CS 221 Analysis of Algorithms Homework

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*All growth functions must be in simplified t(n) = \_\_\_\_ format with only* ***one*** *constant factor,* ***one*** *n factor, etc. Runtime order must be presented in proper big-O notation. All writing is required to be proofread for professional-quality grammar, spelling, capitalization, punctuation, complete sentences, etc.*

*Empirical results to compare with your predicted results come from the pre-compiled AoATester class given with the assignment. Run AoATester directly from the command line. AoATester configures an array of integers appropriate for the specified method and use case and reports the actual number of executed statements. The first command line argument specifies the method to test. The second argument specifies the use case. The optional third argument specifies the length of the array, which must be a positive integer. For the minimum statements use case, the third argument is ignored, even if a value is given. For other use cases, the length defaults to 100 unless specified otherwise.  
AoATester usage:*

$ java AoATester <find|replaceAll|sortIt> <min|best|worst|expected> [array length]

# Algorithm: find()

## Minimum Statements, Constant Factor

What statements are executed in a call to find() before reaching a return statement when the array size is zero (n == 0)? (Do not count the initialization of method arguments or return statements.) What is t(0) for find(), the minimum cost and the constant factor?

If the array size was 0, the for loop would initialize int i and check if that is less than array length, which would be false and that would be the end of the method. So, 2 statements happen no matter what.

Predicted t(0) = 2

### Run: AoATester find min

What is your prediction for t(0)? How many statements does the test report? How do the results compare to your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results?

Predicted t(0) Statements: 2

AoATester find min Statements: 2

AoATester returned 2 as the statement count as predicted, so I think my analysis for minimum statements is correct.

Final t(0) = 2

## Best Case Scenario

Assuming a large array size n and the target element is located at index 0, what statements are executed before the index is returned? What is the best case growth function t(n) under these conditions?

The for loop is going to iterate once for every index in the array. So, whatever happens in the loop is going to be multiplied by the size of the array, which is n for this algorithm.

There are 2 statements that happen if the array length is zero as seen above. If there is an array length, n, then there is an if statement that checks if the integer in the array index is equal to the integer value entered. That will return true if the target element is at index 0.

Predicted tbest(n) = 2 + n(4) = 3n + 2

### Run: AoATester find best 100

What is your predicted number of statements when n == 100? How does the number of reported statements align with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What do you need to modify about your analysis to better align with the empirical results?

Predicted tbest(100) Statements: 302

AoATester find best 100 Statements: 3

The problem with my prediction is that I found the worst-case scenario, when reading the first sentence of best-case scenario I found “Assuming a large array of size n and the target element is located at index 0”. That would mean the return statement “return i” would come before the for loop goes to the next line with i++. So, the three statements that happen are initializing i = 0, then checking if i is less than array length, which would return true, then checking if the integer in the index of the array is equal to the integer value entered which would return true. So, in total there are three statements done.

Final tbest(n) = n + 2

## Worst Case Scenario

Assuming a large array size n, what would be necessary such that the method returns -1? How many times does the loop iterate? What statements are executed in each loop iteration? What is the worst case growth function t(n) under these conditions?

Predicted tworst(n) =

### Run: AoATester find worst 100

What is your predicted number of statements when n == 100? How does the number of reported statements for the actual worst case compare to your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results?

Predicted tworst(100) Statements:

AoATester find worst 100 Statements:

Final tworst(n) =

## Expected Average Case Scenario

Assuming a randomly ordered array of unique elements and the target element is in the array, where would a target element be located **on average**? What is the expected average number of loop iterations if this is the case? What statements are executed in each complete loop iteration? Are there any loop statements that will **not** be executed when the target is found? What is the expected average growth function t(n) under these conditions?

Predicted texp(n) =

### Run: AoATester find expected 100

What is your predicted number of statements when n == 100? How does the average number of statements to find all elements align with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results?

Predicted texp(100) Statements:

AoATester find expected 100 Statements:

Final texp(n) =

## Order

What is the runtime order (big-O) of find()?

O()

# Algorithm: replaceAll()

## Minimum Statements, Constant Factor

What statements are executed in a call to replaceAll() when the array size is zero (n == 0)? Do not overlook statements executed in find() or the assignment of its return value. So what is t(0) for replaceAll(), the minimum cost and constant factor?

Predicted t(0) =

### Run: AoATester replaceAll min

What is your predicted number of statements when n == 0? How do the test results compare to your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results?

Predicted t(0) Statements:

AoATester replaceAll min Statements:

Final t(0) =

## Best Case Scenario

Assuming a large array size n, what would cause the replaceAll() while loop to never iterate? What would be the cost of the first find() call? What statements are executed in replaceAll(), itself? What is the total best case growth function t(n) under these conditions?

