# **ACM ICPC Reference**

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# **Contents**

| 1 | 1.1 Base  | 2<br>2<br>3<br>6           |
|---|---|----------------------------|
| 2 | 2.1 Dinic   | 7<br>7<br>8<br>8<br>9      |
| 3 | Structures       1         3.1 Ordered Set       1         3.2 Treap       1         3.3 Envelope       1         3.4 Centroid       1         3.5 Link Cut Tree       1         3.6 Splay Tree       1   | 1 2 3                      |
| 4 | Strings       1         4.1 Suffix Tree       1         4.2 Z-function       1         4.3 Manacher       1   | 7                          |
| 5 | Math         5.1 FFT       1         5.2 Discrete FFT       1         5.3 Linear System Solver       1         5.4 Simplex       1         5.5 Zeta       2         5.6 Zeta Disjoint Or       2         5.7 Miller-Rabin       2         5.8 Pollard-Rho       2 | .7<br>.8<br>.9<br>.0<br>.0 |
| 6 | 6.1 Ceiling Function       2         6.2 Secret Chamber at Mount Rushmore       2         6.3 Need for Speed       2  | 23<br>23<br>24             |
| 7 | 3   | 25<br>25<br>25<br>25       |

#### 1. workspaces/teclado 2. .vimrc and .bashrc 3. temp.cpp

```
syntax on
colo evening
set ai si noet ts=4 sw=4 sta sm nu rnu so=7 t_Co=8
imap {<CR> {<CR>}<Esc>0

#!/bin/bash
while IFS=$'\n' read -r line; do
    trim=$(echo "$line" | tr -d "[:space:]")
    md5=$(echo -n "${trim%\/\/*}" | md5sum)
    md5=${echo -n "${trim%\/\/*}" | md5sum)
    md5=${md5:0:4}
    [ "${trim: 0}" == "$" ] && md5="@$md5@"
    echo "$md5 $line"
done
```

# 1 Geometry

#### 1.1 Base

```
d41d // typedef double cood; cood eps = 1e-8; // risky: XXX, untested: TODO
00a0 const double pi = acos(-1.);
ccb5 template<typename T> inline T sq(T x) { return x*x; }
87bc struct vec {
b86a ⊳ cood x, y;
6e4f \vdash vec () : x(0), y(0) {} vec (cood a, cood b) : x(a), y(b) {}
741a \rightarrow inline vec operator - (vec o) { return \{x - o.x, y - o.y\}; }
ff7e \triangleright inline vec operator + (vec o) { return {x + o.x, y + o.y}; }
b6dd ⊳ inline vec operator * (cood o) { return {x * o, y * o}; }
2711 \triangleright inline vec operator / (cood o) { return \{x \ / \ o, \ y \ / \ o\}; \ \}
6ac9 ⊳ inline cood operator ^ (vec o) { return x * o.y - y * o.x; }
83dd > inline cood operator * (vec o) { return x * o.x + y * o.y; }
46ef | inline cood cross (vec a, vec b) { return ((*this)-a) ^ ((*this)-b); } // |(this)a||(this)b|sen(angle)
cbad | inline cood inner (vec a, vec b) { return ((*this)-a) * ((*this)-b); } // |(this)a||(this)b|cos(angle)
cddd | inline double angle (vec a, vec b) { return atan2(cross(a,b),inner(a,b)); } // ccw angle from (this)a to
    (this)b in range [-pi,pi]
e4d3 \rightarrow inline int ccw (vec a, vec b) { cood o = cross(a,b); return (eps < o) - (o < -eps); } // this is to the
    (1 left, 0 over, -1 right) of ab
2elf | inline int dir (vec a, vec b) { cood o = inner(a,b); return (eps < o) - (o < -eps); } // a(this) is to
    the (1 same, 0 none, -1 opposite) direction of ab
5d26 | inline cood sq (vec o = vec()) { return inner(o,o); }
e7cf > inline double nr (vec o = vec()) { return sqrt(sq(o)); } //$
4e72 | inline vec operator ~ () { return (*this)/nr(); }
f149 ▷ inline vec proj (vec a, vec b) { return a + (b-a)*(a.inner((*this),b) / a.sq(b)); } // projects this onto
    line ab
1664 \vdash inline vec rotate (double a) { return vec(cos(a) * x - sin(a) * y, sin(a) * x + cos(a) * y); } // ccw by
    a radians
3206 ▷ inline vec rot90 () { return vec(-y,x); } // rotate(pi/2)$
2810 \rightarrow bool in_seg (vec a, vec b) { return ccw(a,b) == 0 && dir(a,b) <= 0; } // tips included
5e56 ▶ double dist2_lin (vec a, vec b) { return a.sq(b) <= eps ? sq(a) : double(::sq(cross(a,b)))/a.sq(b); } //
    see cir.has_inter_lin
8831 b double dist2_seg (vec a, vec b) { return a.dir((*this),b) == (b.dir((*this),a)) ? dist2_lin(a,b) :
    min(sq(a),sq(b)); }
436b | inline bool operator == (const vec & o) const { return abs(x-o.x) <= eps && abs(y-o.y) <= eps; }
5522 \triangleright inline bool operator < (const vec & o) const { return (abs(x-o.x)>eps)?(x < o.x):(y > o.y); } // lex
    compare (inc x, dec y)
d41d ▷ // full ccw angle strict compare beginning upwards (this+(0,1)) around (*this)
d41d \triangleright // incresing distance on ties, this is the first
69ad ▶ bool compare (vec a, vec b) {
a482 \rightarrow if ((*this < a) != (*this < b)) return *this < b;
           int o = ccw(a,b); return o?o>0:((a == *this && !(a == b)) || a.dir(*this,b) < 0);
bdb1 ⊳ ⊳
cbb1 ⊳ }
2145 }; //$
bafe struct lin { // line
6143 \triangleright vec p; cood c; // p*(x,y) = c
1105 ▷ lin () {} lin (vec a, cood b) : p(a), c(b) {}
d036 > lin (vec s, vec t) : p((s-t).rot90()), c(p*s) {}
5c8b → inline lin parll (vec v) { return lin(p,v*p); }
```

```
1263 ▶ inline lin perp () { return lin(p.rot90(),c); }
3838 \triangleright vec inter (lin o) { if (vec(0,0).ccw(p,o.p) == 0) throw 1; cood d = (p^o.p); return vec((c*o.p.y -
    p.y*o.c)/d,(o.c*p.x - o.p.x*c)/d); }
1375 ▶ bool contains (vec v) { return abs(p*v - c) <= eps; }
eda5 \triangleright vec at_x (cood x) { return vec(x,(c-p.x*x)/p.y); }
c0fb \rightarrow vec at_y (cood y) { return vec((c-y*p.y)/p.x,y); }
e1ef > double sign_dist (vec v) { return double(p*v - c)/p.nr(); }
2145 }; //$
3236 struct cir { // circle
b6d3 ⊳ vec c; cood r;
126a \vdash cir () {} cir (vec v, cood d) : c(v), r(d) {}
c118 ⊳ cir (vec u, vec v, vec w) { // XXX untreated degenerates
0fb6 \rightarrow vec mv = (u+v)/2; lin s(mv, mv+(v-u).rot90());
bf5f \triangleright vec mw = (u+w)/2; lin t(mw, mw+(w-u).rot90());
a0c4 \triangleright c = s.inter(t); r = c.nr(u);
cbb1 ⊳ }//$
9e54 \triangleright inline bool contains (vec w) { return c.sq(w) <= sq(r) + eps; } // border included
0549 \rightarrow inline bool border (vec w) { return abs(c.sq(w) - sq(r)) <= eps; }
1cd6 | inline bool has_inter (cir o) { return c.sq(o.c) <= sq(r + o.r) + eps; } // borders included
376d | inline bool has_border_inter (cir o) { return has_inter(o) && c.sq(o.c) + eps >= sq(r - o.r); }
8ab4 | inline bool has_inter_lin (vec a, vec b) { return a.sq(b) <= eps ? contains(a) : sq(c.cross(a,b)) <=
    sq(r)*a.sq(b) + eps; } // borders included XXX overflow
9bf7 | inline bool has_inter_seg (vec a, vec b) { return has_inter_lin(a,b) && (contains(a) || contains(b) ||
    a.dir(c,b)*b.dir(c,a) != -1); } // borders and tips included XXX overflow
7abe ⊳ inline double arc_area (vec a, vec b) { return c.angle(a,b)*r*r/2; } // smallest arc, ccw positive
f967 ⊳ inline double arc_len (vec a, vec b) { return c.angle(a,b)*r; } // smallest arc, ccw positive$
771f ⊳ pair<vec, vec> tan (vec v) { // XXX low precision
84ec ▷ ▷ if (contains(v) && !border(v)) throw 0;
          cood d2 = c.sq(v); double s = sqrt(d2 - r*r); s = (s==s)?s:0;
          double al = atan2(r,s); vec t = ((c-v));
          return pair<vec, vec>(v + t.rotate(al)*s, v + t.rotate(-al)*s);
c56f ⊳ pair<vec, vec> border_inter (cir o) {
c4d4 \rightarrow if (!has\_border\_inter(o) || o.c == (*this).c) throw 0;
2b40 ⊳ ⊳
          double a = (sq(r) + o.c.sq(c) - sq(o.r))/(2*o.c.nr(c));
           vec v = (o.c - c)/o.c.nr(c); vec m = c + v * a;
b647 ⊳ ⊳
65b9 ⊳ ⊳
           double h = sqrt(sq(r) - sq(a)); h = h!=h?0:h;
440c ⊳ ⊳
          return pair<vec, vec>(m + v.rot90()*h, m - v.rot90()*h);
cbb1 ⊳ }//$
5182 pair<vec, vec border_inter_lin (vec a, vec b) { // first is closest to a than second
c6e7 b if (a.sq(b) <= eps) { if (border(a)) return pair<vec, vec>(a,a); throw 0; }
           if (a.dir(b,c) == -1) swap(a,b);
45ab ⊳ ⊳
           if (!has_inter_lin(a,b)) throw 0;
5cb6 ⊳ ⊳
           double d2 = c.dist2\_lin(a,b); vec p = (b-a)/a.nr(b);
0aca ⊳ ⊳
           double h = sqrt(r*r - d2); h = h!=h?0:h;
ddf2 ⊳ ⊳
           double y = sqrt(c.sq(a) - d2); y = y!=y?0:y;
5539 ⊳ ⊳
          return pair<vec, vec>(a + p*(y-h), a + p*(y+h));
cbb1 ▷ }//$
be35 ▶ double triang_inter (vec a, vec b) { // ccw oriented, this with (c,a,b)
53ba ⊳ ⊳
          if (c.sq(a) > c.sq(b)) return -triang_inter(b,a);
148a ⊳ ⊳
           if (contains(b)) return c.cross(a,b)/2;
7434 ⊳ ⊳
           if (!has_inter_seg(a,b)) return arc_area(a,b);
773a ⊳ ⊳
           pair<vec,vec> itr = border_inter_lin(b,a); // order important
12a9 ⊳ ⊳
           if (contains(a)) return c.cross(a,itr.first)/2 + arc_area(itr.first,b);
c2f4 ⊳
           return arc_area(a,itr.second) + c.cross(itr.second,itr.first)/2 + arc_area(itr.first,b);
cbb1 ⊳
2145 }; //$
a71b bool inter_seg (vec a, vec b, vec c, vec d) {
2397 b if (a.in_seg(c, d) || b.in_seg(c, d) || c.in_seg(a, b) || d.in_seg(a, b)) return true;
bbbd \vdash return (c.ccw(a, b) * d.ccw(a, b) == -1 && a.ccw(c, d) * b.ccw(c, d) == -1);
cbb1 }
e0fd double dist2_seg (vec a, vec b, vec c, vec d){return inter_seg(a,b,c,d)?0.:min({ a.dist2_seg(c,d),
    b.dist2_seg(c,d), c.dist2_seg(a,b), d.dist2_seg(a,b) });}
```

