

~~# ghack 2022~~ → find ~~parameters~~

Linear Growth of QC complexity

Jonas Haferkamp

Complexity = min  $N$   $\geq$  local gates  
in decomposition of  
some  $U$

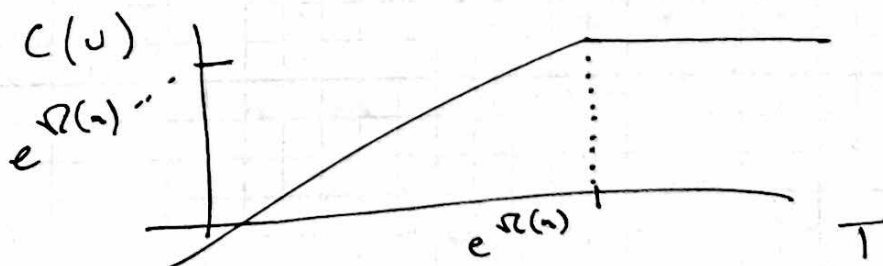
$C(U)$

extremely difficult to bound bc it  
find eventually reach  $P=NP$

talk about: what we can expect from  
typical systems

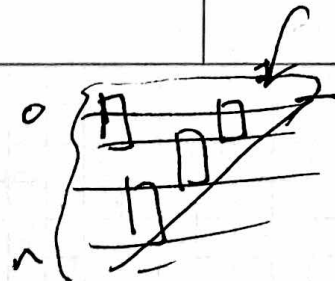
Brown + Siskind

what is  $e^{\Omega(n)}$   
CS lower bound  
/ see Nielsen  
Chuang pg 157



linear growth beyond  
separation of entanglement entropy

"Backboard ~~state~~" ?  
light cone



backward light cone  
bit 0 is connected to all other bits back to bit n

None of connection from a single qubit backward to all initial qubits in circuit

~~from~~ This provides a way to measure connectedness in the architecture & influences the expected bounds on complexity of a circuit

Every unitary can be implemented with  $O(4^n)$  many gates  
upper bound

Theorem

$$C(U) \geq \frac{T}{9} - \frac{n}{9}$$

$T$  = number of disjoint backward lightcones in an architecture

until...

n gates

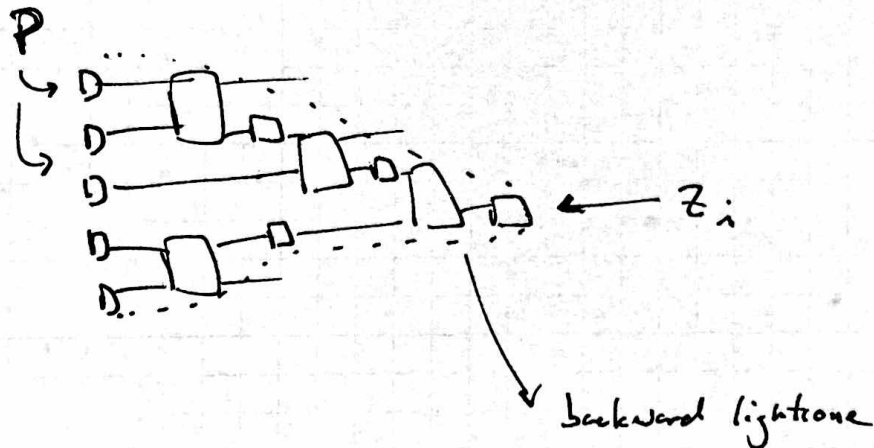
grow and

$$T \geq 4^n - 1$$

Rank of a matrix = num of linearly independent rows or columns

"Conjugate" a unitary operator--

\* Every Pauli operator in a backward lightcone can be conjugated (commuted?) with Clifford group  $U$  gates such that the equivalent circuit can be written as a single  $Z_i$  gate



How do you commute  $P$  operators through a circuit?