.2.1 Typical Oil PVT Workflow

1. Calculate bubble point pressure (P_b) from R_{sb} , API, T , γ_g
2. Check if reservoir is undersaturated ($P_i > P_b$) or saturated ($P_i < P_b$)
3. Calculate $R_s(P)$ at desired pressures
4. Calculate $B_o(P, R_s)$ using McCain or Standing method
5. Calculate $\mu_o(P, R_s)$ using Beggs-Robinson
6. Calculate $\rho_o(B_o, R_s)$ using SWMH method
7. Calculate c_o from numerical derivatives of B_o
8. Generate complete PVT table for simulation

13.2.2 Typical Gas PVT Workflow

1. Calculate pseudo-critical properties (T_c , P_c) from γ_g and impurities
2. Calculate Z-factor at desired pressures using DAK or BUR
3. Calculate $B_g(P, T, Z)$ from real gas equation
4. Calculate gas density $\rho_g(P, T, Z)$
5. Calculate gas viscosity $\mu_g(\rho_g, T)$ using LGE method
6. Calculate gas compressibility c_g from Z-factor derivatives
7. Calculate pseudopressure $\psi(P)$ by integrating $P/(\mu_g Z)$

13.3 Well Performance Analysis

13.3.1 IPR Generation Steps

1. Gather reservoir data: P_i , P_b , API, T , h , k , S , r_e , r_w
2. Calculate PVT properties at average pressure
3. Choose flow geometry: radial (vertical well) or linear (horizontal well)
4. For saturated reservoir ($P_i < P_b$), set Vogel=True
5. Calculate rates at multiple flowing pressures: $P_{wf} = 0$ to P_i
6. Plot q vs P_{wf} to generate IPR curve
7. Identify AOF (absolute open flow = rate at $P_{wf} = 0$)

13.4 Simulation Preparation

13.4.1 Relative Permeability Table Generation

1. Choose table type: SWOF (water-oil), SGOF (gas-oil), or SGWFN (3-phase)
2. Choose correlation: Corey (simple) or LET (flexible)
3. Specify saturation endpoints: S_{wc} , S_{or} , S_{org} , S_{gc}
4. Set maximum relative permeabilities: k_{rw}^{max} , k_{ro}^{max} , k_{rg}^{max}
5. Define correlation parameters (Corey exponents or LET parameters)
6. Generate table with 20-50 saturation points
7. Validate endpoints and curves against core data
8. Export to ECLIPSE/CMG format for simulation

14 References

14.1 Key Publications

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15 Appendix: Nomenclature

15.1 Primary Symbols

Symbol	Units	Description
API	degrees	Oil API gravity
B_o	rb/stb	Oil formation volume factor
c_o	1/psi	Oil compressibility
μ_o	cP	Oil viscosity
ρ_o	lb/ft ³	Oil density
R_s	scf/stb	Solution gas-oil ratio
R_{sb}	scf/stb	Solution GOR at bubble point
P_b	psia	Bubble point pressure
γ_o	-	Oil specific gravity (water=1)
B_g	rcf/scf	Gas formation volume factor
c_g	1/psi	Gas compressibility
μ_g	cP	Gas viscosity
ρ_g	lb/ft ³	Gas density
Z	-	Gas compressibility factor (Z-factor)
γ_g	-	Gas specific gravity (air=1)
P_c	psia	Pseudo-critical pressure
T_c	°R	Pseudo-critical temperature
P_{pr}	-	Pseudo-reduced pressure
T_{pr}	-	Pseudo-reduced temperature
ψ	psia ² /cP	Gas pseudopressure
B_w	rb/stb	Water/brine formation volume factor
c_w	1/psi	Brine compressibility
μ_w	cP	Brine viscosity
ρ_w	lb/ft ³	Brine density
R_w	scf/stb	Gas solubility in brine
w_t	wt%	Salinity (weight percent NaCl)
k	mD	Permeability
h	ft	Pay thickness (net)
ϕ	fraction	Porosity
S_w	fraction	Water saturation
S_o	fraction	Oil saturation
S_g	fraction	Gas saturation
S_{wc}	fraction	Connate water saturation
S_{or}	fraction	Residual oil saturation
P	psia	Pressure
T	°F	Temperature
P_i	psia	Initial/reservoir pressure
P_{wf}	psia	Wellbore flowing pressure
q_o	STB/day	Oil production rate
q_g	MSCF/day	Gas production rate
r_e	ft	Drainage radius
r_w	ft	Wellbore radius
S	-	Skin factor

Symbol	Units	Description
L	ft	Horizontal well length
k_{rw}	-	Water relative permeability
k_{ro}	-	Oil relative permeability
k_{rg}	-	Gas relative permeability
S^*	-	Normalized saturation
L	-	Lorenz coefficient
β	-	Dykstra-Parsons coefficient
y_{CO_2}	fraction	CO ₂ mole fraction
y_{H_2S}	fraction	H ₂ S mole fraction
y_{N_2}	fraction	N ₂ mole fraction

Table 9: Nomenclature - Primary Symbols

15.2 Subscripts

Subscript	Meaning
o	Oil phase
g	Gas phase
w	Water/brine phase
b	At bubble point
i	Initial conditions
wf	Wellbore flowing
c	Critical or connate
r	Relative or residual
pr	Pseudo-reduced
D	Dimensionless
sc	Standard conditions
ST	Stock tank conditions
sp	Separator conditions

Table 10: Common Subscripts

16 Index of Formulas

16.1 By Property

Oil Properties

- Bubble Point Pressure (P_b): Standing (p.4), Valko-McCain (p.4), Velarde (p.4)
- Solution GOR (R_s): Standing (p.5), Valko-McCain, Velarde
- Formation Volume Factor (B_o): McCain (p.6), Standing (p.6)
- Viscosity (μ_o): Beggs-Robinson (p.7)
- Density (ρ_o): SWMH (p.7)
- Compressibility (c_o): Explicit method (p.8)
- API-SG Conversions (p.8)

Gas Properties

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End of Formula Reference Guide

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For the latest version and updates, visit:

<https://github.com/gabrielserrao/pyrestoolbox-mcp>

Built on pyResToolbox:

Original library by Mark W. Burgoyne

<https://github.com/mwburgoyne/pyResToolbox>

Remember: Always verify formulas with original sources before professional use.