#### 1.2 Advanced

```
484c cir min_spanning_circle (vec * v, int n) { // n flea > srand(time(NULL)); random_shuffle(v, v+n); cir c(vec(), 0); int i,j,k;
```

```
b11a \vdash for (i = 0; i < n; i++) if (!c.contains(v[i]))
e5b6 \rightarrow for (c = cir(v[i],0), j = 0; j < i; j++) if (!c.contains(v[j]))
a47c \rightarrow for (c = cir((v[i] + v[j])/2, v[i].nr(v[j])/2), k = 0; k < j; k++) if (!c.contains(v[k]))
3dd3 \; {\scriptscriptstyle |\hspace{-.08cm} \mid} \; {\scriptscriptstyle |\hspace{-.08cm} \mid} \; {\scriptscriptstyle |\hspace{-.08cm} \mid} \; c \; = \; cir(v[i],v[j],v[k]);
807f ⊳ return c;
cbb1 }//$
d45c int convex_hull (vec * v, int n, int border_in) { // nlg | border_in (should border points stay?)
4f17 \triangleright swap(v[0], *min_element(v,v+n)); int s, i;
f37e \Rightarrow sort(v+1, v+n, [&v] (vec a, vec b) { int o = b.ccw(v[0], a); return (o?o==1:v[0].sq(a)<v[0].sq(b)); });
a69c ⊳ if (border_in) {
9492 ⊳ ⊳
           for (s = n-1; s > 1 \& v[s].ccw(v[s-1],v[0]) == 0; s--);
0bb0 ⊳ ⊳
           reverse(v+s, v+n);
cbb1 ⊳ }
c497 \triangleright for (i = s = 0; i < n; i++) if (!s || !(v[s-1] == v[i])) {
           for (; s \ge 2 \& v[s-1].ccw(v[s-2],v[i]) \ge border_in; s--);
cea9 ⊳ ⊳
           swap(v[s++],v[i]);
ceca 🕟 🕟
cbb1 ⊳ }
0478 ⊳ return s;
cbb1 }//$
79b9 int monotone_chain (vec * v, int n, int border_in) { // nlg | border_in (should border points stay?)
5031 \rightarrow vector<vec> r; sort(v, v+n); n = unique(v, v+n) - v;
d885 \rightarrow for (int i = 0; i < n; r.pb(v[i++])) while (r.size() >= 2 && r[r.size()-2].ccw(r.back(),v[i]) <=
    -border_in) r.pop_back();
dd80 > r.pop_back(); unsigned int s = r.size();
c19d \rightarrow for (int i = n-1; i >= 0; r.pb(v[i--])) while (r.size() >= s+2 && r[r.size()-2].ccw(r.back(),v[i]) <=
    -border_in) r.pop_back();
a255 \rightarrow return copy(r.begin(), r.end() - (r.size() > 1), v) - v;
cbb1 }//$
f80f double polygon_inter (vec * p, int n, cir c) { // signed area
2eae return inner_product(p, p+n-1, p+1, c.triang_inter(p[n-1],p[0]), std::plus<double>(), [&c] (vec a, vec b)
    { return c.triang_inter(a,b); });
cbb1 }//$
3214 int polygon_pos (vec * p, int n, vec v) { // lg | p should be simple (-1 out, 0 border, 1 in)
6c2a ▷ int in = -1; // it's a good idea to randomly rotate the points in the double case, numerically safer
6033 \rightarrow for (int i = 0; i < n; i++) {
          vec a = p[i], b = p[i?i-1:n-1]; if (a.x > b.x) swap(a,b);
c9e9 ⊳ ⊳
           if (a.x + eps \le v.x & v.x < b.x + eps) { in *= v.ccw(a,b); }
           else if (v.in_seg(a,b)) { return 0; }
c3b1 ⊳ ⊳
cbb1 ⊳ }
091d ⊳ return in;
cbb1 }//$
271f int polygon_pos_convex (vec * p, int n, vec v) { // lg(n) | (-1 out, 0 border, 1 in) TODO
a868 \triangleright if (v.sq(p[0]) <= eps) return 0;
088f > if (n <= 1) { return 0; } if (n == 2) { return v.in_seg(p[0],p[1])?0:-1; }</pre>
2ceb   if (v.ccw(p[0],p[1]) < 0 | | v.ccw(p[0],p[n-1]) > 0) return -1;
fcfd \Rightarrow int di = lower_bound(p+1,p+n-1,v, [&p](vec a,vec v) { return v.ccw(p[0],a) > 0; }) - p;
adf3 \rightarrow if (di == 1) return v.ccw(p[1],p[2]) >= 0?0:-1;
cfa4 > return v.ccw(p[di-1],p[di]);
cbb1 }//$
d41d // v is the pointset, w is auxiliary with size at least equal to v's
bf98 cood closest_pair (vec * v, vec * w, int 1, int r, bool sorted = 0) { // nlg | r is exclusive TODO (AC on
    cf, no test)
91d7 \vdash if (1 + 1 >= r) return inf;
900b → if (!sorted) sort(v+1,v+r,[](vec a, vec b){ return a.x < b.x; });
89cd \rightarrow int m = (1+r)/2; cood x = v[m].x;
1a44 b cood res = min(closest_pair(v,w,l,m,1),closest_pair(v,w,m,r,1));
d046 \bowtie merge(v+1,v+m,v+m,v+r,w+1,[](vec a, vec b){ return a.y < b.y; });
2dd0 \vdash for (int i = 1, s = 1; i < r; i++) if (sq((v[i] = w[i]).x - x) < res) {
ad96 \rightarrow for (int j = s-1; j >= 1 && sq(w[i].y - w[j].y) < res; j--)
c3b1 ⊳ ⊳
           res = min(res, w[i].sq(w[j]));
1991 ⊳ ⊳
           w[s++] = v[i];
cbb1 ⊳ }
b505 ⊳ return res;
cbb1 }//$
ac2e double union_area (cir * v, int n) { // n^2lg | XXX joins equal circles TODO (AC on szkopul, no tests)
c765 \triangleright struct I { vec v; int i; } c[2*(n+4)];
cf66 > srand(time(NULL)); cood res = 0; vector<bool> usd(n);
dd83 \rightarrow cood lim = 1./0.; for (int i = 0; i < n; i++) lim = min(lim, v[i].c.y - v[i].r - 1);
0b02 \rightarrow for (int i = 0, ss = 0; i < n; i++, ss = 0) {
```

```
dc37 ⊳ ⊳
           vec fp = v[i].c + vec(0,v[i].r).rotate(rand()); // rotation avoids corner on cnt initialization
6e87 ⊳ ⊳
           int cnt = 0, eq = 0;
578e ⊳ ⊳
           for (int j = 0; j < n; j++) {
df48 ⊳ ⊳
           cnt += (usd[j] = v[j].contains(fp));
2311 ⊳ ⊳
               if (!v[i].has_border_inter(v[j])) continue;
8daa ⊳ ⊳
               if (v[i].c == v[j].c) eq++;
           ⊳
4e6b ⊳ ⊳
               else {
e59e ⊳ ⊳
                  pair<vec, vec> r = v[i].border_inter(v[j]);
0782 ⊳ ⊳
           \triangleright
                  c[ss++] = \{r.first, j\}; c[ss++] = \{r.second, j\};
cbb1 ⊳ ⊳
cbb1 ⊳ ⊳
           vec d = vec(v[i].r,0); for (int k = 0; k < 4; k++, d = d.rot90()) c[ss++] = \{v[i].c + d, i\};
d21b ⊳ ⊳
85d3 ⊳ ⊳
           int md = partition(c,c+ss,[v,i,fp](I a){return a.v.ccw(v[i].c,fp) > 0;}) - c;
19c7 ⊳ ⊳
           sort(c,c+md,[v,i](I a,I b)\{return a.v.ccw(v[i].c,b.v) < 0;\});
7430 ⊳ ⊳
           sort(c+md,c+ss,[v,i](I a,I b)\{return a.v.ccw(v[i].c,b.v) < 0;\});
56cd ⊳ ⊳
           for (int j = 0; j < ss; j++) {
2b5e ⊳ ⊳
           if (c[j].i != i) { cnt -= usd[c[j].i]; usd[c[j].i] = !usd[c[j].i]; cnt += usd[c[j].i]; }
b115 ⊳ ⊳ ⊳
               vec a = c[j].v, b = c[(j+1)%ss].v;
7c4a ⊳ ⊳ ⊳
               cood cir = abs(v[i].arc\_area(a,b) - v[i].c.cross(a,b)/2), tra = abs((b.x-a.x)*(a.y+b.y-2*lim)/2);
               cood loc = (a.x<b.x)?cir-tra:tra+cir; res += (cnt==eq)?loc/eq:0;</pre>
cbb1 ▷ ▷ }
cbb1 ⊳ }
b505 ⊳ return res;
cbb1 }//$
4ede pii antipodal (vec * p, int n, vec v) \{ // \lg(n) \mid \text{extreme segments relative to direction v TODO} \}
d41d ⊳ // po: closest to dir, ne: furthest from dir
3bd9 \rightarrow bool sw = ((p[1]-p[0])*v < 0);
d189 \rightarrow if (sw) v = vec(0,0) - v; // lower_bound returns the first such that lambda is false
0303 \rightarrow int md = lower_bound(p+1, p+n, v, [p] (vec & a, vec v) { return (a-p[0])*v > eps; }) - p; // chain
    separation
25f1 \rightarrow int po = lower_bound(p, p+md-1, v, [p,n] (vec & a, vec v) { return (p[(&a+1-p)\%n]-a)\*v > eps; }) - p; //
    positive
9dc9 \rightarrow int ne = (lower_bound(p+md, p+n, v, [p,n] (vec & a, vec v) { return (p[(&a+1-p)\%n]-a)*v <= eps; }) -
    p)%n; // negative
5703 ⊳ if (sw) swap(po,ne);
ef0b ⊳ return pii(po,ne);
cbb1 }//$
34e2 int mink_sum (vec * a, int n, vec * b, int m, vec * r) { // (n+m) | a[0]+b[0] should belong to sum, doesn't
    create new border points TODO
8d81 \triangleright if (!n || !m) { return 0; } int i, j, s; r[0] = a[0] + b[0];
de54 \triangleright for (i = 0, j = 0, s = 1; i < n || j < m; s++) {
1ab0 ⊳ ⊳
          if (i >= n) j++;
1dc4 ⊳ ⊳
           else if (j >= m) i++;
4e6b ⊳ ⊳
           else {
4f09 ⊳ ⊳
           int o = (a[(i+1)\%n]+b[j\%m]).ccw(r[s-1],a[i\%n]+b[(j+1)\%m]);
e43c ⊳ ⊳
              j += (o >= 0); i += (o <= 0);
cbb1 ⊳ ⊳
f5b4 \triangleright r[s] = a[i%n] + b[j%m];
cbb1 ⊳ }
162b ⊳ return s-1;
cbb1 }//$
9e65 int inter_convex (vec * p, int n, vec * q, int m, vec * r) { // (n+m) | XXX
2d76 \rightarrow int \ a = 0, \ b = 0, \ aa = 0, \ ba = 0, \ inflag = 0, \ s = 0;
2a6c \rightarrow while ((aa < n || ba < m) && aa < n+n && ba < m+m) {
b977 \triangleright vec p1 = p[a], p2 = p[(a+1)%n], q1 = q[b], q2 = q[(b+1)\%m];
35b2 ⊳ ⊳
           vec A = p2 - p1, B = q2 - q1;
1479 ⊳ ⊳
           int cross = vec(0,0).ccw(A,B), ha = p1.ccw(p2,q2), hb = q1.ccw(q2,p2);
c6e0 ⊳ ⊳
           if (cross == 0 \& p2.ccw(p1,q1) == <math>0 \& A*B < -eps) {
507h ⊳ ⊳
           \mathbf{if} (q1.in_seg(p1,p2)) r[s++] = q1;
               if (q2.in_seg(p1,p2)) r[s++] = q2;
5e83 ⊳ ⊳
ce58 \rightarrow f if (p1.in_seg(q1,q2)) r[s++] = p1;
526a \triangleright \triangleright \vdash if (p2.in_seg(q1,q2)) r[s++] = p2;
7b25 \triangleright \triangleright if (s < 2) return s;
e2a8 ⊳ ⊳ ⊳
               inflag = 1; break;
5e6d ▷ ▷ } else if (cross != 0 && inter_seg(p1,p2,q1,q2)) {
f420 \triangleright \triangleright if (inflag == 0) aa = ba = 0;
2b81 \triangleright \triangleright r[s++] = lin(p1,p2).inter(lin(q1,q2));
37fd ⊳ ⊳ ⊳
               inflag = (hb > 0) ? 1 : -1;
cbb1 ▷ ▷ }
```

```
5499 ⊳ ⊳
           if (cross == 0 && hb < 0 && ha < 0) return s;
0872 ⊳ ⊳
           bool t = cross == 0 && hb == 0 && ha == 0;
c0ec ⊳ ⊳
           if (t ? (inflag == 1) : (cross \geq 0) ? (ha \leq 0) : (hb \geq 0)) {
9873 ⊳ ⊳
           \rightarrow if (inflag == -1) r[s++] = q2;
1146 ⊳ ⊳
           ba++; b++; b %= m;
9d97 ⊳ ⊳
           } else {
5c98 ⊳ ⊳
               if (inflag == 1) r[s++] = p2;
           ⊳
5ecb ⊳ ⊳
               aa++; a++; a %= n;
cbb1 ⊳
cbb1 ⊳
c1b2 \rightarrow if (inflag == 0) {
           if (polygon_pos_convex(q,m,p[0]) >= 0) { copy(p, p+n, r); return n; }
3880 ⊳ ⊳
           if (polygon_pos_convex(p,n,q[0]) >= 0) { copy(q, q+m, r); return m; }
115c ⊳
cbb1 ⊳ }
fc37 > s = unique(r, r+s) - r;
2629 \rightarrow if (s > 1 \& r[0] == r[s-1]) s--;
0478 ⊳ return s;
cbb1 }//$
03ae bool isear (vec * p, int n, int i, int prev[], int next[]) { // aux to triangulate
7630 \triangleright vec a = p[prev[i]], b = p[next[i]];
2d9f \rightarrow if (b.ccw(a,p[i]) \ll 0) return false;
578e \rightarrow for (int j = 0; j < n; j++) {
97eb \rightarrow if (j == prev[i] || j == next[i]) continue;
          if (p[j].ccw(a,p[i]) >= 0 \&\& p[j].ccw(p[i],b) >= 0 \&\& p[j].ccw(b,a) >= 0) return false;
0ef9 ⊳ ⊳
0639 ⊳ ⊳
          int k = (j+1)\%n;
           if (k == prev[i] || k == next[i]) continue;
a537 ⊳ ⊳
           if (inter_seg(p[j],p[k],a,b)) return false;
cbb1 ⊳ }
8a6c ⊳ return true;
cbb1 }
1851 int triangulate (vec * p, int n, bool ear[], int prev[], int next[], int tri[][3]) { // 0(\hat{n}^2) | n >= 3
d14e \rightarrow int s = 0, i = 0;
78d0 \rightarrow for (int i = 0, prv = n-1; i < n; i++) { prev[i] = prv; prv = i; next[i] = (i+1)%n; ear[i] =
    isear(p,n,i,prev,next); }
6b3b \rightarrow for (int lef = n; lef > 3; lef--, i = next[i]) {
          while (!ear[i]) i = next[i];
ced7 ⊳ ⊳
e7a9 ⊳ ⊳
           tri[s][0] = prev[i]; tri[s][1] = i; tri[s][2] = next[i]; s++; // tri[i][0],i,tri[i][1] inserted
           int c_prev = prev[i], c_next = next[i];
           next[c_prev] = c_next; prev[c_next] = c_prev;
84b6 ⊳ ⊳
           ear[c_prev] = isear(p,n,c_prev,prev,next); ear[c_next] = isear(p,n,c_next,prev,next);
cbb1 ⊳ }
bc1d bc1d rri[s][0] = next[next[i]]; tri[s][1] = i; tri[s][2] = next[i]; s++; // tri[i][0],i,tri[i][1] inserted
0478 ⊳ return s;
cbb1 }
```

