Nassau County Interscholastic Mathematics League

Solutions Contest #1

2004-2005



- 1. Multiply by y to get x + 5xy = 6y + 1, then x 1 = y(6 5x), so $y = \frac{x 1}{6 5x}$ or $y = \frac{1 x}{5x 6}$.
- 2. The ratio of the diameters is 2:3, so the ratio of the areas is 4:9. $\frac{4}{9} = \frac{12.40}{x}$, and x = \$27.90.
- 3. Any number starting with 4 works, and there are $\frac{5!}{2!2!} = 30$ of those. Also, 343212 works as does 343221. There are 32 of them.
- 4. Any one where p is true works; that's 4. If p is false, q must be true and r false; that's one more. There are 5.
- 5. To be geometric, the ratios of successive terms are equal, so $\frac{x-3}{x-1} = \frac{x-1}{3x-7}$, and so $3x^2 16x + 21 = x^2 2x + 1$, thus $2x^2 14x + 20 = 0$, then $x^2 7x + 10 = 0$. Solving, x = 5 or x = 2. If x = 2, than we get -1, 1, -1, 1, If x = 5, it's 2, 4, 8, 16, The fourth term is either 1 or 16.
- 6. Let the sides be x and y, so xy = 64 and $x^2 + y^2 = 196$. Since 2xy = 128, $x^2 + 2xy + y^2 = 324$. Now, $(x+y)^2 = 324$, and x+y=18. The perimeter is 2(x+y)=36.