

## MA4825 Robotics Assignment

Assignment (Due 16/11/24@2359hrs, Saturday)

### Instructions:

1. Answer all questions.
2. Show all your workings and drawings clearly.
3. Submit online thru MA4825 ntulearn course channel> Assignment> MA4825 Assignment 2 submission.

### Question 1

The robot in Figure 1 consists of a rotating links (link 1 and 3) and a translational links (links 2). The angular displacements of rotational joints are  $\theta$  and  $\beta$ , and the displacements of the translational joints are  $d$ . Link 1 is rotating with a constant angular velocity of  $\dot{\theta}$  about the  $Z$ -axis; link 2 is translating horizontally at constant velocity of  $\dot{d}$ ; link 3 is rotating with a constant angular velocity of  $\dot{\beta}$  about the  $X$ -axis. Note that the configuration shown in the figure is the initial position of the system where  $\theta = \beta = 0^\circ$  and  $d = K_1$ . Find the absolute velocity of the end point  $P$  of the robot in terms of  $\theta$ ,  $\beta$ , and  $d$ . (25 marks)

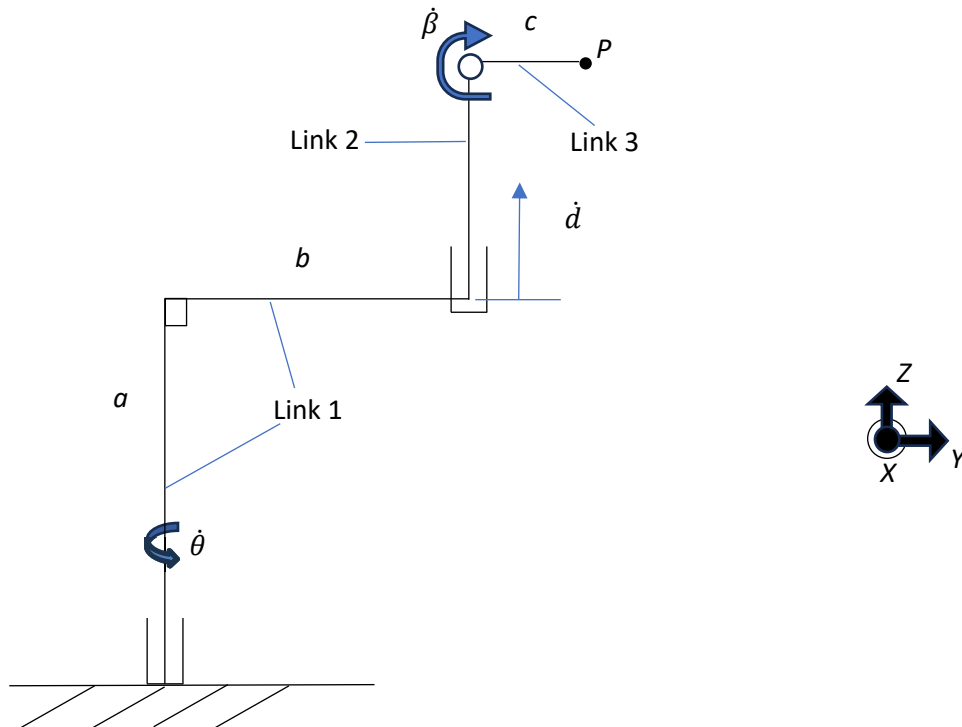


Figure 1

## Question 2

An illustration of an industrial robot (ABB IRB 5720 robot) used for spotwelding is shown in Figure 2 without its end effector and in its initial position. The arm has six joints:  $\mathbf{q} = \{\theta_1, \theta_2, \theta_3, \theta_4, \theta_5, \theta_6\}^T$ .