#### 1.3 3D

```
f61c const double pi = acos(-1);
d41d // typedef double cood; cood eps = 1e-6; // risky: XXX, untested: TODO
3f73 struct pnt { // TODO it's not tested at all :)
5e43 \triangleright cood x, y, z;
cf2f \  pnt () : x(0), y(0), z(0) {} pnt (cood a, cood b, cood c) : x(a), y(b), z(c) {}
4e90 | inline pnt operator - (pnt o) { return pnt(x - o.x, y - o.y, z - o.z); }
2b18 \rightarrow inline pnt operator + (pnt o) { return pnt(x + o.x, y + o.y, z + o.z); }
7470 | inline pnt operator * (cood o) { return pnt(x*o, y*o, z*o); }
8194 b inline pnt operator / (cood o) { return pnt(x/o, y/o, z/o); }
a269 | inline cood operator * (pnt o) { return x*o.x + y*o.y + z*o.z; } // inner: |this||o|*cos(ang)
079c \rightarrow inline pnt operator \hat{} (pnt o) { return pnt(y*o.z - z*o.y, z*o.x - x*o.z, x*o.y - y*o.x); } // cross:
    oriented normal to the plane containing the two vectors, has norm |this||o|*sin(ang)
a2ea b inline cood operator () (pnt a, pnt b) { return (*this)*(a^b); } // mixed: positive on the right-hand
    rule (thumb=this,index=a,mid=b)
d41d
f500 | inline cood inner (pnt a, pnt b) { return (a-(*this))*(b-(*this)); }
4114 • inline pnt cross (pnt a, pnt b) { return (a-(*this))^(b-(*this)); } // its norm is twice area of triangle
fa90 ⊳ inline cood mixed (pnt a, pnt b, pnt c) { return (a-(*this))(b-(*this),c-(*this)); } // 6 times the
    oriented area of thetahedra
4f78 | inline cood sq (pnt o = pnt()) { return inner(o,o); }
```

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```
113b | inline double nr (pnt o = pnt()) { return sqrt(sq(o)); }
6edf > inline pnt operator ~ () { return (*this)/nr(); }
d41d
11c0 | inline bool in_seg (pnt a, pnt b) { return cross(a,b).sq() <= eps && inner(a,b) <= eps; } // tips included
a6b7 ▶ inline bool in_tri (pnt a, pnt b, pnt c) { return abs(mixed(a,b,c)) <= eps && cross(a,b)*cross(b,c) >=
    -eps && cross(a,b)*cross(c,a) >= -eps; } // border included
d41d
7c26 | inline pnt proj (pnt a, pnt b) { return a + (b-a)*a.inner(b,(*this))/a.sq(b); }
3a26 \rightarrow inline pnt proj (pnt a, pnt b, pnt c) { pnt n = a.cross(b,c); return (*this) - n*(n*((*this)-a))/n.sq(); }
d41d
8fbb | inline double dist2_lin (pnt a, pnt b) { return cross(a,b).sq()/a.sq(b); }
1880 ▶ inline double dist2_seg (pnt a, pnt b) { return a.inner(b,(*this))*b.inner(a,(*this)) <= eps ?
    min(sq(a),sq(b)) : dist2_lin(a,b); }
39c1 ▶ inline double dist_pln (pnt a, pnt b, pnt c) { return abs((~a.cross(b,c))*((*this)-a)); }
5bc2 | inline double dist2_tri (pnt a, pnt b, pnt c) { pnt p = proj(a,b,c); return p.in_tri(a,b,c) ? sq(p) :
    min({ dist2_seg(a,b), dist2_seg(b,c), dist2_seg(c,a) }); }
eb48 inline cood area (pnt a, pnt b, pnt c) { return abs(a.cross(b,c).nr()) / 2; }
a6c7 inline cood vol (pnt a, pnt b, pnt c, pnt d) { return abs(a.mixed(b,c,d)) / 6; } // thetahedra
084a pnt inter_lin_pln (pnt s, pnt t, pnt a, pnt b, pnt c) { pnt n = a.cross(b,c); return s +
    (t-s)*(n*(a-s))/(n*(t-s)); } //$
fabc struct sph { // TODO it's also not tested at all
af42 ⊳ pnt c; cood r;
390f \triangleright sph () : c(), r(0) \{ \} sph (pnt a, cood b) : c(a), r(b) \{ \}
baaf | inline pnt operator () (cood lat, cood lon) { return c + pnt(cos(lat)*cos(lon), sin(lon), sin(lat))*r; }
    // (1,0,0) is (0,0). z is height.
171a → inline double area_hull (double h) { return 2.*pi*r*h; }
60a4 | inline double vol_hull (double h) { return pi*h/6 * (3.*r*r + h*h); }
2145 };
```

# 2 Graphs

#### 2.1 Dinic

```
d41d //typedef int num; const int N = ; const int M = * 2; const num eps = 0;
582d struct dinic {
9740 \triangleright int hd[N], seen[N], qu[N], lv[N], ei[N], to[M], nx[M]; num fl[M], cp[M]; int en = 2; int tempo = 0;
1233 ⊳ bool bfs(int s, int t) {
5ff9 \triangleright Fenck Seen[t] = ++tempo; lv[t] = 0; int ql = 0, qr = 0; qu[qr++] = t;
                            while(ql != qr) {
036d \triangleright \triangleright \vdash t = qu[ql++]; ei[t] = hd[t]; if(s == t) return true;
7e80 \rightarrow for(int e = hd[t]; e; e = nx[e]) if(seen[to[e]] != tempo && cp[e ^ 1] - fl[e ^ 1] > eps) {
a74c ⊳ ⊳ ⊳
                                             seen[to[e]] = tempo;
de5c ⊳ ⊳ ⊳
                                              lv[to[e]] = lv[t] + 1;
                                              qu[qr++] = to[e];
f0ff ▷ ▷ ▷ ▷
cbb1 ▷ ▷ ▷ }
cbb1 ▷ ▷ }
d1fe ⊳ return false;
cbb1 ⊳ }
a444 \triangleright num dfs(int s, int t, num f) {
f449 \rightarrow f(s == t) return f;
d4ad \rightarrow for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]] \&\& seen[to[e]] == tempo \&\& cp[e] - fl[e] > eps \&\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]] &\& seen[to[e]] == tempo \&\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo \&\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]]) &\& for(int \&e = ei[to[e]]) if(ei[to[e]]) if(ei[to[e]]) &\& for(int \&e = ei[to[e]]) if(ei[to[e]]) if(ei[to[e
          lv[to[e]] == lv[s] - 1)
7004 \rightarrow \rightarrow if(num rf = dfs(to[e], t, min(f, cp[e] - fl[e]))) {
805c ⊳ ⊳
                                             fl[e] += rf;
                          \triangleright
                                   \triangleright
                                                             ` 1] -= rf;
5226 ⊳ ⊳
                                              fl[e
                           \triangleright
                                   \triangleright
2cb7 ⊳ ⊳
                                              return rf;
                           ⊳
cbb1 ⊳ ⊳
                                    }
bb30 ⊳ ⊳
                           return 0;
cbb1 ⊳ }
d41d ⊳ // public $
de22 > num max_flow(int s, int t) {
6cb2 \triangleright num fl = 0;
1c5e ⊳ ⊳
                            while (bfs(s, t)) for(num f; (f = dfs(s, t, numeric_limits<num>::max())); fl += f);
e508 ⊳ ⊳
                            return fl;
cbb1 ⊳ }
5a3f ⊳ void add_edge(int a, int b, num c, num rc=0) {
```

#### 2.2 MinCost MaxFlow

```
d41d //typedef int val: // type of flow
d41d //typedef int num; // type of cost
d41d //const int N = , M = * 2; const num eps = 0;
1854 struct mcmf {
b6db = int es[N], to[M], nx[M], en = 2, pai[N], seen[N], tempo, qu[N];
ef55 ⊳ val fl[M], cp[M], flow; num cs[M], d[N], tot;
d0cc ⊳ val spfa(int s, int t) {
09b0 \rightarrow tempo++; int a = 0, b = 0;
          for(int i = 0; i < N; i++) d[i] = numeric_limits<num>::max();
e0c6 ⊳ ⊳
68ad ⊳ ⊳
          d[s] = 0; qu[b++] = s; seen[s] = tempo;
9841 ⊳ ⊳
          while(a != b) {
32d9 ⊳ ⊳
          int u = qu[a++]; if (a == N) a = 0; seen [u] = 0;
a86f ⊳ ⊳ ⊳
              for(int e = es[u]; e; e = nx[e]) if(cp[e] - fl[e] > val(0) && d[u] + cs[e] < d[to[e]] - eps) {
a694 ⊳ ⊳
                d[to[e]] = d[u] + cs[e]; pai[to[e]] = e^1;
          ⊳⊳⊳
1889 ⊳ ⊳
                 if(seen[to[e]] < tempo) \{ seen[to[e]] = tempo; qu[b++] = to[e]; if(b == N) b = 0; \}
          \triangleright
cbb1 ⊳ ⊳
cbb1 ⊳ ⊳
8e2a ⊳ ⊳
          if(d[t] == numeric_limits<num>::max()) return false;
91fe ⊳ ⊳
          val mx = numeric_limits<val>::max();
          for(int u = t; u != s; u = to[pai[u]])
285a ⊳ ⊳
          mx = min(mx, cp[pai[u] ^ 1] - fl[pai[u] ^ 1]);
7039 ⊳ ⊳
          tot += d[t] * val(mx);
6de0 - -
          for(int u = t; u != s; u = to[pai[u]])
285a ⊳ ⊳
          p fl[pai[u]] -= mx, fl[pai[u] ^ 1] += mx;
4c48 ⊳ ⊳
b9aa ⊳ ⊳
          return mx;
cbb1 ⊳ }
d41d ⊳ // public $
8662 p num min_cost(int s, int t) {
3b69 \triangleright tot = 0; flow = 0;
e66e ⊳ ⊳
          while(val a = spfa(s, t)) flow += a;
126a ⊳ return tot;
cbb1 ⊳ }
457a ⊳ void add_edge(int u, int v, val c, num s) {
          fl[en] = 0; cp[en] = c; to[en] = v; nx[en] = es[u]; cs[en] = s; es[u] = en++;
1d08 ⊳ ⊳
8015 ⊳ ⊳
           fl[en] = 0; cp[en] = 0; to[en] = u; nx[en] = es[v]; cs[en] = -s; es[v] = en++;
cbb1 ⊳
8537 void reset_flow() { memset(fl, 0, sizeof(val) * en); }
451f ▶ void init(int n) { en = 2; memset(es, 0, sizeof(int) * n); } // XXX must be called
2145 };
```

## 2.3 Cycle Cancelling