Predicted tbest(n) =

### Run: AoATester replaceAll best 100

What is your predicted number of statements when n == 100? How does the number of reported statements compare with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What do you need to modify about your analysis to better align with the empirical results?

Predicted tbest(100) Statements:

AoATester replaceAll best 100 Statements:

Final tbest(n) =

## Worst Case Scenario

Assuming n is large, all values in the array equal oldValue, and newValue does not equal oldValue, how many times will the while loop iterate? What is the cost of the first call to find()? What is the cost of the last call to find()? What is the average cost of a find() call within the while loop? What other statements are executed in every iteration of the while loop? What is the total worst case growth function t(n) under these conditions?

Predicted tworst(n) =

### Run: AoATester replaceAll worst 100

What is your predicted number of statements when n == 100? How does the number of reported statements for the actual worst case align with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results?

Predicted tworst(100) Statements:

AoATester replaceAll worst 100 Statements:

Final tworst(n) =

## Expected Case Scenario

Assuming a large, randomly ordered array of ***unique*** elements and oldValue is a value in the array, how many replaceAll() while loop iterations will occur? What is the expected cost of the first call to find()? What is the expected cost of the second call to find()? What is the expected growth function t(n) for replaceAll() under these conditions?

Predicted texp(n) =

### Run: AoATester replaceAll expected 100

What is your predicted number of statements when n == 100? How does the number of reported statements compare with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results?

Predicted texp(100) Statements:

AoATester replaceAll expected 100 Statements:

Final texp(n) =

## Order

What is the runtime order (big-O) of replaceAll()?

O()

# Algorithm: sortIt()

## Minimum Statements, Constant Factor

What statements are executed in a call to sortIt() when the array size is zero (n == 0) or one (n == 1)? So what is t(0) and t(1), the minimum cost and constant factor for sortIt()?

Predicted t(0 or 1) =

### Run: AoATester sortIt min

How does the number of reported statements compare with your expectations? If there is a discrepancy, go back to the code to figure out why that might be. What do you need to modify about your analysis to better align with the empirical results?

Predicted t(0 or 1) Statements:

AoATester sortIt min Statements:

Final t(0 or 1) =

## Best Case Scenario

Assume a large array size n and elements in the array are already in ascending sorted order. The sortIt() outer loop depends only on n, but the inner loop is sensitive to the ordering of elements in the array and the current index of the outer loop. How many times will the outer loop iterate? How many times will the inner loop iterate? What statements are executed in every iteration of the outer loop? What is the growth function under these conditions?

Predicted tbest(n) =

### Run: AoATester sortIt best 100

What is your predicted number of statements when n == 100? How does the number of reported statements compare with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results? *(Note that the inner loop condition could be legitimately counted as 1, 2, 3, or even 4 statements. AoATester compromises and counts the inner loop condition as 2 statements.)*

Predicted tbest(100) Statements:

AoATester sortIt best 100 Statements:

Final tbest(n) =

## Worst Case Scenario

Assume a large array size n and elements in the array are arranged in descending order. The sortIt() outer loop depends only on n, but the inner loop is sensitive to the ordering of elements in the array and the current index of the outer loop. How many inner loop iterations would there be when next == 1? How many inner loop iterations would there be when next == array.length - 1? What is the average number of inner loop iterations per outer loop iteration under these conditions? What statements are executed for each iteration of the inner loop? What is the total worst case t(n) for sortIt() under these conditions?

Predicted tworst(n) =

### Run: AoATester sortIt worst 100

What is your predicted number of statements when n == 100? How does the number of reported statements compare with your expectation? If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results? *(Note that the inner loop condition could be legitimately counted as 1, 2, 3, or even 4 statements. AoATester compromises and counts the inner loop condition as 2 statements.)*

Predicted tworst(100) Statements:

AoATester sortIt worst 100 Statements:

Final tworst(n) =

## Expected Average Case Scenario

Assume a large array size n and the array contains unique elements in random order. How does the expected average number of inner loop iterations per outer loop iteration compare to the worst case? Why? How many inner loop iterations are expected on average? What is the total expected t(n) growth function for sortIt() under these conditions?

Predicted texp(n) =

### Run: AoATester sortIt expected 100

What is your predicted number of statements when n == 100? How does the number of reported statements for a random case align with your expectation? (You may want to run the test several times.) If there is a discrepancy, go back to the code to figure out why that might be. What (if anything) do you need to modify about your analysis to better align with the empirical results? *(Note that the inner loop condition could be legitimately counted as 1, 2, 3, or even 4 statements. AoATester compromises and counts the inner loop condition as 2 statements.)*

Predicted texp(100) Statements:

AoATester sortIt expected 100 Statements:

Final texp(n) =

## Order

What is the runtime order (big-O) of sortIt()?

O()