- Given the base coordinate system, draw and specify the right-handed coordinate systems  $i$  ( $i = 1$  to 6) of the robot up to the wrist joint. (Note: Sketch a skeletal diagram in isometric view & provide the positions and directions of the coordinate systems in your answer, take note of the positive directions.) (10 marks)
- Tabulate the Denavit-Hartenberg (D-H) parameters for the position of the robot shown in Figure 3 for joints 1 to 6, according to the coordinate systems specified in part (a). Note that  $\theta_i$  ( $i = 1$  to 6) are the joint variables. (6 marks)
- Find the generic D-H matrix  $\mathbf{H}_{03}$  for the robot where  $\mathbf{H}_{14}$  is a 4 x 4 homogeneous matrix transforming a vector from frame 3 to frame 1. (4 marks)
- Figure 3 shows a schematic of the robot from link 1 to link 2 moving  $\theta_2$  and  $\theta_3$  respectively from its initial position. Assume a point mass  $m_1$  and  $m_2$  acting at point  $b$  and  $c$  respectively. Derive the Lagrangian  $L$  of the system. (5 marks)

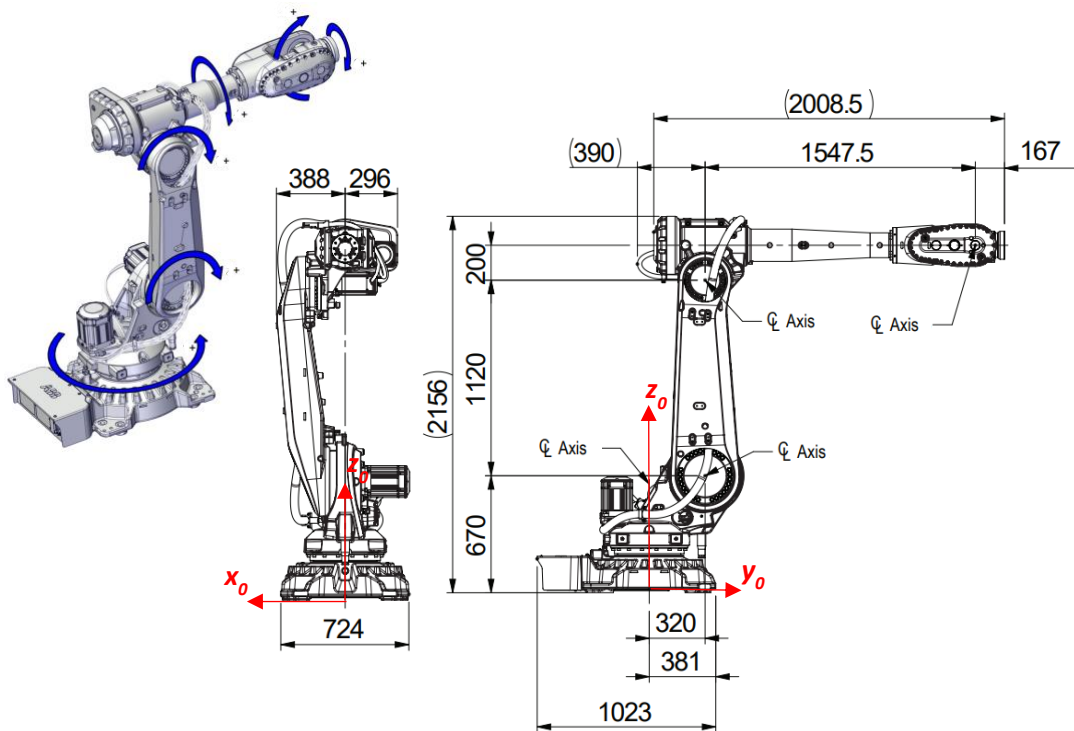


Figure 2

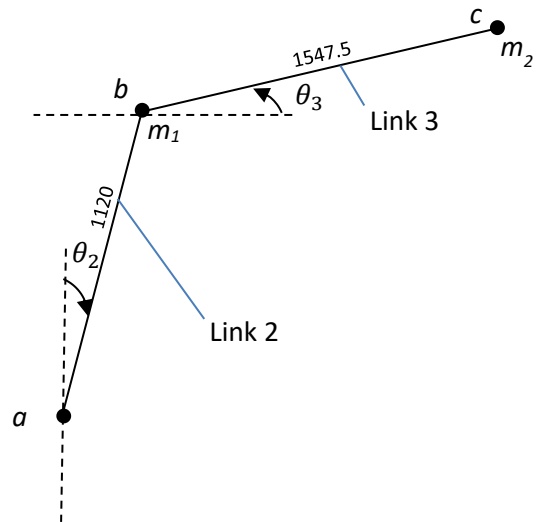


Figure 3

**END**