```
d41d //typedef int val; // type of flow
d41d //typedef int num; // type of cost
d41d //const int N = ; const int M = * 2; const val eps = 0;
afb2 struct cycle_cancel {
2c47 b int hd[N], seen[N], qu[N], lv[N], ei[N], to[M], nx[M], ct[N], pai[N]; val fl[M], cp[M], flow; num cs[M],
    d[N], tot; int en = 2, n; int tempo = 0;
1233 ⊳ bool bfs(int s, int t) {
5ff9 \mapsto seen[t] = ++tempo; lv[t] = 0; int ql = 0, qr = 0; qu[qr++] = t;
a872 ⊳ ⊳
          while(ql != qr) {
          t = qu[ql++]; ei[t] = hd[t]; if(s == t) return true;
              for(int e = hd[t]; e; e = nx[e]) if(seen[to[e]] != tempo && cp[e ^ 1] - fl[e ^ 1] > eps) {
          \triangleright
a74c ⊳ ⊳
              seen[to[e]] = tempo;
           \triangleright
de5c ⊳ ⊳
                  lv[to[e]] = lv[t] + 1;
f0ff ⊳ ⊳
          \triangleright
                  qu[qr++] = to[e];
cbb1 ⊳ ⊳
              }
cbb1 ⊳ ⊳
```

```
d1fe ⊳ ⊳ return false;
cbb1 ⊳ }
e4d9 ⊳ val dfs(int s, int t, val f) {
f449 \rightarrow f(s == t) return f;
                    for(int \&e = ei[s]; e; e = nx[e]) if(ei[to[e]] \&\& seen[to[e]] == tempo \&\& cp[e] - fl[e] > eps \&\& seen[to[e]] == tempo &\& cp[e] - fl[e] > eps &\& seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] - fl[e] > eps && seen[to[e]] == tempo && cp[e] == tempo && 
       lv[to[e]] == lv[s] - 1)
9fe1 \rightarrow \rightarrow if(val rf = dfs(to[e], t, min(f, cp[e] - fl[e]))) {
                                fl[e] += rf;
fl[e ^ 1] -= rf;
805c ⊳ ⊳
                   \triangleright
                          ⊳
5226 ⊳ ⊳
                   ⊳
                         ⊳
                                 return rf;
2cb7 ⊳ ⊳
                   \triangleright
cbb1 ⊳ ⊳
                          }
bb30 ⊳ ⊳
                   return 0;
cbb1 ⊳ }
5cbe ▷ bool spfa() {
a019 ⊳ ⊳
                   tempo++; int a = 0, b = 0, u;
99a4 b
                    for(int \ i = 0; \ i < n; \ i++) \ \{ \ d[i] = 0; \ qu[b++] = i; \ seen[i] = tempo; \ ct[i] = 0; \ \}
9841
                    while(a != b) {
b492 \rightarrow d = qu[a++]; if(a == N) a = 0; seen[u] = 0;
d627 \rightarrow \vec{if}(ct[u]++>=n+1) \{ a--; break; \}
ccce \rightarrow for(int e = hd[u]; e; e = nx[e]) if(cp[e] - fl[e] > val(0) && d[u] + cs[e] < d[to[e]] - eps) {
                                 d[to[e]] = d[u] + cs[e]; pai[to[e]] = e ^ 1;
1889 ⊳ ⊳ ⊳
                                 if(seen[to[e]] < tempo) { seen[to[e]] = tempo; qu[b++] = to[e]; if(b == N) b = 0; }
cbb1 ⊳ ⊳
                   ⊳ }
cbb1 ⊳ ⊳
5c28 ⊳ ⊳
                   if(a == b) return false;
02be ⊳ ⊳
                   val mn = numeric_limits<val>::max();
1fd8 ⊳ ⊳
                   tempo++;
695a ⊳ ⊳
                    for(; seen[u] != tempo; u = to[pai[u]]) seen[u] = tempo;
e539 ⊳ ⊳
                    for(int v = u; seen[v] != tempo + 1; v = to[pai[v]]) {
ff98 ⊳ ⊳
                   \triangleright seen[v] = tempo + 1;
3225 ⊳ ⊳
                         mn = min(mn, cp[pai[v] ^ 1] - fl[pai[v] ^ 1]);
cbb1 ⊳ ⊳
c141 ⊳ ⊳
                    for(int v = u; seen[v] == tempo + 1; v = to[pai[v]]) {
                    \triangleright seen[v] = 0;
7618 ⊳ ⊳
60f1 ⊳ ⊳
                          fl[pai[v]] -= mn;
                          fl[pai[v] ^ 1] += mn;
0329 ⊳ ⊳
cbb1 ⊳ ⊳
                    }
8a6c ⊳ ⊳
                   return true;
cbb1 ⊳ }
2b0e ⊳ val max_flow(int s, int t) {
e7a0 ⊳ ⊳
                    val fl = 0:
                    while (bfs(s, t)) for(val f; (f = dfs(s, t, numeric_limits<val>::max())); fl += f);
036d ⊳ ⊳
e508 ⊳ ⊳
                    return fl;
cbb1 ⊳ }
d41d \triangleright // public $
8662 \triangleright num min_cost(int s, int t) {
94a7 \triangleright flow = max_flow(s, t);
6c9f ⊳ ⊳
                   while(spfa());
ed25 ⊳ ⊳
                   tot = 0;
                    for(int i = 2; i < en; i++)
112e ⊳ ⊳
b951 ⊳ ⊳
                       if(fl[i] > 0)
                   b tot += fl[i] * cs[i];
dae8 ⊳ ⊳
126a ⊳
                   return tot;
cbb1 ⊳
8537 ▶ void reset_flow() { memset(fl, 0, sizeof(val) * en); }
457a ⊳ void add_edge(int u, int v, val c, num s) {
d321 \rightarrow fl[en] = 0; cp[en] = c; to[en] = v; nx[en] = hd[u]; cs[en] = s; hd[u] = en++;
                    fl[en] = 0; cp[en] = 0; to[en] = u; nx[en] = hd[v]; cs[en] = -s; hd[v] = en++;
cbb1 ⊳ }
bfc4 by void init(int n) { this->n = n; en = 2; memset(hd, 0, sizeof(int) * n); } // XXX must be called
2145 };
```

### 2.4 Hungarian

```
d41d //const int N = ; typedef ll num; const num eps = ; d41d // Solves minimum perfect matching in an n by n bipartite graph with edge costs in c d41d // y and z will be such that y[i] + z[j] \le c[i][j] and sum of y and z is maximum 55ad struct hungarian {
```

```
2f6a \vdash int n, MA[N], MB[N], PB[N], mn[N], st[N], sn; bool S[N], T[N];
6cc1 \triangleright num c[N][N], d[N], y[N], z[N];
cd49 ⊳ bool increase(int b) {
03dd ⊳ ⊳
          for (int a = PB[b];;) {
9ae2 ⊳ ⊳
              int n_b = MA[a];
           \triangleright
1ba8 ⊳ ⊳
              MB[b] = a; MA[a] = b;
          ⊳
8f2f ⊳ ⊳
              if(n_b == -1) break;
          ⊳
              b = n_b; a = PB[b];
5af0 ⊳ ⊳
cbb1 ⊳ ⊳
8a6c ⊳
          return true;
cbb1 ⊳
3a3b ⊳ bool visit(int a) {
cdb1 \triangleright \triangleright S[a] = true;
           for(int b = 0; b < n; b++) {
f580 ⊳ ⊳
367c ⊳ ⊳

    if(T[b]) continue;
e782 ⊳ ⊳
              if(c[a][b] - y[a] - z[b] < d[b] - eps) { d[b] = c[a][b] - y[a] - z[b]; mn[b] = a; }
3f25 ⊳ ⊳
              if(c[a][b] - eps \le y[a] + z[b]) {
b46d ⊳ ⊳ ⊳
                  T[b] = true; PB[b] = a; st[sn++] = b;
f8ab ⊳ ⊳ ⊳
                  if(MB[b] == -1) return increase(b);
cbb1 ▷ ▷
cbb1 ▷ ▷ }
d1fe ⊳ ⊳
          return false;
cbb1 ⊳ }
415c ▶ bool update_dual() {
2f63 \triangleright int mb = -1, b; num e;
f135 ⊳ ⊳
           for(b = 0; b < n; b++) if(!T[b] && (mb == -1 || d[b] < d[mb])) mb = b;
04ff ⊳ ⊳
          for(e = d[mb], b = 0; b < n; b++)
3c42 ⊳ ⊳

    if(T[b]) z[b] -= e;
6435 ⊳ ⊳
             else d[b] -= e;
a915 ⊳ ⊳
          for(int a = 0; a < n; a++)
cbbc ⊳ ⊳
           \triangleright if(S[a]) y[a] += e;
           PB[mb] = mn[mb];
7dcf ⊳ ⊳
           if(MB[mb] == -1) return increase(mb);
e309 ⊳ ⊳
           st[sn++] = mb; T[mb] = true;
          return false;
d1fe ⊳ ⊳
cbb1 ⊳ }
c4db ⊳ void find_path() {
2cc3 ⊳ ⊳
          int a; for(a = 0; MA[a] != -1; a++);
           memset(S, 0, sizeof S); memset(T, 0, sizeof T);
0351 ⊳ ⊳
e0c6 ⊳ ⊳
           for(int i = 0; i < N; i++) d[i] = numeric_limits<num>::max();
7160 ⊳ ⊳
           sn = 0; if(visit(a)) return;
           while(true) {
6679 ⊳ ⊳
              if(sn) { if(visit(MB[st[--sn]])) break; }
6656 ⊳ ⊳
              else if(update_dual()) break;
cbb1 ⊳ ⊳
           }
cbb1 ⊳ }
7e1e ⊳ void reset_all() {
52b4 ⊳ ⊳
           for(int i = 0; i < n; i++) { y[i] = *min_element(c[i], c[i] + n); z[i] = 0; }</pre>
e517 ⊳ ⊳
           for(int i = 0; i < n; i++) MA[i] = MB[i] = -1;
cbb1 ⊳ }
d41d ⊳ // public $
957f → num min_match() { // set n and c then call this function
b989 \triangleright reset_all(); num all = 0;
           for(int i = 0; i < n; i++) find_path();</pre>
fe8e ⊳ ⊳
           for(int a = 0; a < n; a++) all += c[a][MA[a]];
64a8 ⊳
           return all;
cbb1 ⊳ }
2145 };
```

### 3 Structures

#### 3.1 Ordered Set

```
7747 #include <ext/pb_ds/assoc_container.hpp>
30f4 #include <ext/pb_ds/tree_policy.hpp>
0d73 using namespace __gnu_pbds;
```

### 3.2 Treap

```
d41d //const int N = ; typedef int num;
5463 num X[N]; int en = 1, Y[N], sz[N], L[N], R[N];
8b25 void calc (int u) { // update node given children info
d4c7 > sz[u] = sz[L[u]] + 1 + sz[R[u]];
d41d ▷ // code here, no recursion
cbb1 }
234f void unlaze (int u) {
e39f ⊳ if(!u) return;
d41d _{\triangleright} // code here, no recursion
cbb1 }
ee5e void split_val(int u, num x, int &l, int &r) \{ // 1 \text{ gets} <= x, r \text{ gets} > x \}
754f \rightarrow unlaze(u); if(!u) return (void) (1 = r = 0);
4bc1 \rightarrow if(X[u] \le x) \{ split_val(R[u], x, l, r); R[u] = 1; l = u; \}
81a7 belse { split_val(L[u], x, l, r); L[u] = r; r = u; }
aaa8 ⊳ calc(u);
cbb1 }
9374 void split_sz(int u, int s, int &l, int &r) { // l gets first s, r gets remaining
754f \rightarrow unlaze(u); if(!u) return (void) (1 = r = 0);
e06d \rightarrow if(sz[L[u]] < s) { split_sz(R[u], s - sz[L[u]] - 1, 1, r); R[u] = 1; 1 = u; }
f524 belse { split_sz(L[u], s, l, r); L[u] = r; r = u; }
aaa8 ⊳ calc(u);
cbb1 }
c870 int merge(int 1, int r) { // els on 1 <= els on r
67f0 \rightarrow unlaze(1); unlaze(r); if(!l || !r) return l + r; int u;
7801 \rightarrow if(Y[1] > Y[r]) \{ R[1] = merge(R[1], r); u = 1; \}
ae90 \rightarrow else \{ L[r] = merge(1, L[r]); u = r; \}
Offd ⊳ calc(u); return u;
cbb1 }
500b void init(int n=N-1) { // XXX call before using other funcs
7d1c  for(int i = en = 1; i \le n; i++) { Y[i] = i; sz[i] = 1; L[i] = R[i] = 0; } 
8c5a \rightarrow random\_shuffle(Y + 1, Y + n + 1);
cbb1 }
```

# 3.3 Envelope

```
d41d // typedef ll num; const num eps = 0;
d41d // XXX double: indicates operations specific to integers, not precision related
d79f template<typename line> struct envelope {
5e0f → deque<line> q; num lo,hi; envelope (num _lo, num _hi) : lo(_lo), hi(_hi) {}
01ca ⊳ void push_front (line 1) { // amort. O(inter) | 1 is best at lo or never
a86b ▷ ▷ if (q.size() && q[0](lo) < l(lo)) return;
          for (num x; q.size(); q.pop_front()) {
cc18 ⊳ ⊳
          x = (q.size() <= 1?hi:q[0].inter(q[1],lo,hi)-1); // XXX double (-1)
4202 ⊳ ⊳
              if (1(x) > q[0](x)) break;
cbb1 ⊳ ⊳
45bc ⊳ ⊳
          q.push_front(1);
cbb1 ⊳ }
f644 by void push_back (line 1) { // amort. O(inter) | 1 is best at hi or never
0334 ⊳ ⊳
          if (q.size() && q[q.size()-1](hi) <= l(hi)) return;</pre>
b71c ⊳ ⊳
          for (num x; q.size(); q.pop_back()) {
4e80 ⊳ ⊳
          ⊳
             x = (q.size() <= 1?lo: q[q.size()-2].inter(q[q.size()-1],lo,hi));
1747 ⊳ ⊳
              if (l(x) >= q[q.size()-1](x)) break;
cbb1 ⊳ ⊳
5e56 ⊳ ⊳
          q.push_back(1);
cbb1 ⊳ }
e732 b void pop_front (num _lo) { for (lo=_lo; q.size()>1 && q[0](lo) > q[1](lo); q.pop_front()); } // amort.
    0(n)
```

```
218a void pop_back (num _hi) { for (hi=_hi; q.size()>1 && q[q.size()-2](hi) <= q[q.size()-1](hi);
    q.pop_back()); } // amort. 0(n)
7155 \triangleright line get (num x) { // O(\lg(R))
           int lo, hi, md; for (lo = 0, hi = q.size()-1, md = (lo+hi)/2; lo < hi; md = (lo+hi)/2)
              if (q[md](x) > q[md+1](x)) \{ lo = md+1; \}
b029 ⊳ ⊳
               else { hi = md; }
adf9 ⊳ ⊳
          return q[lo];
cbb1 ⊳ }
2145 };
b3a6 struct line { // inter = 0(1)
7bd4 ⊳ num a,b; num operator () (num x) const { return a*x+b; }
2417 ▶ num inter (line o, num lo, num hi) { return
    abs(o.a-a) \le eps?((b<o.b)?hi+1:lo):min(hi+1,max(lo,(o.b-b-(o.b-b<0)*(a-o.a-1))/(a-o.a) + 1));
2145 };
16ed struct generic_line { // inter = 0(lg(R))
7bd4 ⊳ num a,b; num operator () (num x) const { return a*x+b; }
3cfe ⊳ num inter (generic_line o, num lo, num hi) { // first point where o strictly beats this
           for (num md = lo+((++hi)-lo)/2; lo < hi; md = lo+(hi-lo)/2) { // XXX double
760b ⊳ ⊳
              if ((*this)(md)<=o(md)) { lo = md+1; } // XXX double
b029 ⊳ ⊳
               else { hi = md; }
cbb1 ▷ ▷ }
2532 ⊳ ⊳
           return lo;
cbb1 ⊳ }
2145 };
11a2 template<typename line> struct full_envelope { // XXX ties are broken arbitrarily
85c9 \triangleright vector<envelope<line> > v; full_envelope(envelope<line> c) : v({c}) {} // v.reserve(30);
6aed ▶ void add (line 1) { // amort. O(lg(n)*inter)
8cca ⊳ ⊳
           envelope<line> cur(v.back().lo,v.back().hi); cur.push_back(l);
bb4a ⊳ ⊳
           while (!v.empty() && v.back().q.size() <= cur.q.size()) {</pre>
ce29 ⊳ ⊳
              dequee> aux; swap(aux,cur.q); int i = 0, j = 0;
           ⊳
31d2 ⊳ ⊳
              for (; i < aux.size(); i++) {</pre>
           \triangleright
           \triangleright
              for (; j < v.back().q.size() && v.back().q[j](cur.hi) > aux[i](cur.hi); j++)
0015 P
           \triangleright
                  cur.push_back(v.back().q[j]);
70a1 ⊳ ⊳
           \triangleright
                  cur.push_back(aux[i]);
cbb1 ⊳ ⊳
a0e7 ⊳ ⊳
              for (; j < v.back().q.size(); j++) cur.push_back(v.back().q[j]);</pre>
deff ⊳ ⊳
              v.pop_back();
cbb1 ⊳ ⊳
           }
026e ⊳ ⊳
           v.push_back(cur);
cbb1 ⊳ }
7155 \vdash line get (num x) { // O(\lg(n)\lg(R)) | pop_back/pop_front can optimize
9351 \triangleright line a = v[0].get(x);
ad67 ⊳ ⊳
           for (int i = 1; i < (int) v.size(); i++) {</pre>
bcbe ⊳ ⊳
              line b = v[i].get(x);
ad0f ⊳ ⊳
              if (b(x)<a(x)) a = b;
cbb1 ⊳ ⊳
           }
3f53 ⊳ ⊳
           return a;
cbb1 ⊳ }
2145 };
```

#### 3.4 Centroid

```
0eca vector<int> adj[N]; int cn_sz[N], n;
c864 vector<int> cn_chld[N]; int cn_dep[N], cn_dist[20][N]; // removable
ace4 void cn_setdist (int u, int p, int depth, int dist) { // removable
989e ⊳ cn_dist[depth][u] = dist;
59dd ⊳ for (int v : adj[u]) if (p != v && cn_sz[v] != -1) // sz = -1 marks processed centroid (not dominated)
4ce5 ⊳ ⊳
          cn_setdist(v, u, depth, dist+1);
cbb1 }
e897 int cn_getsz (int u, int p) {
08c9 \triangleright cn_sz[u] = 1;
59dd \triangleright for (int v : adj[u]) if (p != v && cn_sz[v] != -1)
b2f6 \rightarrow cn_sz[u] += cn_getsz(v,u);
37a9 ⊳ return cn_sz[u];
cbb1 }
912c int cn_build (int u, int depth) {
28a0 \rightarrow int siz = cn_getsz(u,u); int w = u;
0168 ⊳ do {
```

#### 3.5 Link Cut Tree

```
d41d //const int N = ; typedef int num;
8db1 int en = 1, p[N], sz[N], pp[N]; bool lzswp[N];
c7d4 int C[N][2]; // {left, right} children
fc41 inline void calc(int u) { // update node given children info
5665 \triangleright sz[u] = sz[C[u][0]] + 1 + sz[C[u][1]];
d41d \triangleright // code here, no recursion
cbb1 }
93d8 inline void unlaze(int u) {
e39f ⊳ if(!u) return;
a2c4 \rightarrow if(lzswp[u]) {
           swap(C[u][0], C[u][1]);
           if(C[u][0]) lzswp[C[u][0]] ^= 1;
8917 ⊳ ⊳
           if(C[u][1]) lzswp[C[u][1]] ^= 1;
53e1 ⊳ ⊳
           lzswp[u] = 0;
cbb1 ⊳ }
cbb1 }
0584 int rotate(int u, int dir) { // pulls C[u][dir] up to u and returns it
05db \rightarrow int v = C[u][dir];
5b77 ⊳ swap(pp[v], pp[u]);
2116 \triangleright C[u][dir] = C[v][!dir];
6c8a \rightarrow if(C[u][dir]) p[C[u][dir]] = u;
ed1d \triangleright C[v][!dir] = u; p[v] = p[u];
b9c1 \rightarrow if(p[v]) C[p[v]][C[p[v]][1] == u] = v;
6967 \triangleright p[u] = v; calc(u); calc(v);
6dc7 ⊳ return v;
cbb1 }
3ca5 void unlz_back(int u) { if(!u) return; unlz_back(p[u]); unlaze(u); }
81a1 void splay(int u) { // pulls node u to root
c46d ⊳ unlz_back(u);
bdd0 ⊳ while(p[u]) {
           int v = p[u], w = p[p[u]];
           int du = (C[v][1] == u);
448e ⊳ ⊳
           if(!w) { rotate(v, du); assert(!p[u]); }
           else {
4e6b ⊳ ⊳
d499 ⊳ ⊳
           \rightarrow int dv = (C[w][1] == v);
4780
               if(du == dv) { rotate(w, dv); assert(C[v][du] == u); rotate(v, du); }
e576 ⊳ ⊳
               else { rotate(v, du); assert(C[w][dv] == u); rotate(w, dv); }
cbb1 ⊳ ⊳
cbb1 ⊳ }
a7c2 int find_sz(int u, int s) { // returns s-th node (0-index)
d9d5 ⊳ unlaze(u);
3939 ⊳ while(sz[C[u][0]] != s) {
da07 \rightarrow if(sz[C[u][0]] < s) { s -= sz[C[u][0]] + 1; u = C[u][1]; }
afa2 \triangleright \triangleright else u = C[u][0];
d9d5 ⊳ ⊳
           unlaze(u);
cbb1 ⊳ }
49a4 ⊳ splay(u); return u;
cbb1 }
498d int new_node() {
a2cc \rightarrow int i = en++; assert(i < N);
bea5 pp[i] = C[i][0] = C[i][1] = p[i] = 0;
0db4 \triangleright lzswp[i] = 0; sz[i] = 1; return i;
```

```
cbb1 }
c538 int access(int u) {
10c3 ⊳ if(!u) return u;
6d13 \triangleright splay(u);
f206 \rightarrow if(int \ v = C[u][1]) \{ p[v] = 0; pp[v] = u; C[u][1] = 0; \}
aaa8 ⊳ calc(u);
566b ⊳ while(pp[u]) {
0068 ⊳ ⊳
           int w = pp[u]; splay(w);
           if(int v = C[w][1]) { p[v] = 0; pp[v] = w; }
33f4 ⊳ ⊳
           C[w][1] = u; p[u] = w; pp[u] = 0; calc(w); splay(u);
cbb1 ⊳
03f4 ⊳ return u;
cbb1 }
0782 int find_root(int u) { // root o u's tree
29bf ⊳ access(u);
3980 \rightarrow while(C[u][0]) { unlaze(u = C[u][0]); }
c607 ⊳ access(u); return u;
cbb1 }
4d88 int get_parent(int u) { // u's parent, rootify might change it
29bf ⊳ access(u);
c6f1 > if(!C[u][0]) return pp[u];
e123 \triangleright unlaze(u = C[u][0]);
323c \triangleright while(C[u][1]) unlaze(u = C[u][1]);
c607 ⊳ access(u); return u;
cbb1 }
c63a void link(int u, int v) { // adds edge from u to v, v must be root
961c → if(find_root(u) == find_root(v)) return;
78b9 ⊳ access(u); access(v);
612a \rightarrow assert(C[v][0] == 0 && pp[v] == 0 && sz[v] == 1); // v must be root
8e1a \triangleright C[u][1] = v; p[v] = u; calc(u);
d41d // XXX cut + rootify require get_parent, cut unlinks u from parent, rootify makes u root
e166 void cut(int u) { access(u); assert(C[u][0]); p[C[u][0]] = 0; C[u][0] = 0; calc(u); }
1cea void rootify(int u) { access(u); lzswp[u] = 1; access(u); }
b59a void init() { en = 1; } // XXX initialize
```

# 3.6 Splay Tree

```
d41d //const int N = ;
d41d //typedef int num;
d41d
576f int en = 1;
37e4 int p[N], sz[N];
c7d4 int C[N][2]; // {left, right} children
abac num X[N];
d41d
d41d // atualize os valores associados aos nos que podem ser calculados a partir dos filhos
8b25 void calc(int u) {
5665 \triangleright sz[u] = sz[C[u][0]] + 1 + sz[C[u][1]];
cbb1 }
d41d
d41d // Puxa o filho dir de u para ficar em sua posicao e o retorna
0584 int rotate(int u, int dir) {
05db \rightarrow int v = C[u][dir];
2116 \triangleright C[u][dir] = C[v][!dir];
6c8a \rightarrow if(C[u][dir]) p[C[u][dir]] = u;
0928 \triangleright C[v][!dir] = u;
c0a7 \triangleright p[v] = p[u];
b9c1 \rightarrow if(p[v]) C[p[v]][C[p[v]][1] == u] = v;
136e \triangleright p[u] = v;
aaa8 ⊳ calc(u);
b6b0 \triangleright calc(v);
6dc7 ⊳ return v;
cbb1 }
d41d
d41d // Traz o no u a raiz
81a1 void splay(int u) {
bdd0 ⊳ while(p[u]) {
```

```
2a84 ⊳ ⊳
            int v = p[u], w = p[p[u]];
1a8a ⊳ ⊳
            int du = C[v][1] == u;
e764 ⊳ ⊳
            if(!w)
76c8 ⊳ ⊳
                rotate(v, du);
4e6b ⊳ ⊳
            else {
d499 ⊳ ⊳
               int dv = (C[w][1] == v);
            ⊳
                if(du == dv) {
9b57 ⊳ ⊳
6c72 ⊳ ⊳
            \triangleright
                    rotate(w, dv);
                ⊳
            \triangleright
76c8 ⊳ ⊳
                    rotate(v, du);
9d97 ⊳ ⊳
                } else {
            \triangleright
76c8 ⊳ ⊳
                    rotate(v, du);
            \triangleright
                \triangleright
6c72 ⊳ ⊳
            \triangleright
                    rotate(w, dv);
cbb1 ⊳ ⊳
                }
cbb1 ⊳ ⊳
            }
cbb1 ⊳ }
cbb1 }
d41d
d41d // retorna um no com valor x, ou outro no se n foi encontrado (n eh floor nem ceiling)
8975 int find_val(int u, num x) {
93fe \triangleright int v = u;
9a3d ⊳ while(u && X[u] != x) {
766a \triangleright \lor v = u;
1b5b \rightarrow if(x < X[u]) u = C[u][0];
a73d ⊳ ⊳
            else u = C[u][1];
cbb1 ⊳ }
3418 \triangleright if(!u) u = v;
6d13 ⊳ splay(u);
03f4 ⊳ return u;
cbb1 }
d41d
d41d // retorna o s-esimo no (0-indexed)
a7c2 int find_sz(int u, int s) {
3939 \triangleright while(sz[C[u][0]] != s) {
7ef0 \rightarrow \mathbf{if}(sz[C[u][0]] < s)  {
2777 \triangleright \triangleright \triangleright s -= sz[C[u][0]] + 1;
6bdb ⊳ ⊳
            b \quad u = C[u][1];
66d9 ⊳ ⊳
            } else u = C[u][0];
cbb1 ⊳ }
6d13 ⊳ splay(u);
03f4 ⊳ return u;
cbb1 }
d41d
d41d // junte duas splays, assume que elementos l <= elementos r
c870 int merge(int 1, int r) {
db1b \rightarrow if(!l \mid | !r) return l + r;
45ba \triangleright while(C[1][1]) 1 = C[1][1];
bab4 ⊳ splay(1);
0258 ⊳ assert(!C[1][1]);
e3ec > C[1][1] = r;
924c p[r] = 1;
f046 ⊳ calc(1);
792f ⊳ return 1;
cbb1 }
d41d
d41d // Adiciona no x a splay u e retorna x
684a int add(int u, int x) {
e29c \triangleright int v = 0;
9d2d \rightarrow while(u) v = u, u = C[u][X[x] >= X[u]];
f257 \rightarrow if(v) \{ C[v][X[x] >= X[v]] = x; p[x] = v; \}
0b6f \triangleright splay(x);
ea56 ⊳ return x;
cbb1 }
d41d
d41d // chame isso 1 vez no inicio
ca2f void init() {
0cee ▷ en = 1;
cbb1 }
d41d
d41d // Cria um novo no
```

```
3e8b int new_node(num val) {
cecb | int i = en++;
9c38 | assert(i < N);
9029 | C[i][0] = C[i][1] = p[i] = 0;
02c8 | sz[i] = 1;
4281 | X[i] = val;
d9a5 | return i;
cbb1 }</pre>
```

# 4 Strings

#### 4.1 Suffix Tree

```
4623 namespace sf {
d41d // const int NS = ; const int N = * 2;
1506 int cn, cd, ns, en = 1, lst;
f48b string S[NS]; int si = -1;
08ad vector<int> sufn[N]; // sufn[si][i] no do sufixo S[si][i...]
3c9e struct node {
a322 ⊳ int 1, r, si, p, suf;
d3ca ⊳ map<char, int> adj;
499b \rightarrow node() : 1(0), r(-1), suf(0), p(0) {}
2a9f \rightarrow node(int L, int R, int S, int P) : 1(L), r(R), si(S), p(P) {}
a577 \triangleright inline int len() { return r - 1 + 1; }
48b2 | inline int operator[](int i) { return S[si][1 + i]; }
9eae → inline int& operator()(char c) { return adj[c]; }
fbe2 } t[N];
ea71 inline int new_node(int L, int R, int S, int P) { t[en] = node(L, R, S, P); return en++; }
e33b void add_string(string s) {
9a02 \rightarrow s += '$'; S[++si] = s; sufn[si].resize(s.size() + 1); cn = cd = 0;
c5eb \rightarrow int i = 0; const int n = s.size();
f90a \rightarrow for(int j = 0; j < n; j++)
            for(; i <= j; i++) {</pre>
fb3e ⊳ ⊳
               if(cd == t[cn].len() \&\& t[cn](s[j])) { cn = t[cn](s[j]); cd = 0; }
8d90 ⊳ ⊳
465b ⊳ ⊳
               if(cd < t[cn].len() && t[cn][cd] == s[j]) {
c4d2 ⊳ ⊳
                   cd++;
ce02 ⊳ ⊳
           \triangleright
               \triangleright
                   if(j < s.size() - 1) break;
4e6b ⊳ ⊳
           \triangleright
               \triangleright
                   else {
aafd ⊳ ⊳
                       if(i) t[lst].suf = cn;
               \triangleright
                   ⊳
ac68 ⊳ ⊳
                       for(; i <= j; i++) { sufn[si][i] = cn; cn = t[cn].suf; }</pre>
           \triangleright
cbb1 ⊳ ⊳ ⊳
7ced ▷ ▷ } else if(cd == t[cn].len()) {
0a2a \triangleright \triangleright \triangleright \quad sufn[si][i] = en;
0467 \triangleright \triangleright \triangleright  if(i) t[lst].suf = en; lst = en;
aff4 ⊳ ⊳ ⊳
                   t[cn](s[j]) = new_node(j, n - 1, si, cn);
02c2 ⊳ ⊳ ⊳ ⊳
                   cn = t[cn].suf; cd = t[cn].len();
9d97 ▷ ▷ | else {
f287 \triangleright \triangleright \triangleright \vdash int mid = new_node(t[cn].l, t[cn].l + cd - 1, t[cn].si, t[cn].p);
12ed ⊳ ⊳ ⊳
                   t[t[cn].p](t[cn][0]) = mid;
5201 ▷ ▷ ▷ ▷
                   if(ns) t[ns].suf = mid;
0467 ⊳ ⊳ ⊳
                   if(i) t[lst].suf = en; lst = en;
                   sufn[si][i] = en;
0a2a ⊳ ⊳ ⊳
cb00 ⊳ ⊳
                   t[mid](s[j]) = new_node(j, n - 1, si, mid);
           \triangleright
7bfa ⊳ ⊳
           \triangleright
                   t[mid](t[cn][cd]) = cn;
07fe ⊳ ⊳
                   t[cn].p = mid; t[cn].l += cd; cn = t[mid].p;
                   int g = cn? j - cd : i + 1; cn = t[cn].suf;
5967 ⊳ ⊳
c197 ⊳ ⊳
                   while(g < j \&\& g + t[t[cn](S[si][g])].len() <= j) {
6fea ⊳ ⊳
                       cn = t[cn](S[si][g]); g += t[cn].len();
cbb1 ⊳ ⊳
                   if(g == j) { ns = 0; t[mid].suf = cn; cd = t[cn].len(); }
71c3 ⊳ ⊳
                   else { ns = mid; cn = t[cn](S[si][g]); cd = j - g; }
f90d ⊳ ⊳
cbb1 ⊳ ⊳
cbb1 ⊳ ⊳
cbb1 ⊳ }
2145 };
```

#### 4.2 Z-function

```
2a61 void Z(char s[], int n, int z[]) { // z[i] = |lcp(s,s[i..n])|
fc15 > for(int i = 1, m = -1; i < n; i++) {
d69b > z[i] = (m != -1 && m + z[m] >= i)?min(m + z[m] - i, z[i - m]):0;
8a63 > while (i + z[i] < n && s[i + z[i]] == s[z[i]]) z[i]++;
bbe8 > if (m == -1 || i + z[i] > m + z[m]) m = i;
cbb1 > }
cbb1 }
```

#### 4.3 Manacher

```
d41d // max odd pali cent on i: s[i - M[2 * i] / 2..i + M[2 * i] / 2]
d41d // max even pali cent on [i,i+1]: s[i + 1 - (M[2*i+1] + 1) / 2...i + (M[2*i+1] + 1) / 2] (if M[2*i+1] != 0)
2a2b void manacher(char s[], int n, char t[], int M[]) { // t and M should have size 2*n
1df6 \rightarrow for(int i = 0; i < n; i++) t[2 * i] = s[i];
9866 \circ for(int i = 0; i < n - 1; i++) t[2 * i + 1] = 1; // XXX s should not contain 1
5d62 \rightarrow n = 2 * n - 1;
9038 \rightarrow for(int i = 0, m = -1; i < n; i++) {
b39f ⊳ ⊳
          M[i] = 0;
e618 ⊳ ⊳
           if (m != -1 \& m + M[m] >= i) M[i] = min(m + M[m] - i, M[2 * m - i]);
           for (; i + M[i] + 1 < n & i - M[i] - 1 >= 0 & t[i + M[i] + 1] == t[i - M[i] - 1]; M[i] ++);
09a9 ⊳ ⊳
           if (m == -1 || i + M[i] > m + M[m]) m = i;
086c ⊳ ⊳
cbb1 ⊳ }
cbb1 }
```

## 5 Math

#### 5.1 FFT

```
5f83 typedef complex<double> cpx; const double pi = acos(-1.0);
d41d // DFT if type = 1, IDFT if type = -1
d41d // If you are multiplying, remember to let EACH vector with n >= sum of degrees of both polys
d41d // n is required to be a power of 2
d822 void FFT(cpx v[], cpx ans[], int n, int type, int p[]) \{ // p[n] \}
e228 \rightarrow assert(!(n & (n - 1))); int i, sz, o; p[0] = 0;
6be6 \rightarrow for(i = 1; i < n; i++) p[i] = (p[i >> 1] >> 1) | ((i & 1)? (n >> 1) : 0); // repetition can be avoided
d48c \rightarrow for(i = 0; i < n; i++) ans[i] = v[p[i]];
abc7 \rightarrow for(sz = 1; sz < n; sz <<= 1) {
           const cpx wn(cos(type * pi / sz), sin(type * pi / sz));
3d36 ⊳ ⊳
1728 ⊳ ⊳
           for(o = 0; o < n; o += (sz << 1)) {
dfb7 ⊳ ⊳
           \triangleright
               cpx w = 1;
c854 ⊳ ⊳
           \triangleright
               for(i = 0; i < sz; i++) {
d1db ⊳ ⊳
           \triangleright
                  const cpx u = ans[o + i], t = w * ans[o + sz + i];
3f57 ⊳ ⊳
                   ans[o + i] = u + t;
e817 ⊳ ⊳
                   ans[o + i + sz] = u - t;
                   w *= wn;
d2cd ⊳ ⊳
           \triangleright
cbb1 ⊳ ⊳
               }
cbb1 ⊳ ⊳
cbb1 ⊳ }
cde2 \rightarrow if(type == -1) for(i = 0; i < n; i++) ans[i] /= n;
cbb1 }
```

#### 5.2 Discrete FFT

```
c9bc inline num s_mod (ll x, ll p) {

02ae → if (x >= p) return x-p;

6d8b → else if (x < 0) return x += p;

ea56 → return x;

cbb1 }

6554 num fexp (ll x, int e, num p) {

ef50 → ll r = 1;

6244 → for (; e; x = (x*x)%p, e >>= 1) if (e&1) r = (r*x)%p;

4c1f → return r;

cbb1 }

55a7 void rou (int n, int p, num w[]) { // w[i] = (n-th root of unity of p)^i
```

```
df57 \bowtie w[0] = 1; bool ok = 0;
c238 \rightarrow for (num i = 2; !ok && i < p; i++) {
1145 \triangleright ok = 1;
4d9f ⊳ ⊳
             for (11 j = 2; ok && j*j \le p-1; j++)
155e ⊳ ⊳
            \rightarrow if ((p-1)%j == 0)
8ee4 \rightarrow \rightarrow \rightarrow ok = !(fexp(i,j,p) == 1 || fexp(i,(p-1)/j,p) == 1);
8fe3 \rightarrow if (ok) w[1] = fexp(i,(p-1)/n,p);
cbb1 ⊳ }
1862 ⊳ assert(ok);
4dd2 \Rightarrow  for (int i = 2; i <= n; i++)
6580 \triangleright w[i] = (ll(w[i-1])*w[1])%p;
cbb1 }
03fd void fft_finite (num v[], num ans[], int n, int type, num p, int pr[], num w[]) { // pr[n], w[n]
4794 \triangleright assert(!(n \& (n-1)));
13c0 \rightarrow rou(n,p,w); 11 invn = fexp(n,p-2,p); // repetition can be avoided
b3e7 \triangleright if (type == -1) reverse(w, w+n+1);
4fc1 \Rightarrow pr[0] = 0;
a8cf \ \ for (int i = 1; i < n; i++) \ pr[i] = ((pr[i>>1] >> 1) | ((i&1)?(n>>1):0)); // repetition can be avoided
b514 \rightarrow for (int i = 0; i < n; i++) ans[i] = v[pr[i]];
f5fd \triangleright for (int sz = 1; sz < n; sz <<= 1) {
849c \rightarrow for (int o = 0; o < n; o += (sz<<1)) {
8873 \triangleright \triangleright for (int i = 0; i < sz; i++) {
7a0c \triangleright \triangleright \triangleright \triangleright  const num u = ans[o+i], t = (w[(n/sz/2)*i]*ans[o+sz+i])%p;
                     ans[o+i] = s_mod(u+t,p);
8881 > > >
                     ans[o+i+sz] = s_mod(u-t,p);
cbb1 \;\; \triangleright \;\;\; \triangleright \;\;\; \}
cbb1 ⊳ ⊳
cbb1 ⊳ }
f8e2 \rightarrow if(type == -1) for(int i = 0; i < n; i++) ans[i] = (ans[i]*invn)%p;
cbb1 }
d41d
```

## 5.3 Linear System Solver

```
d41d //const int N = ;
d41d
46cc double a[N][N];
3793 double ans[N];
d41d
d41d // sum(a[i][j] * x_j) = a[i][n] para 0 <= i < n
d41d // guarda a resposta em ans e retorna o determinante de a
c42a double solve(int n) {
f99b ⊳ double det = 1;
6033 \rightarrow for(int i = 0; i < n; i++) {
0268 \triangleright \triangleright int mx = i;
197a ⊳ ⊳
            for(int j = i + 1; j < n; j++)
b83d ⊳ ⊳
           if(abs(a[j][i]) > abs(a[mx][i]))
672f ⊳ ⊳
           \triangleright \bowtie mx = j;
28c6 ⊳ if(i != mx) {
e83f ⊳ ⊳
           \rightarrow swap_ranges(a[i], a[i] + n + 1, a[mx]);
0143 ⊳ ⊳
                det = -det;
cbb1 ⊳ ⊳
997e ▷ ▷ if(abs(a[i][i]) < 1e-6); // singular matrix
2f40 b det *= a[i][i];
94fe \rightarrow for(int j = i + 1; j < n; j++) {
12fe \rightarrow \rightarrow for(int k = i + 1; k \le n; k++)
ea32 \rightarrow a[j][k] -= (a[j][i] / a[i][i]) * a[i][k];
efbc ⊳ ⊳ ⊳
               a[j][i] = 0;
cbb1 ▷ ▷ }
cbb1 ⊳ }
45bd \rightarrow for(int i = n - 1; i >= 0; i--) {
7634 \Rightarrow ans[i] = a[i][n];
197a \triangleright \triangleright for(int j = i + 1; j < n; j++)
9b00 \triangleright \triangleright \Rightarrow ans[i] -= a[i][j] * ans[j];
35e5 ⊳ ⊳
           ans[i] /= a[i][i];
cbb1 ⊳ }
7a32 ⊳ return det;
cbb1 }
```

# 5.4 Simplex

```
d41d //typedef long double dbl;
bec0 const dbl eps = 1e-6;
d41d //const int N = , M = ;
d41d
79ee struct simplex {
0643 \rightarrow \text{int } X[N], Y[M];
6b50 \rightarrow dbl A[M][N], b[M], c[N];
e268 ⊳ dbl ans:
14e0 ⊳ int n, m;
a00d ⊳ dbl sol[N];
c511 ⊳ void pivot(int x,int y){
eb91 \triangleright swap(X[y], Y[x]);
c057 \triangleright b[x] /= A[x][y];
8300 \rightarrow for(int i = 0; i < n; i++)
7f61 ▷ ▷ if(i != y)
d311 \triangleright \triangleright \triangleright A[x][i] /= A[x][y];
3fa2 \rightarrow A[x][y] = 1. / A[x][y];
94f7 \rightarrow for(int i = 0; i < m; i++)
a325 \triangleright \triangleright if(i != x && abs(A[i][y]) > eps) {
6856 \; \triangleright \quad \triangleright \quad \triangleright \quad b[i] \; \text{-= A[i][y] * b[x];}
f90a \triangleright \triangleright \triangleright for(int j = 0; j < n; j++)
6739 \triangleright \triangleright \triangleright \vdash if(j != y)
             8c78 ⊳ ⊳
                              A[i][j] -= A[i][y] * A[x][j];
             ▷ ▷
▷ }
e112 ⊳ ⊳
cbb1 ⊳ ⊳
8c7e \rightarrow ans += c[y] * b[x];
8300 \triangleright for(int i = 0; i < n; i++)
7f61 ▷ ▷ if(i != y)
bec1 \triangleright \triangleright \triangleright c[i] -= c[y] * A[x][i];
0997 \triangleright c[y] = -c[y] * A[x][y];
cbb1 ⊳ }
d41d
d41d ▷ // maximiza sum(x[i] * c[i])
d41d ⊳ // sujeito a
d41d \rightarrow // sum(a[i][j] * x[j]) \leftarrow b[i] para 0 \leftarrow i < m (Ax \leftarrow b)
d41d \rightarrow // x[i] >= 0 para 0 <= i < n (x >= 0)
d41d ▷ // (n variaveis, m restricoes)
d41d \triangleright // guarda a resposta em ans e retorna o valor otimo
59d9 ⊳ dbl solve(int n, int m) {
1f59 \rightarrow this->n = n; this->m = m;
f1bf ⊳ ⊳
              ans = 0.;
b1c6 ⊳ ⊳
              for(int i = 0; i < n; i++) X[i] = i;
3e36 ⊳ ⊳
             for(int i = 0; i < m; i++) Y[i] = i + n;
6679 ⊳ ⊳
             while(true) {
ee39 ⊳ ⊳
             int x = min_element(b, b + m) - b;
             \triangleright if(b[x] >= -eps)
988b ⊳ ⊳
c2be ▷ ▷ ▷ break;
49a2 \rightarrow int y = find_if(A[x], A[x] + n, [](dbl d) { return d < -eps; }) - A[x];
6f8c \triangleright \triangleright if(y == n) throw 1; // no solution
7fb4 ▷ ▷ ▷ pivot(x, y);
cbb1 ▷ ▷ }
6679 ⊳ while(true) {
f802 \triangleright \triangleright \vdash int y = max_element(c, c + n) - c;
b7b6 \triangleright \triangleright if(c[y] \le eps) break;
d6b5 \triangleright \triangleright  int x = -1;
06d7 \triangleright \triangleright \land db1 mn = 1. / 0.;
94f7 \triangleright \triangleright for(int i = 0; i < m; i++)
5877 \triangleright \triangleright \vdash \mathbf{if}(A[i][y] > eps && b[i] / A[i][y] < mn)
832b \triangleright \triangleright \triangleright \triangleright mn = b[i] / A[i][y], x = i;
ff22 \triangleright \triangleright if(x == -1) throw 2; // unbounded
7fb4 ⊳ ⊳
             pivot(x, y);
cbb1 ⊳ ⊳
d094 \triangleright memset(sol, 0, sizeof(dbl) 94f7 \triangleright for(int i = 0; i < m; i++)
             memset(sol, 0, sizeof(dbl) * n);
cff4 ⊳ ⊳
             \rightarrow if(Y[i] < n)
09d7 \triangleright \triangleright \triangleright sol[Y[i]] = b[i];
```

```
ba75 | return ans;
cbb1 | }
2145 };
```

#### 5.5 Zeta

```
d41d // To calculate c[i] = sum (a[j] * b[k]) st j | k == i
d41d // Use c = itf(tf(a) * tf(b)), where * is element by element multiplication
d41d
d41d // Common transformations and inverses:
d41d // OR - (a, b) \Rightarrow (a, a + b) | (a, b) \Rightarrow (a, b - a)
d41d // AND - (a, b) \Rightarrow (a + b, b) | (a, b) \Rightarrow (a - b, b)
d41d // XOR - (a, b) \Rightarrow (a + b, a - b) | (a, b) \Rightarrow ((a + b) / 2, (a - b) / 2)
d41d //typedef ll num;
d41d
d41d // Transform a inplace (OR), initially l = 0, r = 2^n - 1
10ea void tf(num a[], int l, int r) {
8ce4 \rightarrow if(1 == r) return;
ee49 \rightarrow int m = (1 + r) / 2;
b34b ⊳ tf(a, 1, m);
ba7b \rightarrow tf(a, m + 1, r);
1e28 \rightarrow for(int i = 1; i \le m; i++)
95f6 ⊳ ⊳
           a[m + 1 + (i - 1)] += a[i];
cbb1 }
d41d
d41d // Inverse transforms a inplace (OR), initially l = 0, r = 2^n - 1
0772 void itf(num a[], int 1, int r) {
8ce4 \triangleright if(1 == r) return;
ee49 \rightarrow int m = (1 + r) / 2;
1e28 \rightarrow for(int i = 1; i \le m; i++)
            a[m + 1 + (i - 1)] -= a[i];
27fa ⊳ ⊳
5001 \rightarrow itf(a, 1, m);
ebd6 \rightarrow itf(a, m + 1, r);
cbb1 }
```

# 5.6 Zeta Disjoint Or

```
d41d //const int K = ;
d41d //typedef ll num;
d41d
d41d // overwrites b such that b[i] = sum (a[j]) such that (j | i) == i and popcount(j) = k
a6e5 void tf(int k, num a[], num b[], int l, int r) {
9fae b if(1 == r) return (void) (b[1] = a[1] * (_builtin_popcount(1) == k));
ee49 \rightarrow int m = (1 + r) / 2;
6d7f ⊳ tf(k, a, b, 1, m);
33d9 \rightarrow tf(k, a, b, m + 1, r);
1e28 \rightarrow for(int i = 1; i \le m; i++)
a168 \rightarrow b[m + 1 + (i - 1)] += b[i];
cbb1 }
d41d
d41d // Ranked mobius transform (transform above for all k)
29b2 void tf(int k, num a[], num b[K+1][1 << K]) {
2380 \rightarrow for(int i = 0; i <= k; i++)
0b85 \rightarrow tf(i, a, b[i], 0, (1 << k) - 1);
cbb1 }
d41d
d41d // Convolutes two transforms. c[j][i] = sum(a[g][i] * b[k - g][i]) for 0 <= g <= j
f78d void conv(int k, num a[K+1][1 << K], num b[K+1][1 << K], num c[K+1][1 << K]) {
55df > for(int j = 0; j \le k; j++)
          for(int i = 0; i < (1 << k); i++) {
9ccb ⊳ ⊳
5b1b \triangleright \triangleright
               c[j][i] = 0;
               for(int g = 0; g \le j; g++)
b8c7 ⊳ ⊳
                  c[j][i] += a[g][i] * b[j - g][i];
cbb1 ⊳
           }
cbb1 }
d41d
```

```
d41d // Inverse of ranked mobius transform for k
0772 void itf(num a[], int 1, int r) {
8ce4 \rightarrow if(1 == r) return;
ee49 \rightarrow int m = (1 + r) / 2;
1e28 \rightarrow for(int i = 1; i <= m; i++)
27fa \rightarrow a[m + 1 + (i - 1)] -= a[i];
5001 \rightarrow itf(a, 1, m);
ebd6 \rightarrow itf(a, m + 1, r);
cbb1 }
d41d
d41d // Inverse of ranked mobius transform for all k
dde8 void itf(int k, num a[K+1][1 << K], num b[]) {
85c1 \rightarrow for(int j = 0; j <= k; j++) {
            itf(a[j], 0, (1 << k) - 1);
2341 ⊳ ⊳
252d ⊳ ⊳
            for(int i = 0; i < (1 << k); i++)
8363 .
           b if(__builtin_popcount(i) == j)
e738 ⊳ ⊳
           \triangleright \triangleright b[i] = a[j][i];
cbb1 ⊳ }
cbb1 }
d41d
d41d // use when you want to calculate c[i] = sum (a[j] * b[k]) such that (j | k) == i and (j & k) = 0
d41d // example use (if the size of a and b is (1 << k))
d41d // tf(k, a, a_{-});
d41d // tf(k, b, b_);
d41d // conv(k, a_, b_, ans);
d41d // itf(k, ans, c);
d41d // the answer will now be stored in c
```

#### 5.7 Miller-Rabin

```
a288 llu llrand() { llu a = rand(); a<<= 32; a+= rand(); return a;}
0a9c int is_probably_prime(llu n) {
8dbf
        if (n <= 1) return 0;
2373
        if (n <= 3) return 1;
7de1
        llu s = 0, d = n - 1;
66b4
        while (d % 2 == 0) {
90f4
           d/= 2; s++;
cbb1
        for (int k = 0; k < 64; k++) {
6b3a
12c0
           llu \ a = (llrand() \% (n - 3)) + 2;
dc17
           llu x = exp_mod(a, d, n);
1181
           if (x != 1 \&\& x != n-1) {
f0ea
               for (int r = 1; r < s; r++) {
708d
                   x = mul_mod(x, x, n);
61d9
                  if (x == 1)
bb30
                      return 0;
68b2
                   if (x == n-1)
c2be
                      break;
cbb1
34hc
               if (x != n-1)
hh30
                  return 0;
cbb1
           }
cbb1
        }
6a55
        return 1;
cbb1 }
```

#### 5.8 Pollard-Rho

```
4d51 \triangleright  } while (d == 1);
be24 ⊳ return d;
cbb1 }
4722 map <llu,int> F;
6b0e void factor(llu n) {
e7f6 \rightarrow if (n == 1)
505b ⊳ ⊳
            return;
1b21 > if (is_probably_prime(n)) {
d64d ⊳ ⊳
             F[n]++;
505b \triangleright \triangleright
             return;
cbb1 ⊳
3462 \triangleright 11u d = rho(n);
3ad0 ▶ factor(d);
d6f6 ⊳ factor(n/d);
cbb1 }
```

# 6 Old Solutions

# 6.1 Ceiling Function

```
2b74 #include <bits/stdc++.h>
ca41 using namespace std;
35b1 #define fst first
6507 #define snd second
ad11 typedef long long 11;
ff0b typedef pair<int, int> pii;
efel #define pb push_back
924e #define for_tests(t, tt) int t; scanf("%d", &t); for(int tt = 1; tt <= t; tt++)
5a83 const 11 modn = 10000000007;
cbba inline 11 mod(11 x) { return x % modn; }
d41d
c2b3 const int N = 112345;
3606 int L[N], R[N], v[N];
576f int en = 1;
d41d
7296 int add(int r, int x) {
       if(r == 0) {
9dc6
d6f0
           r = en++;
b557
           v[r] = x;
4c1f
           return r;
cbb1
       }
8b66
       if(x < v[r])
           L[r] = add(L[r], x);
dba8
2954
bb73
           R[r] = add(R[r], x);
4c1f
       return r;
cbb1 }
d41d
9c15 string get_str(int r) {
239b
       if(r == 0) return "";
       return "(" + get_str(L[r]) + "," + get_str(R[r]) + ")";
2ec6
cbb1 }
d41d
0114 string s[112345];
d41d
e8d7 int main() {
762a
       int n, k, i, j, x;
        scanf("%d %d", &n, &k);
e459
       for(i = 0; i < n; i++) {
3f35
           int root = 0;
caa4
           for(j = 0; j < k; j++) {
fb39
e456
               scanf("%d", &x);
95b4
               root = add(root, x);
cbb1
6c08
           s[i] = get_str(root);
cbb1
       }
60eb
       sort(s, s + n);
```

```
b8ba printf("%d\n", int(unique(s, s + n) - s)); cbb1 }
```

#### 6.2 Secret Chamber at Mount Rushmore

```
2b74 #include <bits/stdc++.h>
ca41 using namespace std;
35b1 #define fst first
6507 #define snd second
ad11 typedef long long 11;
ff0b typedef pair<int, int> pii;
efel #define pb push_back
924e #define for_tests(t, tt) int t; scanf("%d", &t); for(int tt = 1; tt <= t; tt++)
5a83 const 11 modn = 1000000007;
cbba inline 11 mod(11 x) { return x % modn; }
d41d
a8d9 char adj[256][256];
38f1 char seen[256];
d41d
4674 void go(char p, char u) {
2ac0
        if(seen[u] == p) return;
        seen[u] = p;
0886
6c58
        adj[p][u] = 1;
9d57
        for(int v = 'a'; v <= 'z'; v++)</pre>
111a
           if(adj[u][v])
1ac3
               go(p, v);
cbb1 }
d41d
aba0 char s[1123], t[1123];
d41d
e8d7 int main() {
       int i, m, n, j;
94c3
        scanf("%d %d", &m, &n);
7676
        for(i = 0; i < m; i++) {</pre>
cc5c
37b2
           char a, b;
64f2
           scanf(" %c %c", &a, &b);
d7dd
           adj[a][b] = 1;
cbb1
        }
        for(i = 'a'; i <= 'z'; i++)</pre>
419d
c6b2
           go(i, i);
3£35
        for(i =0 ; i < n; i++) {
96b1
           scanf("%s %s", s, t);
abae
           if(strlen(s) != strlen(t)) { puts("no"); continue; }
           for(j = 0; s[j]; j++)
41d3
a92d
               if(!adj[s[j]][t[j]])
c2be
                   break;
85c9
           if(s[j]) puts("no");
b8ef
           else puts("yes");
cbb1
cbb1 }
```

# 6.3 Need for Speed

```
2b74 #include <bits/stdc++.h>
ca41 using namespace std;
35b1 #define fst first
6507 #define snd second
ad11 typedef long long ll;
ff0b typedef pair<int, int> pii;
efe1 #define pb push_back
924e #define for_tests(t, tt) int t; scanf("%d", &t); for(int tt = 1; tt <= t; tt++)
5a83 const ll modn = 10000000007;
cbba inline ll mod(ll x) { return x % modn; }
d41d
c49e const int N = 1123;
5319 int d[N], s[N];</pre>
```

```
e8d7 int main() {
a1d4
        int n, t, i;
2f9a
        scanf("%d %d", &n, &t);
a2ed
       long double 1 = -2e7, r = 1502;
e668
        for(i = 0; i < n; i++) scanf("%d %d", &d[i], &s[i]);
        for(int x = 0; x < 200; x++) {
6c58
8591
           long double c = (1 + r) / 2;
cb4e
           long double tot = 0;
3£35
           for(i = 0; i < n; i++) {
31b2
               long double ss = s[i] - c;
05c3
               if(ss <= 0) break;</pre>
f7ab
               tot += d[i] / ss;
cbb1
           if(tot >= t || i < n) r = c;
e2ae
0399
           else 1 = c;
cbb1
e11b
        printf("%.10f\n", -double(1));
d41d
cbb1 }
```

# 6.4 Amalgamated Artichokes

```
2b74 #include <bits/stdc++.h>
ca41 using namespace std;
d41d
e8d7 int main() {
79eb
       int p, a, b, c, d, n;
       scanf("%d %d %d %d %d %d", &p, &a, &b, &c, &d, &n);
1a4f
       double mx = -1. / 0.;
97e4
e9cc
       double ans = 0;
       for(int i = 1; i \le n; i++) {
78ac
           double x = p * (sin(a * i + b) + cos(c * i + d) + 2);
3ab3
314d
           mx = max(mx. x):
c387
           ans = max(ans, mx - x);
cbb1
       printf("%.10f\n", ans);
3ccd
cbb1 }
```

#### 6.5 Low Power

```
2b74 #include <bits/stdc++.h>
ca41 using namespace std;
d41d
ad11 typedef long long 11;
70cf typedef pair<ll, ll> pii;
efel #define pb push_back
d41d
4d42 const int N = 1e6+7;
dca6 int n, k;
5e7a ll a[N];
d41d
91a0 bool solve (ll d) {
d179 \rightarrow 11 s = 0, m = n;
22f9 \triangleright for (int i = 0; m && i < 2*n*k - 1; i++) {
a7bf \rightarrow if (a[i+1] - a[i] \le d) {
76b4 ⊳ ⊳
              m--;
           ⊳
0dd5 ⊳ ⊳
               i++;
              s += 2*(k-1);
           } else if (!s) return 0;
b579 ⊳ ⊳
5e99 ⊳ ⊳
           else s--;
cbb1 ⊳ }
6a55 ⊳ return 1;
cbb1 }
d41d
e8d7 int main () {
e459 ⊳ scanf("%d %d",&n, &k);
```

# 7 Anotações

# 7.1 Intersecção de Matróides

Sejam  $M_1=(E,I_1)$  e  $M_2=(E,I_2)$  matróides. Então  $\max_{S\in I_1\cap I_2}|S|=\min_{U\subseteq E}r_1(U)+r_2(E\setminus U).$ 

#### 7.2 Möebius

Se 
$$F(n) = \sum_{d|n} f(d)$$
, então  $f(n) = \sum_{d|n} \mu(d)F(n/d)$ .

#### 7.3 Burnside

Seja  $A: GX \rightarrow X$  uma ação. Defina:

- w := número de órbitas em X.
- $S_x := \{g \in G \mid g \cdot x = x\}$
- $\bullet \ \ F_g := \{x \in X \mid g \cdot x = x\}$

Então 
$$w = \frac{1}{|G|} \sum_{x \in X} |S_x| = \frac{1}{|G|} \sum_{g \in G} |F_g|.$$

#### 7.4 Landau

Existe um torneio com graus de saída  $d_1 \le d_2 \le ... \le d_n$  sse:

- $d_1 + d_2 + \ldots + d_n = \binom{n}{2}$
- $d_1 + d_2 + \ldots + d_k \ge {k \choose 2}$   $\forall 1 \le k \le n$ .

Para construir, fazemos 1 apontar para 2, 3, ...,  $d_1 + 1$  e seguimos recursivamente.

#### 7.5 Erdös-Gallai

Existe um grafo simples com graus  $d_1 \ge d_2 \ge ... \ge d_n$  sse:

- $d_1 + d_2 + ... + d_n$  é par
- $\sum_{i=1}^{k} d_i \le k(k-1) + \sum_{i=k+1}^{n} \min(d_i, k) \quad \forall 1 \le k \le n.$

Para construir, ligamos 1 com 2, 3, ...,  $d_1$  + 1 e seguimos recursivamente.

#### 7.6 Gambler's Ruin

Em um jogo no qual ganhamos cada aposta com probabilidade p e perdemos com probabilidade q := 1 - p, paramos quando ganhamos B ou perdemos A. Então Prob(ganhar B) =  $\frac{1 - (p/q)^B}{1 - (p/q)^{A+B}}$ .

## 7.7 Extra

• Fib(x + y) = Fib(x + 1)Fib(y) + Fib(x)Fib(y - 1)